Basic Data Structures: Stacks and Queues

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Data Structures Data Structures and Algorithms

Outline

1 Stacks

Queues

Stack: Abstract data type with the following operations:

Push(Key): adds key to collection

- Push(Key): adds key to collection
- Key Top(): returns most recently-added key

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- Key Top(): returns most recently-added key
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- Push(Key): adds key to collection
- Key Top(): returns most recently-added key
- Key Pop(): removes and returns most recently-added key
- Boolean Empty(): are there any elements?

Balanced Brackets

Input: A string *str* consisting of '(', ')', '[', ']' characters.

']' characters.

Output: Return whether or not the string's parentheses and square brackets are balanced.

Balanced Brackets

```
Balanced:
```

```
"(([])[]()",
"((([([])]))())"
```

Unbalanced:

```
"([]]()"
```

""]["

IsBalanced(str)

```
Stack stack
for char in str:
  if char in ['(', '[']:
    stack.Push(char)
  else:
    if stack.Empty(): return False
```

 $top \leftarrow stack.Pop()$

return False

return stack.Empty()

if (top = '[' and char != ']') or (top = '(' and char != ')'):

numElements: 0



numElements: 0

Push(a)

numElements: 1

a

Push(a)

numElements: 1

a

numElements: 1

a

Push(b)

numElements: 2

a b

Push(b)

numElements: 2

a b

numElements: 2

a b

Top()

numElements: 2

ab

 $Top() \rightarrow b$

numElements: 2

a b

numElements: 2

a b

Push(c)

numElements: 3

a b c

Push(c)

numElements: 3

a b c

numElements: 3

a b c

Pop()

numElements: 2

a b

 $Pop() \rightarrow c$

numElements: 2

a b

numElements: 2

a b

Push(d)

numElements: 3

a b d

Push(d)

numElements: 3

a b d

numElements: 3

a b d

Push(e)

numElements: 4

Push(e)

numElements: 4

a b d e

numElements: 4

Push(f)

numElements: 5

Push(f)

numElements: 5

a b d e f

numElements: 5

Push(g)

numElements: 5

 $Push(g) \rightarrow ERROR$

numElements: 5

a b d e f

numElements: 5

Empty()

numElements: 5

 $Empty() \rightarrow False$

numElements: 5

a b d e f

numElements: 5

Pop()

numElements: 4

 $Pop() \rightarrow f$

numElements: 4

a b d e

numElements: 4

Pop()

numElements: 3

a b d

 $Pop() \rightarrow e$

numElements: 3

a b d

numElements: 3

a b d

Pop()

numElements: 2

ab

 $Pop() \rightarrow d$

numElements: 2

a b

numElements: 2

a b

Pop()

numElements: 1

a

 $Pop() \rightarrow b$

numElements: 1

a

numElements: 1

a

Pop()

numElements: 0

 $Pop() \rightarrow a$

numElements: 0



numElements: 0

Empty()

numElements: 0

 $Empty() \rightarrow True$

numElements: 0



head

head

Push(a)



Push(a)





Push(b)



Push(b)





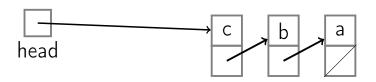
Top()



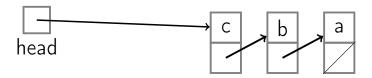


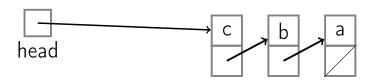


Push(c)



Push(c)



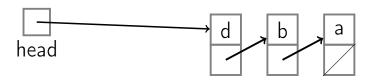




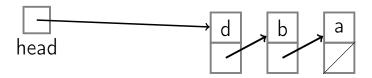


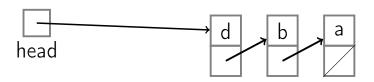


Push(d)

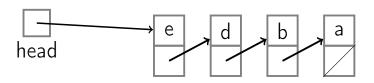


Push(d)

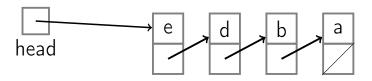


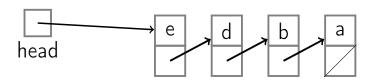


Push(e)

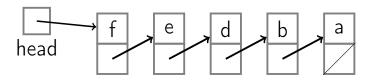


Push(e)

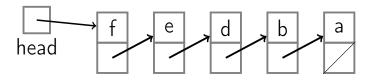


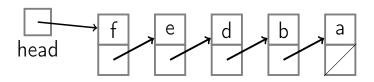


Push(f)

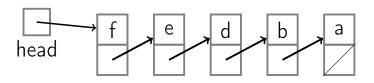


Push(f)

