

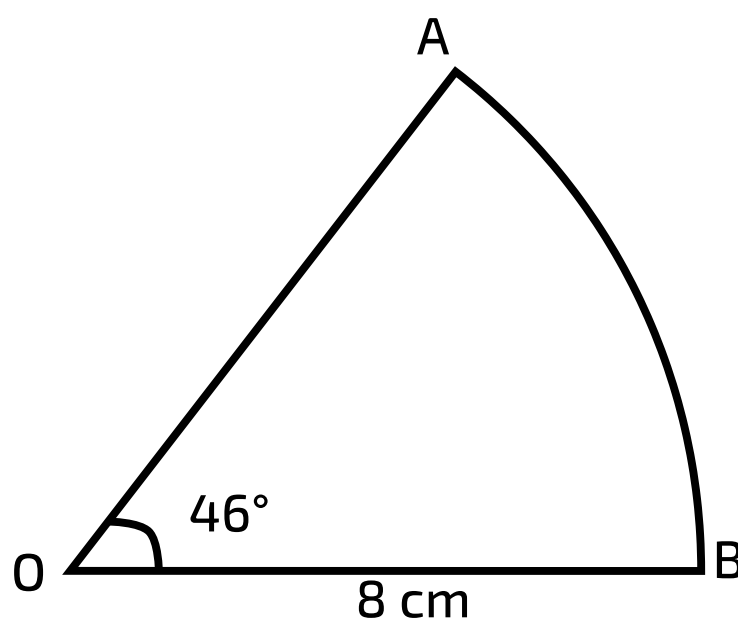
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# Radians-problems involving area 5ii

A Level



**Figure 1** shows a sector  $OAB$  of a circle, centre  $O$  and radius 8 cm. The angle  $AOB$  is  $46^\circ$ .



**Figure 1:** Sector  $OAB$ .

## Part A Convert angle to radians

Express  $46^\circ$  in radians, correct to 3 significant figures.

## Part B Arc length

Find the length of the arc  $AB$ .

## Part C Area of sector

Find the area of the sector  $OAB$ .

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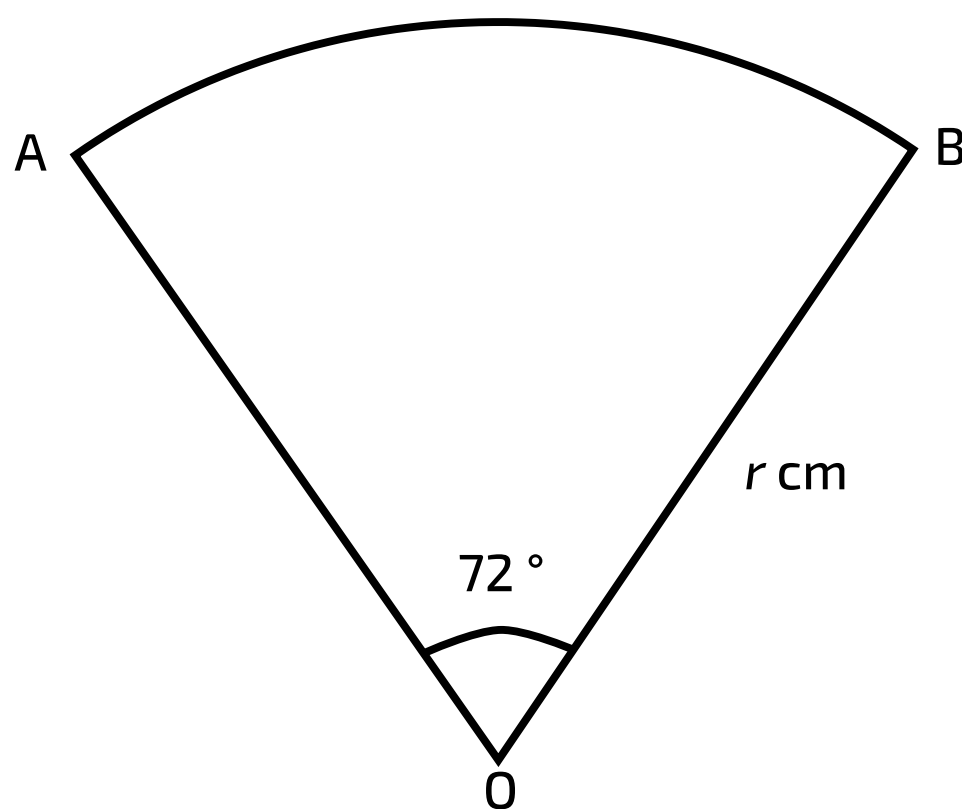
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## Radians-problems involving area 3ii

A Level



**Figure 1** shows a sector  $AOB$  of a circle, centre  $O$  and radius  $r$  cm. Angle  $AOB = 72^\circ$ .



**Figure 1:** Sector  $AOB$ .

The area of the sector  $AOB$  is  $45\pi \text{ cm}^2$ .

