

# Lecture 07

## Multiple Market Failures and Second-Best Policies

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AEM 4510

# Roadmap

1. What happens when we have another distortion like market power?
2. How do second-best policies like output taxes or intensity standards work?

# Market power and pollution

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# Market power

Lets consider two extreme cases to understand whether and how market power matters

1. Perfect competition
2. Monopoly

# Market power

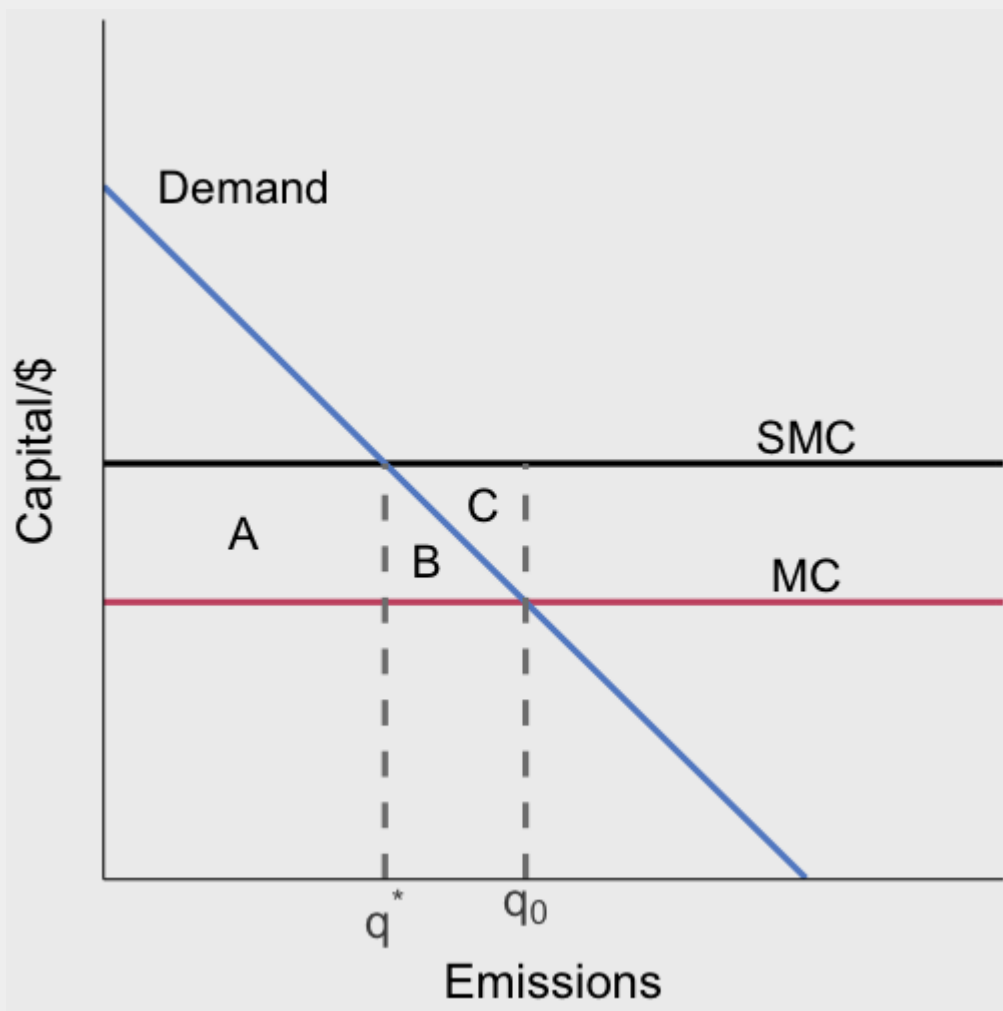
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1. Perfect competition
2. Monopoly

In both cases we assume that:

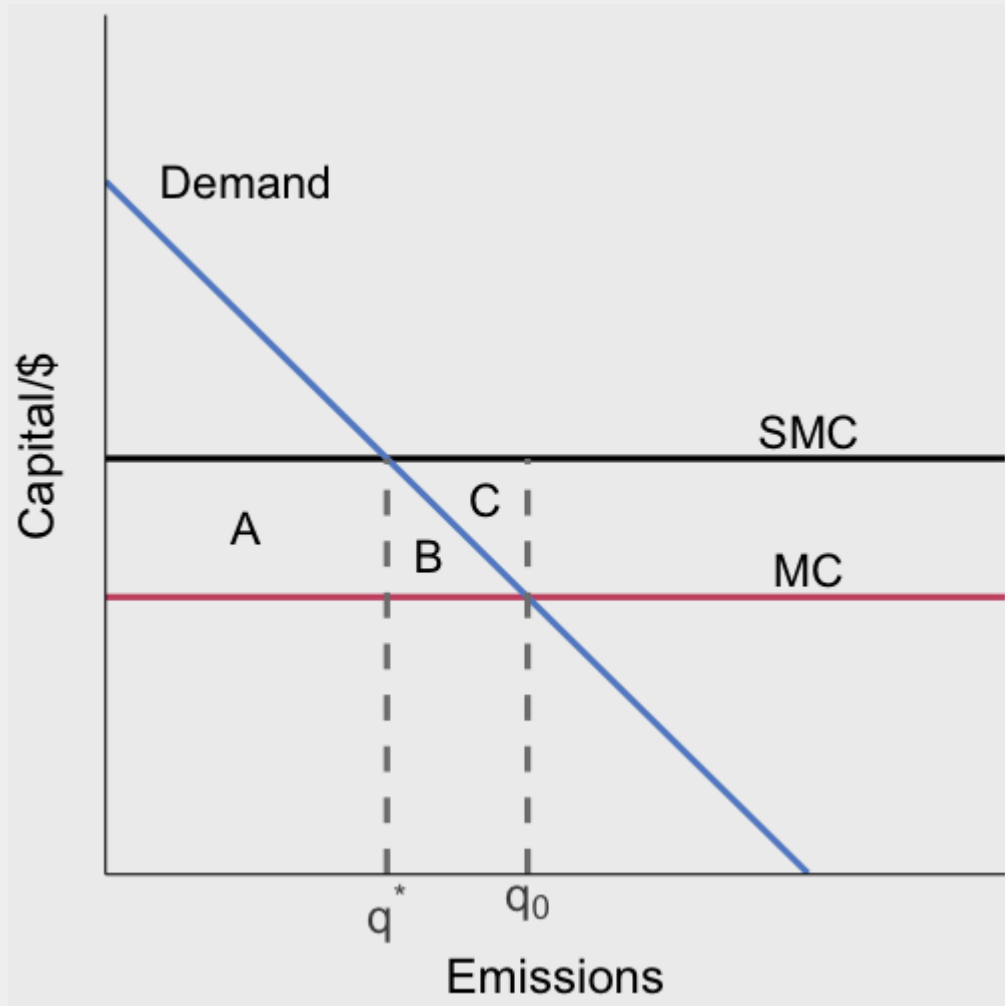
1. Marginal costs of production are constant  $MC$
2. The marginal damage from a unit of output is constant giving us constant social marginal costs  $SMC = MC + MD$

# Perfect competition



The effect of moving from  $q_0 \rightarrow q^*$  using a tax equal to marginal damage (SMC - MC):

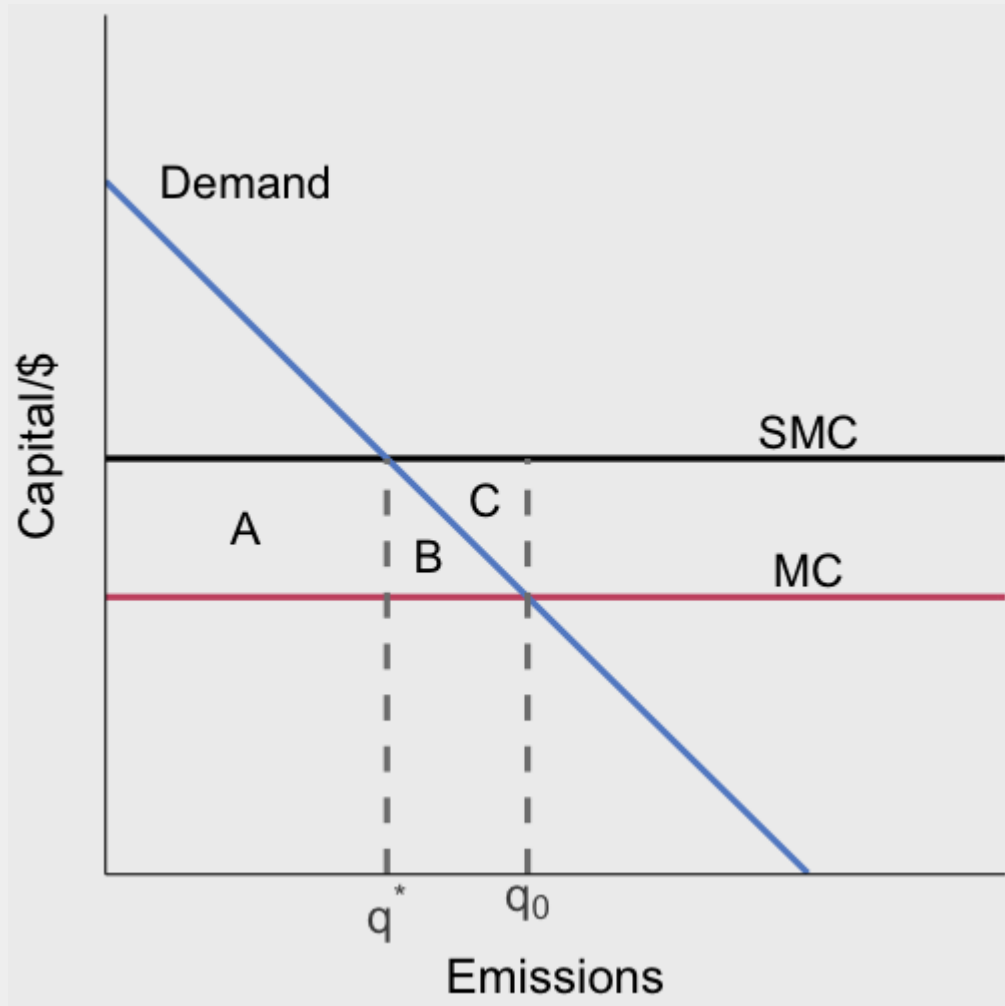
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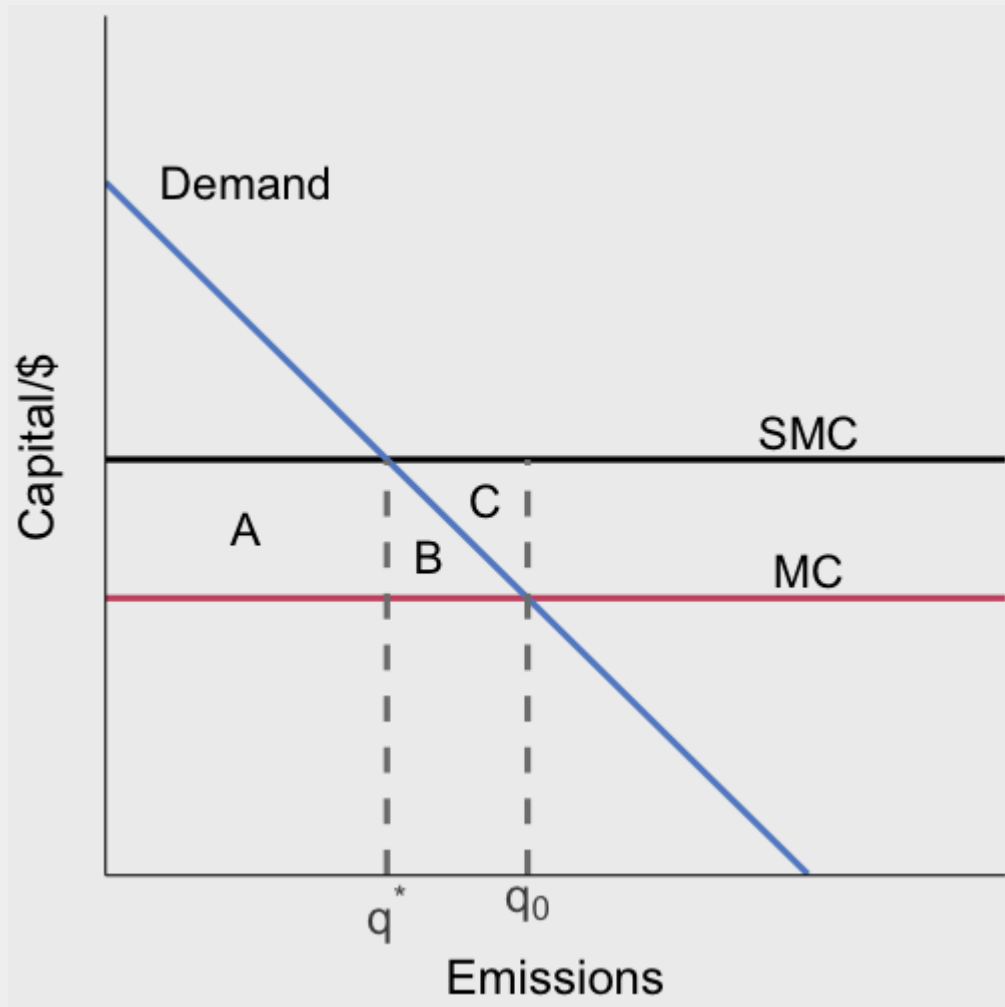
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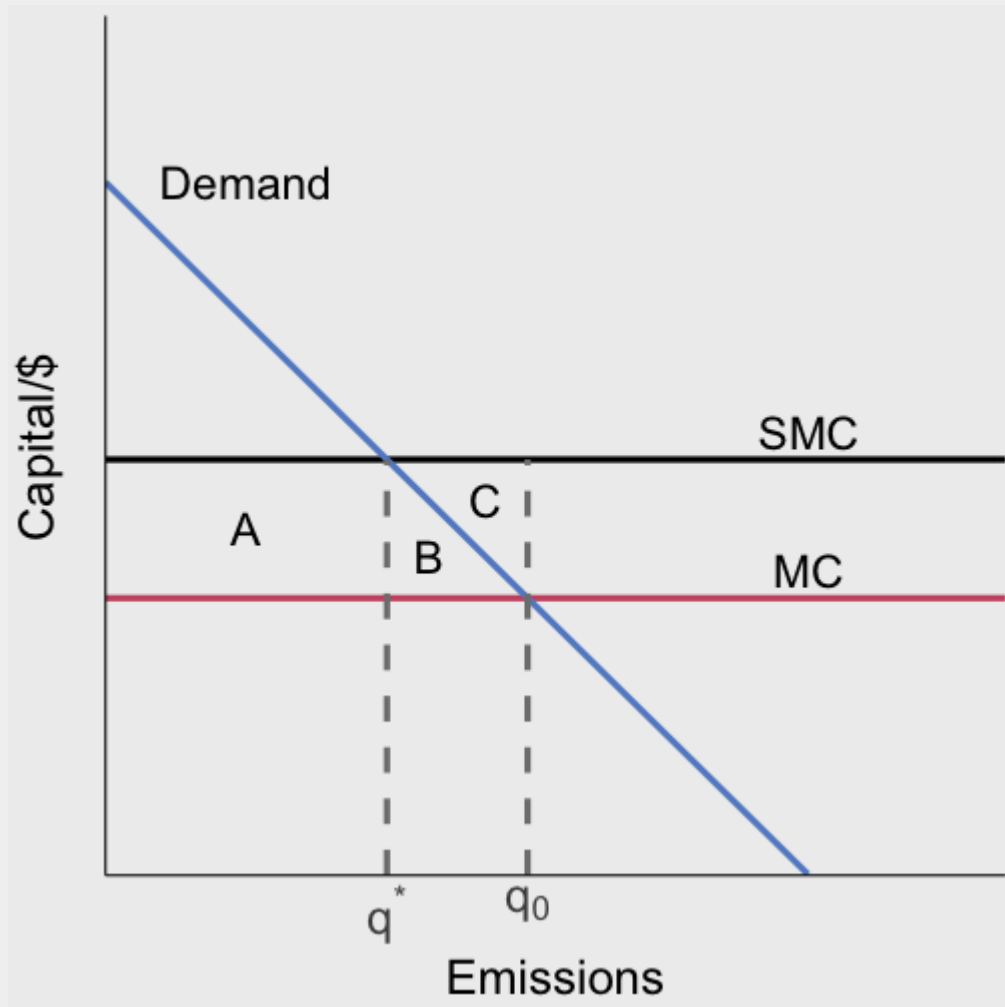
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Tax revenue:  $A$