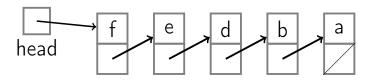


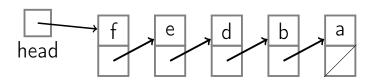


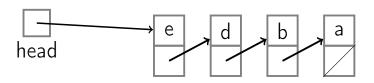
Empty()



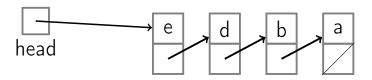
 $Empty() \rightarrow False$

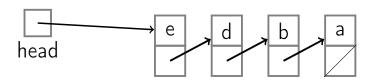




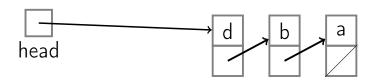


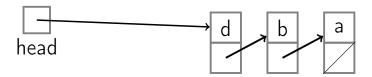
$$Pop() \rightarrow f$$

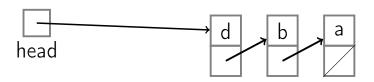




Pop()



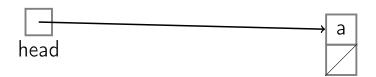
















head

 $Empty() \rightarrow True$

Stack Implementation with

Linked List

Stack Implementation with

Linked List

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Summary

Stacks can be implemented with either an array or a linked list.

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- Each stack operation is O(1): Push, Pop, Top, Empty.

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- Each stack operation is O(1): Push, Pop, Top, Empty.
- Stacks are ocassionaly known as LIFO queues.

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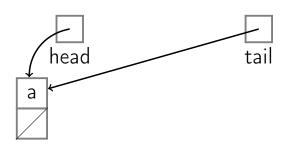
FIFO: First-In, First-Out

head tail

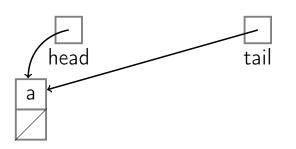
head

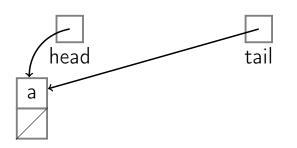
tail

Enqueue(a)

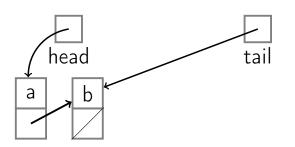


Enqueue(a)

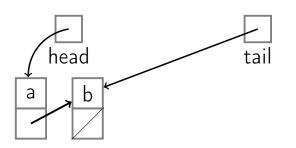


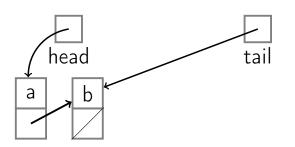


Enqueue(b)

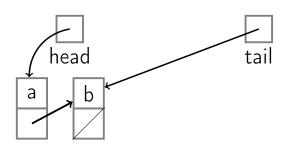


Enqueue(b)

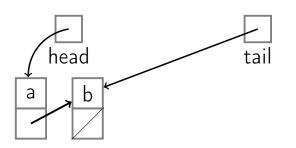


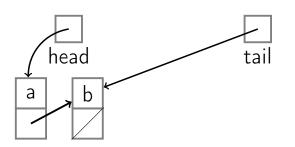


Empty()

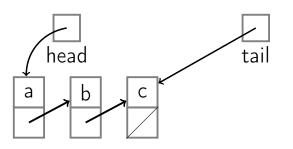


 $Empty() \rightarrow False$

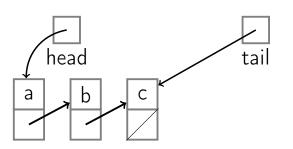


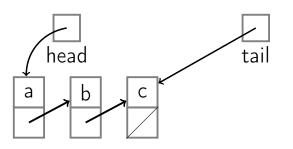


Enqueue(c)

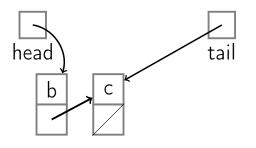


Enqueue(c)

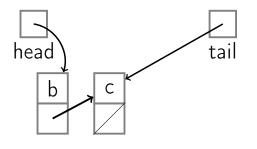


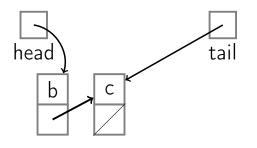


Dequeue()

