

# Grammar-based Testing



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# Outcomes

At the end of Today's Lecture you will be able to:

- Understand the use of mutation testing in source code
- Understand several of the Java Mutation operators
- Understand mutation coverage criteria for source code



# Inspiration

"A tester has the heart of a developer...

in a jar on the desk..." – Anonymous

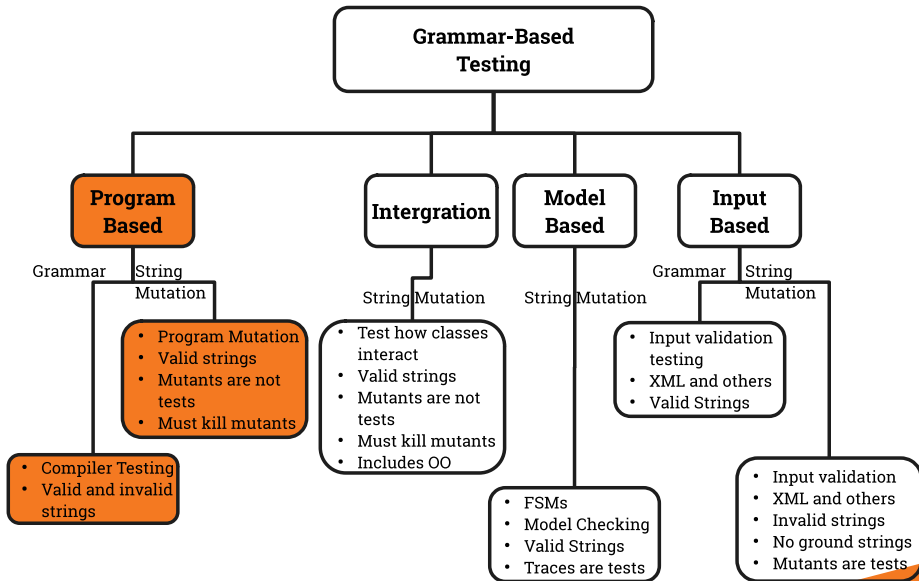


# Applying Syntax-Based Testing

- Syntax-based criteria **originated** with programs and have been used mostly with programs
- **BNF criteria** are most commonly used to test compilers
- **Mutation testing** criteria are most commonly used for unit testing and integration testing of classes



# Instantiating Grammar-Based Testing





# BNF Testing for Compilers

- Testing **compilers** is very complicated
  - Millions of **correct** programs!
  - Compilers must recognize and reject **incorrect** programs
- **BNF criteria** can be used to generate programs to test all language features that compilers must process
- This is a very **specialized** application and not discussed in detail



# Program-based Grammars

- The original and most widely known application of syntax-based testing is to **modify programs**
- **Operators** modify a **ground string** (program under test) to create **mutant program**
- Mutant programs must compile correctly (**valid strings**)
- Mutants are **not tests**, but used to find tests
- Once mutants are defined, **tests** must be found to cause mutants to fail when executed
- This is called "**Killing Mutants**"



# Killing Mutants

Given a mutant  $m \in M$  for a ground string program  $P$  and a test  $t$ ,  $t$  is said to **kill**  $m$  if and only if the output of  $t$  on  $P$  is different from the output of  $t$  on  $m$ .

- If mutation operators are designed well, the resulting tests will be very powerful
- Different operators must be defined for programming languages and different goals
- Testers can keep adding tests until all mutants have been killed
  - **Dead mutant**: A test case has killed it
  - **Stillborn mutant**: Syntactically illegal
  - **Trivial mutant**: almost every test can kill it
  - **Equivalent mutant**: No test can kill it (same behavior as original)





# Program-based Grammars

## Original Method

```
int Min(int A, int B) {  
    int minVal;  
    minVal = A;  
    if (B < A)  
    {  
        minVal = B;  
    }  
    return(minVal);  
} // end Min
```

6 mutants

Each represents a  
separate program

## With Embedded Mutants

```
int Min(int A, int B) {  
    int minVal;  
    minVal = A;  
    Δ1 minVal = B;  
    if (B < A)  
    Δ2 if (B > A)  
    Δ3 if (B < minVal)  
    {  
        minVal = B;  
    Δ4 Bomb();  
    Δ5 minVal = A;  
    Δ6 minVal = failOnZero(B);  
    }  
    return(minVal);  
} // end Min
```

Replace one variable  
with another

Replaces operator

Immediate runtime  
failure ... if reached

Immediate runtime  
failure if B == 0, else  
does nothing

# Syntax-Based Coverage Criteria

## Mutation Coverage (MC):

For each  $m \in M$ , TR contains exactly one requirement, to kill  $m$ .

