

# Lecture 5

## Environmental policy with pre-existing distortions

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AEM 7510

# Roadmap

So far we have looked at single sector economies with:

- Pollution distortions
- Competitive markets
- Market power distortions

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- Pollution distortions
- Competitive markets
- Market power distortions

Now we will learn about multi-sector economies

How does environmental policy spillover into these other sectors?

How does environmental policy interact with revenue-raising taxes (e.g. income taxes)?

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- There is a representative household

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This allows us to treat individual and aggregate behavior the same

1: The underlying critical assumption is that utility and profit functions take what's called a Gorman form.

# Environmental policy with leisure

Define the following:

- $X$  is consumption of the polluting good
- $Z$  is consumption of the *numeraire* good (i.e. the relative good)
- $N$  is the hours of leisure time
- $E$  is aggregate emissions

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where  $U_{XX}, U_{NN} < 0$  and  $U_{XX}U_{NN} - U_{NX}^2 > 0$  and the person is endowed with some amount of time  $T$  to allocate between work and leisure

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Household income is then:  $w \cdot (T - N)$

We can now write the households utility maximization problem as:

$$\max_{X, N, Z} U(X, Z, N, E) = U(X, N) + Z - D(E)$$

$$\text{subject to: } w \cdot (T - N) = Z + pX$$

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with FOCs:

$$U_X = p \quad U_N = w$$

which implicitly define the demand function for consumption  $X(p, w)$  and the demand function for leisure  $N(p, w)$

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We have two equations and two unknowns so we can solve to get:

$$\frac{\partial N}{\partial p} = \frac{-U_{XN}}{U_{XX}U_{NN} - U_{XN}^2} \quad \frac{\partial X}{\partial p} = \frac{U_{NN}}{U_{XX}U_{NN} - U_{XN}^2}$$

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If  $X$  and  $N$  are substitutes,  $-U_{XN} > 0$ , and leisure increases in the price of the consumption good

If they are complements,  $-U_{XN} < 0$ , and leisure decreases in the price of the consumption good

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The firm side of the economy will be the same as before: it produces  $X$  and emits  $E$  and for simplicity we will focus on the specific case:

$$\Pi = pX - C(X) \text{ where } E = \delta X$$

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We will also assume:

- $\delta = 1$  so we can use  $E$  and  $X$  interchangeably
- $C'(X) > 0, C''(X) \geq 0$
- The polluting industry's demand for labor is small relative to the entire economy, i.e. wages are effectively fixed for the household

# Environmental policy with leisure

Now lets solve for the social optimum:

$$\max_X W = \underbrace{U(X, N) + w \cdot (T - N) - pX - D(X)}_{\text{Consumer Utility}} + \underbrace{pX - C(X)}_{\text{Firm profit}}$$

To focus on interactions with non-regulated industries, we assume the regulator cannot determine the allocation of leisure and labor

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The consumer chooses  $N$  according to the FOC  $U_N(X^*, N) = w$  and then  $Z$  given the budget constraint  $Z = w(T - N) - pX^*$

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One way you can think about this is as if the regulator imposes a quantity standard  $X^*$  and then a market price  $p^*$  arises which affects leisure demand

# Environmental policy with leisure

The FOC for the optimum is:

$$U_X - D'(X) - C'(X) + [U_N - w] \frac{\partial N}{\partial X} = 0$$

where the last term captures the households **indirect** leisure response to the regulator's policy choice

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Given household utility maximization  $U_N - w = 0$  and the condition is then:

$$U_X - C'(X) = D'(X)$$

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Given household utility maximization  $U_N - w = 0$  and the condition is then:

$$U_X - C'(X) = D'(X)$$

Marginal abatement cost ( $U_X - C'(X)$ ) equals marginal damage ( $D'(X)$ ) !

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It needs to finance a budget of size  $G$

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Now suppose the government needs to raise revenue with a labor income tax  $m$  in order to finance government services

It needs to finance a budget of size  $G$

The consumer's utility maximization problem is:

$$\max_{X,Z,N} U = u(X, N) + Z - D(E)$$

$$\text{subject to } (1 - m)w(T - N) = Z + pX$$

Where the budget is scaled down by  $(1 - m)$  reflecting the income tax

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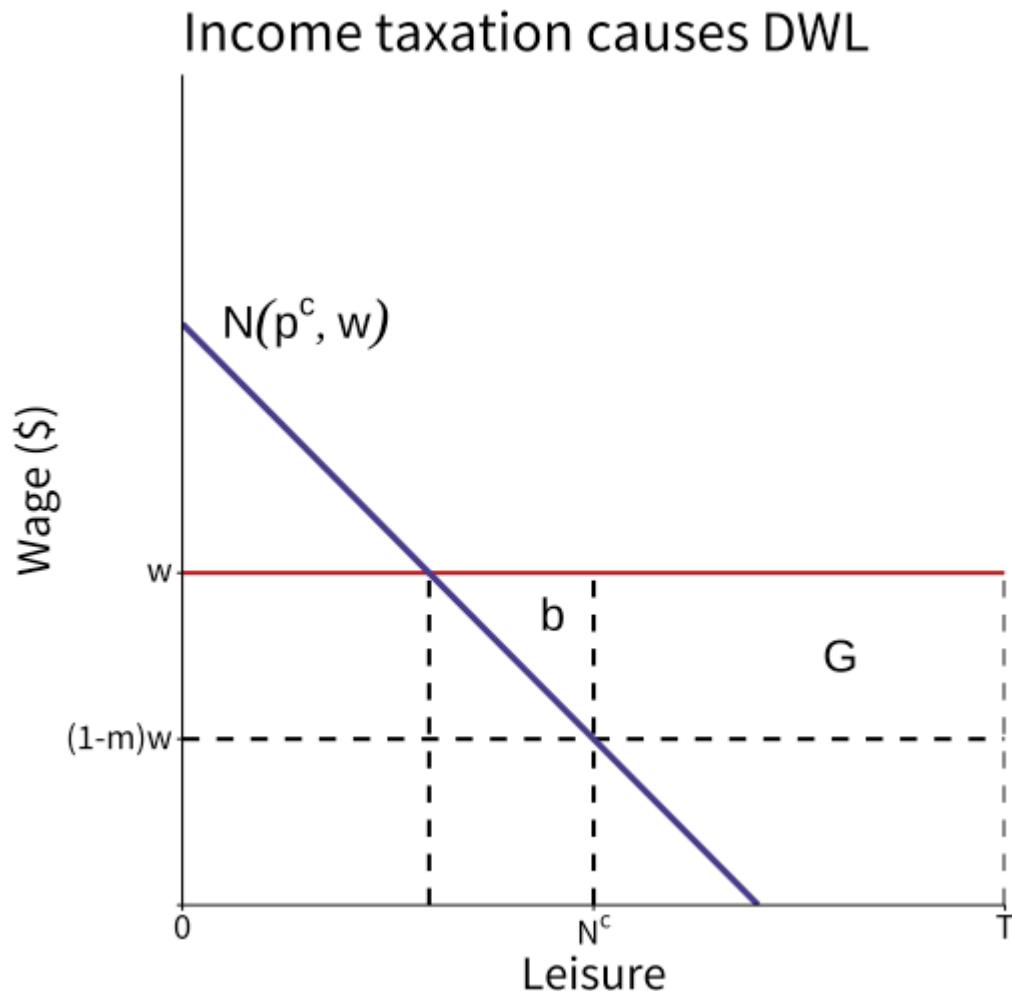
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The tax  $m$  makes the consumer act as if there is a subsidy  $mw$  on leisure

# Environmental policy with labor market distortions



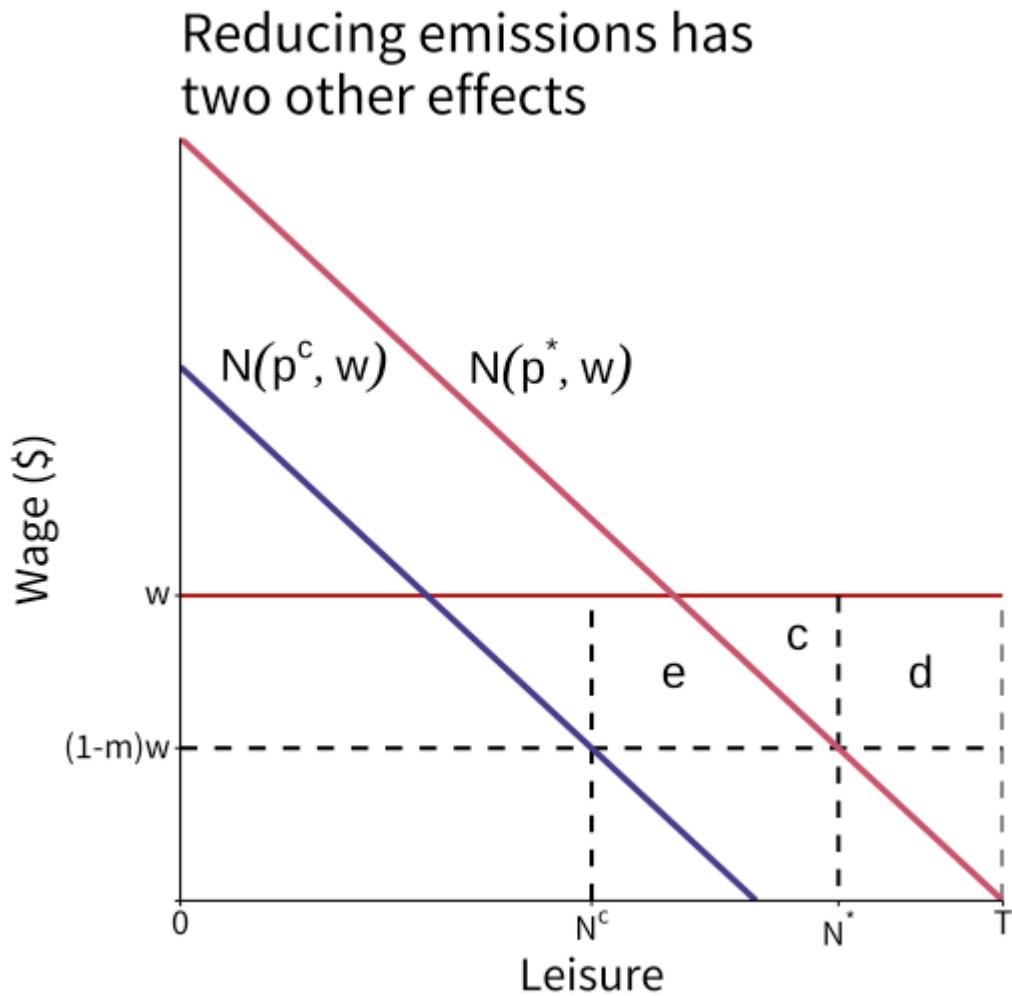
$w$  is the perfectly elastic demand for labor

$N^c$  is how much leisure the consumer chooses, since  $(1 - m)w < w$  this is too much and induces DWL equal to  $b$