**Net gain:  $-(A+B) + (B+C) + A = C$**

# Monopoly

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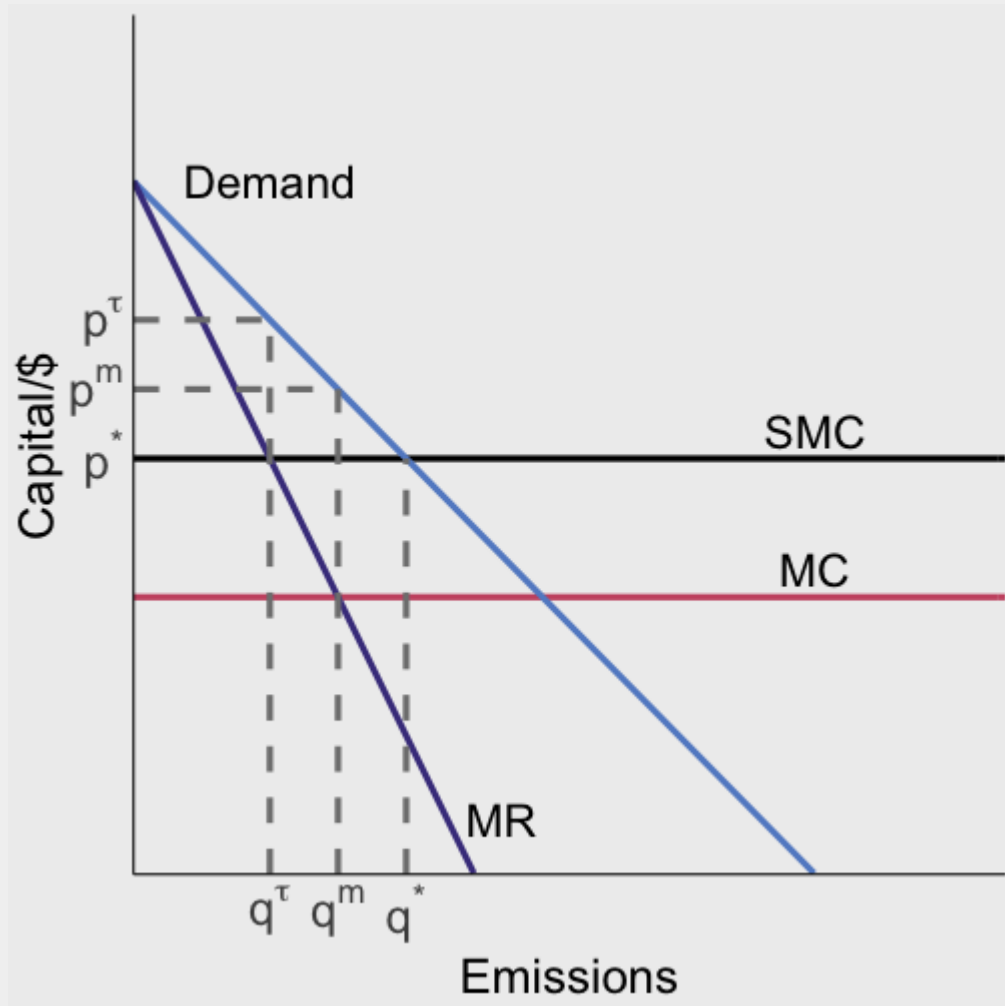
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Why?

The monopolist accounts for how additional output lowers the market price on inframarginal units



# Monopoly

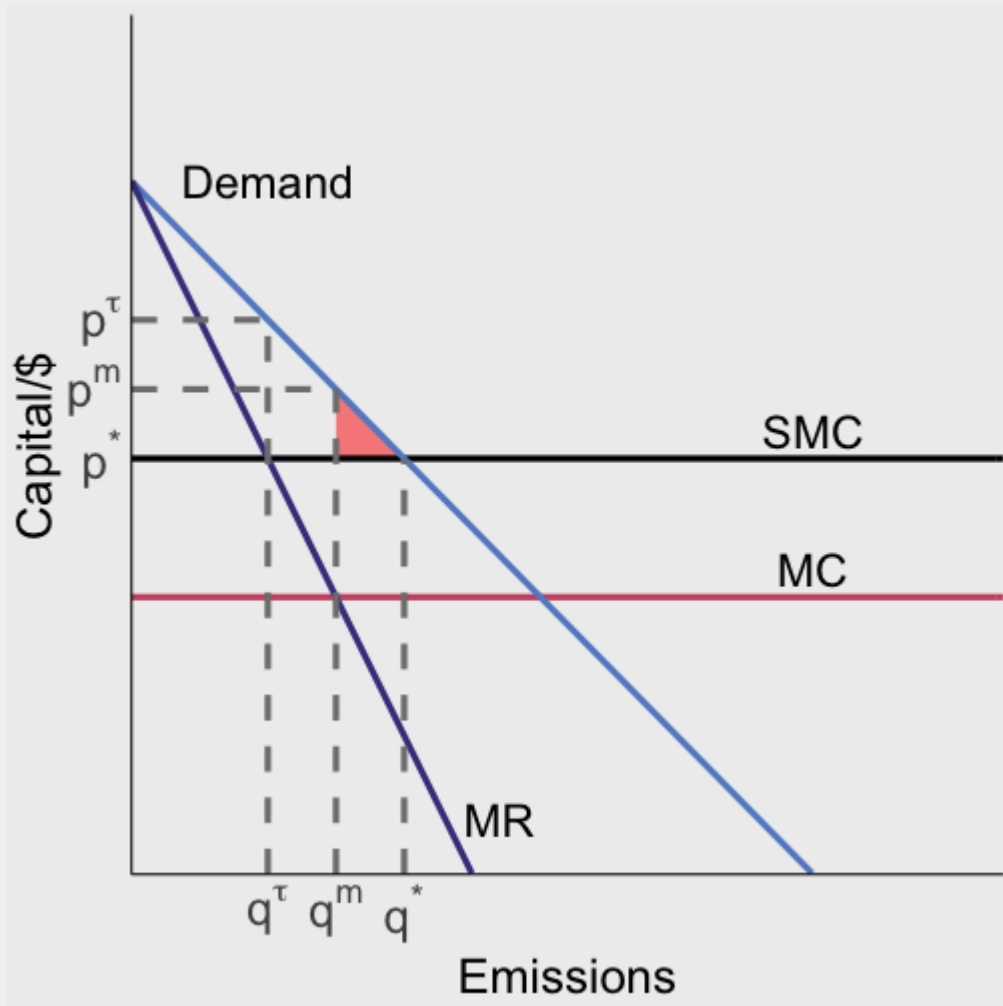


The socially efficient allocation is where social marginal cost is equal to the social marginal benefit

This is where SMC crosses the demand curve:  $(q^*, p^*)$

What is the welfare outcome under the unregulated monopolist outcome?

# Monopoly

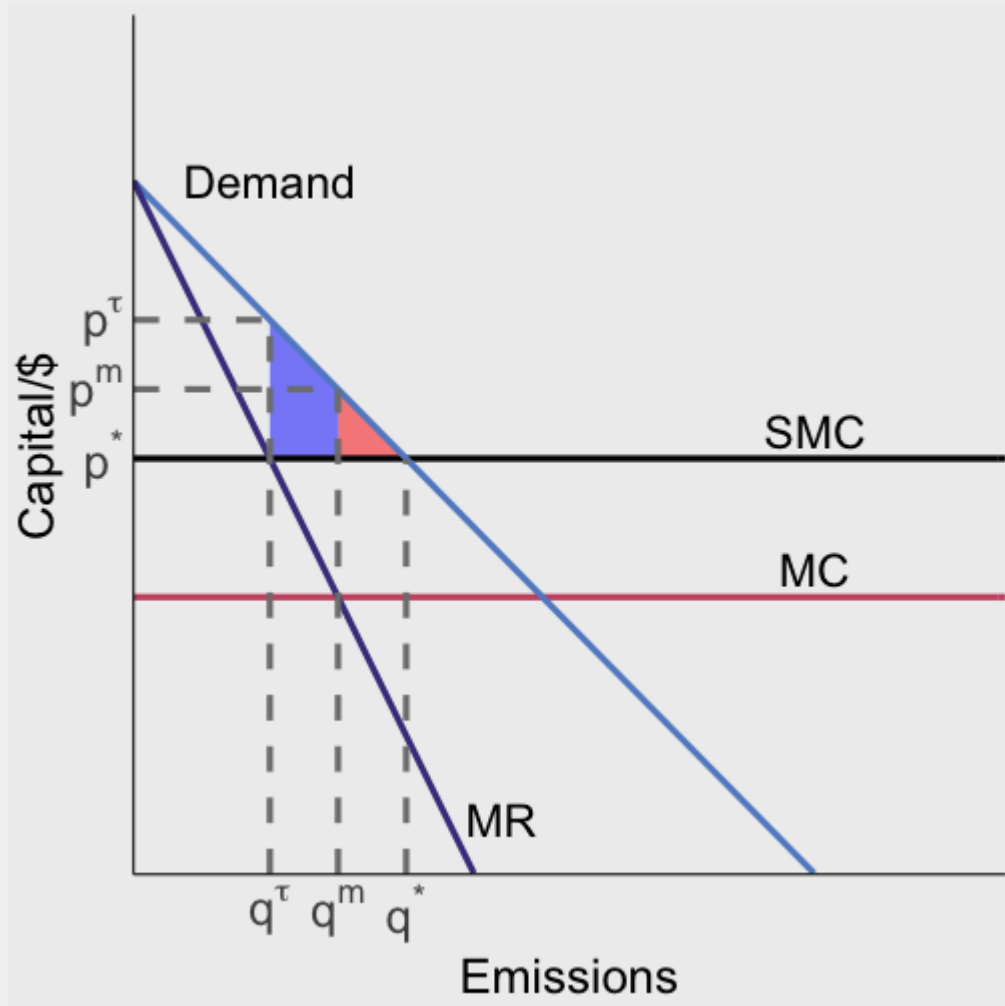


In the absence of regulation, the monopolist maximizes profit where  $MR = MC: (q^m, p^m)$

This results in deadweight loss equal to the **red** area

Now what happens if we set a Pigouvian tax equal to marginal damage?