### Part A Convert angle to radians

Express  $72^\circ$  exactly in radians, simplifying your answer.

The following symbols may be useful:  $\pi$

### Part B Value of $r$

Find the value of  $r$  in cm.

## Part C    Area of segment

Find the area of the segment bounded by the arc  $AB$  and the chord  $AB$ , giving your answer in  $\text{cm}^2$  correct to 3 significant figures.

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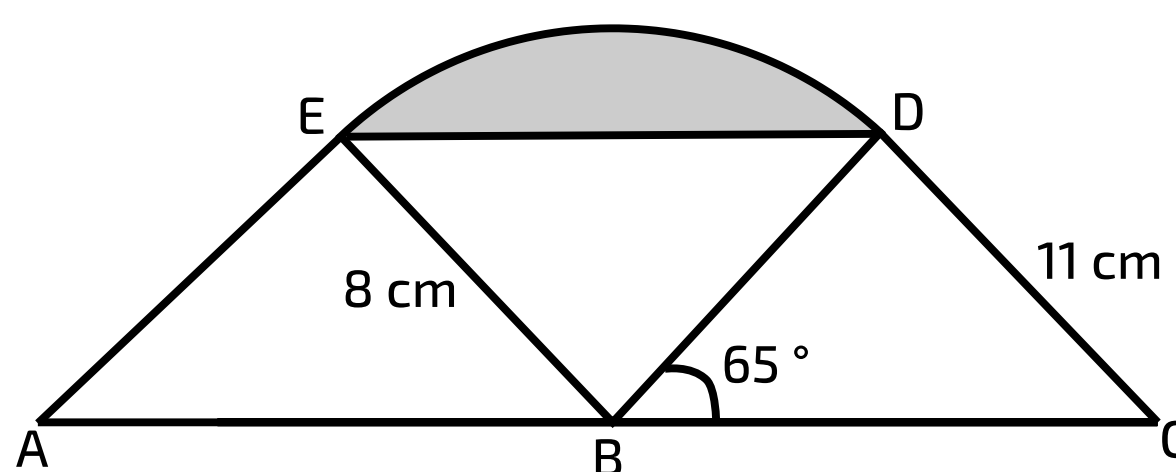
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## Radians-problems involving area 2ii

A Level



**Figure 1** shows two congruent triangles,  $BCD$  and  $BAE$ , where  $ABC$  is a straight line. In triangle  $BCD$ ,  $BD = 8$  cm,  $CD = 11$  cm and angle  $CBD = 65^\circ$ . The points  $E$  and  $D$  are joined by an arc of a circle with centre  $B$  and radius 8 cm.



**Figure 1:** Diagram of the triangles.

### Part A Angle $BCD$

Find angle  $BCD$ . Give your answer in radians, correct to 3 significant figures.

### Part B Angle $EBD$

Find the angle  $EBD$ , giving your answer in radians correct to 3 significant figures.

### Part C Area of shaded segment

Hence find the area (in  $\text{cm}^2$ ) of the shaded segment bounded by the chord  $ED$  and the arc  $ED$ , giving your answer correct to 3 significant figures.