This is called **excess burden**

The tax raises revenues equal to  $G$ :  
 $m w \times (T - N^c)$

# Environmental policy with labor market distortions



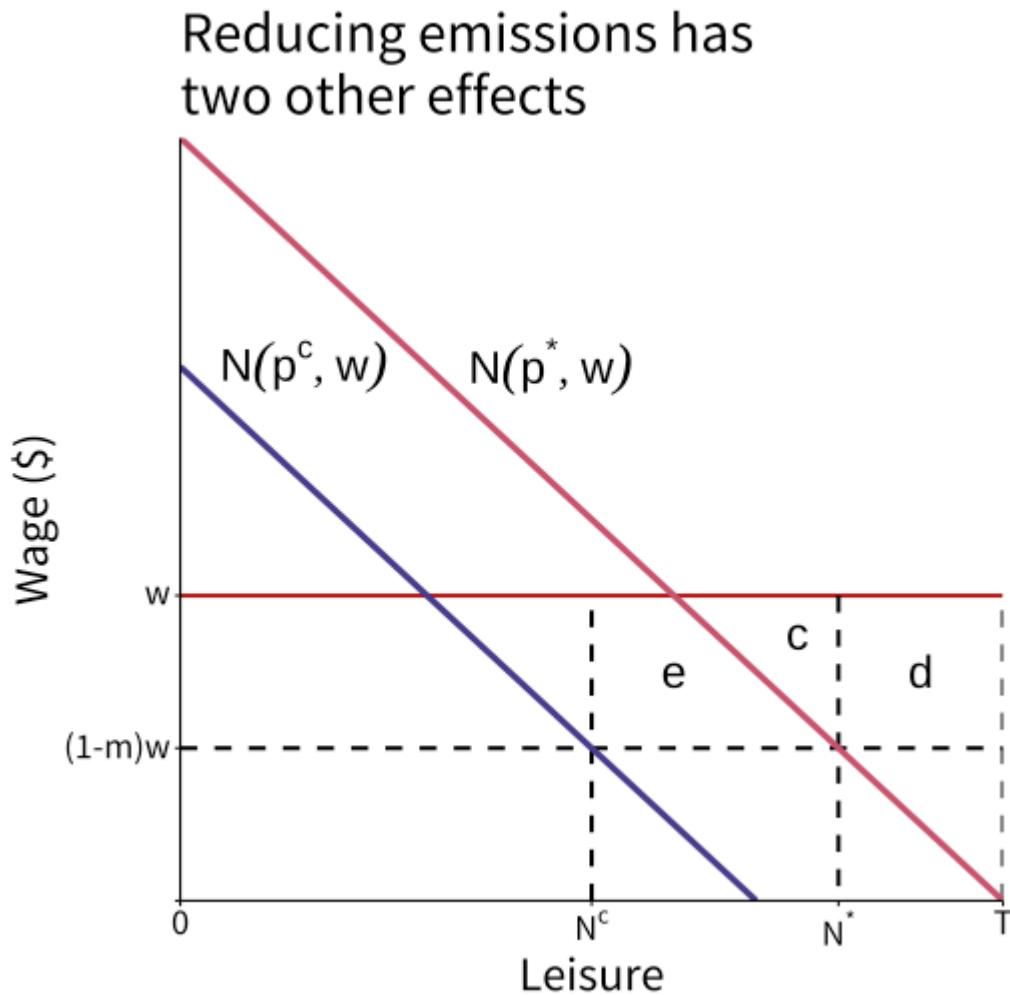
Suppose  $N$  and  $X$  are substitutes, and the regulator sets  $X = X^*$  where  $X^* \rightarrow MAC = MD$

This raises the price of  $X$ , shifts leisure demand to the **right**

New DWL is  $c$ , and government revenues are now only  $d$

Change in DWL from  $X^c \rightarrow X^*$  is indeterminant

# Environmental policy with labor market distortions



Fixing the pollution externality had two effects:

1. Indeterminant effect on the distortion in the labor market
2. Reduced the amount of revenue the government raised through labor taxation

# Second-best environmental policy

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First let's consider the case where they can only raise revenue via a labor tax: this is non-revenue raising environmental policy

# Second-best non-revenue raising environmental policy

If we cannot raise revenue with the environmental policy, the regulator chooses  $X$  (and  $E$ ) and the marginal tax rate  $m$  to maximize the sum of profit and utility, subject to the budget constraint

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The household consumes leisure according to the FOC:

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given the regulator chose  $X = \bar{X}$

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given the regulator chose  $X = \bar{X}$

The firm obtains profits:

$$\Pi = p\bar{X} - C(\bar{X})$$

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Let's do the comparative statics: differentiate the consumer's two FOCs with respect to  $\bar{X}$

# Second-best non-revenue raising environmental policy

$$u_{XX} \frac{\partial \bar{X}}{\partial \bar{X}} + u_{XN} \frac{\partial N}{\partial \bar{X}} = \frac{\partial p}{\partial \bar{X}} \quad (\text{X FOC})$$

$$u_{NX} \frac{\partial \bar{X}}{\partial \bar{X}} + u_{NN} \frac{\partial N}{\partial \bar{X}} = 0 \quad (\text{N FOC})$$

$\frac{\partial \bar{X}}{\partial \bar{X}} = 1$  so two equations, two unknowns;

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$\frac{\partial \bar{X}}{\partial \bar{X}} = 1$  so two equations, two unknowns; solving the system gives us:

$$\frac{\partial N}{\partial \bar{X}} = -\frac{u_{XN}}{u_{NN}}$$

$$\frac{\partial p}{\partial \bar{X}} = \frac{u_{XX}u_{NN} - u_{NN}^2}{u_{NN}} < 0$$

sign( $\frac{\partial N}{\partial \bar{X}}$ ) depends on whether  $X$  and  $N$  are complements or substitutes