# Monopoly

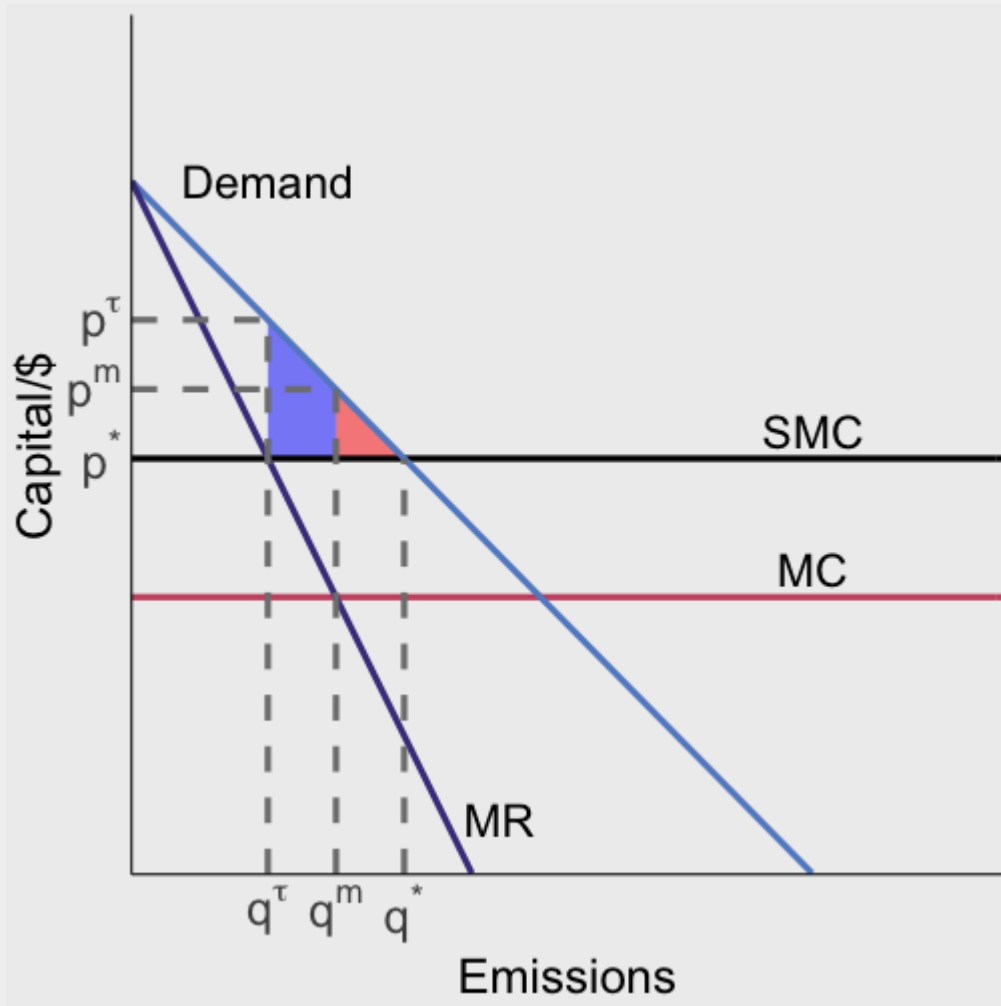


The Pigouvian tax restricts output even more, adding deadweight loss equal to the **blue** area on top of the deadweight loss in the **red** area

The tax actually made us worse off by the blue area!

Why?

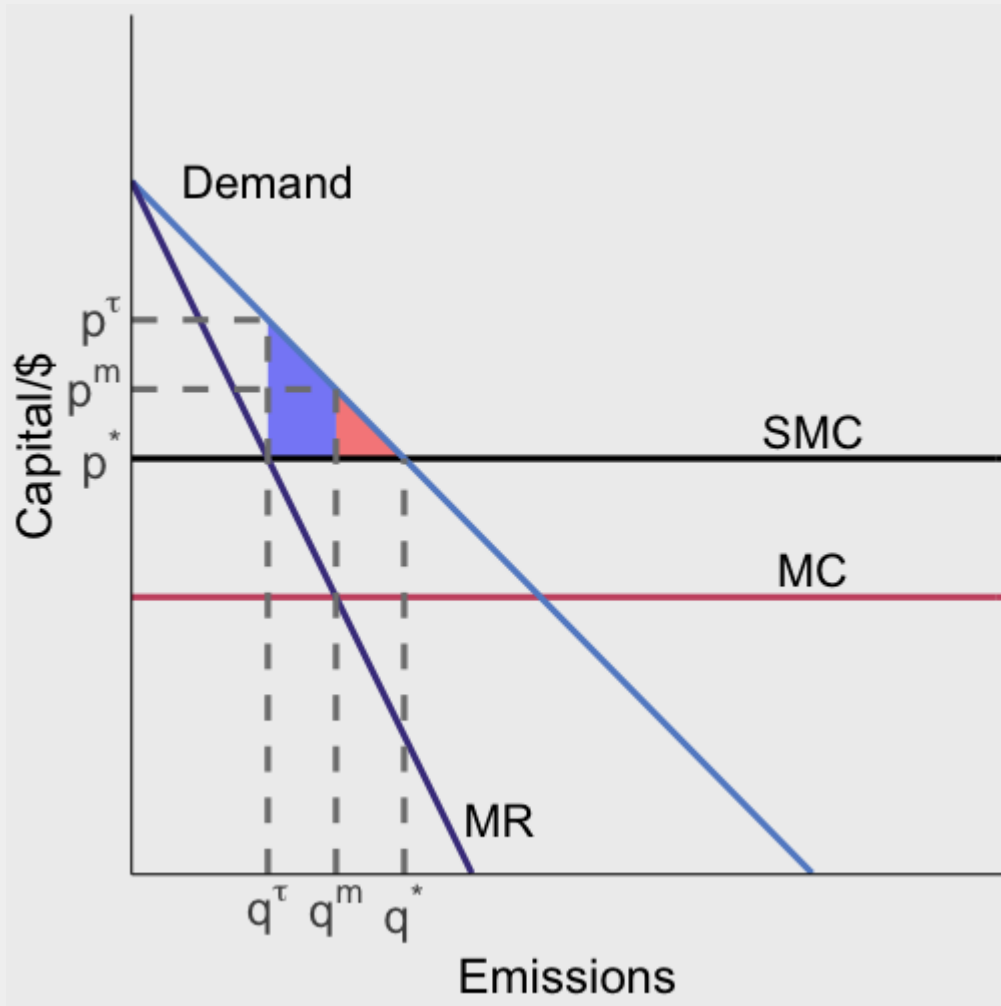
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We now have two distortions:

1. Market power
2. Pollution externality

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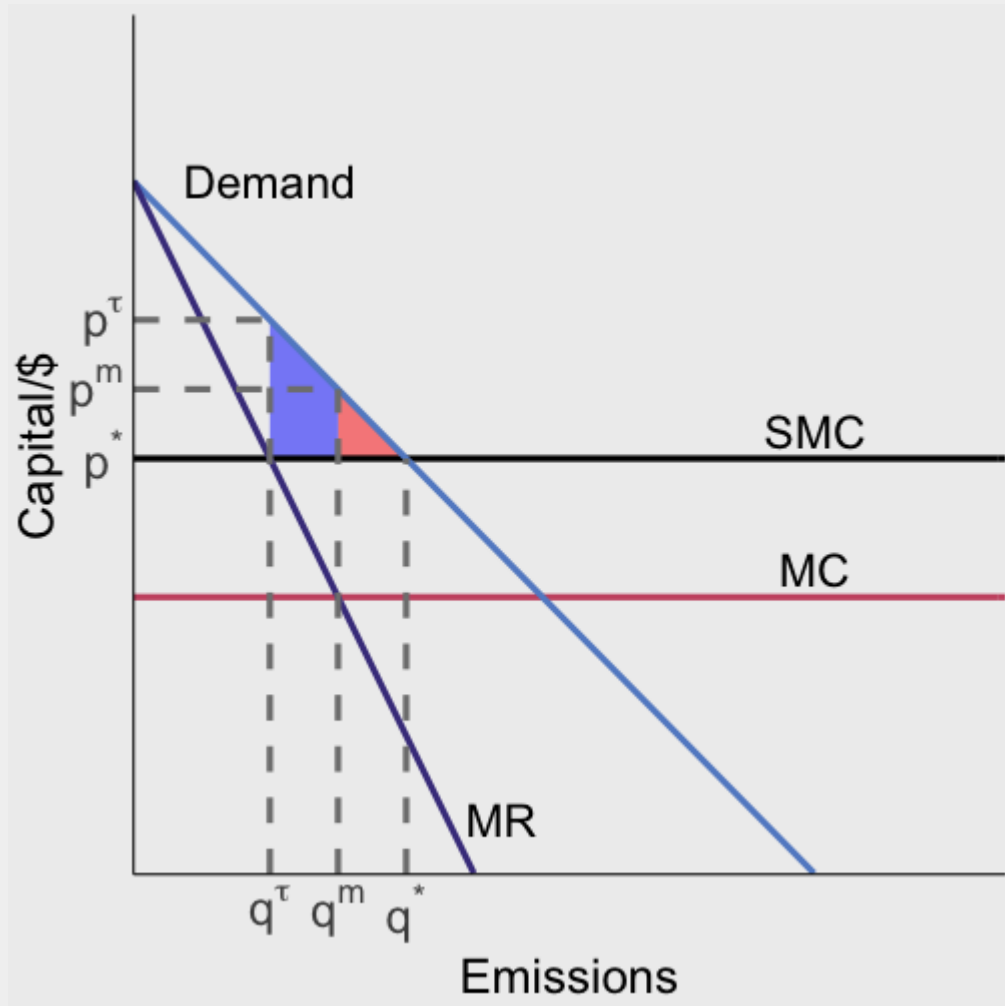


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With market power, the unregulated equilibrium quantity is **too low**

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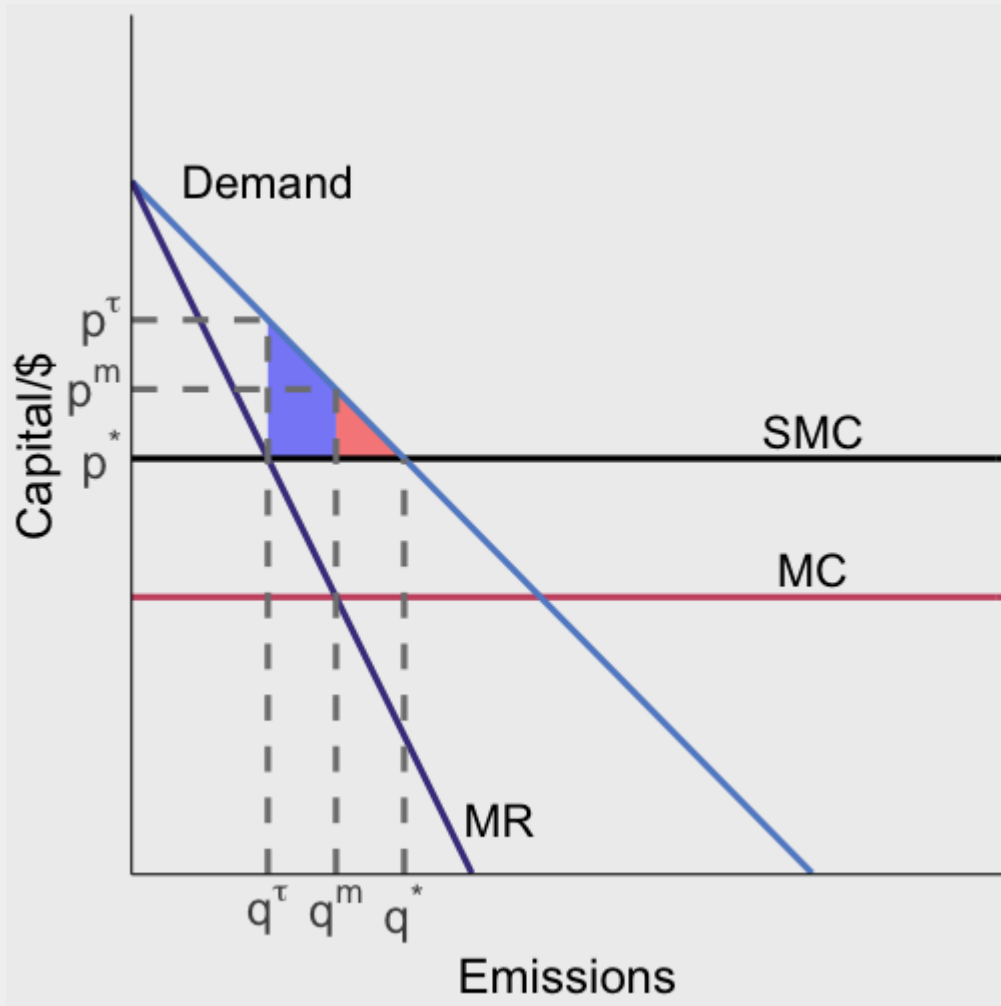
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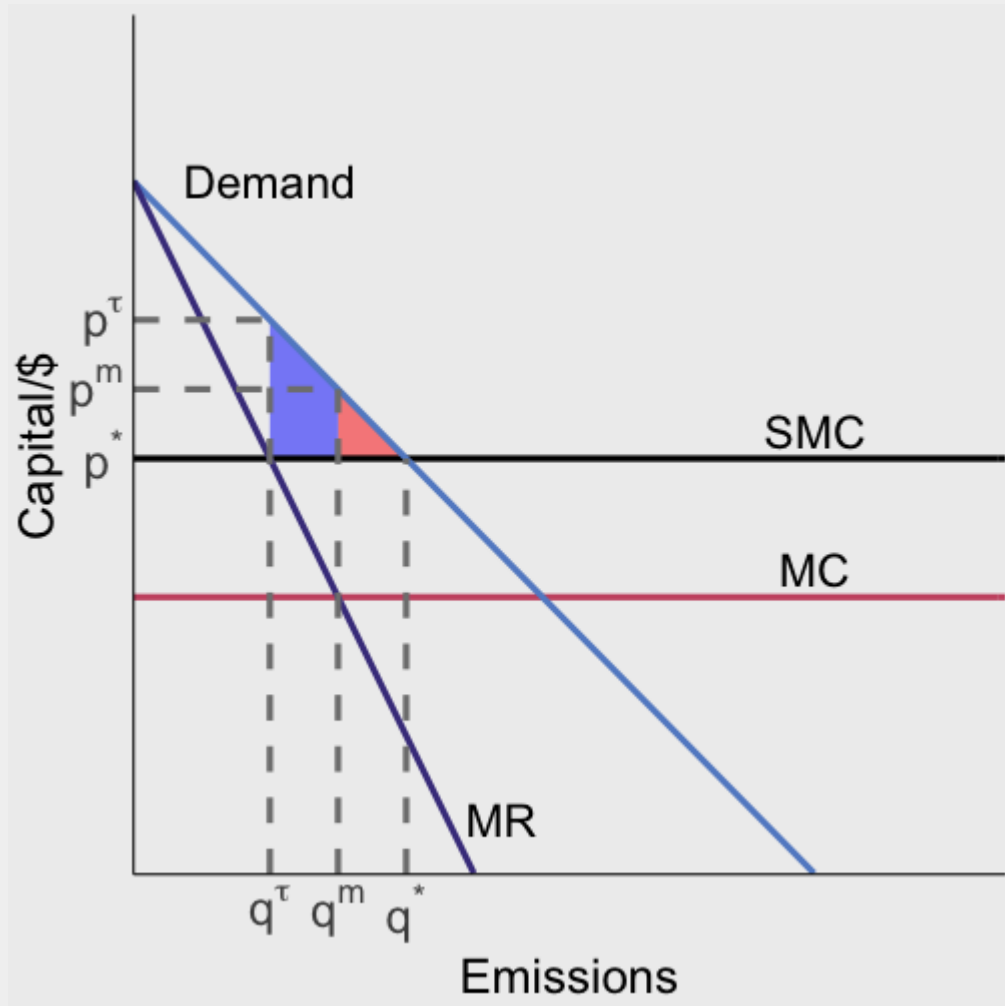
With a pollution externality, the unregulated equilibrium quantity is **too high**

