

# Lecture 11

## Hedonics

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AEM 4510

# Roadmap

- What can we use to infer the demand for environmental goods?
- What do housing prices tell us?
- When do changes in house prices give us welfare measures

# Hedonic valuation

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# Revealed preference approaches

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Is there a way we can reveal the value of these goods?

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If there are changes in the environmental good, holding everything else fixed, that should be reflected in *some way* in changes in the price of the related private good

This change in price can tell us something about how people value the change in the environmental good

# Revealed preference approaches: example

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What does this price change mean?

# Hedonics: Property value models

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- Bathrooms
- School quality
- **Environmental quality**

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Homes located in pristine areas are likely to be more valuable than identical homes located near toxic facilities

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Real estate is virtually ideal for measuring environmental changes

Real estate markets are often competitive and thick

Property purchases are large and consequential: buyers and sellers are likely to be well-informed

It is uncontroversial that property values should reflect local attributes

e.g. homes in better school districts are typically more expensive

# BCA of Superfund

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By 2005: \$35 billion in federal funding has been spent at roughly 800 sites



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How do we do it?

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Main idea: Take two otherwise very similar houses: one in a neighborhood surrounding a site that has been cleaned up and one in a neighborhood surrounding a site that has not

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Main idea: Take two otherwise very similar houses: one in a neighborhood surrounding a site that has been cleaned up and one in a neighborhood surrounding a site that has not

How do their prices differ?



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Ridker and Henning (1967) first applied method to environmental valuation in a study of the effect of air pollution on property values in St. Louis

It motivated the conceptual model of Rosen (1974) of how we might use hedonic prices to estimate peoples' values for site-specific amenities

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Environmental quality (air quality, noise, etc)

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Lets get some intuition for how housing markets reveal the value of environmental goods

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At the current equilibrium price of \$200,000 per house, all 200 hundred homes on either lake are equally preferred

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Lake A prices **increase** to bring the market back into equilibrium

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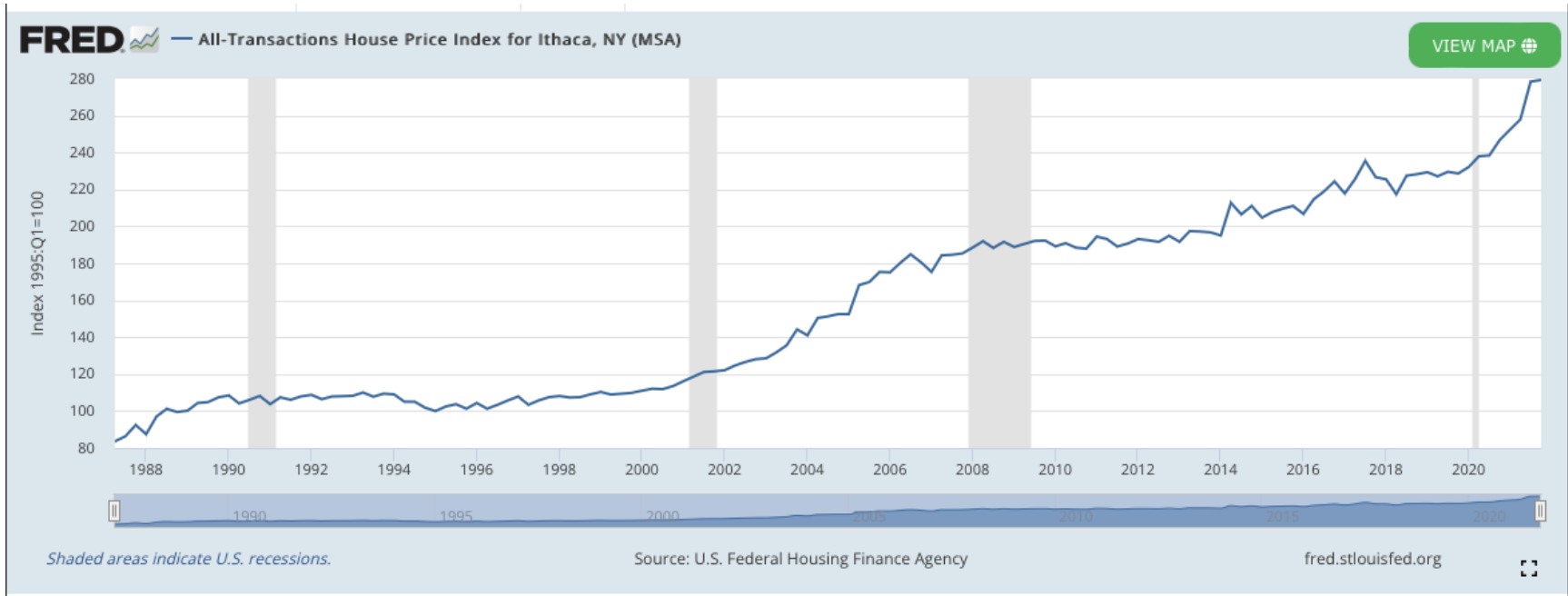
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**Sidebar:** think about US cities in the last 20 years and urban residential prices

