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# Indefinite integrals 1



Find the following indefinite integrals.

$$\textbf{Part A} \quad \ \, \textbf{Integrate} \ (3x-1)(x+1) \\$$

Find 
$$\int (3x-1)(x+1)dx$$
.

The following symbols may be useful:  $k\,\text{,}\ \ x$ 

## Part B Integrate $(\sqrt{p}-(1/p))^2$

Find 
$$\int \left(\sqrt{p}-rac{1}{p}
ight)^2 \mathrm{d}p$$
.

The following symbols may be useful: k, p

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# **Equation of curve**



A function 
$$v(u)$$
 is such that  $rac{\mathrm{d}v}{\mathrm{d}u}=rac{1}{3}u^{rac{1}{3}}\left(1-rac{1}{u}
ight)$  and  $v(8)=-1.$ 

Find the equation of the function v(u).

The following symbols may be useful:  $\boldsymbol{u}_{\text{+}} \boldsymbol{v}$ 

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# Indefinite integrals 2



Find the following indefinite integrals.

Part A Integrate 
$$(q^2+3)/q^{rac{5}{2}}$$

Find 
$$\int rac{q^2+3}{q^{5/2}} \mathrm{d}q$$
.

The following symbols may be useful: k, q

Part B Integrate 
$$2z(z^2-1)(z^2+1)$$

Find 
$$\int 2z(z^2-1)(z^2+1)dz$$
.

The following symbols may be useful: k,  $\ z$ 

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Area under a curve 3

## Area under a curve 3



A graph of the functions  $y=\frac{1}{2\sqrt{x}}$  and  $y=2x\sqrt{x}$  for  $x\geq 0$  is shown in **Figure 1**. Find the area of the shaded region OPQR.

Figure 1: A graph of the functions  $y=\frac{1}{2\sqrt{x}}$  and  $y=2x\sqrt{x}$  for  $x\geq 0$ . The shaded region OPQR is bounded by the line x=0, the line y=1, the curve  $y=\frac{1}{2\sqrt{x}}$  and the curve  $y=2x\sqrt{x}$ .

#### Part A The x coordinate of Q

Deduce the x coordinate of the point Q.

#### Part B The x coordinate of R

Find the  $\boldsymbol{x}$  coordinate of the point R.

#### Part C The area of OPOR

Find the area of the shaded region OPQR, giving your answer in an exact form.

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## **Integrating Powers 4**



Part A Integrate  $(A/r^7 - B/r^{13})$ 

Find 
$$\int_{a}^{\infty} \left( rac{A}{r^7} - rac{B}{r^{13}} 
ight) \mathrm{d}r.$$

(The force between, for example, two atoms of an inert gas, a distance r apart is given by  $\left(\frac{A}{r^7} - \frac{B}{r^{13}}\right)$ , where A and B are (negative) constants; the first term is the attractive force between them (the van der Waals interaction, due to their fluctuating induced dipoles) and the second is the repulsive force due to the overlap of their electron shells. The integral describes the potential energy of such a system i.e. the work done bringing one atom from infinity to within a distance a of the other atom.)

Find 
$$\int_a^\infty \left(rac{A}{r^7} - rac{B}{r^{13}}
ight) \mathrm{d}r.$$

The following symbols may be useful: A, B, a

Part B Integrate  $(C/x^2 + D)$ 

Find 
$$\int_{x_1}^{x_2} \left( rac{C}{x^2} + D 
ight) \mathrm{d}x.$$

(The function  $\left(\frac{C}{x^2}+D\right)$  could describe the component of an electric field in the x-direction due to a combination of the field due to a point charge at the origin and a uniform field in the x-direction. The integral is then the potential difference between two points  $x_1$  and  $x_2$  on the x-axis.)

Find 
$$\int_{x_1}^{x_2} \left( rac{C}{x^2} + D 
ight) \mathrm{d}x.$$

The following symbols may be useful: C, D,  $x_1$ ,  $x_2$ 

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# **Integrating Powers 2**

### Part A Integrate $ax^{-8}$

Find the indefinite integral of  $ax^{-8}$ , where a is a constant.

The following symbols may be useful: a,  $\ k$ ,  $\ x$ 

## Part B Integrate $4/x^2$

Find 
$$\int_1^2 \frac{4}{x^2} dx$$
.

The following symbols may be useful:  $k\,\text{,}\ \ x$ 

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