

Name : _____

Date : _____ 200 _____

Examination : _____ Branch/Semester _____

Subject : _____ Hebbian

Junior Supervisor's full
Signature with Date

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Question No.	1	2	3	4	5	6	7	8	9	10	11	12	Total
Marks Obtained													

Hebbian Learning Rule (Unsupervised Learning)

Q $X_1 = \begin{bmatrix} 1 \\ -2 \end{bmatrix}$, $X_2 = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$, $X_3 = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$

$$X_4 = \begin{bmatrix} 0 \\ -1 \end{bmatrix}$$

$$W_1 = \begin{bmatrix} 1 & -1 \end{bmatrix}^t, \quad c = 1$$

↓
learning constant

Bipolar binary

$$\begin{aligned} \text{net}_i &= W_i^t X \\ O_i &= f(\text{net}_i) = \text{sign}(\text{net}_i) \\ \Delta W_i &= c O_i X \end{aligned}$$

Step 1 : set $X = X_1$

$$X = \begin{bmatrix} 1 \\ -2 \end{bmatrix}$$

$$\text{net}_1 = W_1^t X = \begin{bmatrix} 1 & -1 \end{bmatrix} \begin{bmatrix} 1 \\ -2 \end{bmatrix} = 3$$

$$o_1 = \text{sign}(\text{net}_1) = \boxed{1}$$

$$\Delta w_1 = c o_1 x$$

$$= (1)(1) \begin{bmatrix} 1 \\ -2 \end{bmatrix} = \begin{bmatrix} 1 \\ -2 \end{bmatrix}$$

$$w_2 = w_1 + \Delta w_1 = \begin{bmatrix} 1 \\ -1 \end{bmatrix} + \begin{bmatrix} 1 \\ -2 \end{bmatrix} = \begin{bmatrix} 2 \\ -3 \end{bmatrix}$$

Step 2: Set $x = x_2$

$$x = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

$$\begin{aligned} \text{net}_2 &= w_2^T x \\ &= \begin{bmatrix} 2 & -3 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} = -3 \end{aligned}$$

$$o_2 = \text{sign}(-3) = \boxed{-1}$$

$$\Delta w_2 = c o_2 x$$

$$= (1)(-1) \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ -1 \end{bmatrix}$$

$$w_3 = w_2 + \Delta w_2 = \begin{bmatrix} 2 \\ -3 \end{bmatrix} + \begin{bmatrix} 0 \\ -1 \end{bmatrix}$$

$$w_3 = \begin{bmatrix} 2 \\ -4 \end{bmatrix}$$

Step 3: Set $X = X_3$

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$$X = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$$

$$\text{net}_3 = W_3^T X$$

$$= \begin{bmatrix} 2 & -4 \end{bmatrix} \begin{bmatrix} 2 \\ 3 \end{bmatrix} = -8$$

$$O_3 = \text{sign}(-8) = -1$$

$$\Delta W_3 = C O_3 X$$

$$= (1)(-1) \begin{bmatrix} 2 \\ 3 \end{bmatrix} = \begin{bmatrix} -2 \\ -3 \end{bmatrix}$$

$$W_4 = W_3 + \Delta W_3$$

$$= \begin{bmatrix} 2 \\ -4 \end{bmatrix} + \begin{bmatrix} -2 \\ -3 \end{bmatrix} = \begin{bmatrix} 0 \\ -7 \end{bmatrix}$$

Step 4: Set $X = X_4$

$$X = \begin{bmatrix} 0 \\ -1 \end{bmatrix}$$

$$\text{net}_4 = W_4^T X$$

$$= \begin{bmatrix} 0 & -7 \end{bmatrix} \begin{bmatrix} 0 \\ -1 \end{bmatrix} = 7$$

$$O_4 = \text{sign}(7) = 1$$

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$$\Delta w_4 = c o_4 x$$

$$= (1)(1) \begin{bmatrix} 0 \\ -1 \end{bmatrix} = \begin{bmatrix} 0 \\ -1 \end{bmatrix}$$

$$w_5 = w_4 + \Delta w_4$$

$$= \begin{bmatrix} 0 \\ -7 \end{bmatrix} + \begin{bmatrix} 0 \\ -1 \end{bmatrix}$$

$$= \begin{bmatrix} 0 \\ -8 \end{bmatrix}$$

Use bipolar continuous

$$net_i = w_i t x$$

$$o_i = f(net_i) = \frac{2}{1 + e^{-\lambda net}} - 1$$

$$\lambda = 1$$

$$\Delta w_i = c o_i x$$

$$net_1 = 3$$

$$o_1 = 0.9053$$

$$\Delta w_1 = \begin{bmatrix} 0.905 \\ -1.810 \end{bmatrix}$$

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$$w_2 = w_1 + \Delta w_1 = \begin{bmatrix} 1.905 \\ -2.81 \end{bmatrix}$$

$$\text{Set } x = x_2 \quad x = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

$$\text{net}_2 = -2.81$$

$$o_2 = f(\text{net}_2) = \frac{2}{1 + e^{2.81}} - 1$$

$$= -0.886$$

$$\Delta w_2 = \begin{bmatrix} 0 \\ -0.886 \end{bmatrix}$$

$$w_3 = w_2 + \Delta w_2$$

$$= \begin{bmatrix} 1.905 \\ -3.696 \end{bmatrix}$$

$$\text{Set } x = x_3 = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$$

$$\text{net}_3 = -7.278$$

$$o_3 = -0.9986$$

$$\Delta w_3 = c o_2 x$$

$$w_4 = w_3 + \Delta w_3$$

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$$w_4 = \begin{bmatrix} -0.092 \\ -6.691 \end{bmatrix}$$

$$\text{Set } x = x_4 = \begin{bmatrix} 0 \\ -1 \end{bmatrix}$$

$$\text{net}_4 = 6.691$$

$$o_4 = 0.9975$$

$$\Delta w_4 =$$

$$w_5 = w_4 + \Delta w_4$$