# Housing prices in Ithaca are increasing **fast**, why?

## Study shows Ithaca home prices rising far faster than nation's



# Another Dyson professor's house



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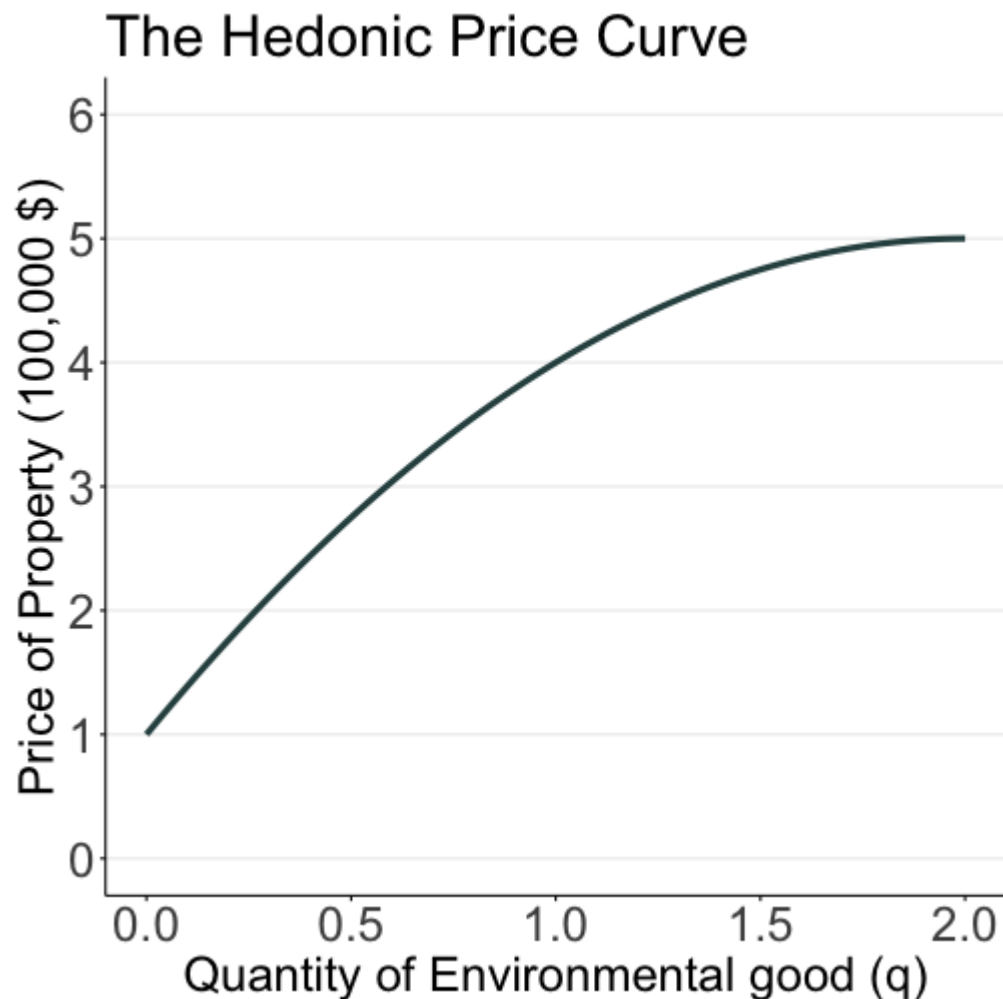
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Here we will assume the supply of houses is fixed in the short run so the price curve arises solely from buyer behavior

# The hedonic model: the price curve



The hedonic price curve is  $P(x, q)$

It's increasing in  $q$  ( $q$  is good) but at a decreasing rate (decreasing marginal utility)

This is holding  $x$  fixed

Analogous to regular demand curves holding income fixed

# The hedonic model: the price curve



The implicit price curve for  $q$  is

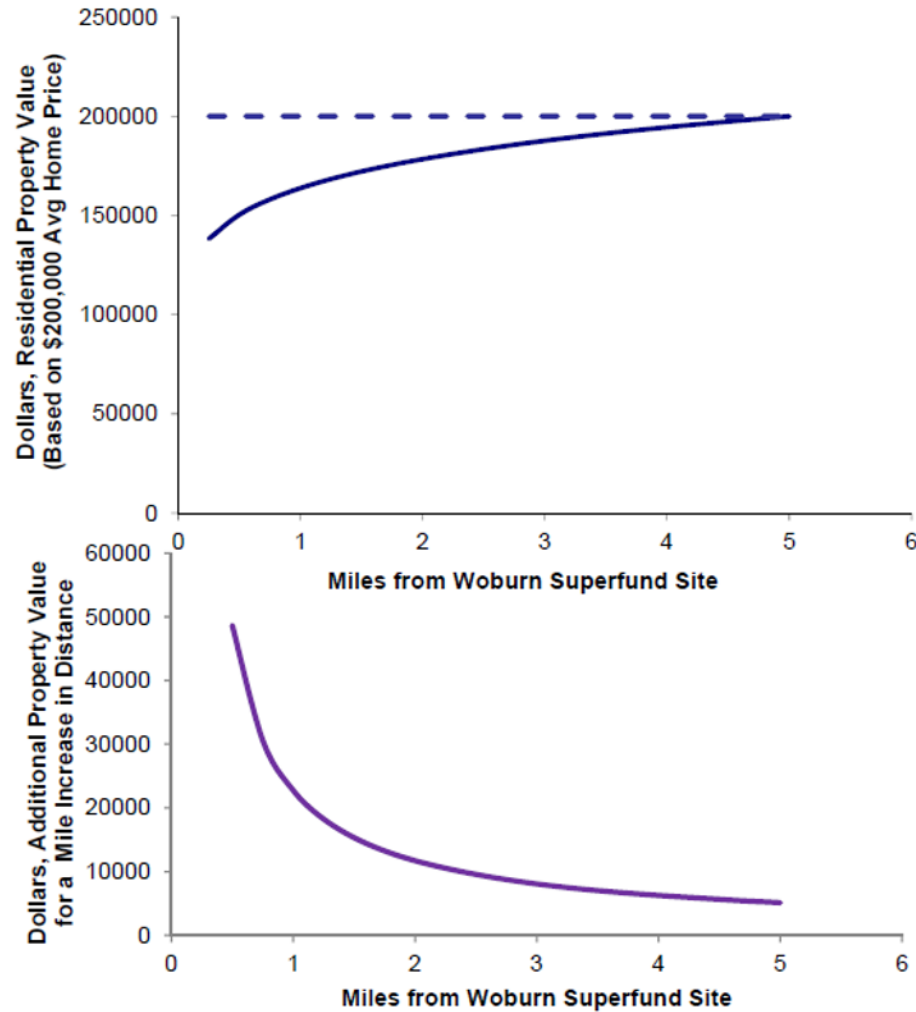
$$\frac{\partial P(x, q)}{\partial q}$$

It tells us how the price changes in  $q$

It's positive, but downward sloping

This is effectively the environmental good demand curve

# Price curve example



Total Value

“Marginal” Value  
(one mile increment)