# Second-best non-revenue raising environmental policy

Now that we know how the firm responds, return to the regulator's problem:

$$\max_{X,m} u(X, N) + Z - D(X) + pX - C(X) \quad \text{s.t.} \quad w m(T - N) = G$$

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For convenience, we assume it's returned to the consumer as a lump sum transfer so that:

$$\begin{aligned} Z &= (1 - m)w(T - N) - pX + G = (1 - m)w(T - N) - pX + w m(T - N) \\ &\Rightarrow Z = w(T - N) - pX \end{aligned}$$

Income is unchanged for a given level of  $N$  under the tax and transfer

# Second-best non-revenue raising environmental policy

The regulator's problem is then:

$$\max_{X,m} u(X, N) + \underbrace{w(T - N)}_Z - D(X) - C(X) + \lambda[wm(T - N) - G]$$

$\lambda$  is called the **marginal welfare cost of public funds**

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It measures the welfare cost of raising revenue by taxing labor

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What's the FOC for  $m$ ?

# Second-best non-revenue raising environmental policy

The FOC for  $m$  is:

$$(u_N - w) \frac{\partial N}{\partial m} + \lambda \left[ w(T - N) - w m \frac{\partial N}{\partial m} \right] = 0$$

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What's the interpretation of the right hand side?

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This times the **tax wedge**  $mw$ , the gap between  $w$  and actual wage after taxes, gives us the change in excess burden (i.e. the DWL  $d$  in the graph)

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The change in tax revenue from higher  $m$

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First term is the increase in revenue on the inframarginal hours worked

Second term is the decrease in revenue from reduced hours worked

- Similar to  $P(X) + P'(X)X$  for a monopolist

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This is the change in welfare from a change in tax revenue!

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So that we can substitute in the consumer leisure response:

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What's the interpretation?

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Suppose  $N$  and  $X$  are substitutes, what does this mean?

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It's more socially costly to reduce  $X$  because the household increases  $N$  in response

This **exacerbates** the distortion caused by the income tax: the household was already undersupplying labor because of the income tax

Now the household undersupplies labor to an even greater extent

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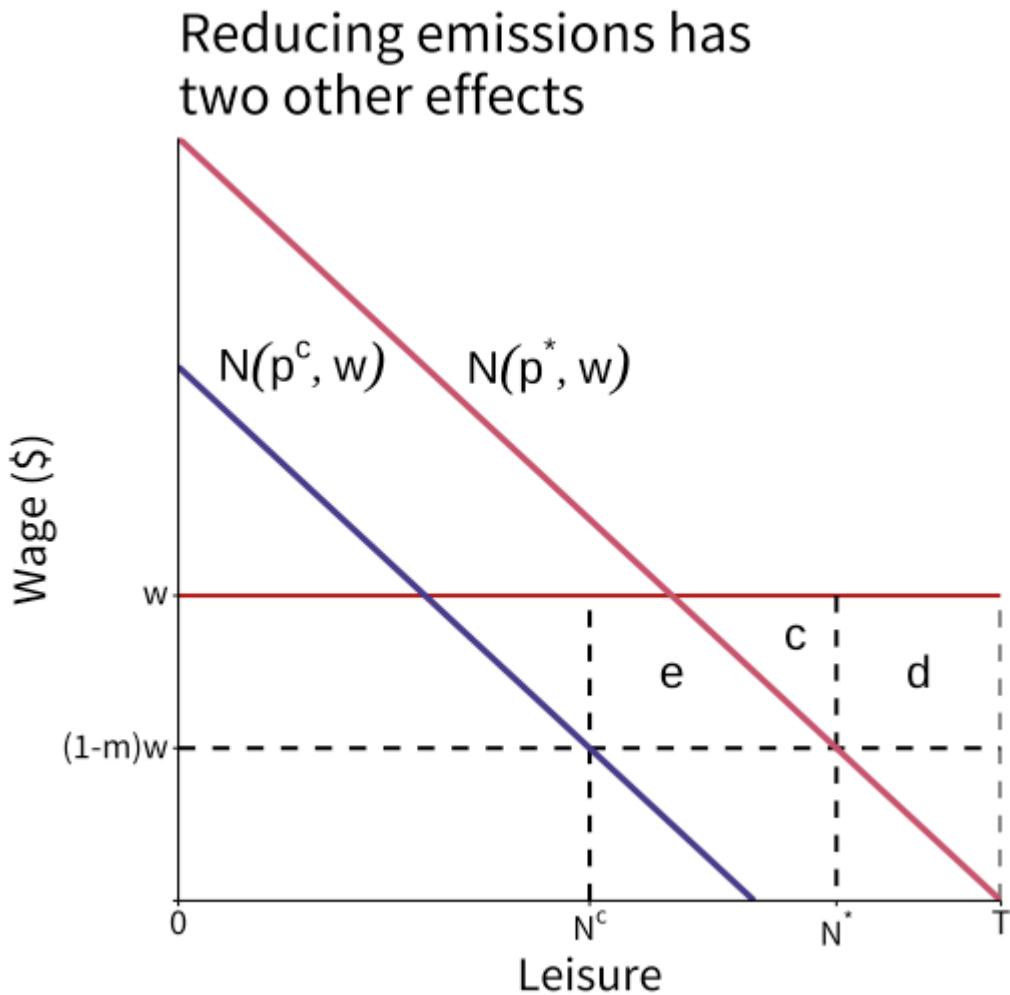
The marginal social cost of abatement ( $MAC + MIE$ ) has become **smaller**

Intuition?