# Monopoly



They have opposing forces on quantities, so the market failures offset each other (partially)

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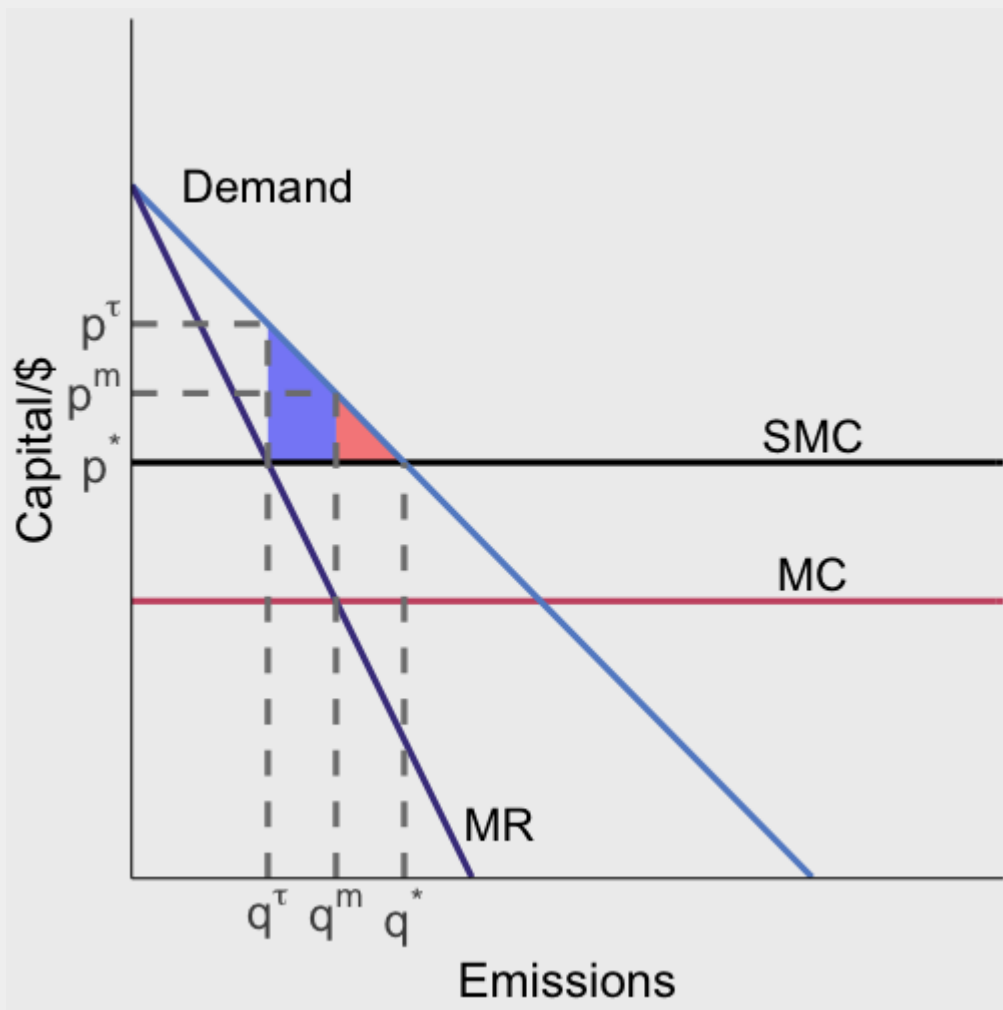


They have opposing forces on quantities, so the market failures offset each other (partially)

This means that if we fully correct the pollution externality, we no longer get the off-setting benefit and have the full welfare cost of market power

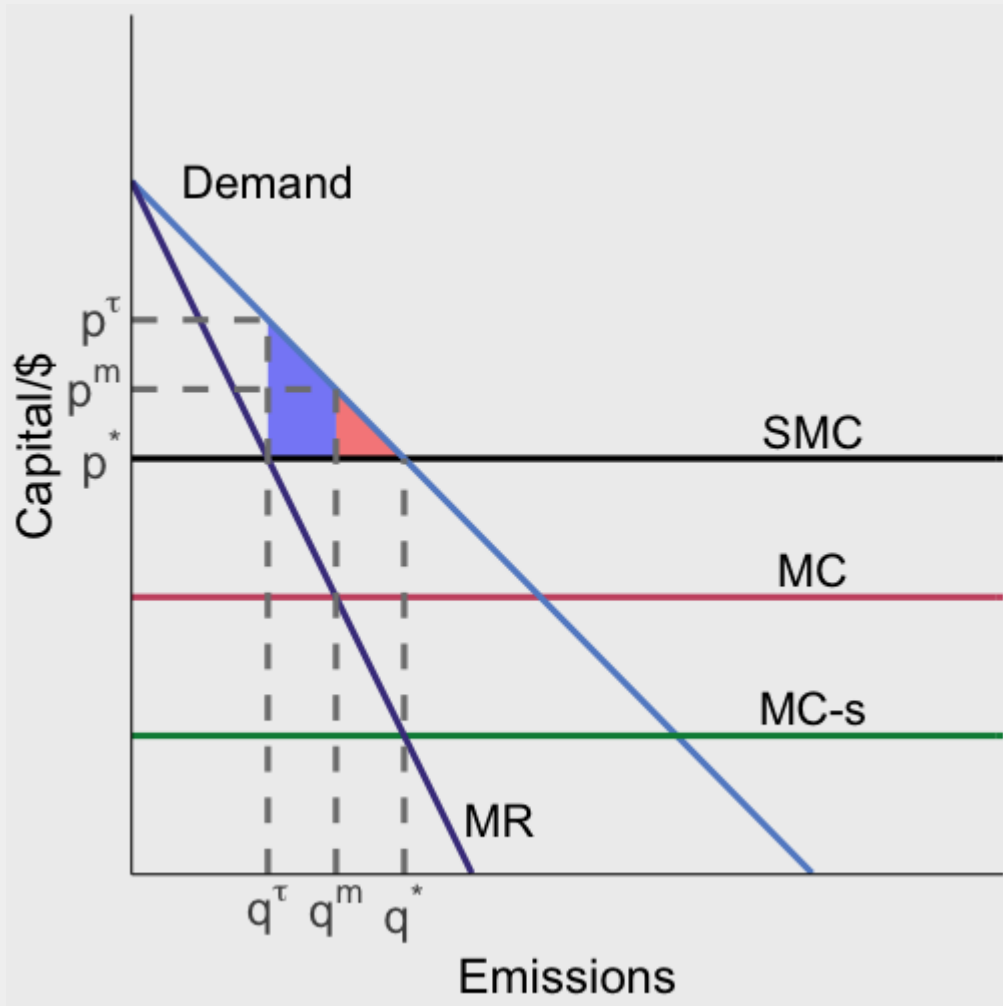


# Monopoly



What is the actual optimal thing to do here?

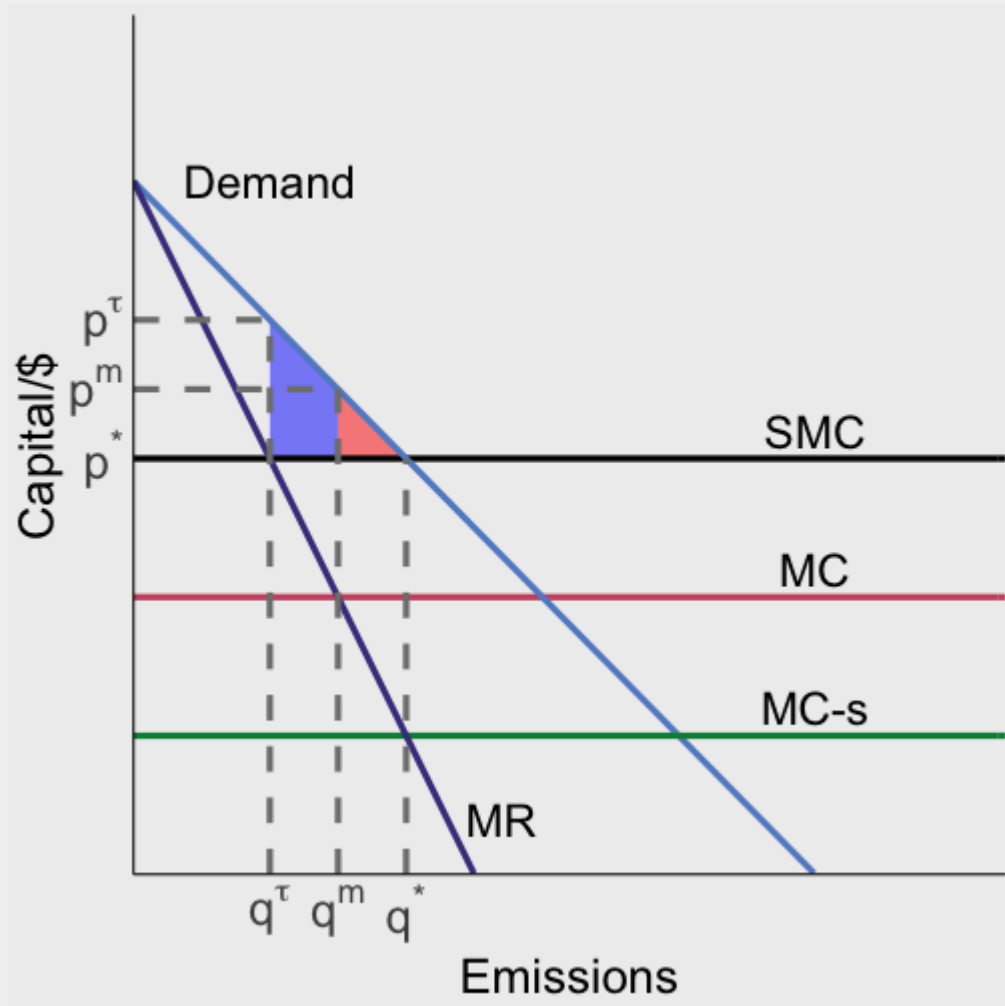
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In this example, the market power externality dominates the pollution externality: we need to increase output

# Monopoly

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With multiple market failures we don't necessarily want to **fully** correct for a single market failure

In this example we actually wanted to do the **opposite** of what you likely thought

You can always draw this example in a different way where you should tax output

You just need marginal damages to be sufficiently large relative to the market power effect on quantity



# Monopoly: more generally

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If we generalize this so that the emission and output decisions are separate, we still have the two opposing market failures<sup>1</sup>

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If we generalize this so that the emission and output decisions are separate, we still have the two opposing market failures<sup>1</sup>

What changes is we can no longer fix them both with just a pollution tax/subsidy

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What does that mean here?

We need:

1. Pollution tax
2. Output subsidy

The tax incentivizes abatement, the subsidy incentivizes production

# Output taxes

Sometimes emission taxes and abatement subsidies are difficult to administer because monitoring is hard



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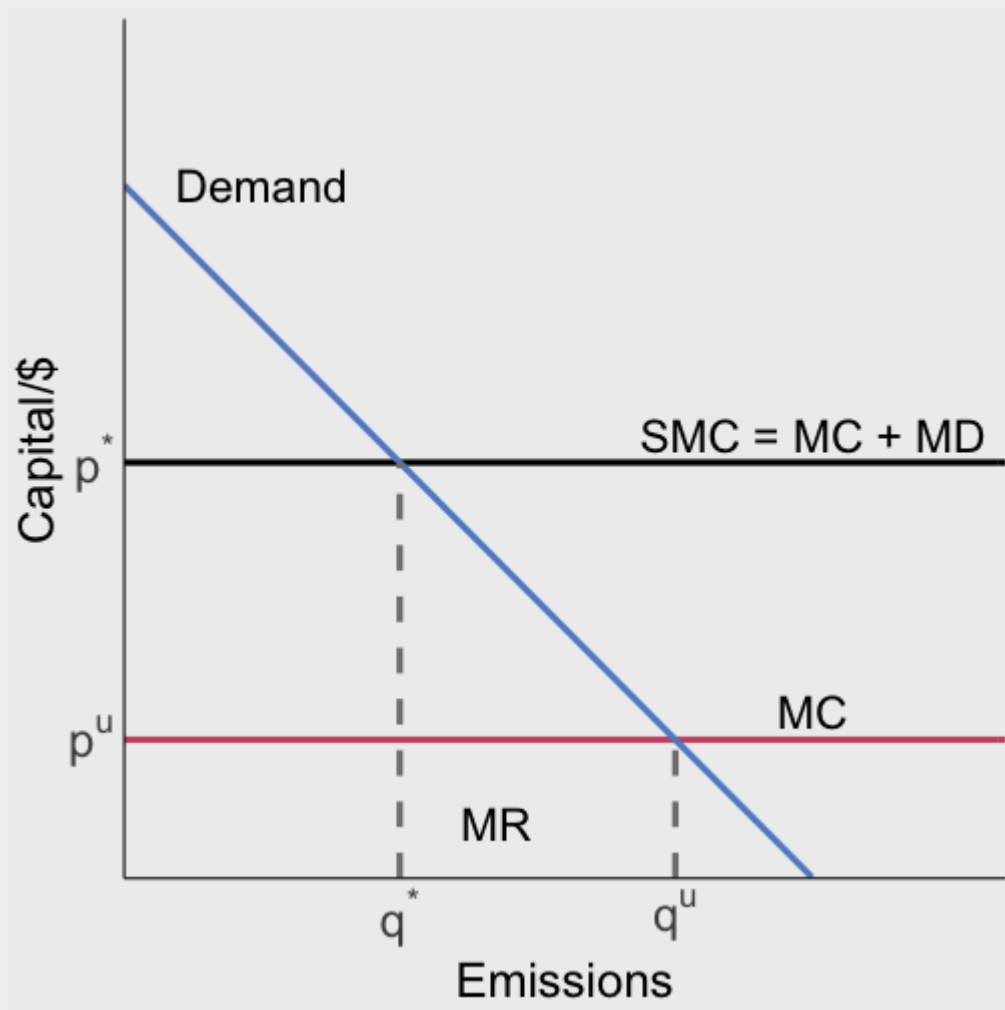
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Will this be efficient?