Source: Messer et al. *Env. and Res. Econ.* 2006

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- $z$  is the numeraire good (spending on other private goods)
- $y$  is income
- $s$  is the set of the household's characteristics like family size, ages, etc

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Another is that you just can't purchase some sets of  $x$  (i.e. a huge lot in downtown Manhattan with a farm)

We won't touch on this in class because it's a lot more complicated, but economists know how to deal with these problems

# Choosing $q$

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We are thus also implicitly assuming  $q$  varies across space so that households can sort into areas they prefer

- $q$  is really picking up **local** environmental goods

# What is $P(x, q)$

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For homeowners we are basically assuming they rent from themselves every year

# The hedonic model: consumer's choice problem

$$\max_{x,q,z} U(x, q, z; s) \quad \text{subject to: } y = z + P(x, q)$$

Plug in the constraint for  $z$  to get:

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The FOCs for this problem are:

$$\begin{aligned} \frac{\partial U}{\partial x_j} &= \frac{\partial U}{\partial z} \frac{\partial P}{\partial x_j} & j = 1, \dots, J & \quad \text{(house characteristics)} \\ \frac{\partial U}{\partial q} &= \frac{\partial U}{\partial z} \frac{\partial P}{\partial q} & & \quad \text{(environmental good)} \end{aligned}$$



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What does this mean?

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**Recall from intro/intermediate micro:** the MRS tells us how the household trades off  $q$  and  $z$  while keeping utility constant



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**This means that the MRS is the WTP for  $q$ :** the reduction in income needed to compensate for an additional unit of  $q$ , while maintaining the same level of utility

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How prices change in the environmental good tells us about WTP

# The hedonic model: bid functions

Now let's dive deeper by looking at some reference level of utility  $\bar{u}$ :

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This equation just defines some indifference curve

Next we will define something called a **bid function**  $b(x, q, y, s, \bar{u})$

# The hedonic model: bid functions

The bid function  $b(x, q, y, s, \bar{u})$  is the **WTP** of the household for:

- A house with characteristics  $x, q$
- Given income  $y$  and household characteristics  $s$
- That achieves utility  $\bar{u}$

By definition how WTP changes in  $q$  is the  $q$ - $z$  MRS:

$$\frac{\partial b}{\partial q} = \frac{\partial P}{\partial q} = \frac{\partial U}{\partial q} \bigg/ \frac{\partial U}{\partial z}$$



# The hedonic model: deriving MWTP

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By assuming  $q$  is a part of a larger bundle of house characteristics, we are able to characterize its demand through its relationship to the housing market

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Our ultimate empirical goal is to estimate  $\frac{\partial b}{\partial q}$ , which is a kind of demand curve

It's called a **Hicksian** demand curve, whereas our regular demand curves are **Marshallian**

# The hedonic model: deriving MWTP

The difference is that with **Marshallian** demand curves, we are holding **income** constant on the curve, income changes are demand shifters, utility changes as you move along the curve

# The hedonic model: deriving MWTP

The difference is that with **Marshallian** demand curves, we are holding **income** constant on the curve, income changes are demand shifters, utility changes as you move along the curve

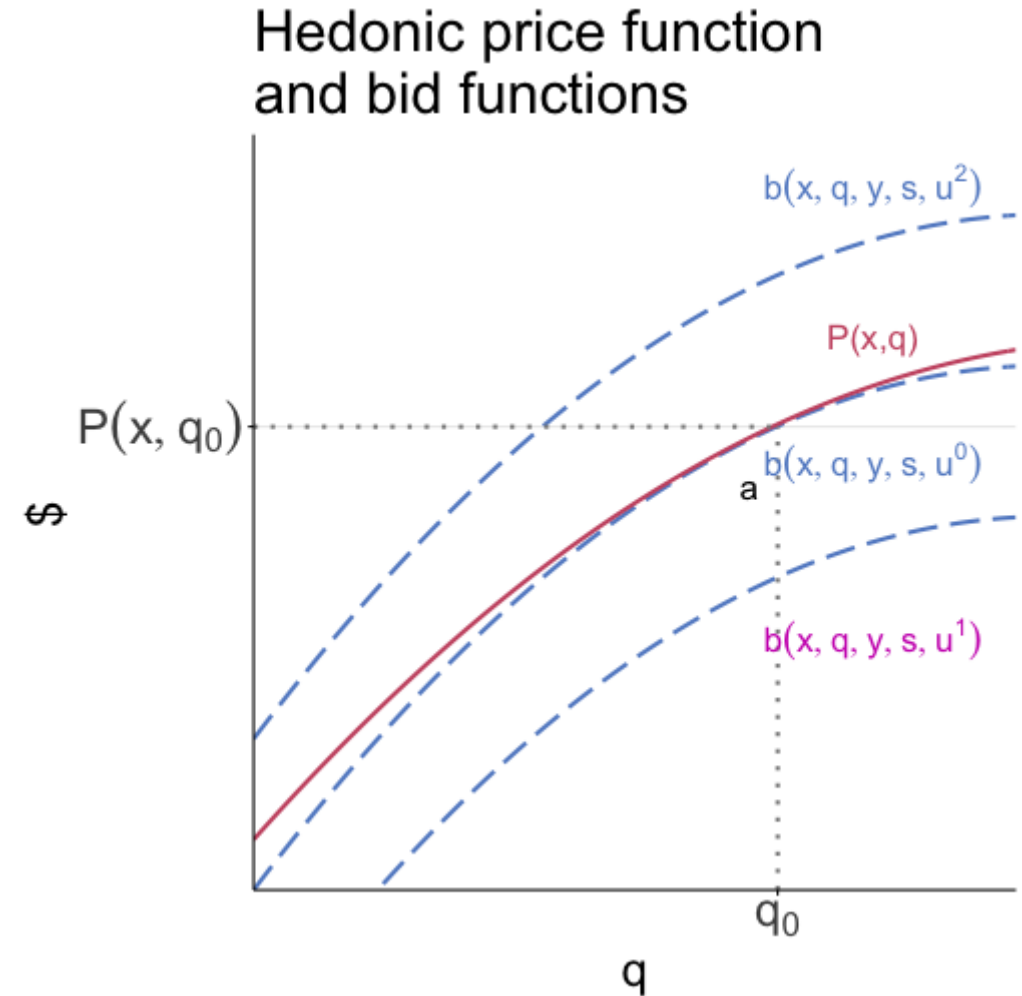
With **Hicksian** demand curves, we are holding **utility** constant, income can change along the curve, utility changes are demand shifters

