

# Logic Coverage Overview part 1



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# Outcomes

At the end of Today's Lecture you will be able to:

- Understand the basic concepts and notation for logic coverage
- Understand the different types of logic coverage criteria

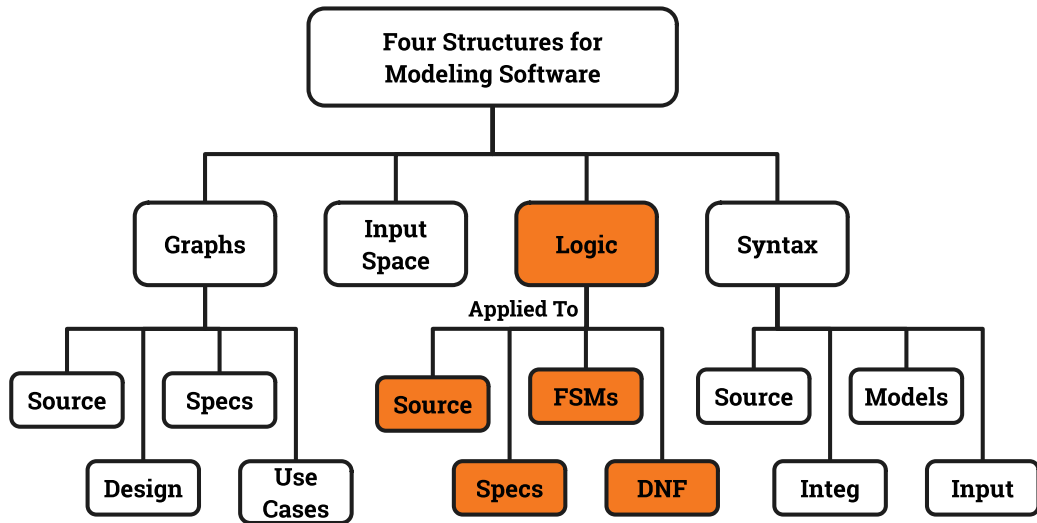


# Inspiration

“The trouble with programmers is that you can never tell what a programmer is doing until it's too late.” – Seymour Cray



# Logic Coverage





# Semantic Logic Criteria

- Logic expressions show up in many situations
- Covering logic expressions is required by the US Federal Aviation Administration for safety critical software
  - Used by other transportation industries
- Logical expressions can come from many sources
  - Decisions in programs
  - FSMs and statecharts
  - Requirements
- Tests are intended to choose some subset of the total number of truth assignments to the expressions



# Logic Predicates and Clauses

- A **predicate** is an expression that evaluates to a **Boolean** value
- Predicates can contain
  - **Boolean variables**
  - non-Boolean variables that contain  $>$ ,  $<$ ,  $==$ ,  $>=$ ,  $<=$ ,  $!=$
  - Boolean **function** calls
- Internal structure is created by logical operators
  - $\neg$  – the negation operator
  - $\wedge$  – the and operator
  - $\vee$  – the or operator
  - $\Rightarrow$  – the implication operator
  - $\oplus$  – the exclusive or operator
  - $\Leftrightarrow$  – the equivalence operator



# Example and Facts

- $(a < b) \vee f(z) \wedge D \wedge (m \geq n * o)$  has four clauses:
  - $(a < b)$  - relational expression
  - $f(z)$  - Boolean-valued function
  - $D$  - Boolean variable
  - $(m \geq n * o)$  - relational expression
- Most predicates have **few clauses**
  - 88.5% have 1 clause
  - 9.5% have 2 clauses
  - 1.35% have 3 clauses
  - Only 0.65% have 4 or more



# Example and Facts

- **Sources** of predicates
  - Decisions in **programs**
  - Guards in **finite state machines**
  - Decisions in **UML** activity graphs
  - **Requirements**, both formal and informal
  - **SQL** queries





# Translating from English

- “I am interested in CS 4422 and CS 4458”
- course = cs4422 **OR** course = cs4458
  - Humans have trouble translating from English to Logic
- “If you leave before 6:30 AM, take Braddock to 495, if you leave after 7:00 AM, take Prosperity to 50, then 50 to 495”
- $(time < 6 : 30 \Rightarrow path = Braddock) \wedge (time > 7 : 00 \Rightarrow path = Prosperity)$
- Hmm ... this is incomplete!
- $(time < 6 : 30 \Rightarrow path = Braddock) \wedge (time \geq 6 : 30 \Rightarrow path = Prosperity)$



# Logic Coverage Criteria

- We use predicates in testing as follows:
  - Developing a model of the software as one or more predicates
  - Requiring tests to satisfy some combination of clauses
- Abbreviations:
  - $P$  is the set of predicates
  - $p$  is a single predicate in  $P$
  - $C$  is the set of clauses in  $P$
  - $C_p$  is the set of clauses in predicate  $p$
  - $c$  is a single clause in  $C$

# Predicate and Clause Coverage

- The first (and simplest) two criteria require that each predicate and each clause be evaluated to both true and false

## Predicate Coverage (PC)

For each  $p$  in  $P$ ,  $TR$  contains two requirements:  $p$  evaluates to true, and  $p$  evaluates to false.

- When predicates come from conditions on edges, this is equivalent to edge coverage
- PC does not evaluate all the clauses, so ...