- The RIPR model from Chapter 2:
  - **Reachability**: The test causes the **faulty statement** to be reached (in mutation – the **mutated** statement)
  - **Infection**: The test causes the faulty statement to result in an **incorrect state**
  - **Propagation**: The incorrect state **propagates** to incorrect output
  - **Revealability**: The tester must **observe** part of the incorrect output
- The RIPR model leads to **two variants** of mutation coverage...



# Syntax-Based Coverage Criteria

- ① **Strongly Killing Mutants:** Given a mutant  $m \in M$  for a program  $P$  and a test  $t$ ,  $t$  is said to **strongly kill**  $m$  iff the **output** of  $t$  on  $P$  is different from the output of  $t$  on  $m$
- ② **Weakly Killing Mutants:** Given a mutant  $m \in M$  that modifies a location  $l$  in a program  $P$ , and a test  $t$ ,  $t$  is said to **weakly kill**  $m$  iff the **state** of the execution of  $P$  on  $t$  is different from the state of the execution of  $m$  on  $t$  immediately after  $l$ 
  - Weakly killing satisfies **reachability** and **infection**, but not **propagation**



# Weak Mutation

## Weak Mutation Coverage (WMC):

For each  $m \in M$ , TR contains exactly one requirement, to weakly kill  $m$ .

- “Weak mutation” is so named because it is **easier to kill** mutants under this assumption
- Weak mutation also requires **less analysis**
- A few mutants can be killed under weak mutation but not under strong mutation (**no propagation**)
- Studies have found that test sets that weakly kill all mutants also strongly kill most mutants



# Weak Mutation Example

- Mutant 1 in the Min() example is:

```
minVal = A;  
Δ1 minVal = B;  
if (B < A)  
    minVal = B;
```

- The complete test specification to kill mutant 1:
  - **Reachability:** `true` // Always get to that statement
  - **Infection:**  $A \neq B$
  - **Propagation:**  $(B < A) = \text{false}$  // skip the next assignment
  - **Full Test Specification:**  $\text{true} \wedge (A \neq B) \wedge ((B < A) = \text{false})$   
 $\equiv (A \neq B) \wedge (B \geq A)$   
 $\equiv (B > A)$
  - Weakly kill mutant 1, but not strongly?



# Equivalent Mutation Example

- Mutant 3 in the Min() example is equivalent:

```
minVal = A;  
if (B < A)  
Δ3 if(B < minVal)
```

- The infection condition is “**(B < A) != (B < minVal)**”
- However, the previous statement was “**minVal = A**”
  - Substituting, we get: “**(B < A) != (B < A)**”
  - This is a logical **contradiction!**
- **Thus no input can kill this mutant**



# Strong Versus Weak Mutation

```
1  boolean isEven(int X)
2  {
3      if (X < 0)
4          X = 0 - X;
5      Δ4    X = 0;
6      if ((double) (X / 2) == ((double) X) / 2.0)
7          return true;
8      else
9          return false;
10 }
```

Reachability:  $X < 0$

Infection:  $X \neq 0$

( $X = -6$ ) will kill  
mutant 4 under  
weak mutation

Propagation:

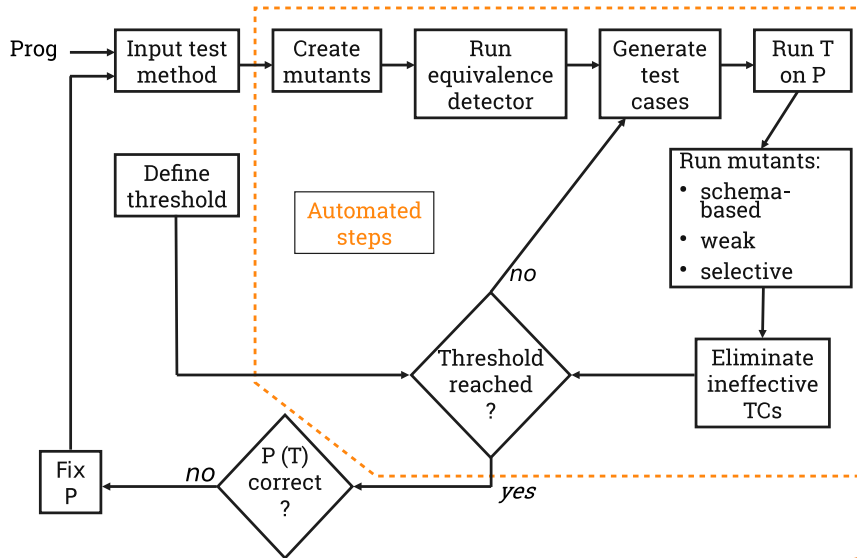
$((double) ((0 - X)/2) == ((double) 0 - X) / 2.0)$   
 $!= ((double) (0 / 2) == ((double) 0) / 2.0)$

That is, X is not even ...

