



Physics. *You work it out.*

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Stationary Points 2ii

A Level



Part A Find coordinate

Find the coordinates of the stationary points on the curve $y = x^3 - 3x^2 + 4$. Enter the x and y coordinates of the stationary point with the greatest x coordinate.

Enter the x -coordinate:

The following symbols may be useful: x

Enter the y -coordinate:

The following symbols may be useful: y

Part B Stationary point

Determine whether the stationary point whose coordinates you entered is a maximum point or a minimum point.

- ☐ Inconclusive
 - ☐ Minimum
 - ☐ Maximum
-

Part C **Range of x**

For which range of values of x does $x^3 - 3x^2 + 4$ decrease as x increases?

What form does your answer take? Choose from the list below, where a and b are constants and $a < b$, and then find a and/or b .

- ☐ $x < a$
 - ☐ $x \leq a$
 - ☐ $x > a$
 - ☐ $x \geq a$
 - ☐ $a < x < b$
 - ☐ $a \leq x \leq b$
 - ☐ $x < a$ or $x > b$
 - ☐ $x \leq a$ or $x \geq b$
-

Write down the value of a .

Write down the value of b (or if your chosen form has no b , write "n").

The following symbols may be useful: n

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Maxima and Minima: Problems 2ii



A curve has equation $y = 3x^3 - 7x + \frac{2}{x}$

Part A Verify stationary point

Verify the curve has a stationary point when $x = 1$.

[More practice questions?](#)

Part B Nature of stationary point

Determine the nature of this stationary point.

- ☐ Minimum
- ☐ Neither/inconclusive
- ☐ Maximum

Part C Tangent to curve

The tangent to the curve at this stationary point meets the y -axis at the point Q . Find the y -coordinate of Q .

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Stationary Points 2i

A Level



Part A Find minimum

Find the coordinates of the minimum point of the curve $y = (x + 2)(x^2 - 3x + 5)$. Enter the x and y coordinates below.

Enter the x -coordinate:

The following symbols may be useful: x

Enter the y -coordinate:

The following symbols may be useful: y

Part B Finding nature of stationary point

How did you know that the stationary point in part A was a minimum point?

- ☐ At this point, $\frac{d^2y}{dx^2}$ is negative.
- ☐ At this point, $\frac{dy}{dx}$ is zero.
- ☐ At this point, $\frac{d^2y}{dx^2}$ is positive.
-

Part C Calculate discriminant

Calculate the discriminant of $x^2 - 3x + 5$. Enter the exact value.

Part D Explain

Explain why $(x + 2)(x^2 - 3x + 5)$ is always positive whenever $x > -2$.

Easier question?

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Minimising the area

A Level Further A



A rectangular cuboid has a base with sides of length a and b and a height c . Its volume V and height c are fixed. By following the steps below find expressions in terms of V and c for the values of a and b which will minimise the surface area A of the cuboid, find an expression for this minimum surface area and check that this is indeed a minimum.

Write down the equation for the volume V of the rectangular cuboid in terms of a , b and c .

The following symbols may be useful: V , a , b , c

Write down the equation for the surface area A of the rectangular cuboid in terms of a , b and c .

The following symbols may be useful: A , a , b , c

From your equation for V deduce an expression for b in terms of V , a and c . Hence, by substitution, obtain an equation for A in terms of V , a and c .

The following symbols may be useful: A , V , a , c

Part B Expressions for a and b

Differentiate with respect to a the expression for A you found in Part A (since V and c are fixed you may treat them as constants). Hence find in terms of V and c an expression for the value of a for which the surface area A is minimised.

The following symbols may be useful: V , c

Find, in terms of V and c , the expression for b corresponding to this value of a .

The following symbols may be useful: V , c

Part C The minimum area

Find an expression for the minimum surface area in terms of V and c .

The following symbols may be useful: V , c

Part D Check that the area is a minimum

Find, at the value of a deduced in Part B, an expression in terms of V and c for the second derivative of A with respect to a ; convince yourself that the value of the second derivative indicates that the value of A is a minimum at this point.

The following symbols may be useful: v , c

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Stationary Points 4ii

A Level



Part A Find coordinates

Find the coordinates of the stationary point on the curve $y = x^4 + 32x$. Enter the x and y coordinates below.

Enter x coordinate:

The following symbols may be useful: x

Enter y coordinate:

The following symbols may be useful: y

Part B Maxima or Minima

Determine whether this stationary point is a maximum or a minimum.

☐ Maximum

☐ Minimum

Part C **Range of x**

For what range of values of x does $x^4 + 32x$ increase as x increases? Give your answer in the form of an inequality.

The following symbols may be useful: $<$, \leq , $>$, \geq , \times

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Physics. *You work it out.*

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Maxima and Minima: Problems 1i



A cuboid has an volume of exactly 8 m^3 . The base of the cuboid is a square with side length x metres. The surface area of the cuboid is $A \text{ m}^2$.

Part A Find expression for A

Show that A can be expressed in the form $ax^2 + \frac{b}{x}$, where a and b are constants, and find this expression.

The following symbols may be useful: x

Part B Find $\frac{dA}{dx}$

Find $\frac{dA}{dx}$.

The following symbols may be useful: x

Part C Find minimum

Find the value of x which gives the smallest surface area of the cuboid.

The following symbols may be useful: x

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Stationary Points 1ii



The curve $y = x^3 - kx^2 + x - 3$ has two stationary points.

Part A Differentiate

Find $\frac{dy}{dx}$.

The following symbols may be useful: k , x

Part B Find k

Given that there is a stationary point when $x = 1$, find the value of k .

The following symbols may be useful: k

Part C Differentiate twice

Find $\frac{d^2y}{dx^2}$.

The following symbols may be useful: x

Hence determine whether the stationary point is a minimum or a maximum.

☐ Maximum

☐ Minimum

Part D Find coordinate

Find the x -coordinate of the other stationary point.

The following symbols may be useful: x

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Stationary Points 1i

A Level



Part A Find stationary points

Find the coordinates of the stationary points on the curve $y = 2x^3 - 3x^2 - 12x - 7$. Enter the x and y coordinates of the stationary point with the largest x coordinate.

Enter the x coordinate:

The following symbols may be useful: x

Enter the y coordinate:

The following symbols may be useful: y

Part B Nature of stationary points

Determine whether each stationary point is a minimum or maximum point. Identify the nature of the stationary point whose coordinates you have entered in Part A.

☐ Minimum

☐ Maximum

Part C Expand and simplify

Expand and simplify $(x + 1)^2(2x - 7)$.

The following symbols may be useful: x

Part D Sketch

Hence sketch the curve $y = 2x^3 - 3x^2 - 12x - 7$, indicating the coordinates of all stationary points and intercepts with the axes. In order to check your answer, give the value of the intercept with the y -axis.

The following symbols may be useful: y

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Maxima and Minima: Problems 1ii



Figure 1: The diagram shows a rectangular enclosure, with a wall forming one side. A rope, of length 20 metres, is used to form the remaining three sides. The width of the enclosure is x metres, and the area of the enclosure is $A \text{ m}^2$.

Part A Express as equation

Show that A can be expressed in the form $px - qx^2$, and find this expression.

The following symbols may be useful: x

Part B Use differentiation

Use differentiation to find the maximum value of A .

The following symbols may be useful: A

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