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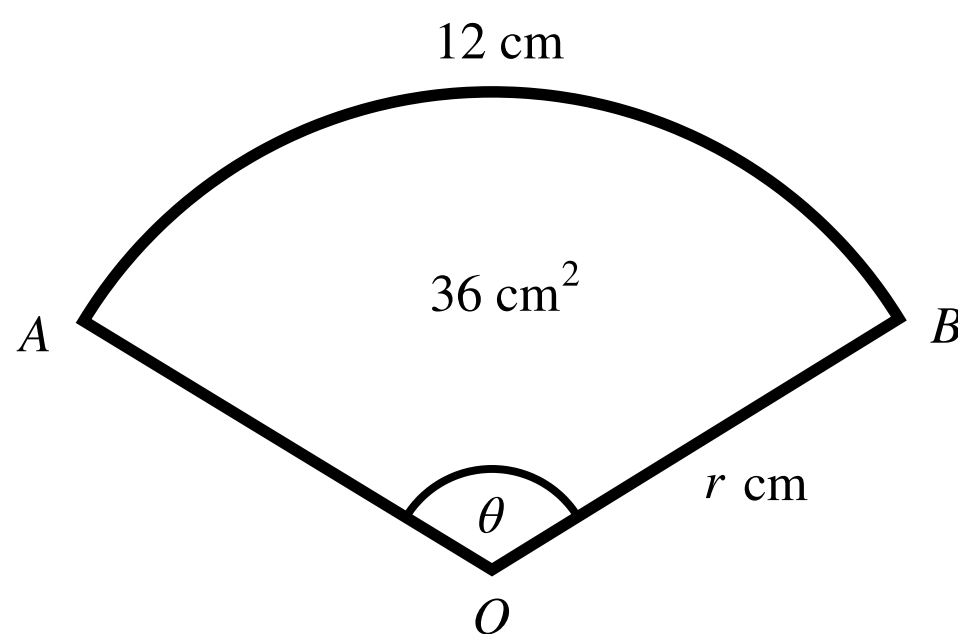


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## Radians-problems involving area 1ii

A Level  
P P P



**Figure 1:** The sector  $OAB$ .

A sector  $OAB$  of a circle of radius  $r$  cm has angle  $\theta$  radians. The length of the arc of the sector is 12 cm and the area of the sector is  $36 \text{ cm}^2$  (see **Figure 1**).

### Part A First equation

By considering the length of the arc of the sector, write down an equation involving  $r$  and  $\theta$ , where one side of the equation is a numerical constant.

The following symbols may be useful:  $r$ ,  $\theta$

### Part B Second equation

By considering the area of the sector, write down another equation involving  $r$  and  $\theta$ , where one side of the equation is a numerical constant.

The following symbols may be useful:  $r$ ,  $\theta$

**Part C** Values of  $r$  and  $\theta$ 

Hence show that  $r = 6 \text{ cm}$  and find the value of  $\theta$ .

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**Part D** Area of segment

Find the area of the segment bounded by the arc  $AB$  and the chord  $AB$ . Answer to 3 sf.

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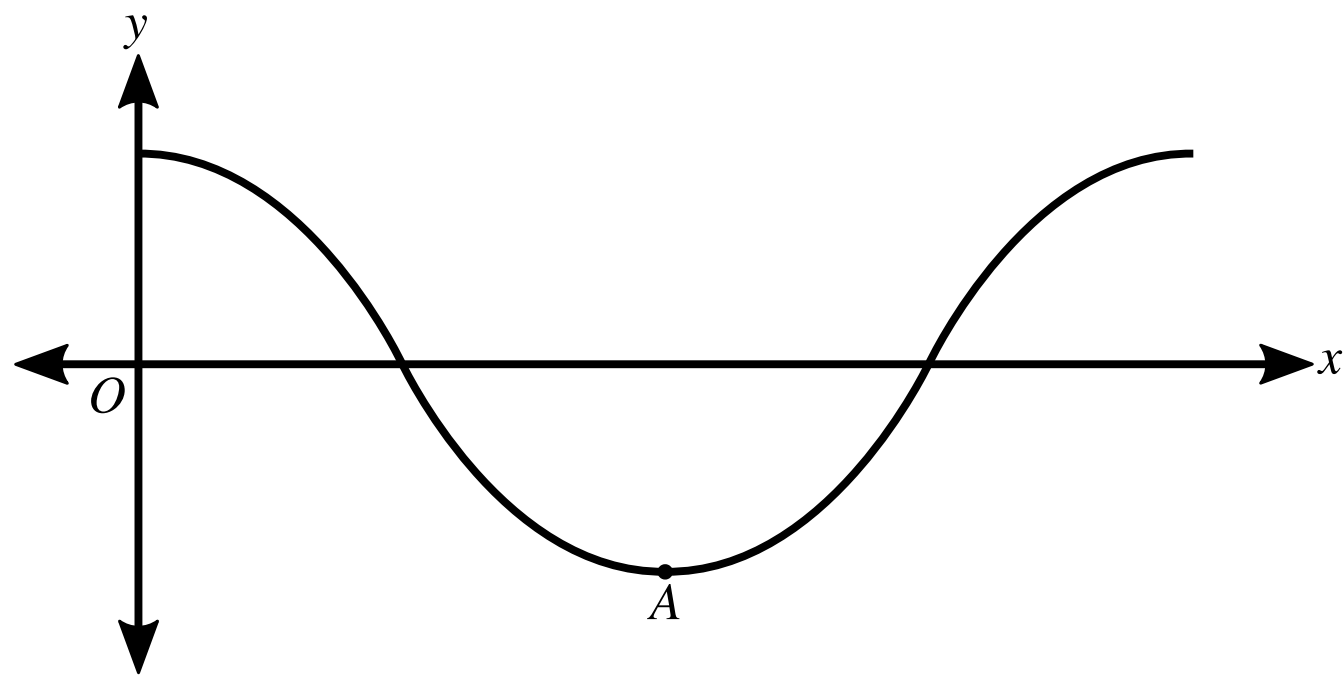
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# Radians and Trig Functions 2i