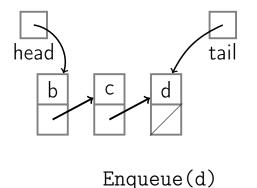


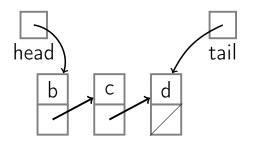
 $Dequeue() \rightarrow a$

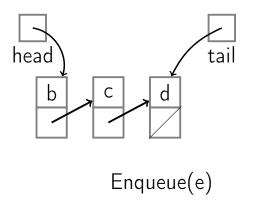


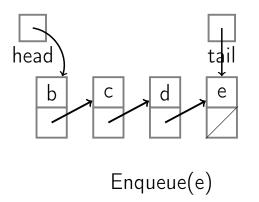


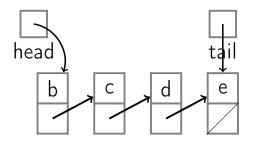
Enqueue(d)

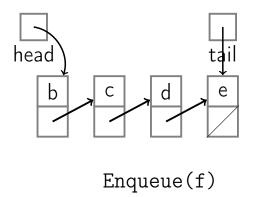


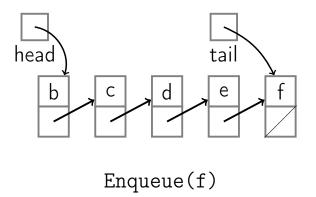


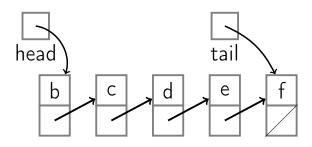


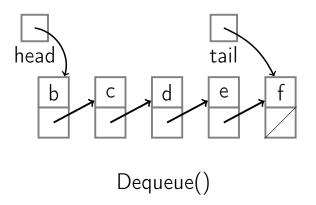


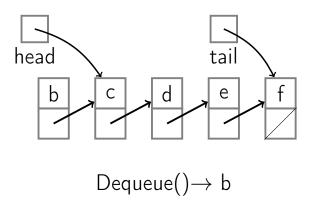


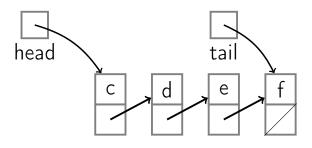


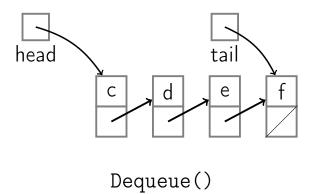


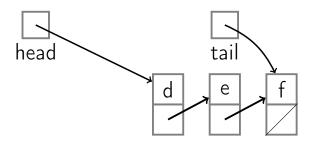




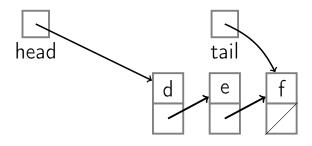


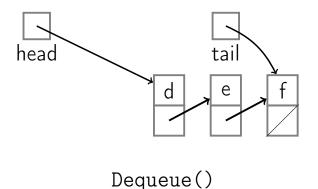


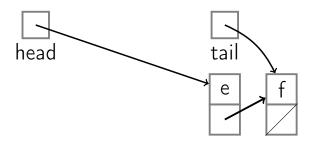




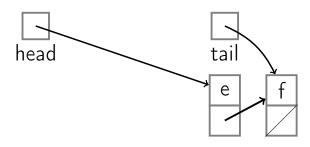
Dequeue() \rightarrow c

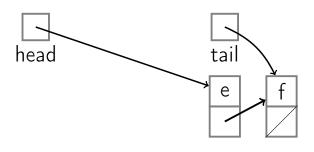




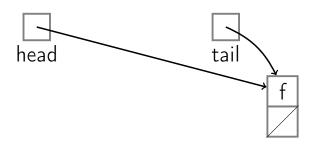


Dequeue() \rightarrow d

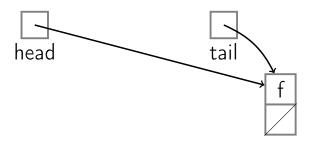


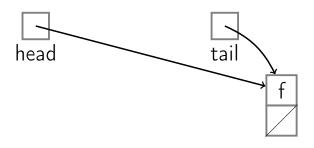


Dequeue()



 $Dequeue() \rightarrow e$





Dequeue()

head

∠ tail

Dequeue() \rightarrow f

head tail

head

tail

Empty()

head

tail

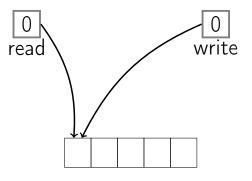
 $Empty() \rightarrow True$

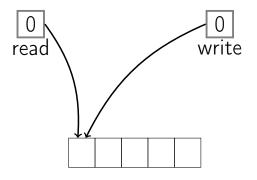
head tail

■ Enqueue: use List.PushBack

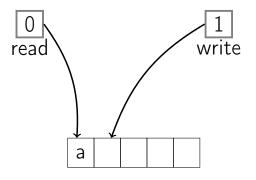
- Enqueue: use List.PushBack
- Dequeue: use List.TopFront and List.PopFront