# Bid functions and housing prices

The red line is the hedonic price function

The blue lines are a single household's bid functions at different reference utility levels

Moving to the bottom-right increases utility

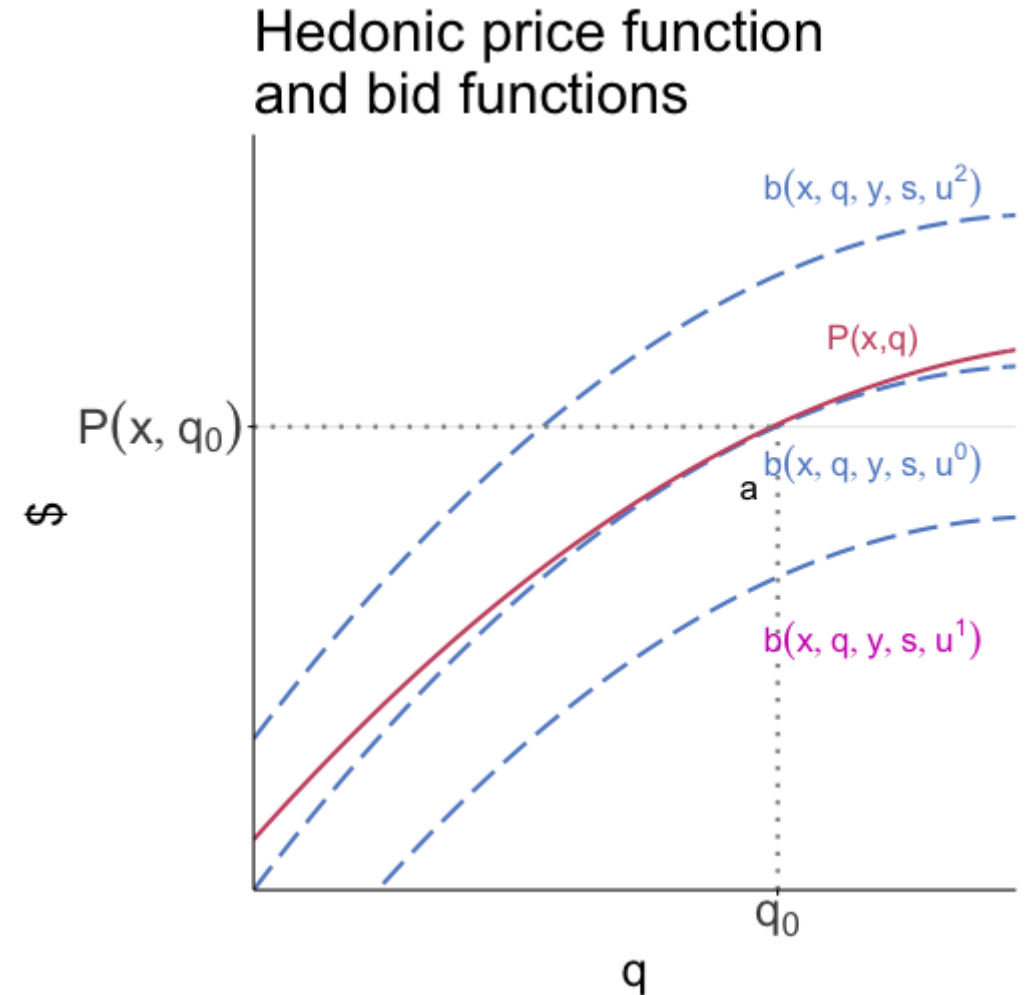


# Bid functions and housing prices

Optimal choice is where the household's bid function is tangent to the hedonic price schedule:  $a$

This gives us an observed consumption level  $q_0$ , observed price  $P(x, q_0)$ , and realized utility  $u^0$

Different households will have different tangency points, different  $q$  and  $P(x, q)$