A Level



**Figure 1** shows part of the curve  $y = \cos 2x$ , where  $x$  is in radians. The point  $A$  is the minimum point of this part of the curve.



**Figure 1:** The graph of  $y = \cos 2x$ .

## Part A Period

State the period of  $y = \cos 2x$ .

The following symbols may be useful:  $\pi$ ,  $t$

## Part B Coordinates of $A$

What is the  $x$  coordinate of  $A$ ?

The following symbols may be useful:  $\pi$ ,  $x$

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What is the  $y$ -coordinate of  $A$ ?

The following symbols may be useful:  $\pi$ ,  $y$

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## Part C The inequality $\cos 2x \leq \frac{1}{2}$

Solve the inequality  $\cos 2x \leq \frac{1}{2}$  for  $0 \leq x \leq \pi$ , giving your answer as a range of angles  $x$ .

Give the exact lower bound, in the form  $x > a$  or  $x \geq a$ .

The following symbols may be useful:  $<$ ,  $\leq$ ,  $>$ ,  $\geq$ ,  $\pi$ ,  $x$

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Give the exact upper bound, in the form  $x < b$  or  $x \leq b$ .

The following symbols may be useful:  $<$ ,  $\leq$ ,  $>$ ,  $\geq$ ,  $\pi$ ,  $x$

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# Radians and Trig Functions 2ii

A Level



## Part A The equation $2 \cos x = \tan 2x$

Write down the exact values of  $\cos \frac{\pi}{6}$  and  $\tan \frac{\pi}{3}$  (where the angles are in radians). Hence verify that  $x = \frac{\pi}{6}$  is a solution of the equation

$$2 \cos x = \tan 2x.$$

[More practice questions?](#)

## Part B Sketch

Sketch, on a single diagram, the graphs of  $y = 2 \cos x$  and  $y = \tan 2x$ , for  $x$  (radians) such that  $0 \leq x \leq \pi$ .

[More practice questions?](#)

## Part C Other solutions

Hence state, in terms of  $\pi$ , the other values of  $x$  between 0 and  $\pi$  satisfying the equation.

Give the exact  $x$ -coordinate of the root of the equation furthest from the  $y$ -axis.

The following symbols may be useful:  $\pi$ ,  $x$

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Give the  $x$ -value of the central point of intersection of the graphs  $y = 2 \cos x$  and  $y = \tan 2x$  for  $0 \leq x \leq \pi$ .

The following symbols may be useful:  $\pi$ ,  $x$

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# Radians and Trig Functions 1i

A Level



A curve has equation  $y = \sin(ax)$ , where  $a$  is a positive constant and  $x$  is in radians.

## Part A Time Period

State the period of  $y = \sin(ax)$ , giving your answer in an exact form in terms of  $a$ .

The following symbols may be useful:  $a$ ,  $\pi$ ,  $t$

## Part B $\sin(ax) = k$

Given that  $x = \frac{1}{5}\pi$  and  $x = \frac{2}{5}\pi$  are the two smallest positive solutions of  $\sin(ax) = k$ , where  $k$  is a positive constant. Find the values of  $a$  and  $k$ .