## Clause Coverage (CC)

For each  $c$  in  $C$ ,  $TR$  contains two requirements:  $c$  evaluates to true, and  $c$  evaluates to false.

# Predicate Coverage Example

$$((a < b) \vee D) \wedge (m \geq n * o)$$

Predicate = true

$$\begin{aligned} a = 5, b = 10, D = \text{true}, m = 1, n = 1, o = 1 \\ &= (5 < 10) \vee \top \wedge (1 \geq 1 * 1) \\ &= t \vee t \wedge \top \\ &= \top \end{aligned}$$

Predicate = false

$$\begin{aligned} a = 10, b = 5, D = \text{false}, m = 1, n = 1, o = 1 \\ &= (10 < 5) \vee \text{false} \wedge (1 \geq 1 * 1) \\ &= \text{false} \vee \text{false} \wedge \top \\ &= \text{false} \end{aligned}$$

# Clause Coverage Example

## True Cases

expression	a	b	D	m	n	o
$(a < b)$	5	10	–	–	–	–
D	–	–	true	–	–	–
$(m \geq n * o)$	–	–	–	1	1	1

## False Cases

expression	a	b	D	m	n	o
$(a < b)$	10	5	–	–	–	–
D	–	–	false	–	–	–
$(m \geq n * o)$	–	–	–	1	2	2

These yield the following two tests:

- 1 a = 5, b = 10, D = true, m = 1, n = 1, o = 1
- 2 a = 10, b = 5, D = false, m = 1, n = 2, o = 2



# Problems with PC and CC

- PC does not **fully exercise** all the clauses, especially in the presence of short circuit evaluation
- CC does not always **ensure PC**
  - That is, we can satisfy CC without causing the predicate to be both true and false
  - This is definitely not what we want!
- The simplest solution is to test **all combinations...**



# Combinatorial Coverage

- CoC requires every possible combination
- Sometimes called Multiple Condition Coverage

## Combinatorial Coverage (CoC)

For each  $p$  in  $P$ ,  $TR$  has test requirements for the clauses in  $C_p$  to evaluate to each possible combination of true values

	$a < b$	$D$	$m \geq n * o$	$((a < b) \vee D) \wedge (m \geq n * o)$
1	T	T	T	T
2	T	T	F	F
3	T	F	T	T
4	T	F	F	F
5	F	T	T	T
6	F	T	F	F
7	F	F	T	F
8	F	F	F	F



# Combinatorial Coverage

- This is simple, neat, clean, and comprehensive
- But quite **expensive!**
- $2^N$  tests, where  $N$  is the number of clauses
  - Impractical for predicates with more than 3 or 4 clauses
- The literature has lots of suggestions - some confusing
- The general idea is simple: **Test each clause independently from the other clauses**
- Getting the details right is hard
- What exactly does “independently” mean?
- The book presents this idea as “**making clauses active**” ...



# Active Clauses

- Clause coverage has a **weakness**: The values do not always make a difference
- Consider the first test for **clause coverage**, which caused each clause to be true:
  - $(5 < 10) \vee \text{true} \vee (1 \geq 1 * 1)$
- Only the first clause **counts**!
- To really test the results of a clause, the clause should be the **determining factor** in the value of the predicate

## Definition (Determination)

A clause  $C_i$  in predicate  $p$ , called the major clause, **determines**  $p$  if and only if the values of the remaining minor clauses  $C_j$  are such that changing  $C_i$  changes the value of  $p$ .

- This is called **making the clause active**

# Determining Predicates

$$\underline{P = A \vee B}$$

If  $B = \text{true}$ ,  $p$  is always true.  
so if  $B = \text{false}$ ,  $A$  determines  $p$   
if  $A = \text{false}$ ,  $B$  determines  $p$ .

$$\underline{P = A \wedge B}$$

If  $B = \text{false}$ ,  $p$  is always false.  
so if  $B = \text{true}$ ,  $A$  determines  $p$   
if  $A = \text{true}$ ,  $B$  determines  $p$ .

- **Goal:** Find tests for each clause when the clause determines the value of the predicate
- This is formalized in a **family of criteria** that have subtle, but very important, differences

# Active Clause Coverage

## Active Clause Coverage (ACC)

for each  $p \in P$  and each major clause  $c_i \in C_p$ , choose minor clauses  $c_j, j \neq i$ , so that  $c_i$  determines  $p$ .  $TR$  has two requirements for each  $c_i$ ;  $c_i$  evaluates to true and  $c_i$  evaluates to false.

$$p = a \vee b$$

- ① **a = true**, b = false
- ② **a = false**, b = false
- ③ a = false, **b = true**
- ④ ~~a = false~~, ~~b = false~~

in 1 & 2  $a$  is major, and in  
3 & 4  $b$  is major.

- This is a form of **MCDC**, which is required by the FAA for safety critical software
- **Ambiguity**: Do the minor clauses have to have the **same values** when the major clause is true and false?



# Resolving the Ambiguity

$$p = a \vee (b \wedge c)$$

Major clause:  $a$

$a = \text{true}, b = \text{false}, c = \text{true}$

$a = \text{false}, b = \text{false}, c = \text{false}$

is  $c = \text{false}$  allowed?

- This question caused **confusion** among testers for years
- Considering this carefully leads to **three** separate criteria:
  - Minor clauses **do not** need to be the same
  - Minor clauses **do** need to be the same
  - Minor clauses **force the predicate** to become both true and false



**Are there any questions?**