- Enqueue: use List.PushBack
- Dequeue: use List.TopFront and List.PopFront
- Empty: use List.Empty

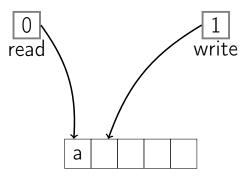


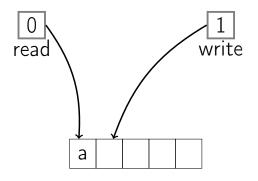


Enqueue(a)

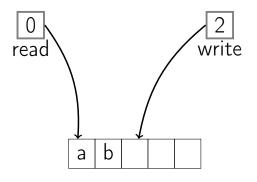


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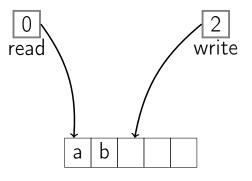


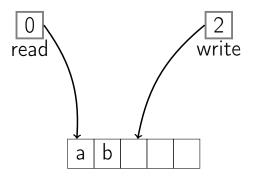


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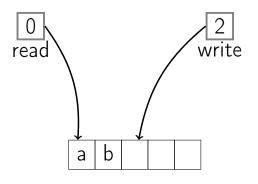


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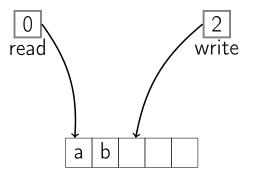


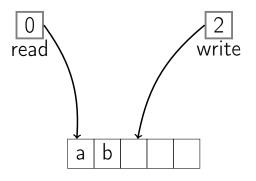


Empty()

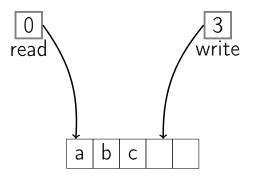


 $Empty() \rightarrow False$

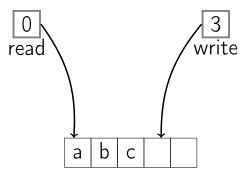


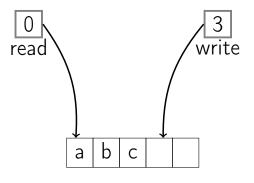


Enqueue(c)

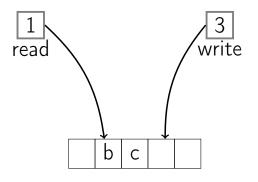


Enqueue(c)

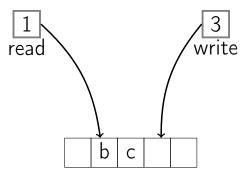


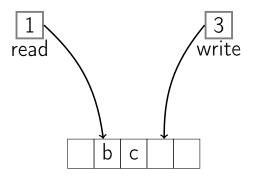


Dequeue()

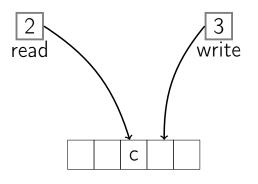


 $Dequeue() \rightarrow a$

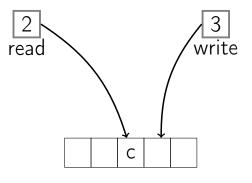


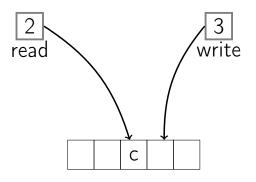


Dequeue()

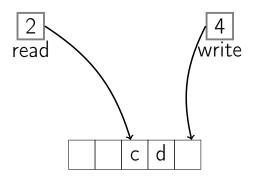


Dequeue() \rightarrow b

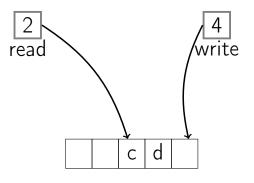


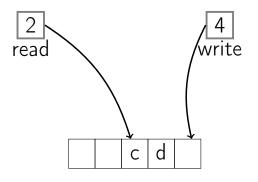


Enqueue(d)

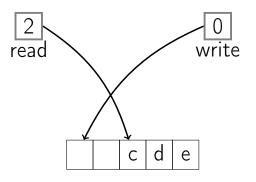


Enqueue(d)

