Name	CSU ID #

Be sure to read each question fully and carefully. Multiple choice answer bubbles must be fully filled in. There is space to the right of each multiple choice question to show work, if your work is correct you can get points even with an incorrect multiple choice answer.

1. For questions 1a through 1f consider the following information:

The CSU Math Club is holding an election for President. Adam, Brenda, and Carlos are the candidates. The members vote, and the following preference schedule shows the results:

Number of votes	9	6	3	2	1
1 st choice		Adam			
2 nd choice	Carlos	Carlos	Adam	Adam	Brenda
$3^{\rm rd}$ choice	Adam	Brenda	Brenda	Carlos	Carlos

	3 Choice Adam Dienda Dienda Carlos Carlos
a)	How many people voted in the Math Club presidential election? (2 points)
	\bigcirc 1
	\bigcirc 3
	\bigcirc 9
	○ 11
	○ 21
(b)	Who is the plurality winner in this election? (2 points)
	○ Adam
	○ Brenda
	○ Carlos
	○ Nobody won, majority wasn't reached
	○ There's a tie, so a tiebreaking process is necessary
(c)	How many points does Adam score using the Borda count method? (2 points)
	○ 21
	\bigcirc 40
	O 44
	O 46
	○ 63

(d) What ha	ppens in a pairwis	e compari	son betwe	en Bren	da and Ca	rlos? (4 points)
\subset	Brenda wins aga	inst Carlos	s, 12 votes	to 9		
\subset	Brenda ties with	Carlos, 10	votes eac	h		
\subset	Brenda wins aga	inst Carlos	s, 9 votes t	to 12		
C	Carlos wins agai	nst Brenda	a, 12 votes	to 9		
(e) How ma	ny first-place vote	s are need	ed for a m	ajority?	(2 points)	
\subset) 9					
\subset) 10					
\subset) 11					
C) 15					
C	20					
	the complete rank (6 points)	ing of the	candidate	es using	the plural	ity with elimination
\subset	Adam, Brenda, C	arlos				
\subset	Adam, Carlos, Br	enda				
\subset	Brenda, Adam, C	arlos				
\subset	Brenda, Carlos, A	Adam				
C	Carlos, Adam, Br	enda				
C	Carlos, Brenda, A	Adam				
For questions	2a through 2i cons	sider the fo	ollowing i	nformat	ion:	
into a fund.	They will take thei they each inverte	r decision	s via a W	eighted	Voting Scl	nave invested money heme based on how information on the
	Person	Markus	Natalie	Oscar	Pauline	
	Invested Money	??	\$12000	\$7000	\$4000	
	of money Markus of the quota for this	-		n and w	rill be the	subject of our ques-

2.

(a) If each person gets a vote per each \$1000 they put into the fund, write down the weighted voting scheme for this setting assuming Markus gets M votes: (3 points)

[24:M: , ,]

(b) Find the minimum and maximum values for Markus' share of votes M , pick 2 options (4 points)
\bigcirc 4
\bigcirc 7
\bigcirc 12
○ 21
\bigcirc 23
O 24
(c) Which value of M results in someone being a dictator? (2 points)
\bigcirc 4
O 7
O 12
O 13
O 21
O 23
\bigcirc 24
(d) Using the value of M you chose in the previous item, who is a dictator, why? (points)
 Markus is a dictator because they have enough votes to pass a motion single handedly.
 Markus and Natalie are dictators because any motion can pass without their votes.
 Natalie is a dictator because the other people can pass motions withouthem.
 Both Markus and Natalie are dictators because no motion can pass without both of their votes.
(e) Recall a player in a Weighted Voting Scheme has <i>no power</i> when they have no say is the outcome of the voting. For there to be exactly one player with no power, the value of M must be between Pick 2 options: (4 points)
\bigcirc 4
O 7
O 12
O 13
O 21
\bigcirc 23
O 24

(f) For the previous values of M who is the player with no power? (2 points)
Oscar has no power because no motion can pass without their votes.
 Oscar has no power because both Markus and Natalie or Markus and Pauline can pass resolutions on their own meaning Oscar's vote doesn't influence the decision.
O Pauline has no power because they can pass motions single-handedly.
 Pauline has no power because both Markus and Natalie or Markus and Os car can pass resolutions on their own meaning Pauline's vote doesn't influ ence the decision.
(g) Which values of M result in players (can be one, or more than one) with veto power Pick 2 options: (4 points)
\bigcirc 4
\bigcirc 7
\bigcirc 12
\bigcirc 13
○ 21
\bigcirc 23
O 24
(h) Which values of M result in <i>exactly two</i> players with veto power? (2 points)
(ii) Which values of M restain statety two players with vere powers (2 points)
\bigcirc 7
\bigcirc 12
\bigcirc 13
○ 21
\bigcirc 23
O 24
(i) For the previous value, which players have veto power, why? (2 points)
 Both Natalie and Oscar have veto power because all motions can pass with out their consideration.
 Both Markus and Natalie have veto power because no motion can pass with out both of their votes.
 Both Oscar and Pauline have veto power because no coalition can pass any motion at all.
 Both Natalie and Pauline have veto power because they need the suppor of all the players to pass a motion.

3. Assume your family consists of your grandparents G, your parents P, your siblings S (you're part of this group), and your nephews N. When taking decisions as a family each group gets together and emits a vote.

The weight distribution is as follows:

- Your grandparents hold four times as many votes as your parents.
- Your parents hold twice as many votes as your siblings.
- Your siblings hold eight times as many votes as your nephews.
- And your nephews have only 3 votes.

The quota is the simple majority of the votes. We will show that your grandparents are dictators in this scheme by doing the following:

- (a) Calculate the number of votes each party has and then find the quota by simple majority. (Hint: Remember you might need to round up). (8 points).
- (b) Write down the Weighted Voting Scheme for this situation. (6 points).
- (c) Verify that, indeed, your grandparents are dictators by comparing their number of votes with the quota. (4 points).