If so, what assumptions do we need about the production process?

# Output taxes



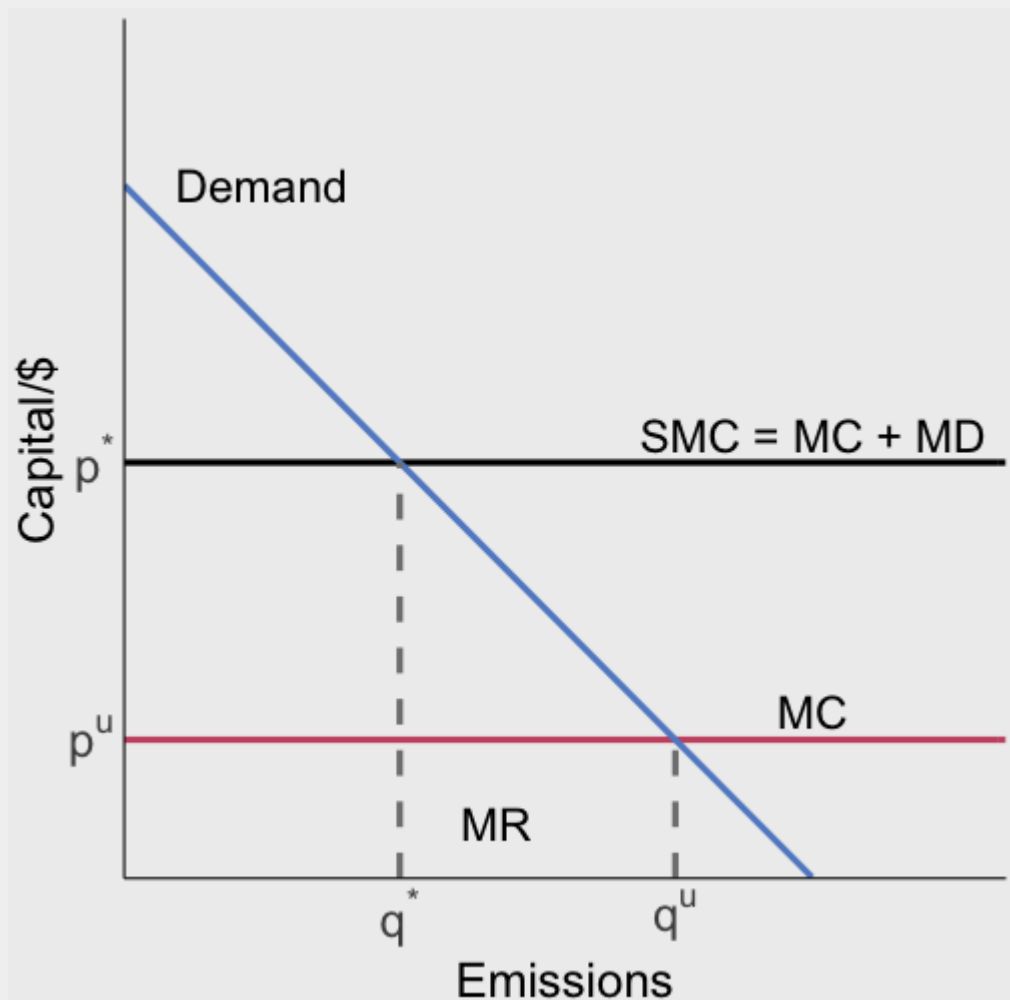
Assume emissions are proportional to output

And MD is constant

The firm chooses to produce/emit at  $q^u$  in the unregulated equilibrium

If we tax output equal to MD we can achieve the socially optimal allocation  $q^*$

# Output taxes



An output tax can be efficient, if we assume that emissions are proportional to output

Now let's break the tight link between output and emissions by writing down a slightly more complicated model where the firm chooses emissions and output separately

# Output taxes, part two

Here's our model:

- Cobb-Douglas production using labor and emissions as inputs:  $L^\alpha E^{1-\alpha}$
- The firm pays wages  $w$ , rental rate  $r$  to emissions (capital)
- The firm receives a price  $p$  per unit of output
- Emissions cause marginal damage  $d$



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What does an output tax  $\tau_o$  do versus a regular emission tax  $\tau_e$ ?

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The for a social optimum we want to equate the MR (left hand side) with the SMC (right hand side) for both inputs

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The output tax penalizes the use of clean labor despite it not causing any externalities at a marginal rate of:  $\tau_o L^{\alpha-1} E^{1-\alpha}$ , this is **not efficient**

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A tax of  $\tau_e = d$  can achieve the efficient allocation!

# Output taxes takeaways

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If emissions can be chosen separately from outcome by the firm, this is no longer true

In this case an output tax incorrectly taxes our clean inputs



# Intensity standards

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Intensity of ethanol in the fuel supply

# Intensity standards: RPS

## What is a Renewables Portfolio Standard (RPS)?

aka Renewable Energy/Electricity Standard (RES)

### Renewables Portfolio Standard

A requirement on retail electric suppliers...  
To supply a minimum percentage or amount of their retail load...  
With eligible sources of renewable energy

<i>Typically</i>	Backed with penalties of some form
<i>Often</i>	Accompanied by a tradable renewable energy certificate (REC) program to facilitate compliance
<i>Never</i>	Designed the same in any two states

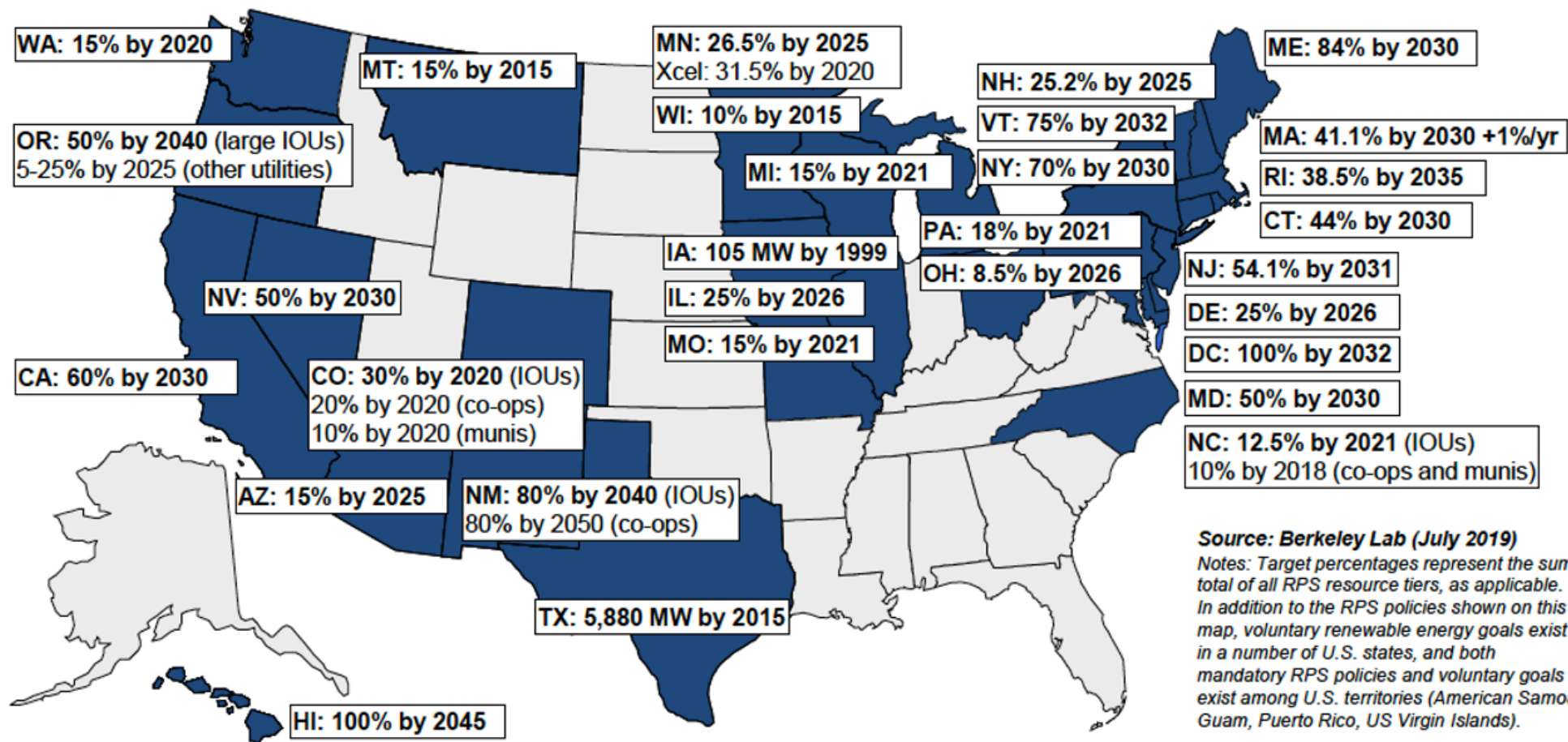
***This report covers U.S. state RPS policies. It does not cover:***

- ▣ Voluntary renewable electricity goals
- ▣ Broader clean energy requirements without a renewables-specific component (briefly discussed in a side-bar)
- ▣ RPS policies outside of the United States or in U.S. territories

# Intensity standards: RPS

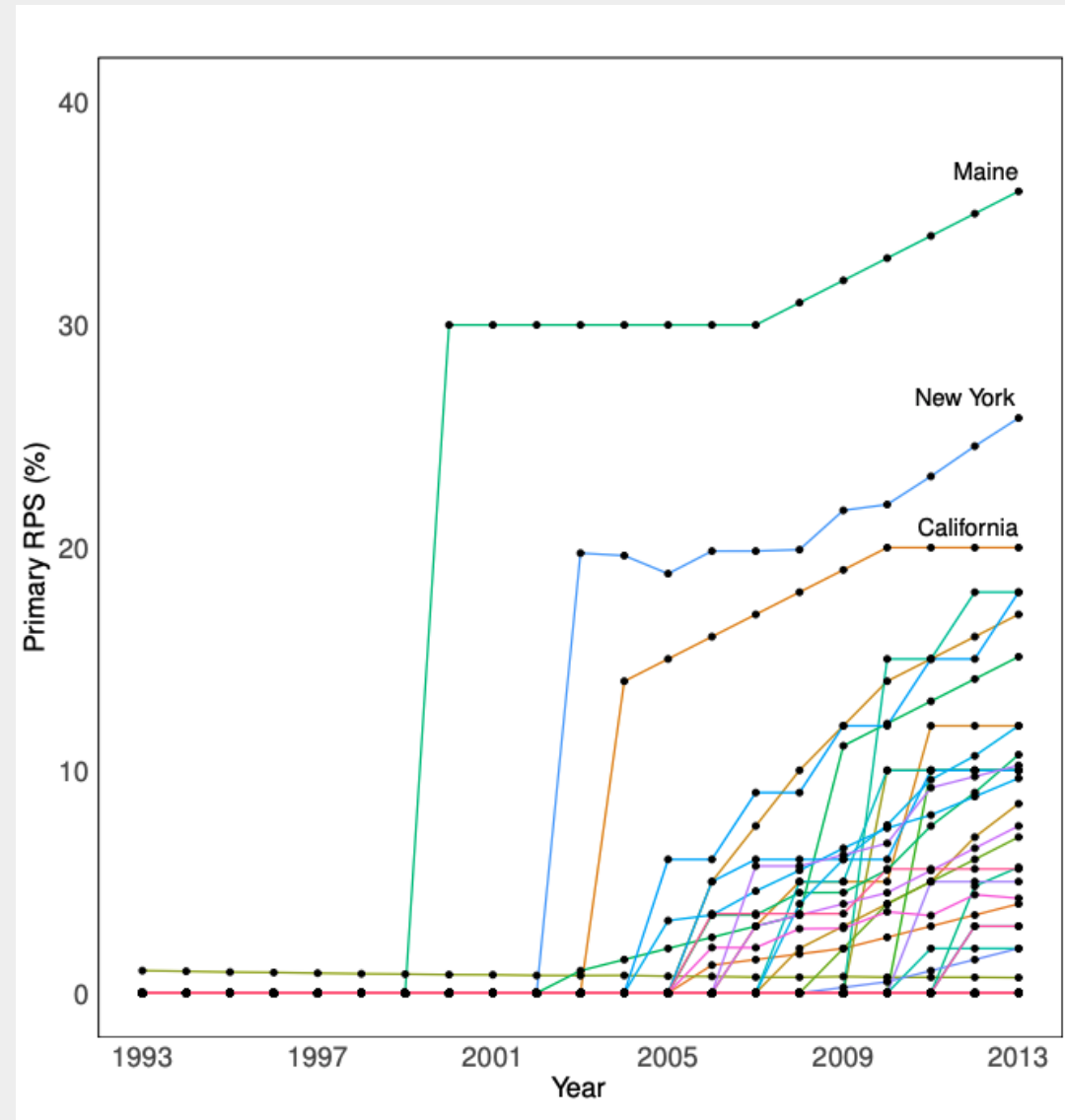
## RPS Policies Exist in 29 States and DC