Find the value of  $a$ .

The following symbols may be useful:  $a$

Find the value of  $k$ .

The following symbols may be useful:  $k$

**Part C**  $\sin(ax) = \sqrt{3} \cos(ax)$ 

Given instead that  $\sin(ax) = \sqrt{3} \cos(ax)$ , find the two smallest positive solutions for  $x$ , giving your answers in an exact form in terms of  $a$ .

Give the smallest positive solution.

The following symbols may be useful:  $a$ ,  $\pi$ ,  $x$

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Give the second smallest positive solution.

The following symbols may be useful:  $a$ ,  $\pi$ ,  $x$

---

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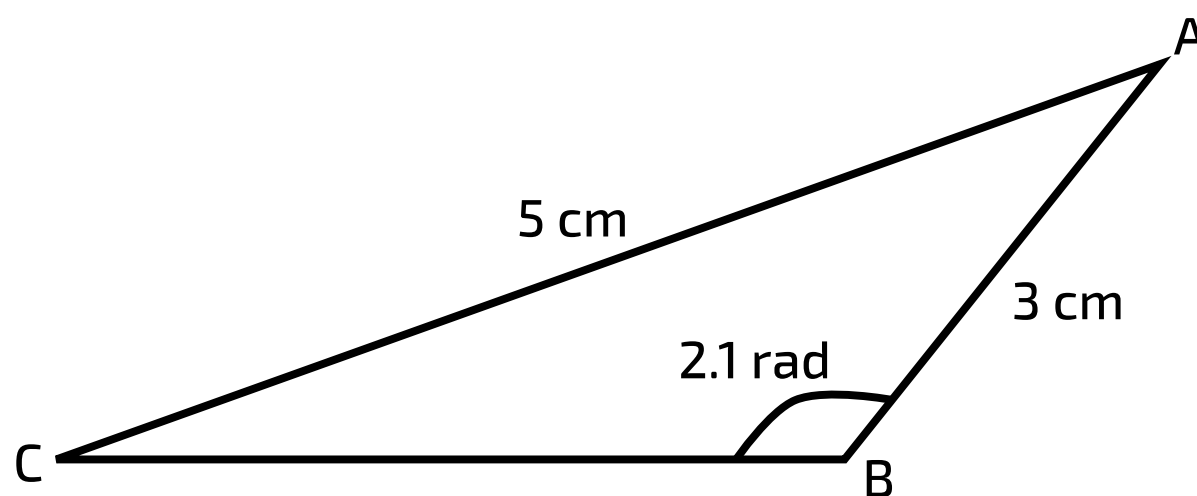
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# Radians 3i

A Level



**Figure 1** shows a triangle  $ABC$ , in which  $AB = 3\text{ cm}$ ,  $AC = 5\text{ cm}$  and angle  $ABC = 2.1\text{ radians}$ .



**Figure 1:** A triangle  $ABC$ .

## Part A Angle $ACB$

Calculate angle  $ACB$ , giving your answer in radians.

## Part B Area

Calculate the area of the triangle.

## Part C Perimeter of a sector

An arc of a circle with centre  $A$  and radius  $3\text{ cm}$  is drawn, cutting  $AC$  at the point  $D$ .

Calculate the perimeter of the sector  $ADB$ .

## Part D Area of a sector

An arc of a circle with centre  $A$  and radius 3 cm is drawn, cutting  $AC$  at the point  $D$ .

Calculate the area of the sector  $ADB$ .

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# Small Angle Approximations 1ii

A Level



$$f(x) = \frac{\sin(x) + \tan(2x)}{\tan(x) + 2}$$

## Part A Small angle approximation

Use the small angle approximation to write an approximate expression to second order for  $f(x)$ , valid when  $x$  is small.

The following symbols may be useful:  $f$ ,  $x$

## Part B Estimation

Use your expression to estimate the value of  $f(0.1)$  to 4 significant figures.

## Part C Percentage error

What is the percentage error in this estimate? Give your answer to 3 significant figures.