It's less socially costly to reduce  $X$  because the household decreases  $N$  in response

This **alleviates** the distortion caused by the income tax: the household was undersupplying labor because of the income tax, but now reducing  $X$  increases labor supply, shrinking the labor market DWL

# Second-best non-revenue raising environmental policy



$N^c \rightarrow N^*$  when  $p^c \rightarrow p^*$  because of a change in  $X$

This is  $-\frac{\partial N}{\partial p} \frac{\partial p}{\partial X}$

This reduces tax revenue by  $e + c$  which is just

$$\begin{aligned}(N^* - N^c)(w - (1 - m)w) \\ = \underbrace{(N^* - N^c)mw}_{\approx -\frac{\partial N}{\partial p} \frac{\partial p}{\partial X}}\end{aligned}$$

## Second-best non-revenue raising environmental policy

The marginal welfare cost of recovering the lost tax revenue (in order to maintain gov't revenues  $G$ ) by raising  $m$  is  $\lambda$  giving us a total welfare cost of:

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But  $(N^* - N^c)mw$  also happens to be the increase in excess burden: its a **direct welfare loss** in addition to the loss from having to increase  $m$

So the total welfare loss is:

$$(1 + \lambda)(N^* - N^c)mw$$

The discrete version of MIE!

# Findings recap

If there's a government revenue constraint, and it can only be met with labor taxes then:

1. The marginal social cost of reducing  $X$  is higher if  $X$  and  $N$  are substitutes and lower if they are complements

# Findings recap

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# Findings recap

If there's a government revenue constraint, and it can only be met with labor taxes then:

1. The marginal social cost of reducing  $X$  is higher if  $X$  and  $N$  are substitutes and lower if they are complements
2. The optimal level of pollution is larger if they are substitutes, lower if they are complements
3. The absolute value of the difference in first and second-best pollution levels is larger if:
  - Demand for  $X$  is more inelastic
  - Elasticity of substitution between  $N$  and  $X$  is greater

# Second-best non-revenue raising environmental policy

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First define:

- $\varepsilon_x$  as the own price elasticity  $\frac{\partial X}{\partial p} \frac{p}{X}$
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and take advantage of the **Slutsky symmetry condition**  $\partial N / \partial p = \partial X / \partial w$

We can then use these to substitute into the MIE and get:

$$MIE = (1 + \lambda) \left[ -\frac{\eta_{XN}}{\varepsilon_X} \right] p \frac{m}{1 - m}$$

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MIE bigger if  $|\eta_{XN}|$  is bigger (higher elasticity of substitution)

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MIE bigger if  $|\eta_{XN}|$  is bigger (higher elasticity of substitution)

MIE bigger if  $|\varepsilon_X|$  is smaller (more inelastic demand for  $X$ )

-->

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The regulator's problem is thus to select two tax rates:  $m$  and  $\tau$

For simplicity we still assume all tax revenues are returned lump sum to households

# Revenue raising environmental policy

First derive household spending on the numeraire good:

$$Z = (1 - m)w(T - N) - pX + G = w(T - N) - pX + \tau X$$

where the second equality comes from substituting out the govt's budget constraint:  $G = wm(T - N) + \tau X$

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These are a function of the govt's choice of  $m$  and  $\tau$

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Next, as usual, differentiate the FOCs wrt  $\tau$

# Revenue raising environmental policy

This gives us 3 equations and 3 unknown partial derivatives:

$$u_{XX} \frac{\partial X}{\partial \tau} + u_{XN} \frac{\partial N}{\partial \tau} = \frac{\partial p}{\partial \tau} \quad (\text{Household X FOC})$$

$$u_{XN} \frac{\partial X}{\partial \tau} + u_{NN} \frac{\partial N}{\partial \tau} = 0 \quad (\text{N FOC})$$

$$C''(X) \frac{\partial X}{\partial \tau} = \frac{\partial p}{\partial \tau} - 1 \quad (\text{Firm X FOC})$$

Substitute and solve...

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$$\frac{\partial X}{\partial \tau} = \frac{u_{NN}}{H} < 0$$

$$\frac{\partial N}{\partial \tau} = \frac{-u_{XN}}{H} \leqslant 0$$

$$\frac{\partial p}{\partial \tau} = \frac{u_{XX}u_{NN} - u_{XN}^2}{H} > 0$$

where  $H = u_{XX}u_{NN} - u_{XN}^2 - C''(X)u_{NN} > 0$

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Substitute in for  $Z$  from household spending:

$$Z = w(T - N) - pX + \tau X$$

And look at the  $\tau$  FOC

# Revenue raising environmental policy

$$[u_X - C'(X) - D'(X)] \frac{\partial X}{\partial \tau} + \left[ \underbrace{u_N - w}_{-wm} - \lambda w m \right] \frac{\partial N}{\partial \tau} + \lambda \left[ X + \tau \frac{\partial X}{\partial \tau} \right] = 0$$

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Just follow the same steps as we did with the non-revenue raising case and divide by  $\frac{\partial X}{\partial \tau}$  to get:

$$\underbrace{u_x - C'(X)}_{MAC} + \underbrace{(1 + \lambda)wm \left[ -\frac{\partial N}{\partial \tau} / \frac{\partial X}{\partial \tau} \right]}_{MIE} + \underbrace{\lambda \left[ \tau + X / \frac{\partial X}{\partial \tau} \right]}_{MRE} = D'(X)$$

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Since the tax is per unit, we have that:  $\frac{\partial N}{\partial \tau} / \frac{\partial X}{\partial \tau} = \frac{\partial N}{\partial p} / \frac{\partial X}{\partial p}$ , MIE is similar in revenue and non-revenue raising contexts

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MRE changes the marginal social cost of  $X$  because changes in  $\tau$  affect how much revenue we need to raise with distorting labor taxation

Let's get some intuition at the corner case of  $\tau = 0$

What's the sign of  $MRE$ ?

