

**Exercise 1.** Consider a *wing of a plane* with density  $\rho(x) = \frac{1}{x+1}$ . The wing of the plane is bounded by the curves  $y=0$ ,  $x=0$ ,  $x=3$ , and a line  $L$  connecting  $(0,1)$  and  $(3,1/3)$ .

- i) Make a drawing which represents the wing in question.
- ii) Use the point slope formula to determine an equation for the line  $L$ .
- iii) If the wing is flat, in which order should we setup the integral to find its mass?  $dx$  or  $dy$ ?
- iv) Indicate in your diagram the bounds of integration. Write them as well as  $a \leq x \leq b$  or  $c \leq y \leq d$  depending on your choice for order of integration.
- v) Find the **GREATER** and **LOWER** curves. Label them.
- vi) Use the previous information to find the mass of the wing in question.

**Exercise 2.** Consider the region in the 1<sup>st</sup> quadrant enclosed by the curves

$$y = x - 2, \quad \text{and} \quad x = 3.$$

Now suppose we rotate the region about the axis  $x = 2$ . Do the following:

- i) Draw the region in question.
- ii) Draw the solid of revolution obtained after rotation.
- iii) Which 2 methods can we use to find the volume of this shape? Recall the possibilities are rings/shells on  $x/y$ .
- iv) Given your method of choice, find the bounds of the region. Label them either as  $a \leq x \leq b$  or  $c \leq y \leq d$ .
- v) Find the **GREATER** and **LOWER** curves. Label them.
- vi) Use the previous information find the pair of parameters  $R, r$  or  $r, h$  given your choice of method. Label them.
- vii) Construct the area function of your method. Label it.
- viii) With the previous information, find the volume of the shape in question.