

# Midterm Exam #1

CS97: Principles and Practices of Computing

Wednesday, October 25, 2017

|    |    |
|----|----|
| 1. | 2. |
| 3. | 4. |

Name: \_\_\_\_\_

ID: \_\_\_\_\_

Rules of the game:

- **Write your name and ID number above.**
- The exam is closed-book and closed-notes.
- Please write your answers directly on the exam. Do not turn in anything else.
- The exam ends promptly at 3:50pm.
- Read questions carefully. Understand a question before you start writing.
- Relax!

1. (2 points each) Consider this function, where **x**, **y**, and **z** are integers:

```
def secret(x,y,z):  
    if x < y:  
        answer = 0  
    if y < z:  
        answer = 1  
    elif z < x:  
        answer = 2  
    else:  
        answer = 3  
    return answer
```

- (a) What is the result of `secret(1,2,3)`?

- i. 0
- ii. 1
- iii. 2
- iv. 3

ii

- (b) What is the result of `secret(2,2,1)`?

- i. 0
- ii. 1
- iii. 2
- iv. 3

iii

- (c) What is the result of `secret(3,1,2)`?

- i. 0
- ii. 1
- iii. 2
- iv. 3

ii

2. (5 points) The federal income tax plan currently being considered in Congress imposes a 12% tax on the first \$37,500 of a person's income, a 25% tax on all income above \$37,500 and less than or equal to \$112,500, and a 35% tax on all income above \$112,500. For example, someone earning \$30,000 would owe  $30,000 * 0.12 = \$3600$  in taxes, while someone earning \$40,000 would owe  $(37,500 * 0.12) + (2500 * 0.25) = \$5125$  in taxes. Implement the function `taxes` that is declared below, which takes an income (a number) as an argument and returns the taxes owed.

```
def taxes(income):  
    # your code goes here
```

```
def taxes(income):  
    if income <= 37500:  
        return income * 0.12  
    elif income <= 112500:  
        return 37500 * 0.12 + (income - 37500) * 0.25  
    else:  
        return 37500 * 0.12 + (112500 - 37500) * 0.25 + (income - 112500) * 0.35
```

3. (2 points each) Consider this function, where `lst` is a list and `n` is an integer:

```
def mystery(lst, n):  
    if n == 0:  
        return lst  
    elif lst == []:  
        return lst  
    else:  
        return mystery(lst[1:], n-1) + [lst[0]]
```

- (a) What does `mystery([1,3,5,7,9], 2)` return?  
[5,7,9,3,1]
- (b) How many times is `mystery` called during the execution of `mystery([1,3,5,7,9], 2)`, including the initial call to `mystery`?  
3
- (c) What are the first two lists to be concatenated together (via execution of the `+` operator) during the execution of `mystery([1,3,5,7,9], 2)`?  
[5,7,9] and [3]

4. (5 points) In mathematics, the *dot product* of two vectors of numbers  $[a_1, a_2, \dots, a_N]$  and  $[b_1, b_2, \dots, b_N]$  is defined as  $a_1*b_1 + a_2*b_2 + \dots + a_N*b_N$ . Implement the function `dotProduct` declared below, where Python lists are used to represent the vectors. For example, `dotProduct([1,2,3], [4,5,6])` should return 32 (since that is  $1*4 + 2*5 + 3*6$ ). You may assume that the two argument lists have the same length.

```
def dotProduct(vec1, vec2):  
    # your code goes here
```

```
def dotProduct(vec1, vec2):  
    if vec1 == []:  
        return 0  
    else:  
        return vec1[0] * vec2[0] + dotProduct(vec1[1:], vec2[1:])
```