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# Small Angle Approximations 1i

A Level  
P P P

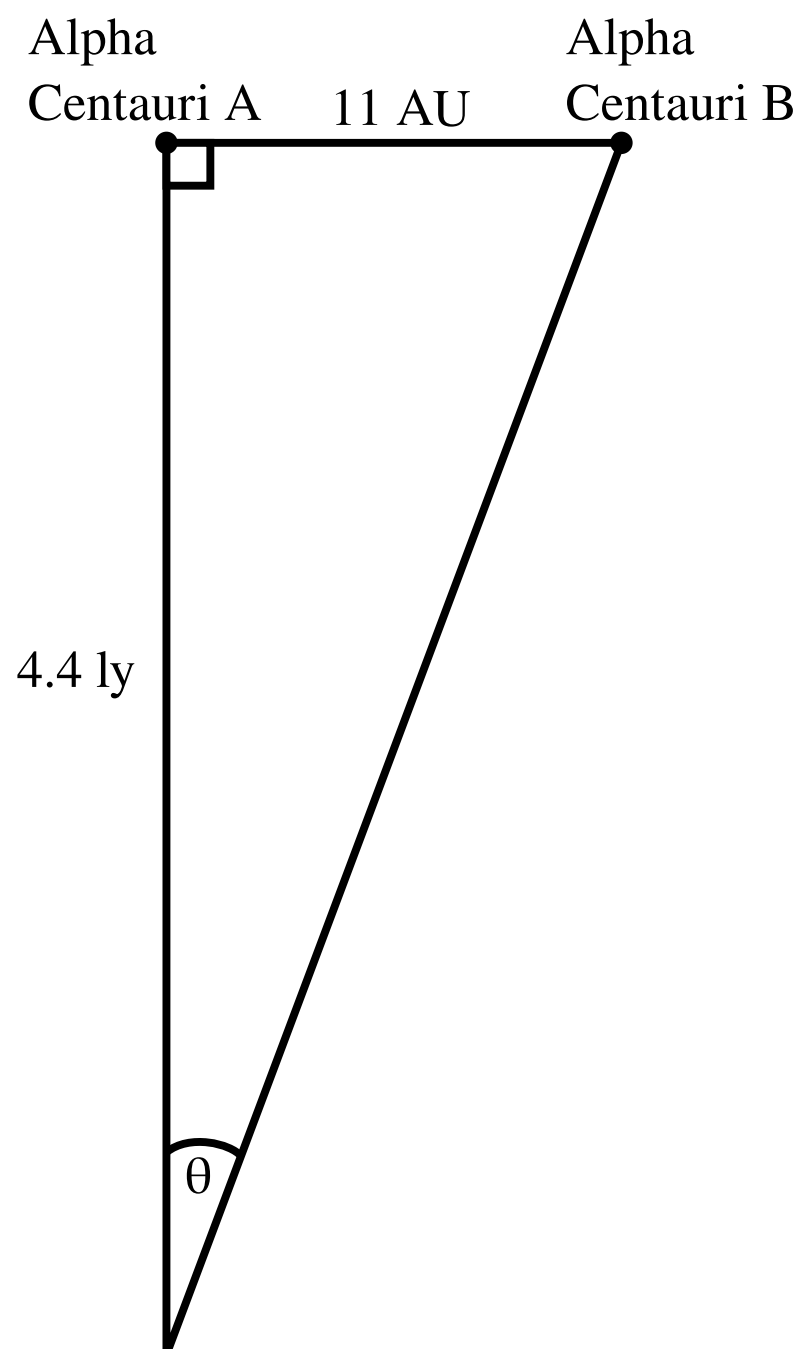
The small angle approximation is used when measuring distances in astronomy.

The two stars Alpha Centauri A and Alpha Centauri B are in a binary pair (they orbit one another). The distance between them is an average of 11 Astronomical Units, and they are an average of 4.4 light years from Earth.

1 AU = 1 Astronomical Unit = 149 597 870 700 m

1 ly = 1 Light Year =  $9.4607 \times 10^{15}$  m

Assume that a telescope is pointing straight at Alpha Centauri A with the geometry shown in [Figure 1](#).



**Figure 1:** A telescope pointing straight at Alpha Centauri A

Use the small angle approximation to estimate  $\theta$ , the angular separation between the stars as seen by the telescope. Give your answer to 2 significant figures.

## Part A   Radians

Give the answer in radians.

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## Part B   Degrees

Give the answer in degrees.

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## Part C   Arc Seconds

Give the answer in Arc Seconds. (Where 1 arc second is one  $(\frac{1}{3600})^{\text{th}}$  of a degree.)

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**Pure Maths Practice: Small Angle Approximations**

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