



## Solving Equations & Logs 3ii



### Part A Express log

Express  $\log_3(4x + 7) - \log_3 x$  as a single logarithm.

The following symbols may be useful:  $\ln()$ ,  $\log()$ ,  $\times$

### Part B Solve equation

Hence solve the equation  $\log_3(4x + 7) - \log_3 x = 2$ . Give your answer in decimal form.

### Part C Use logs

Use logarithms to solve the equation  $7^x = 2^{x+1}$ , giving the value of  $x$  correct to 3 significant figures.

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# Log Laws 2ii

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## Part A Express as a single log (i)

Express  $\log_a 2 + \log_a 3$  as a single logarithm.

The following symbols may be useful:  $a$ ,  $\log()$

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## Part B Express as a single log (ii)

Express  $2\log_{10} x - 3\log_{10} y$  as a single logarithm.

The following symbols may be useful:  $\log()$ ,  $x$ ,  $y$

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# Log Laws 1i



## Part A Log laws

Given that  $\log_a(x) = p$  and  $\log_a(y) = q$ , express  $\log_a(xy)$  in terms of  $p$  and  $q$ .

The following symbols may be useful:  $p$ ,  $q$

## Part B Simplify 1

Given that  $\log_a(x) = p$  and  $\log_a(y) = q$ , express  $\log_a\left(\frac{a^2x^3}{y}\right)$  in terms of  $p$  and  $q$ .

The following symbols may be useful:  $p$ ,  $q$

## Part C Simplify 2

Express  $\log_{10}(x^2 - 10) - \log_{10}x$  as a single logarithm

The following symbols may be useful:  $\log()$ ,  $x$

## Part D Solve equation

Solve the equation  $\log_{10}(x^2 - 10) - \log_{10}x = 2\log_{10}3$ .



# Solving Equations & Logs 3i



## Part A Solve equation

Solve the equation  $2^{4x-1} = 3^{5-2x}$ , giving your answer in the form  $x = \frac{\log_{10} a}{\log_{10} b}$ .

The following symbols may be useful:  $\log()$ ,  $\times$

## Part B Find integer

Find the smallest integer  $n$  which satisfies the inequality  $7^{2n} > e^{600}$ .

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# Exponential equation 1

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A Level Further A



Solve the following for  $y$ :  $4^y = 8^{y+1}$

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## Exponential equation 3

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A Level Further A



Solve the following for  $m$ :  $\frac{1}{9^m} = 27^{1-m}$ .

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## Exponential equation 2

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A Level   Further A



Solve the following for  $x$ :  $3^x = \frac{1}{9^{x-\frac{9}{4}}}$ .

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# Log Laws 1ii



## Part A Express in terms of $\log_2(x)$ (i)

Express  $\log_2(x^2)$  in terms of  $\log_2(x)$ .

The following symbols may be useful:  $\ln()$ ,  $\log()$ ,  $\times$

## Part B Express in terms of $\log_2(x)$ (ii)

Express  $\log_2(8x^2)$  in terms of  $\log_2(x)$ .

The following symbols may be useful:  $\ln()$ ,  $\log()$ ,  $\times$

## Part C Find $\log_3 y$

Given that  $y^2 = 27$ , find the value of  $\log_3 y$ .

The following symbols may be useful:  $\ln()$ ,  $\log()$ ,  $y$





## Solving Equations & Logs 1ii

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### Part A Solve equation (i)

Use logarithms to solve the equation  $5^{x-1} = 120$  for  $x$ , giving your answer correct to 3 significant figures.

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### Part B Solve equation (ii)

Solve the equation  $\log_2 x + 2\log_2 3 = \log_2(x + 5)$ . Give the value of  $x$  correct to 3 significant figures.

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# Log Laws 1i



It is given that  $\ln x = p + 2$  and  $\ln y = 3p$

## Part A   Log laws

Express  $\ln(xy)$  in terms of  $p$ .

The following symbols may be useful:  $p$

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## Part B   Simplify 1

Express  $\ln(x^3)$  in terms of  $p$ .

The following symbols may be useful:  $p$

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## Part C   Simplify 2

Express  $\ln\left(\frac{y}{e}\right)$  in terms of  $p$ .

The following symbols may be useful:  $p$

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## Part D   Solve equation

Express  $y$  in terms of  $x$  and  $e$ , simplifying your answer.

The following symbols may be useful:  $e$ ,  $x$ ,  $y$

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