

Lambda Calculus Week2

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1 Ker Comp Practice 1c

1c For each occurrence of a variable in each of these terms, say whether it is free or bound:

- i $\lambda xyz. xyz$
 $x = \text{bound}$
 $y = \text{bound}$
 $z = \text{bound}$
- ii $\lambda xyz. yz(\lambda p. xyz)$
 $(\lambda xyz. (yz)(\lambda p. (xy)z))$
 $y = \text{bound}$
 $z = \text{bound}$
 $x = \text{free}$
 $y = \text{free}$
 $z = \text{free}$
- iii $\lambda xy. yz(\lambda z. zz)$
 $y = \text{bound}$
 $z = \text{free}$
 $z = \text{bound}$
 $z = \text{bound}$

2 Ker Exercises 1.3

1.3 List all the free variables in

- i $\lambda xy. (\lambda u. uvxy)z$
 $u = \text{bound}$
 $v = \text{free}$
 $x = \text{free}$
 $y = \text{free}$
 $z = \text{free}$
- ii $\lambda xy. z(\lambda u. uvxy)$
 $z = \text{free}$
 $u = \text{bound}$
 $v = \text{free}$
 $x = \text{free}$
 $y = \text{free}$
- iii $\lambda wx. z(\lambda u. uvwx)$
 $z = \text{free}$
 $u = \text{bound}$
 $v = \text{free}$

$w = \text{free}$

$x = \text{free}$

iv $\lambda vw.z(\lambda u.uvww)$

$z = \text{free}$

$u = \text{bound}$

$v = \text{free}$

$v = \text{free}$

$w = \text{free}$

v $\lambda yx.z(\lambda u.uvyx)$

$z = \text{free}$

$u = \text{bound}$

$v = \text{free}$

$y = \text{free}$

$x = \text{free}$