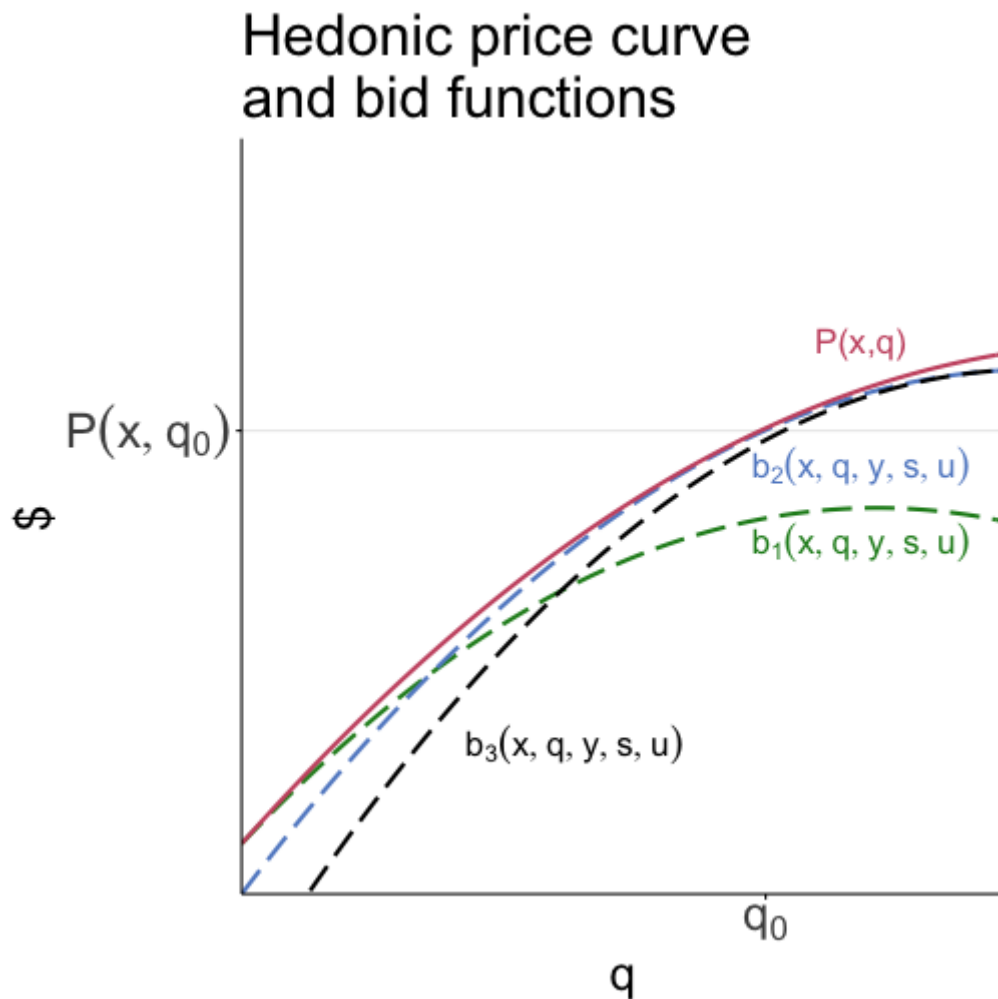
# Bid functions and housing prices

The hedonic price function is the **upper envelope** of all the bid functions

i.e. all the bid functions are tangent to it

The other piece of the story is we need the landlord problem

It's almost identical to the buyer, but replace utility with profit





# Hedonic price curve and willingness to pay

The hedonic price curve shows how a house varies with attributes (such as air quality)

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At a given point on the curve, the slope also gives the marginal WTP of the consumer who purchase that level of attributes

But we don't know the whole marginal WTP schedule for **that person**, why?

Their bid curve is only tangent at that one point, we don't see their whole bid curve, people don't buy 1,000 houses to trace out the whole curve

# Estimating the effect of ozone

Let's work through an example where we estimate the effect of ozone

You have a dataframe `house_data` available on RStudio Cloud:

```
house_data
```

```
## # A tibble: 757 × 7
##   house_num ozone num_bedrooms num_bathrooms sq_feet log_price price
##   <int> <dbl>      <int>          <dbl>    <dbl>    <dbl>
## 1         1  9.60           4            3      577.     12.7 341991.
## 2         2  4.49           4            3     1111.     12.7 334851.
## 3         3 15.6           4            1      820.     12.0 159567.
## 4         6 10.2           3            2      886.     12.7 325459.
## 5         8 30.8           4            3     4909.     12.9 399579.
## 6         9 14.7           2            1.5     798.     11.9 152339.
## 7        10  3.80           4            1.5     946.     12.5 278165.
## 8        11  5.62           4            1     1912.     12.2 206147.
## 9        12  8.62           3            1.5     720.     12.3 226051.
## 10       13 16.0           1            1     3057.     12.0 301760.
```

# Estimating the effect of ozone

We want to understand the effect of ozone on housing prices: how much does a unit increase in ozone cost?

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Let's take a look at the summary statistics of our dataset first:

```
summary(house_data)
```

##	house_num	ozone	num_bedrooms	num_bathrooms	sq_feet	log_price
##	Min. : 1.0	Min. : 0.8242	Min. :1.00	Min. :1.000	Min. : 501.4	Min. :10.47
##	1st Qu.: 245.0	1st Qu.: 7.9529	1st Qu.:1.00	1st Qu.:1.500	1st Qu.: 892.3	1st Qu.:12.10
##	Median : 491.0	Median : 15.3680	Median :2.00	Median :2.000	Median : 1395.0	Median :12.49
##	Mean : 494.4	Mean : 23.1940	Mean :2.49	Mean :1.977	Mean : 2055.0	Mean :12.51
##	3rd Qu.: 745.0	3rd Qu.: 28.6273	3rd Qu.:4.00	3rd Qu.:2.500	3rd Qu.: 2415.5	3rd Qu.:12.92
##	Max. :1000.0	Max. :192.8742	Max. :4.00	Max. :3.000	Max. :21001.0	Max. :14.49



