Exercise 1. Consider a region R bounded by the curves

$$y=x$$
, $y=-x$, and $x=1$,

additionally the region has density $\rho(y) = e^y$. Now suppose we rotate the region about the axis y = -4. Do the following:

- I) Draw the region in question.
- II) Draw the solid of revolution obtained after rotation.
- III) Which method should we use to find the volume of this shape?
- IV) Find the bounds of the region. Label them either as $a \le x \le b$ or $c \le y \le d$.
- v) Find the GREATER and LOWER curves by writing their equations.
- VI) Find the parameters (either R, r or r, h) used to build your area function.
- VII) With the previous information, write out the integral which represents the mass of the solid obtained.
 - I) See diagram.
 - II) See diagram.
 - III) As we have a rotation about a y = b line, we can either use shells in y or rings in x. The density is in terms of y so we should use shells in y.
 - IV) The regions starts at y = -1 and ends at y = 1. So $-1 \le y \le 1$.
 - V) We must divide the region into two pieces:

VI) As we are using shells we must find r,h. These are:

$$\begin{cases} h_1 = \text{GREATER-LOWER1} = [1 - (-y)] & \text{for } -1 \leq y \leq 0 \\ h_2 = \text{GREATER-LOWER2} = [1 - (y)] & \text{for } 0 \leq y \leq 1 \\ r = \text{dist(axis,coordinate)} = y - (-4) \end{cases}$$

VII) Adding this facts together we get

ether we get
$$m = \int_{-1}^{0} 2\pi (y+4)(1+y)e^{y} dy + \int_{0}^{1} 2\pi (y+4)(1-y)e^{y} dy.$$

Exercise 2. Consider the tank formed after rotating the curve $y = x^3$ with $0 \le x \le 1$ about the axis x = 0. Suppose tank is filled with *radioactive waste* with density $\rho(y) = 100 + 25y^2$. Do the following:

| Math161S1 | Quiz 6 - Solutions | Name: |
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