

**Exercise 1** (Bessel Function). Consider the series  $\sum_{n=1}^{\infty} \frac{(-1)^n}{2^{2n}(n!)^2}$ , this is  $J_0(1)$  where  $J$  is called the Bessel J function. Do the following:

- I) From the convergence tests we've seen in class name a test that proves that the series converges.
- II) State the conditions needed to verify the validity of the test.
- III) Apply the test to prove that  $J_0(1)$  converges.

1. It is possible to use either Dirichlet's Alternating Series test or the Ratio test.