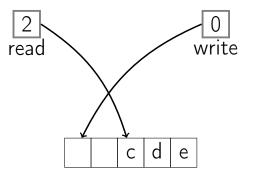


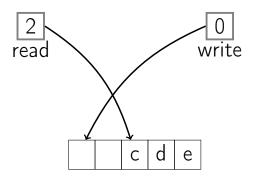


Enqueue(e)

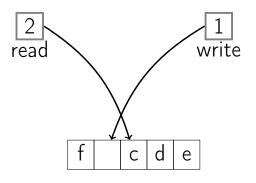


Enqueue(e)

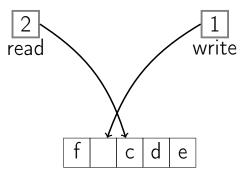


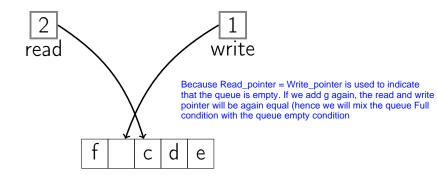


Enqueue(f)

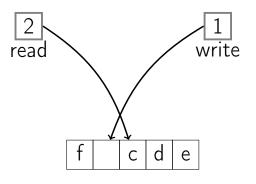


Enqueue(f)

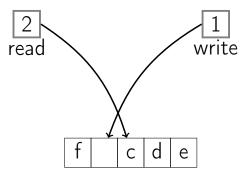


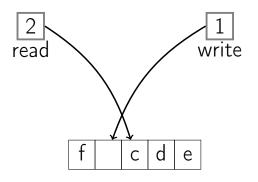


Enqueue(g)

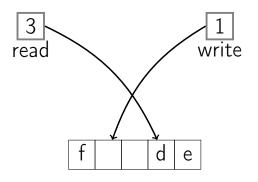


 $Enqueue(g) \rightarrow ERROR$

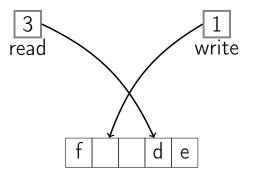


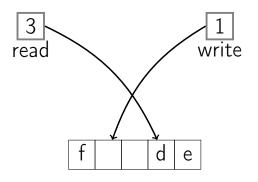


Dequeue()

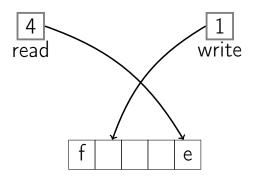


Dequeue() \rightarrow c

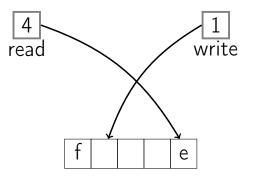


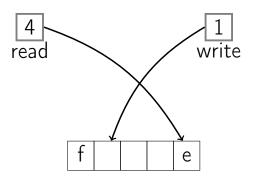


Dequeue()

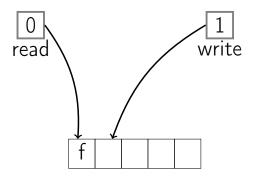


Dequeue() \rightarrow d

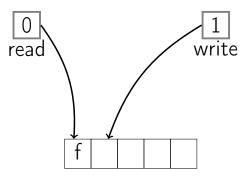


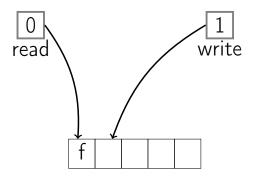


Dequeue()

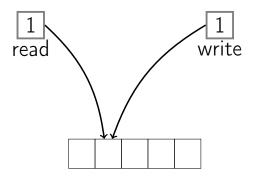


Dequeue() \rightarrow e

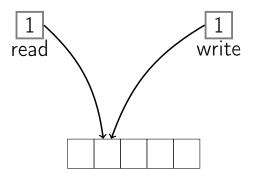


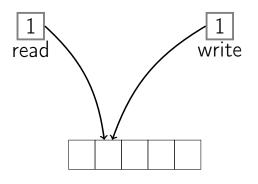


Dequeue()

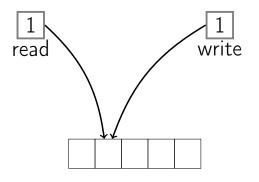


 $Dequeue() \rightarrow f$





Empty()



 $Empty() \rightarrow True$

Summary

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Queues can be implemented with either a linked list (with tail pointer) or an array.

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- Queues can be implemented with either a linked list (with tail pointer) or an array.
- Each queue operation is O(1): Enqueue, Dequeue, Empty.