Apply to 56% of Total U.S. Retail Electricity Sales



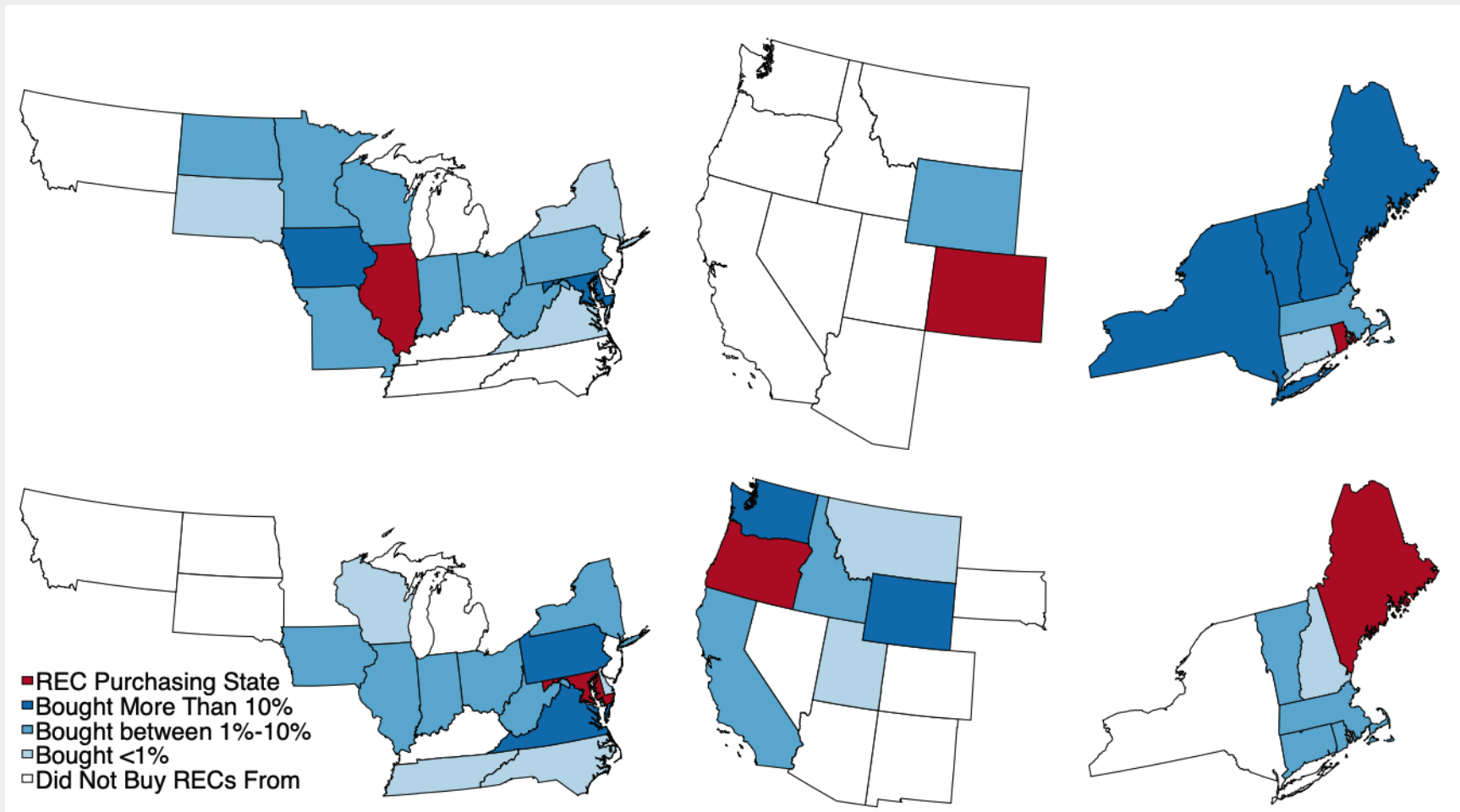


# Intensity standards: RPS



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RPSs combine intensity standards and tradable credit markets (Holt, 2014)



# Intensity standards: gas flaring

Flaring of natural gas at oil wells in North Dakota is regulated with an intensity standard

## **North Dakota Industrial Commission Order 24665 Policy/Guidance** **Version 041718**

### **Policy Goals:**

- 1) reduce the flared volume of gas
- 2) reduce the number of wells flaring
- 3) reduce the duration of flaring from wells

# Intensity standards: gas flaring

Mandates a minimum fraction of gas captured (max fraction of gas flared)

The Commission establishes the following gas capture goals:

74% October 1, 2014 through December 31, 2014

77% January 1, 2015 through March 31, 2016

80% April 1, 2016 through October 31, 2016

85% November 1, 2016 through October 31, 2018

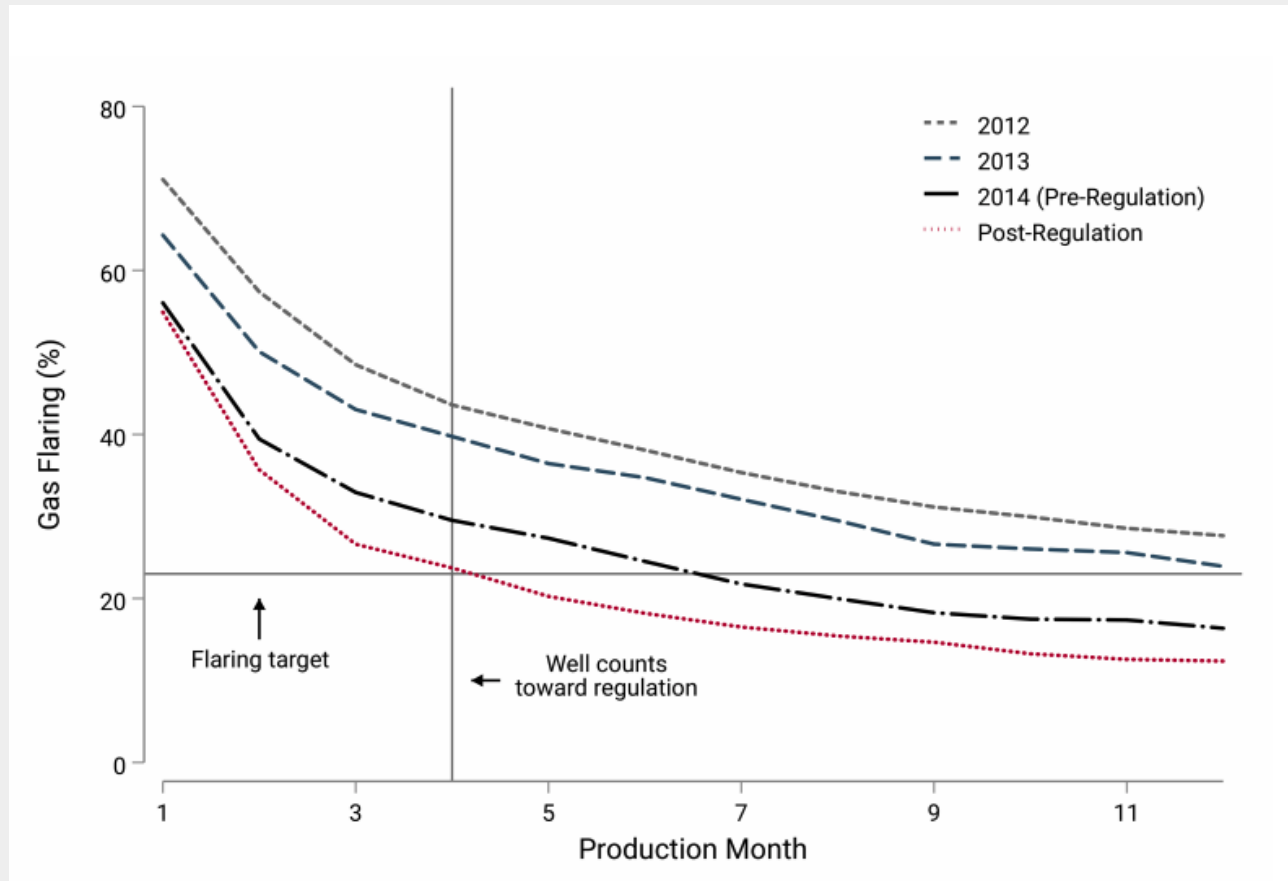
88% November 1, 2018 through October 31, 2020

91% beginning November 1, 2020

The gas capture percentage is calculated by summing monthly gas sold plus monthly gas used on lease plus monthly gas processed in a Commission approved beneficial manner, divided by the total monthly volume of associated gas produced.

# Intensity standards: gas flaring

The regulation pushed flaring rates down



# Intensity standards

Consider a case where we have a good with two types:

- a high type  $H$  that results in a high level of emissions
- a low type  $L$  that results in a low level of emissions

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The marginal damage from emissions is  $d$



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The cost function to produce each type of output is  $C_H(Q_H)$  and  $C_L(Q_L)$

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The marginal damage from emissions is  $d$

The cost function to produce each type of output is  $C_H(Q_H)$  and  $C_L(Q_L)$

The social benefit of consuming the goods is given by a social utility function  $U(Q_H, Q_L)$

# Intensity standards: social planner

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The social planner's problem is:

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Maximize the social utility of the good, minus the private and external costs

The first-order conditions tell us how social welfare is maximized:

$$\frac{\partial U(Q_H, Q_L)}{\partial Q_i} = \frac{\partial C_i(Q_i)}{\partial Q_i} + \tau\beta_i \quad i = L, H$$

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Now what if we try to address the pollution externality with an intensity standard: a cap on the emissions per unit of output?

# Intensity standards: social planner

An emission standard might look something like this:

$$\frac{\beta_H Q_H + \beta_L Q_L}{Q_H + Q_L} = \sigma$$

# Intensity standards: social planner

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The left hand side is emissions (top) per unit of total output (bottom)

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For the standard to make any sense it must be:  $\beta_L \leq \sigma \leq \beta_H$ , otherwise it doesn't do anything  $\sigma > \beta_H$  or its unattainable  $\sigma < \beta_L$

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The firm's problem is:

$$\max_{Q_H, Q_L} \pi(Q_H, Q_L) = p_H Q_H + p_L Q_L - C_H(Q_H) - C_L(Q_L)$$

$$\text{subject to: } \frac{\beta_H Q_H + \beta_L Q_L}{Q_H + Q_L} = \sigma$$



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Next, the first-order condition for a maximum

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The first-order condition is:

$$p_H \frac{\sigma - \beta_L}{\beta_H - \sigma} + p_L = \frac{\sigma - \beta_L}{\beta_H - \sigma} MC_H + MC_L$$

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To get to the final part of the intuition let:

$$\lambda \equiv (p_i - MC_i)/(\beta_i - \sigma)$$

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This lets us write the  $Q_L$  FOC as:

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and it turns out if we instead framed the problem instead of  $Q_H$  we'd get the same FOC:

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What are these FOCs telling us about the firm's problem:

$$p_i = MC_i(Q_i) + \lambda(\beta_i - \sigma) \quad i = L, H$$

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The firm equates marginal revenue  $p_i$  and total marginal cost for each type  $i$



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Is the intensity standard efficient?

# Intensity standards: efficiency

Social welfare is maximized when:

$$\frac{\partial U(Q_H, Q_L)}{\partial Q_i} = \frac{\partial C_i(Q_i)}{\partial Q_i} + \tau\beta_i \quad i = L, H$$

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The firm maximizes profit under the intensity standard at:

$$p_i = MC_i(Q_i) + \lambda(\beta_i - \sigma) \quad i = L, H$$

$$\frac{\partial U(Q_H, Q_L)}{\partial Q_i} = p_i \text{ from household utility maximization}^1$$

<sup>1</sup>Prices reflect the marginal value of consumption.

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Social efficiency:

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Firm choice:

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Why?

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The intensity standard cannot reach the efficient allocation because it is subsidizing a good that produces a negative externality<sup>1</sup>

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The intensity standard cannot reach the efficient allocation because it is subsidizing a good that produces a negative externality<sup>1</sup>

We call policies that can't achieve the social optimum **second-best**

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# Intensity standards: graphical

Now lets look at intensity standards graphically

A few things you'll need to know:

1. **Iso-profit curves:** ovals that tell us the combinations of  $Q_H, Q_L$  that achieve the same profit
2. **Iso-welfare curves:** ovals that tell us the combinations of  $Q_H, Q_L$  that achieve the same social welfare

# Intensity standards: graphical

These are like indifference curves for consumers, but are ovals instead of convex curves

Why ovals?