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- this reduces the distortionary tax in the labor market
- this reduces welfare losses in the labor market
- this reduction in welfare losses reduces the marginal social cost of reducing  $X$ , decreasing the optimal level of  $X$

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$$MRE \equiv \lambda \left[ \tau + X / \frac{\partial X}{\partial \tau} \right] = \lambda \left[ \tau + X / \frac{\partial X}{\partial p} \right] = \lambda [\tau + p / \varepsilon_X] = \lambda \tau [1 + 1 / \varepsilon_X^\tau]$$

where  $\varepsilon_X < 0$  is the elasticity of demand for the dirty good and  $\varepsilon_X^\tau$  is the elasticity with respect to the tax

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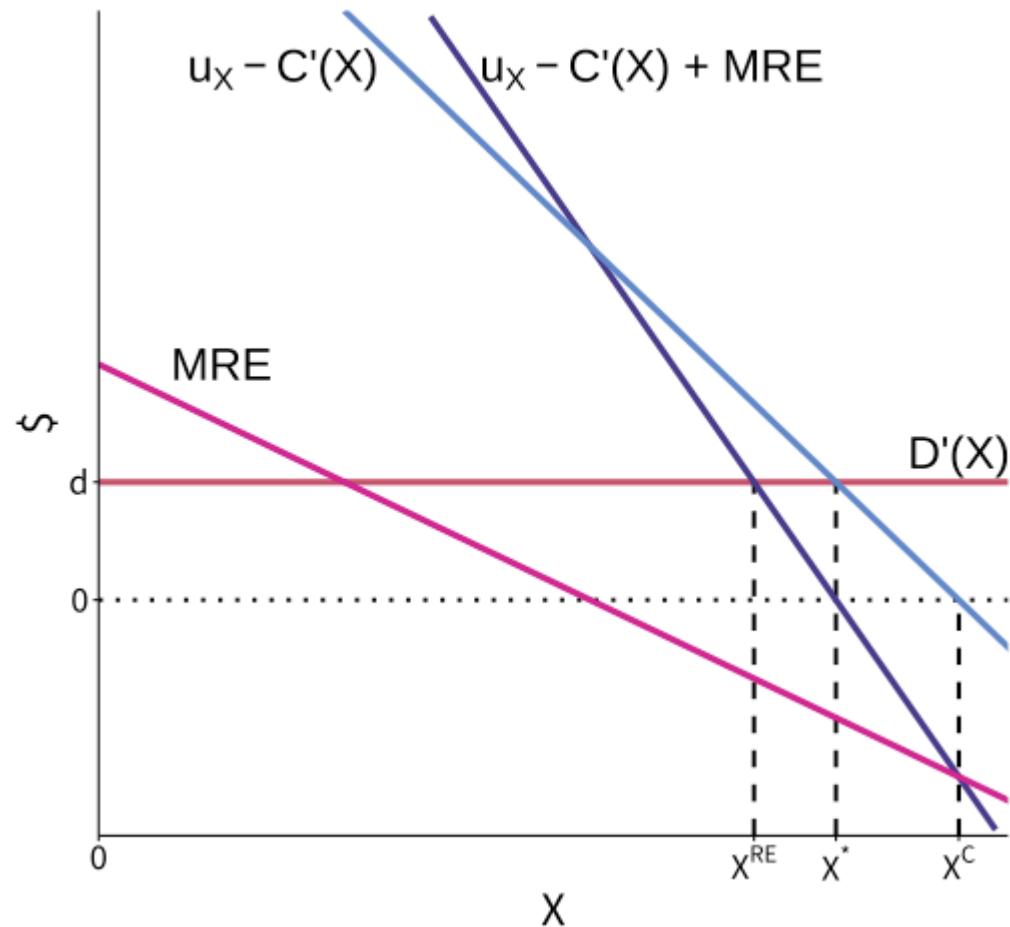
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Why?