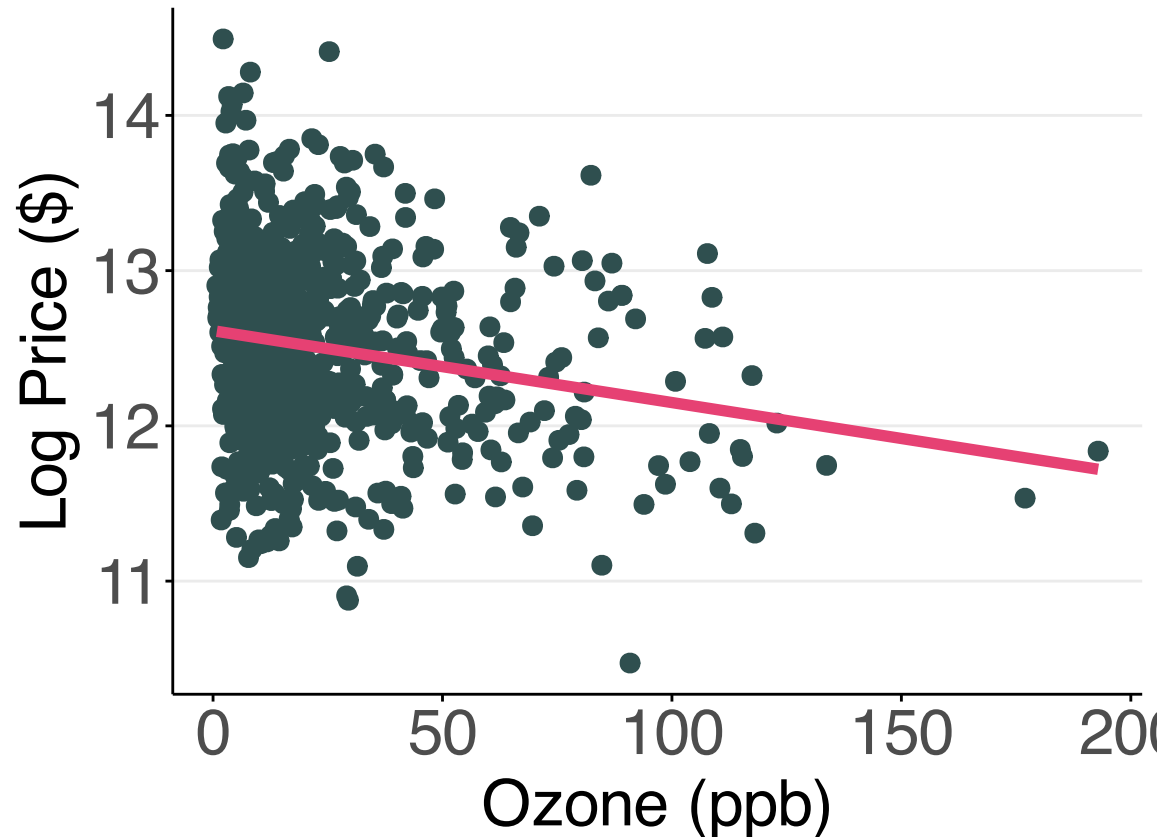
# Estimating the effect of ozone

Now let's plot the relationship between log house prices and ozone to see what the data actually look like:

```
ggplot(house_data, aes(x = ozone, y = log_price)) +    # start plot
  geom_point(size = 3, color = "darkslategray") +      # plot points
  geom_smooth(formula = y ~ x, se = F, method = "lm", size = 2, color = red_pink) +
  theme_regular +                                     # apply theme
  labs(x = "Ozone (ppb)", y = "Log Price ($)")         # assign labels
```

# Estimating the effect of ozone

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# Estimating the effect of ozone

Now it's time to do the regression (try one out):

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```
lm(log_price ~ num_bedrooms + num_bathrooms + sq_feet + ozone, house_data) %>%  
  broom::tidy()
```