# Intensity standards: graphical

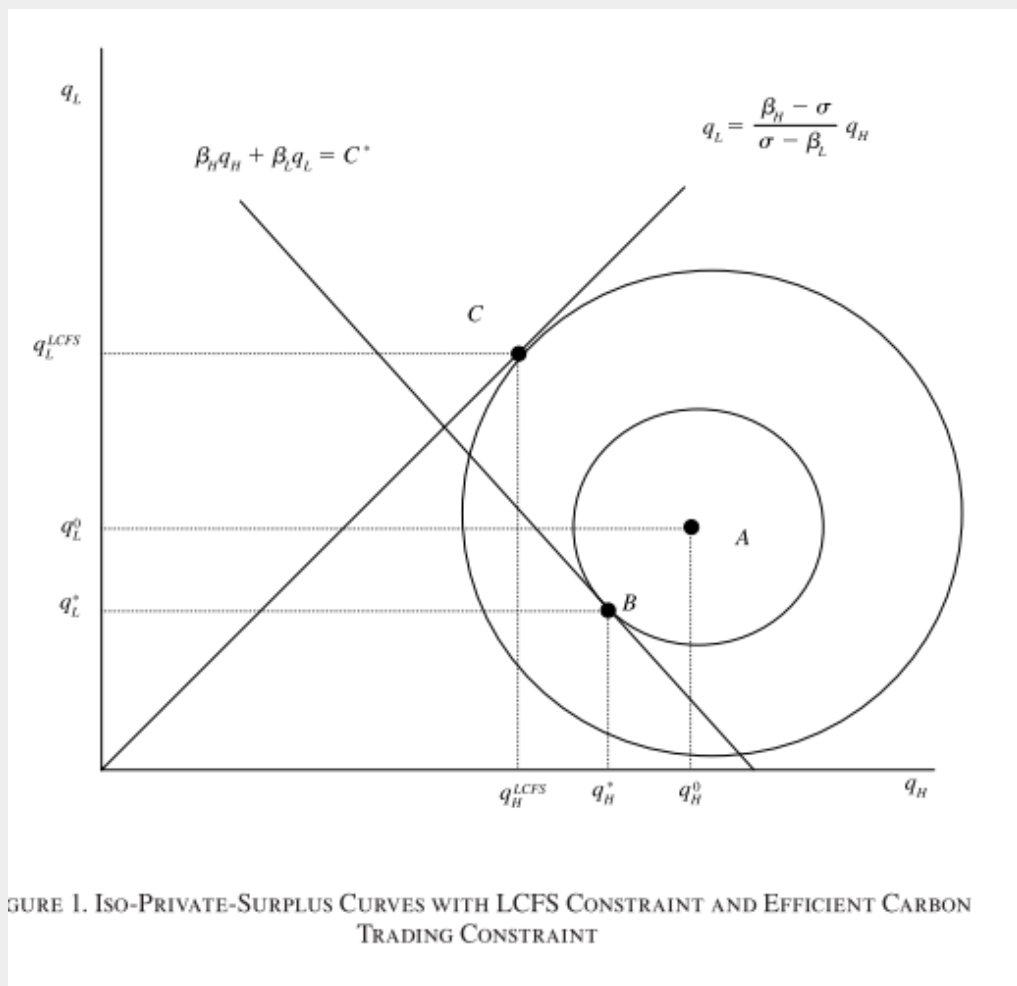
These are like indifference curves for consumers, but are ovals instead of convex curves

Why ovals?

Producing too much can decrease profit and/or welfare so eventually profit starts falling

With consumption, more is always better so increasing consumption always moves onto higher ICs

# Intensity standards: what happens?



The circles are iso-private welfare (iso-profit) curves

A is where profit is maximized for the firm

The line  $Q_L = \frac{\beta_H - \sigma}{\sigma - \beta_L} Q_H$  tells us which combos of  $Q_L, Q_H$  satisfy the intensity standard

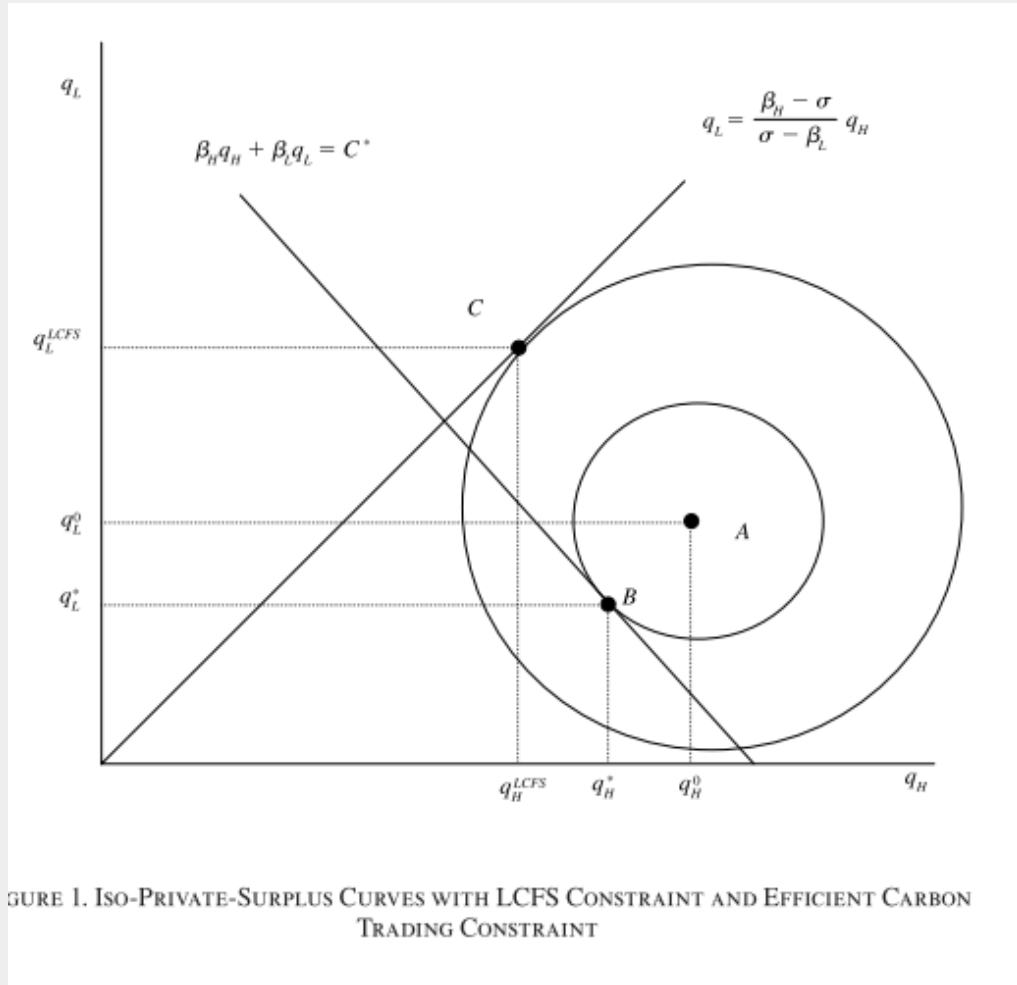
Holland, Hughes, and Knittel (2010)

# Intensity standards: what happens?

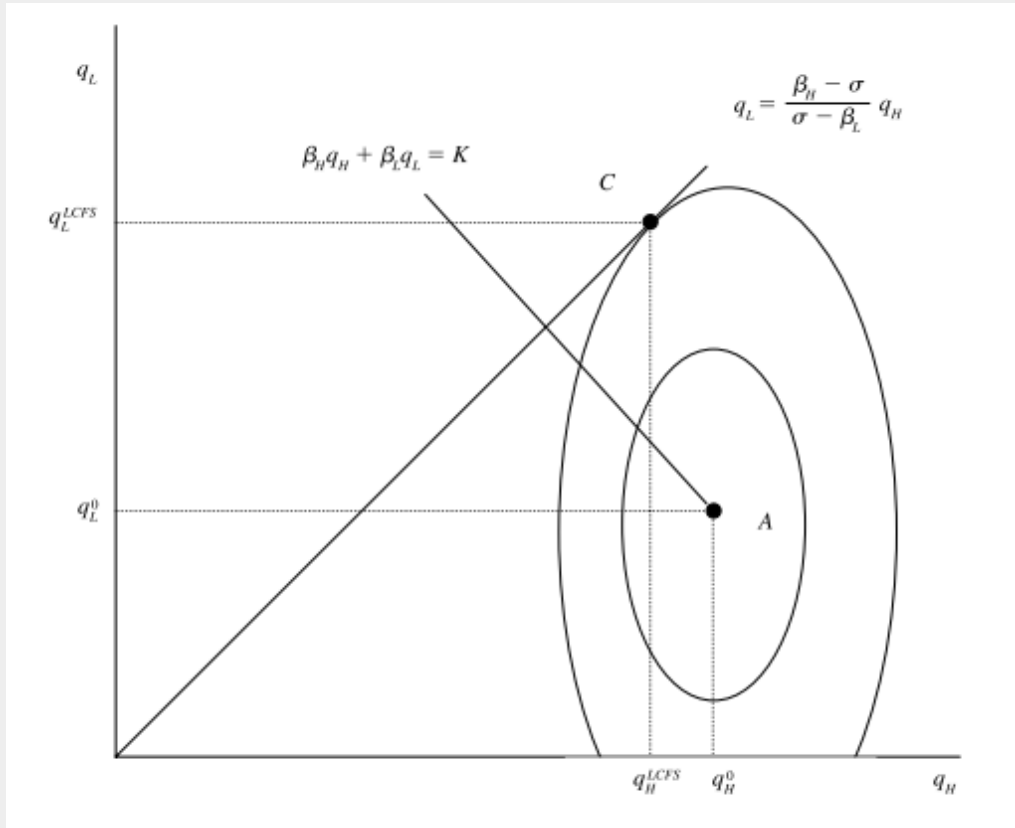
The intensity standard forces the firm to produce on the line

The highest iso-profit curve it can achieve is at point C

This is more  $Q_L$  and less  $Q_H$  than is optimal, consistent with the subsidy/tax combination implicit in the policy



# Intensity standards: perverse incentives

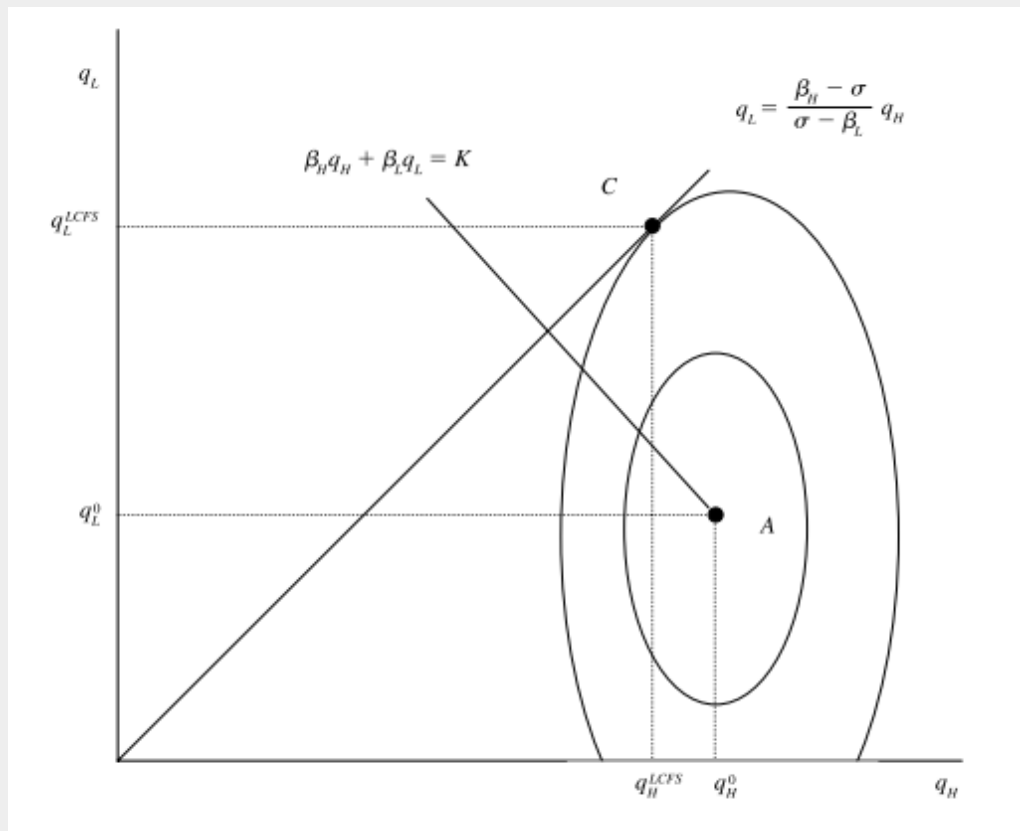


Intensity standards can actually backfire and increase emissions

How?