# Revenue raising environmental policy

Inelastic demand means MRE < 0



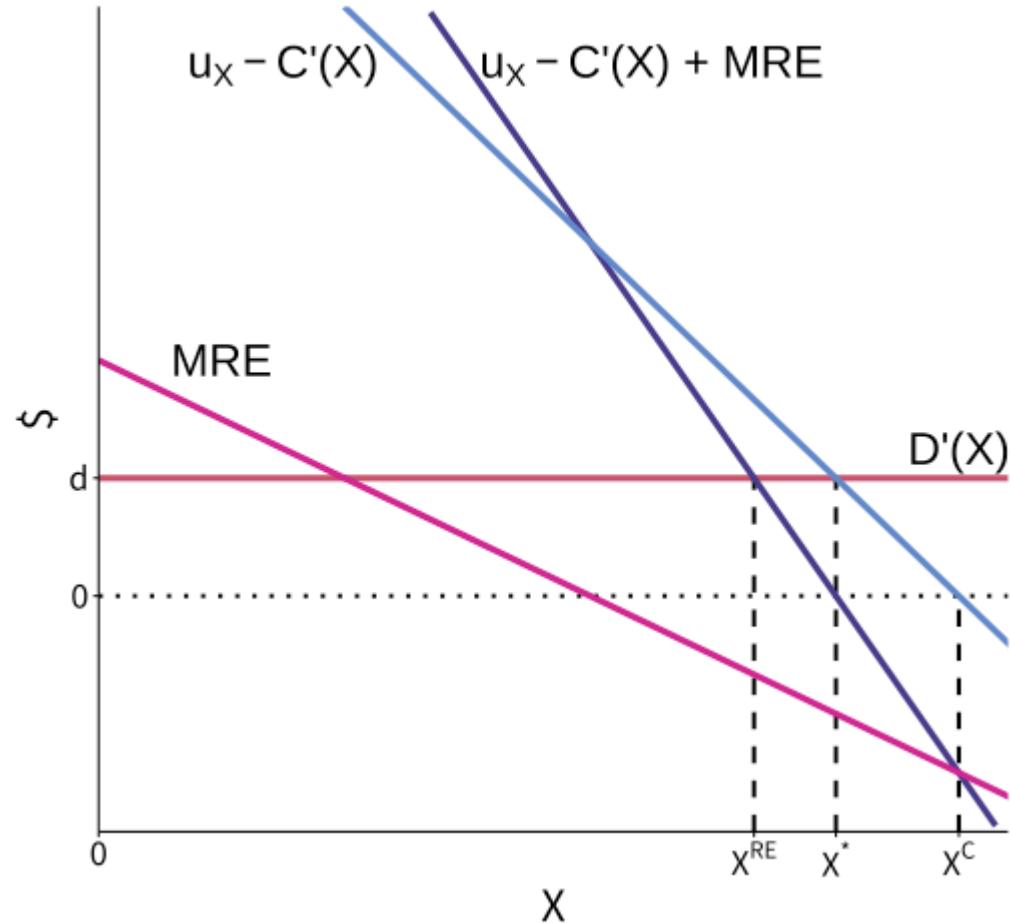
**Demand for dirty good is sufficiently inelastic:**

Suppose  $\frac{\partial N}{\partial p} = 0$  so  $MIE = 0$ ,  
 $C'(X) = c$ ,  $D'(X) = d$

Inelastic demand lets us raise more revenue from a small change in the tax

# Revenue raising environmental policy

Inelastic demand means  $MRE < 0$



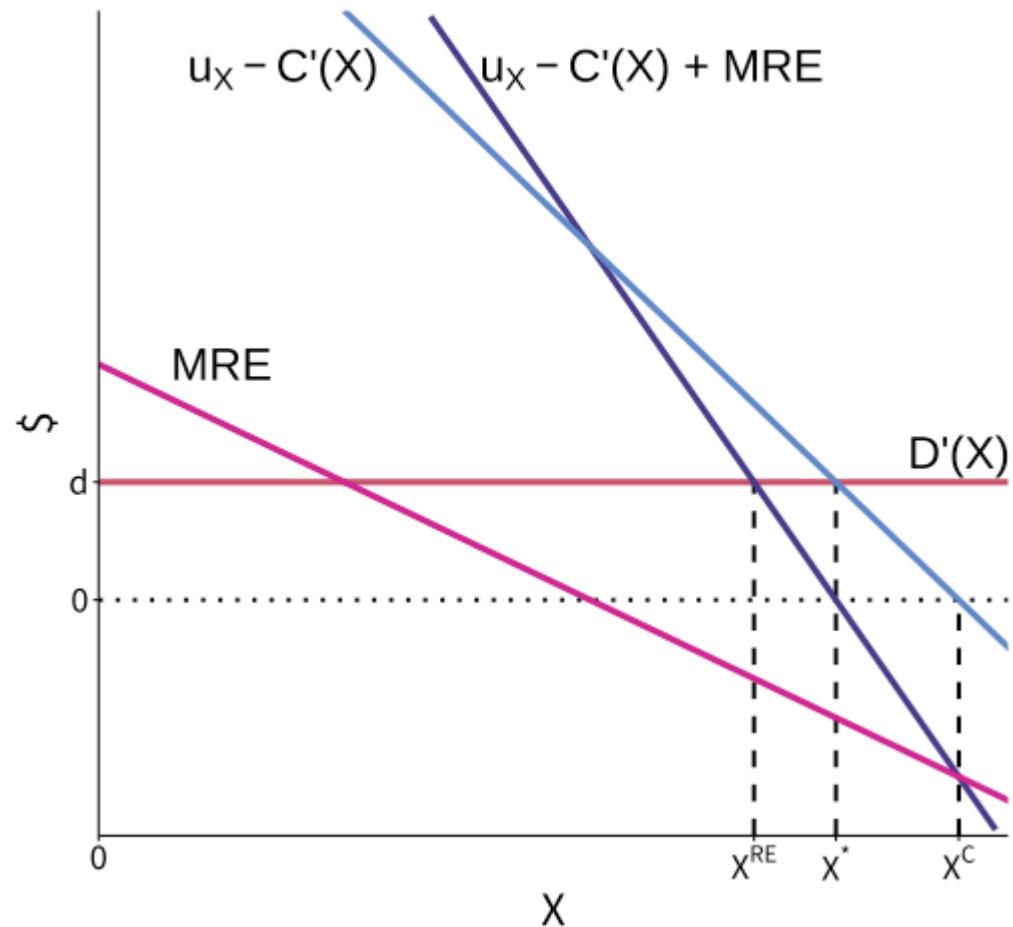
Inelastic demand lets us raise more revenue from a small change in the tax