```
## # A tibble: 5 × 5  
##   term          estimate std.error statistic  p.value  
##   <chr>          <dbl>      <dbl>     <dbl>    <dbl>  
## 1 (Intercept)    11.7        0.0722     163.      0  
## 2 num_bedrooms   0.136        0.0163      8.39 2.45e-16  
## 3 num_bathrooms  0.161        0.0256      6.29 5.54e-10  
## 4 sq_feet        0.00000971 0.00000900    10.8 2.46e-25  
## 5 ozone         -0.00432    0.000767     -5.63 2.52e- 8
```

A 1 unit increase in ozone decreases housing values by 0.466%!

# Housing prices and superfund clean up

Greenstone, Michael, and Justin Gallagher (2008). “Does Hazardous Waste Matter? Evidence from the Housing Market and the Superfund Program.”  
Quarterly Journal of Economics

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**Main question:** How does superfund site clean up affects the housing price in the adjacent areas?

**How they do it:** Compare housing market outcomes in the areas surrounding the first 400 hazardous sites chosen for Superfund clean-ups to the areas surrounding the 290 sites that narrowly missed qualifying for these clean-ups

# Housing prices and superfund clean up

Each site is given a Hazardous Ranking System (HRS) Score (0-100)



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Places right below 28.5 probably aren't systematically different than those right above 28.5

**Key idea:** Any differences between housing values in these locations is most likely due to Superfund clean up, not other factors

# Superfund location



Figure IIa  
GEOGRAPHIC DISTRIBUTION OF HAZARDOUS WASTE SITES IN THE 1982 HRS SAMPLE  
SITES WITH 1982 HRS SCORES EXCEEDING 28.5



Figure IIb  
GEOGRAPHIC DISTRIBUTION OF HAZARDOUS WASTE SITES IN THE 1982 HRS SAMPLE  
SITES WITH 1982 HRS SCORES BELOW 28.5

# Regression

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They regress:

$$\log(2000 \text{ median home price})_c = \underbrace{\theta 1(\text{cleaned up in 2000})_c}_{= 1 \text{ if true, } = 0 \text{ otherwise}} + \beta \underbrace{X_c}_{\text{controls}} + \varepsilon_c$$

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They are interested in  $\theta$  which tells us the percent change in a census tract median home price if it was cleaned up

— $\theta$  is telling us the **cost** of a superfund site to households

# Superfund results: "quasi-experimental"

QUASI-EXPERIMENTAL ESTIMATES OF THE EFFECT OF NPL STATUS ON HOUSE PRICES, SAMPLES BASED ON THE 1982 HRS SAMPLE SITES

	<u>RD-Style Estimators</u>						
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
<u>A. Own Census Tract</u>							
1(NPL Status by 2000)	0.035	0.037	0.043	0.047	0.007	0.022	0.027
	(0.031)	(0.035)	(0.031)	(0.027)	(0.063)	(0.042)	(0.038)
<u>B. Adjacent Census Tracts</u>							
1(NPL Status by 2000)	0.071	0.066	0.012	0.015	-0.006	-0.002	0.001
	(0.031)	(0.035)	(0.029)	(0.022)	(0.056)	(0.035)	(0.035)
<u>C. 2-Mile Radius from Hazardous Waste Sites</u>							
1(NPL Status by 2000)	0.021	0.019	0.011	0.001	0.023	-0.018	-0.007
	(0.028)	(0.032)	(0.029)	(0.023)	(0.054)	(0.035)	(0.034)
Ho: > 0.138, P-Value	0.000	0.000	0.000	0.000	0.018	0.000	0.000

Last three columns are the important ones

# Superfund results

Superfund cleanups had **economically and statistically insignificant effects** on property values, rental rates, housing supply, population, who lives near the site

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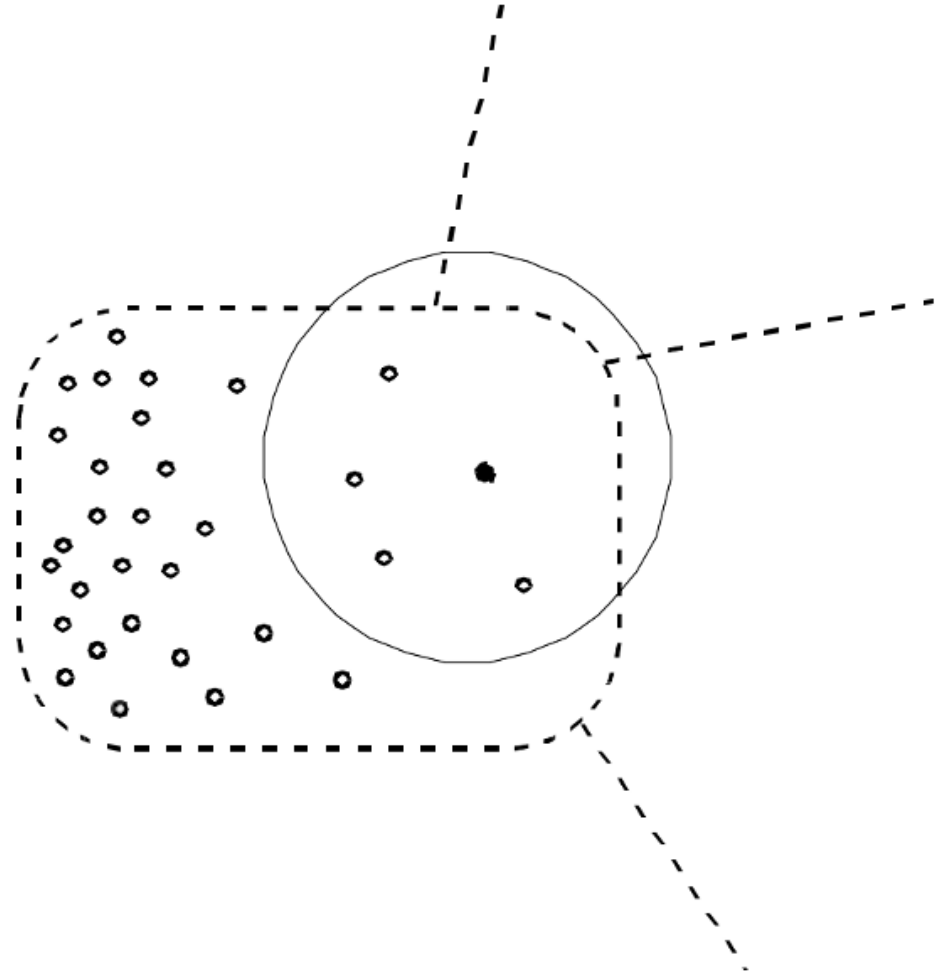
Why does granularity matter?

# Superfund: zoom in

Superfund sites are a localized disamenity

Previous attempts to value cleanup looked at changes in census tract median housing values and found no impacts

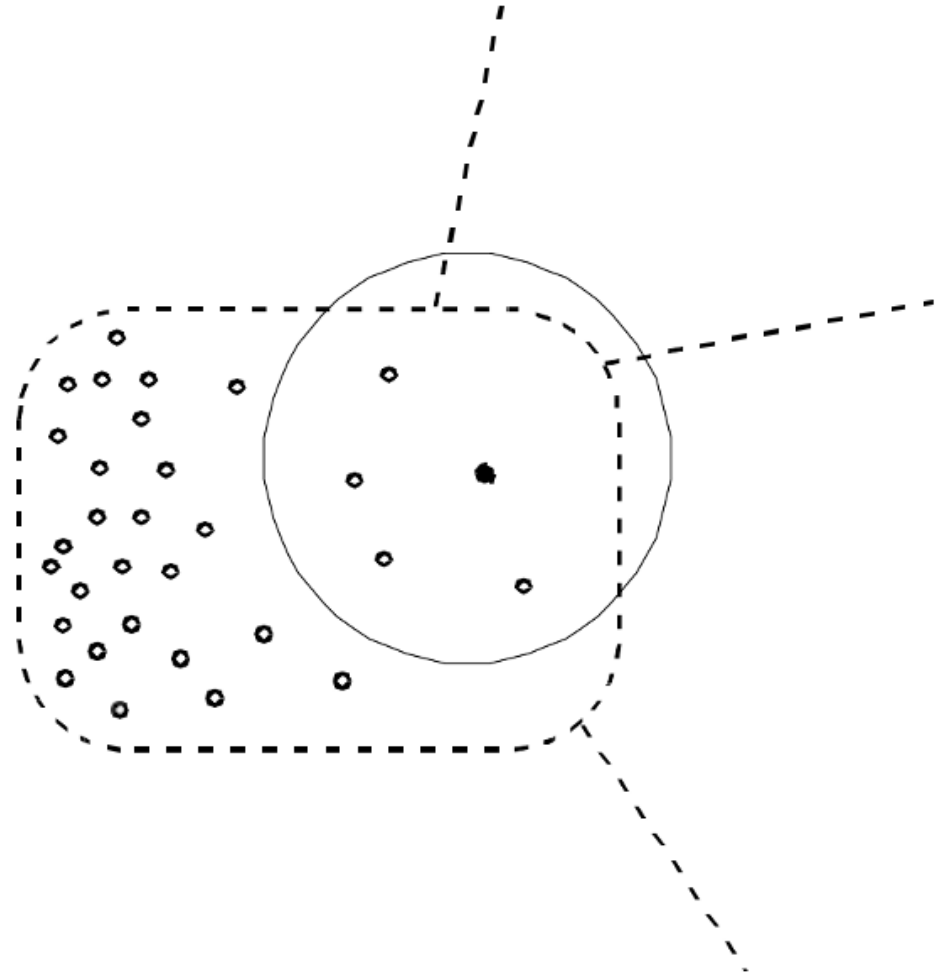
Need to look **within** census tracts



# Superfund: zoom in

Consider changes in other percentiles of within-tract house value distribution:

*deletion of a site raises tract-level housing values by 18.2% at the 10th percentile, 15.4% at the median, and 11.4% at the 60th percentile*





# Value of a statistical life (VSL)

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A statistical life is a probabilistic concept

VSL reflects willingness to pay for a reduction in the risk of death

VSL is more appropriately called the **value of mortality risk**