# Intensity standards: perverse incentives

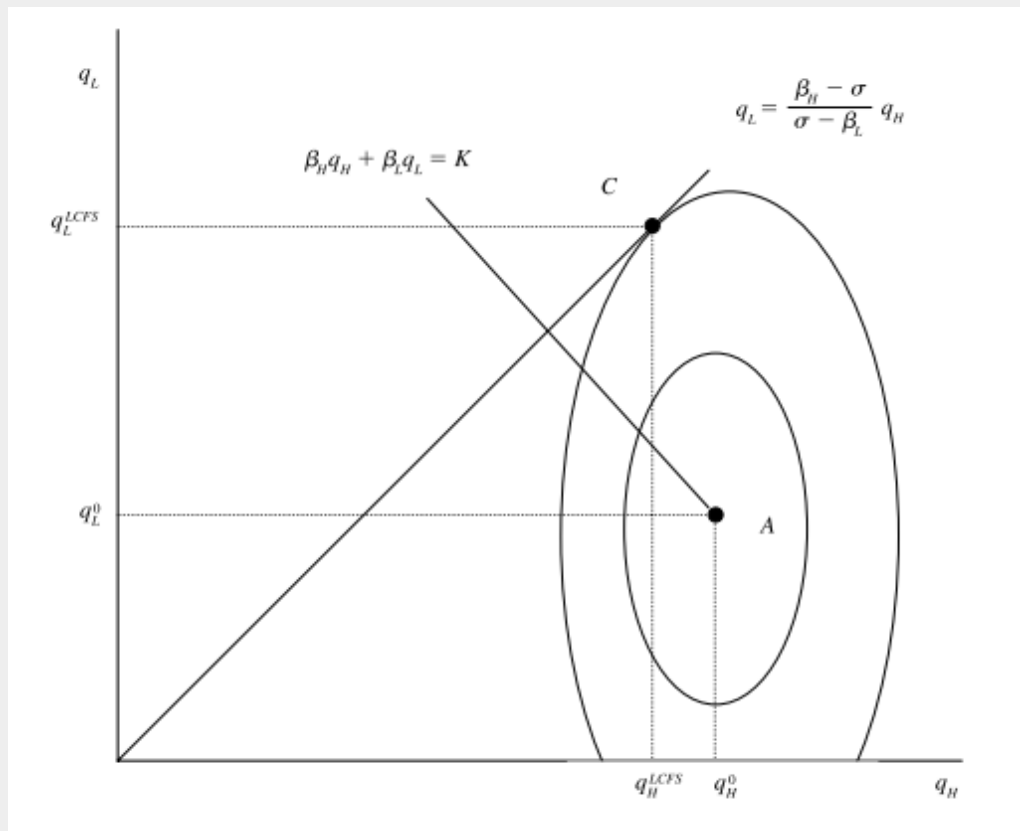


$\beta_H Q_H + \beta_L Q_L = K$  is the line showing all combinations of  $Q_L, Q_H$  that generate  $K$  units of emissions

$K$  crosses through point  $A$  which is the unregulated profit-maximizing choice by the firm

Anything to the top right of the line is **more emissions**

# Intensity standards: perverse incentives



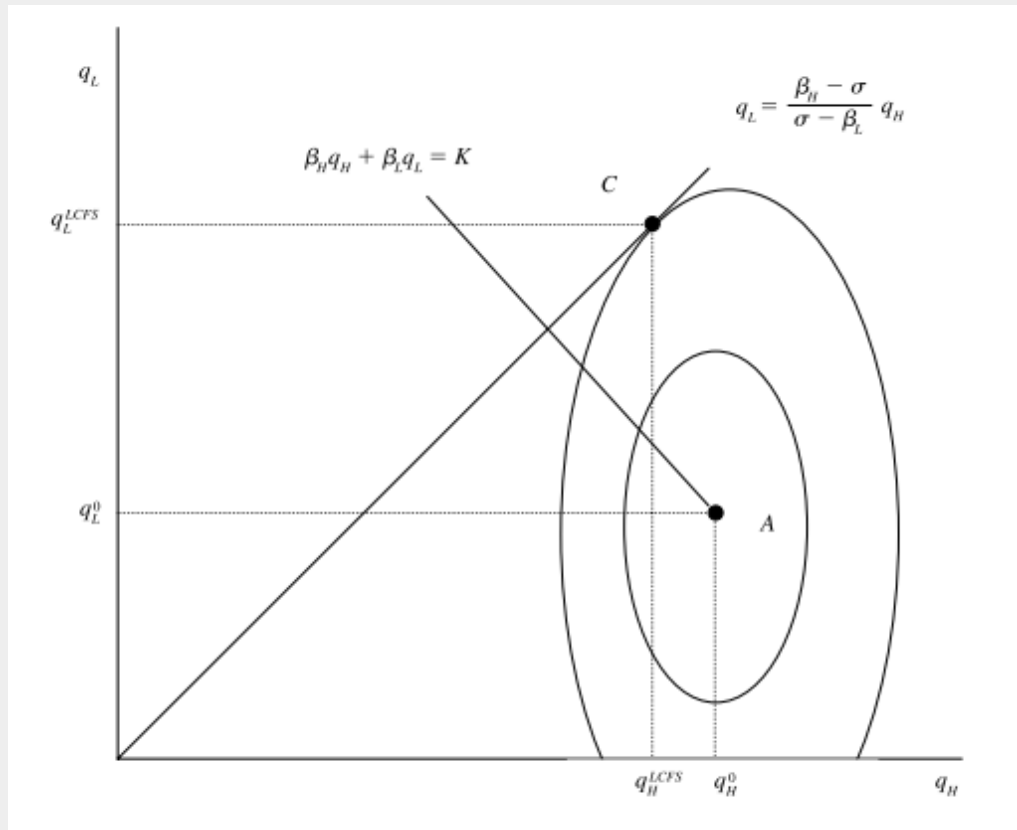
The regulation induces the firm to move to point  $C$

This is slightly less  $Q_H$ , but **a lot** more  $Q_L$

The increase in emissions from  $Q_L$  is more than the decrease from the lowering of  $Q_H$

Overall emissions went up!

# Intensity standards: perverse incentives



This perverse outcome was possible because production of the  $L$  type was very elastic while the  $H$  type was inelastic

# Intensity standards: second-best

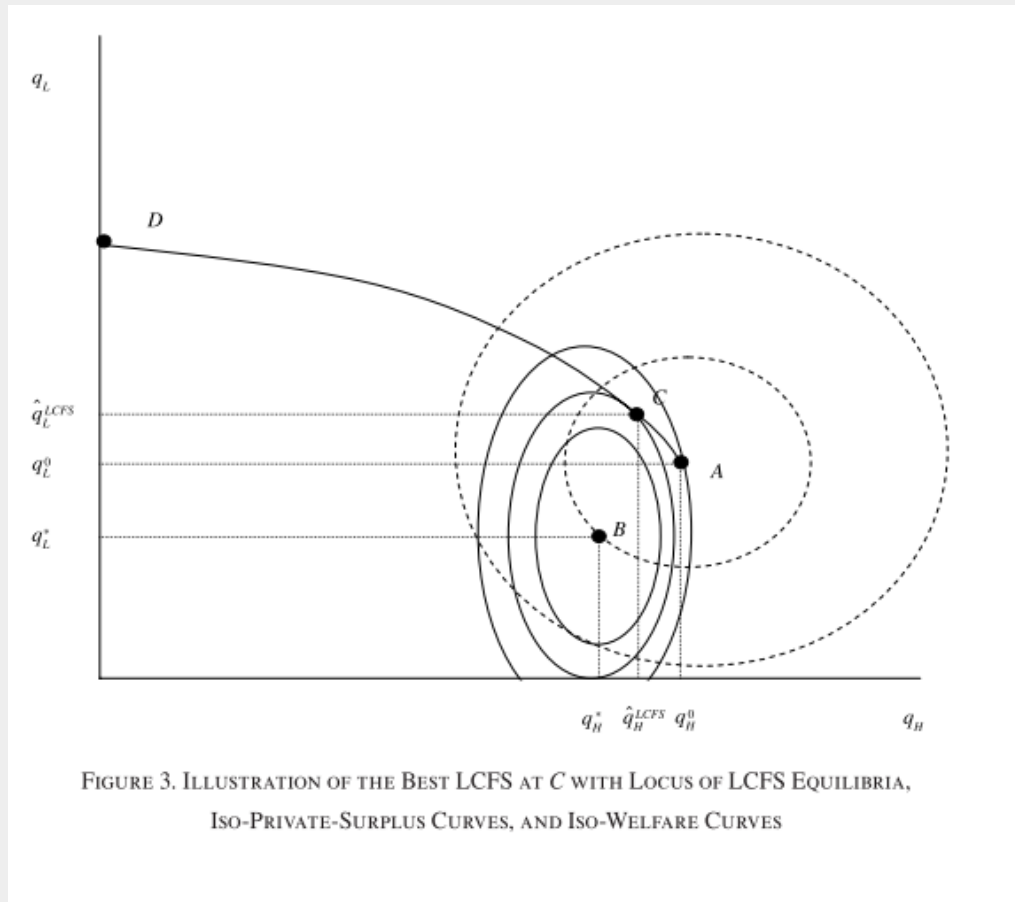
What is the best intensity standard?

The dashed ovals are the iso-profit curves

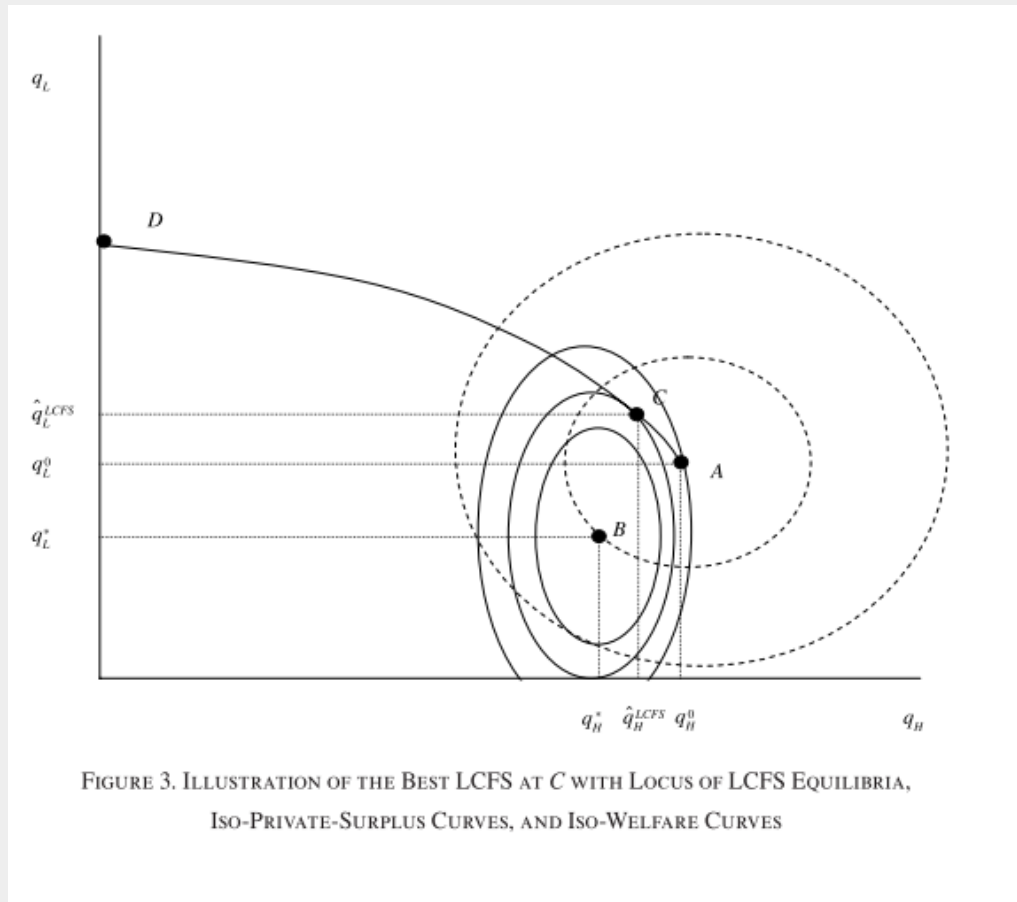
The solid ovals are the iso-welfare curves

Welfare is maximized at point B

Profit is maximized at point A



# Intensity standards: second-best



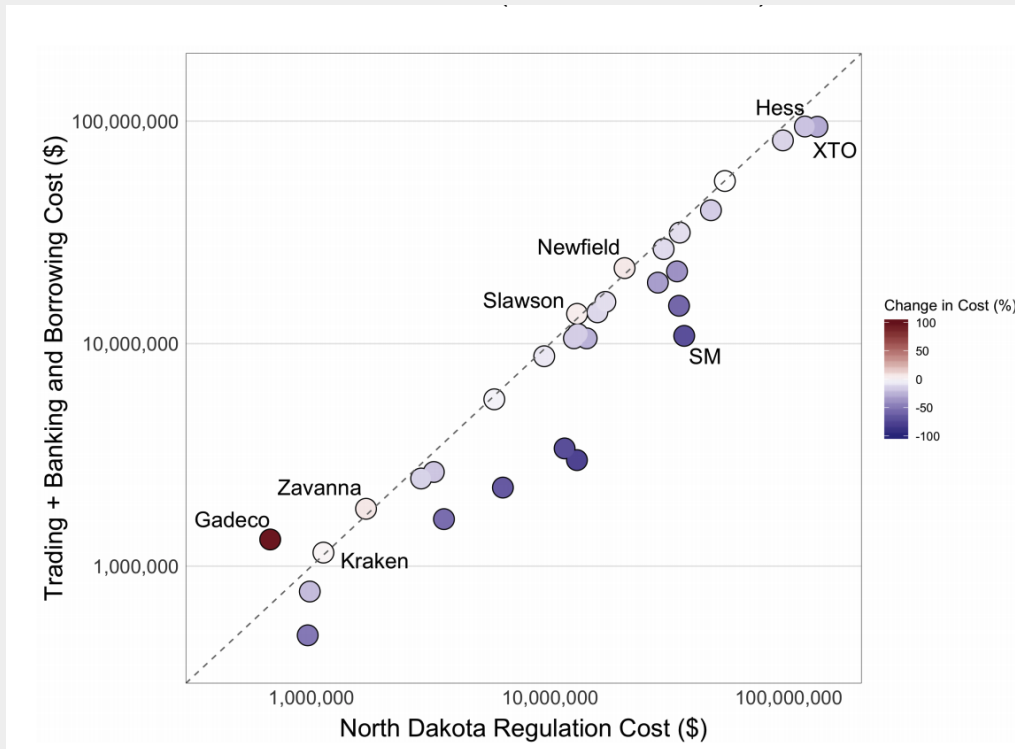
The solid line shows the firm's choices of  $Q_L$ ,  $Q_H$  as we increase the intensity standard  $\sigma$

Increasing  $\sigma$  pivots the intensity standard counter-clockwise:

$$Q_L = \frac{\beta_H - \sigma}{\sigma - \beta_L} Q_H$$

The optimal intensity standard is the one that lets us get on the highest iso-welfare curve, which is at point  $C$

# Intensity standards: gas flaring



Moving from a flaring intensity standard to tradable permits or a tax generates massive welfare gains!

A tax that captures the same quantity of gas would have >40% lower cost than the actual intensity standard