This reduces the marginal social cost of reducing  $X$

Optimal  $X$  with revenue-raising is lower than without:  $X^{RE} < X^*$

# Revenue raising environmental policy

Inelastic demand means  $MRE < 0$



We can also see that if  $D'(X)$  was very large, making  $\tau$  larger, we would be where  $MRE > 0$

# Double dividend

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There is a **weak double dividend** if welfare is always greater when revenue raised via environmental taxation is used to reduced distortionary taxation rather than refunded lump sum

- This is always true

There is a **strong double dividend** if the emission tax should always be set above the  $MAC = MD$  level, resulting in greater pollution reductions and more revenue raised

- This may or may not be true

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Price of  $X$  rises from  $\tau$ , demand for leisure goes down, labor goes up

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Let's look at this pathway in more detail

# Double dividend

Again, assume  $C'(X) = c$ , this gives us that:

$$MIE = \lambda \left( -\frac{\eta_{XN}}{\varepsilon_X} \right) \frac{p}{\varepsilon_L} \quad MRE = \lambda \left( \frac{p}{\varepsilon_X} + \tau \right)$$

where

$$\eta_{XN} = \overbrace{\frac{\partial X}{\partial w} \frac{(1-m)w}{X}}^{\text{cross-price elasticity}} \quad \varepsilon_L = -\overbrace{\frac{\partial N}{\partial w} \frac{(1-m)w}{L}}^{\text{labor supply elasticity}} = \frac{\partial L}{\partial w} \frac{(1-m)w}{L}$$

# Double dividend

Suppose N and X are *average substitutes* which means the negative cross-price elasticity is equal to the the labor supply elasticity  $\eta_{XN} = \varepsilon_L$

This is true if a 1% wage increase gives a  $\eta_{XN}\% = \varepsilon_L\%$  spending increase

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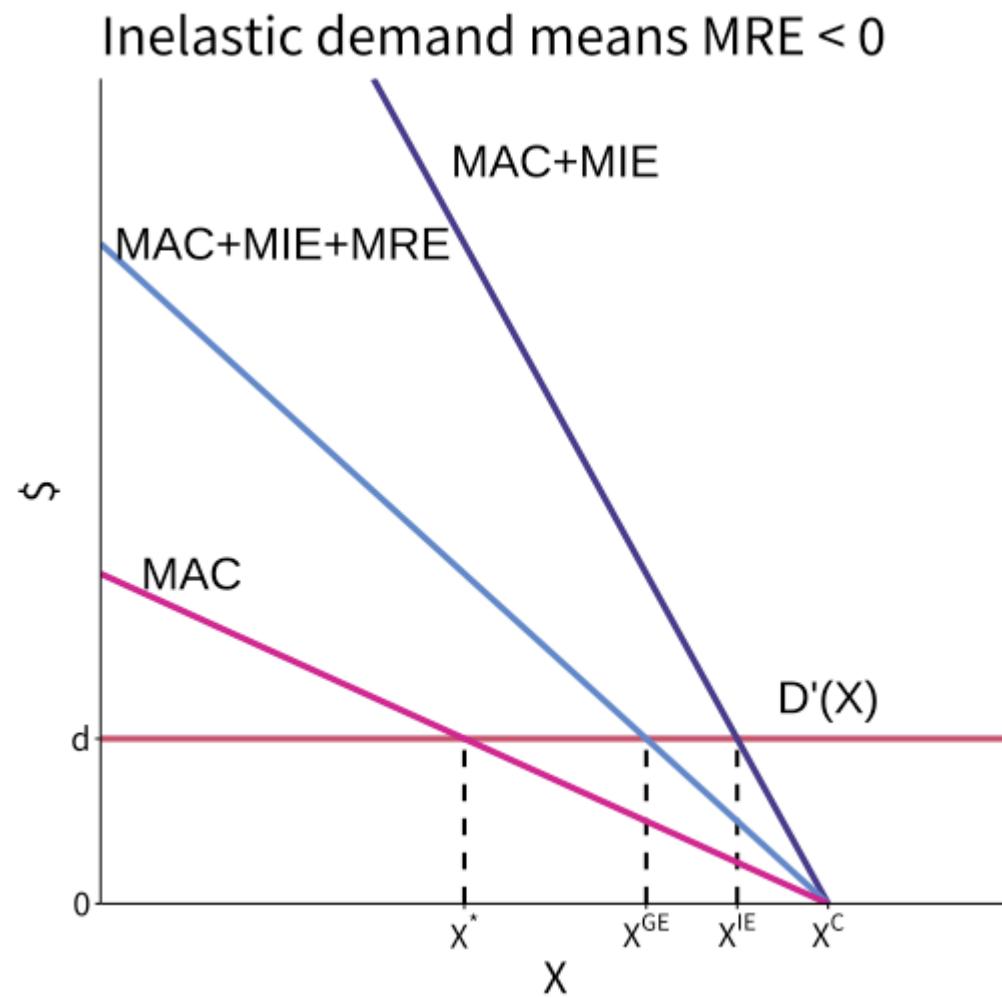
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$$MIE = \lambda \left( -\frac{p}{\varepsilon_X} \right) < \lambda \left( \frac{p}{\varepsilon_X} + \tau \right) = MRE$$

$\Rightarrow$  we shouldn't expect a strong double dividend because  $MIE + MRE = \lambda\tau > 0$

# Revenue raising environmental policy



Even though there isn't a double dividend, MIE and MRE **still matter** for the optimal second-best pollution level

Optimal pollution  $X^{GE}$  is larger than first-best  $X^*$ , but less than the level without revenue recycling  $X^{IE}$

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What about freely allocated permits or command and control?

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Without revenue from permits or taxes, the optimal pollution level is higher