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How do you get a credible estimate of the VSL?

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How?

See tradeoffs people make between cost and safety

# Value of a statistical life (VSL)

Some examples:

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Some examples:

Driving speed

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Wage-risk relationship

# Value of a statistical life (VSL)

Some examples:

Driving speed

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Wage-risk relationship

There's lots of studies, and lots of different answers

# VSL

EPA recommends that the central estimate of \$7.4 million (\$2006), updated to the year of the analysis, be used in all benefits analyses that seek to quantify mortality risk reduction benefits regardless of the age, income, or other population characteristics of the affected population until revised guidance becomes available

# VSL thought experiment

Suppose that individuals are willing to adopt a safety procedure, for which they have to give up 25 cents per hour, to reduce risk of on-the-job fatality by 1 in 10,000 (annual risk)



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This procedure would result in one fewer person dying on average

$VSL = \$500 \times 10,000 = 5 \text{ million dollars}$

# Estimating a hedonic wage function

We can estimate a **hedonic wage function**:

$$w_i = \alpha + \beta_1 H_i + \beta_2 X_i + \beta_3 p_i H_i + \gamma_1 p_i + \gamma_2 q_i + \gamma_3 q_i W C_i + \varepsilon_i$$

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$w$ : wage

$H$ : worker personal characteristics

$X$ : job characteristics

$p$ : **risk of death at the job**

$q$ : non-fatal risk at the job

$WC$ : workers' compensation benefits for injury

$\frac{\partial w}{\partial p}$  is the wage-risk trade off for marginal changes in risk

# VSL from the hedonic wage function

Suppose:

- Wages were in thousands of dollars
- Risk is deaths per 10,000 people
- Coefficient on mortality risk  $p$  is  $\gamma_1 = 0.4$

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This implies an average WTP (reduced wage) of



# VSL from the hedonic wage function

Suppose:

- Wages were in thousands of dollars
- Risk is deaths per 10,000 people
- Coefficient on mortality risk  $p$  is  $\gamma_1 = 0.4$

This implies an average WTP (reduced wage) of 400 dollars to reduce risk by 1 in 10,000

# VSL from the hedonic wage function

WTP (reduced wage) of 400 dollars to reduce risk by  $1/10,000$

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Suppose a policy reduces mortality risk by 1/10,000 for 60,000 people (saves 6 lives on average)

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This policy has a value of:

$$400 * 60,000 = 24 \text{ million dollars}$$

# VSL estimates

Exhibit 7-3 Value of Statistical Life Estimates (mean values in 1997 dollars)

Study	Method	Value of Statistical Life
Kneisner and Leeth (1991 - U.S.)	Labor Market	\$0.7 million
Smith and Gilbert (1984)	Labor Market	\$0.8 million
Dillingham (1985)	Labor Market	\$1.1 million
Buder (1983)	Labor Market	\$1.3 million
Miller and Guria (1991)	Contingent Valuation	\$1.5 million
Moore and Viscusi (1988)	Labor Market	\$3.0 million
Viscusi, Magat and Huber (1991)	Contingent Valuation	\$3.3 million
Marin and Psacharopoulos (1982)	Labor Market	\$3.4 million
Gegax et al. (1985)	Contingent Valuation	\$4.0 million
Kneisner and Leeth (1991 - Australia)	Labor Market	\$4.0 million
Gerking, de Haan and Schulze (1988)	Contingent Valuation	\$4.1 million
Cousineau, Lecroix and Girard (1988)	Labor Market	\$4.4 million
Jones-Lee (1989)	Contingent Valuation	\$4.6 million
Dillingham (1985)	Labor Market	\$4.7 million
Viscusi (1978, 1979)	Labor Market	\$5.0 million
R.S. Smith (1976)	Labor Market	\$5.6 million
V.K. Smith (1976)	Labor Market	\$5.7 million
Olson (1981)	Labor Market	\$6.3 million
Viscusi (1981)	Labor Market	\$7.9 million
R.S. Smith (1974)	Labor Market	\$8.7 million
Moore and Viscusi (1988)	Labor Market	\$8.8 million
Kneisner and Leeth (1991 - Japan)	Labor Market	\$9.2 million
Herzog and Schlotman (1987)	Labor Market	\$11.0 million
Leigh and Folsom (1984)	Labor Market	\$11.7 million
Leigh (1987)	Labor Market	\$12.6 million
Garen (1988)	Labor Market	\$16.3 million
Derived from EPA (1997) and Viscusi (1992).		