

Exercise 1. Answer the following prompts, little to no explanation needed:

i) Consider the a geometric sequence (a_n) with initial condition $c = \frac{1}{3}$ and common ratio $r = \frac{-1}{2}$.

- Write an expression for the **general term** of a_n .

- What is the **value** of a_2 ?

- Is this sequence **monotonic**?

- What is the **limit** of this sequence? [**Hint:** If $\lim_{n \rightarrow \infty} |a_n| = 0$ then $\lim_{n \rightarrow \infty} a_n = 0$.]

- What can you say about the behavior of the series $\sum_{n=0}^{\infty} a_n$? Is it **convergent** or **divergent**?

ii) Consider the sequence whose general term is $b_n = \frac{2n}{3n+1}$ for $n=0,1,2,\dots$

- Write the **values** of b_0 , b_1 , b_2 and b_3 .

- Is this sequence monotonic? **Increasing** or **decreasing**?

- Is this sequence **bounded**? Above, below or neither?

- What is the **limit** of this sequence as $n \rightarrow \infty$?

- What can you say about the behavior of the series $\sum_{n=0}^{\infty} b_n$? Is it **convergent** or **divergent**?