Thus ( $X = -6$ ) does not kill the mutant under  
strong mutation



# Testing Programs with Mutation







# Why Mutation Works

## Fundamental Premise of Mutation Testing

If the software contains a fault, there will usually be a set of mutants that can only be killed by a test case that also detects that fault.

- This is not an absolute!
- The mutants guide the tester to an effective set of tests
- A very challenging problem:
  - Find a **fault** and a set of **mutation-adequate tests** that do **not** find the fault
- Of course, this depends on the mutation operators...



# Designing Mutation Operators

- At the **method level**, mutation operators for different programming languages are similar
- Mutation operators do one of **two things**:
  - Mimic typical programmer **mistakes** (incorrect variable name)
  - Encourage common test **heuristics** (cause expressions to be 0)
- Researchers design lots of operators, then experimentally **select** the most useful

## Effective Mutation Operators

If tests that are created specifically to kill mutants created by a collection of mutation operators  $O = o_1, o_2, \dots$  also kill mutants created by all remaining mutation operators with very high probability, then  $O$  defines an **effective** set of mutation operators.

# Mutation Operators for Java

- ① **ABS** – Absolute Value Insertion
- ② **AOR** – Arithmetic Operator Replacement
- ③ **ROR** – Relational Operator Replacement
- ④ **COR** – Conditional Operator Replacement
- ⑤ **SOR** – Shift Operator Replacement
- ⑥ **LOR** – Logical Operator Replacement
- ⑦ **ASR** – Assignment Operator Replacement
- ⑧ **UOI** – Unary Operator Insertion
- ⑨ **UOD** – Unary Operator Deletion
- ⑩ **SVR** – Scalar Variable Replacement
- ⑪ **BSR** – Bomb Statement Replacement



# Mutation Operators for Java

## ① ABS – Absolute Value Insertion:

Each arithmetic expression (and subexpression) is modified by the functions `abs()`, `negAbs()`, and `failOnZero()`

Examples:

```
a = m * (o + p);
```

```
Δ1 a = abs(m * (o + p));
```

```
Δ2 a = m * abs((o + p));
```

```
Δ3 a = failOnZero(m * (o + p));
```

## ② AOR – Arithmetic Operator Replacement:

Each occurrence of one of the arithmetic operators `+`, `-`, `*`, `/`, and `%` is replaced by each of the other operators. In addition, each is replaced by the special mutation operators `leftOp` and `rightOp`

Examples:

```
a = m * (o + p);
```

```
Δ1 a = m + (o + p);
```

```
Δ2 a = m * (o * p);
```

```
Δ3 a = m leftOp (o + p);
```



# Mutation Operators for Java (2)

## ③ ROR – Relational Operator Replacement:

Each occurrence of one of the relation operators ( $<$ ,  $\leq$ ,  $>$ ,  $\geq$ ,  $=$ ,  $\neq$ ) is replaced by each of the other operators and by `falseOp` and `trueOp`

Examples:

if ( $X \leq Y$ )

Δ1 if ( $X > Y$ )

Δ2 if ( $X < Y$ )

Δ3 if ( $X \text{ falseOp } Y$ ) // always returns false

## ④ COR – Conditional Operator Replacement:

Each occurrence of one of the logical operators (and - `&&`, or - `||`, and with no conditional evaluation - `&`, or with no conditional evaluation - `|`, not equivalent - `^`) is replaced by each of the other operators; in addition, each is replaced by `falseOp`, `trueOp`, `leftOp`, and `rightOp`

Examples:

if ( $X \leq Y \ \&\& \ a > 0$ )

Δ1 if ( $X \leq Y \ || \ a > 0$ )

Δ2 if ( $X \leq Y \ \text{leftOp} \ a > 0$ ) // returns result of left clause



# Mutation Operators for Java (3)

## 5 SOR – Shift Operator Replacement:

Each occurrence of one of the shift operators `<<`, `>>`, and `>>>` is replaced by each of the other operators. In addition, each is replaced by the special mutation operator `leftOp`

Examples:

```
byte b = (byte) 16;  
b = b >> 2;  
Δ1 b = b << 2;  
Δ2 b = b leftOp 2; // result if b
```

## 6 LOR – Logical Operator Replacement:

Each occurrence of one of the logical operators (bitwise and - `&`, bitwise or - `|`, exclusive or - `^`) is replaced by each of the other operators; in addition, each is replaced by `leftOp` and `rightOp`

Examples:

```
int a = 60; int b = 13;  
int c = a & b;  
Δ1 int c = a | b;  
Δ2 int c = a rightOp b; // result is b
```



# Mutation Operators for Java (4)

## 7 ASR – Assignment Operator Replacement:

Each occurrence of one of the assignment operators (`=`, `+=`, `-=`, `*=`, `/=`, `%=`, `&=`, `|=`, `^=`, `<<=`, `>>=`, `>>>=`) is replaced by each of the other operators

Examples:

```
a = m * (o + p);  
Δ1 a += m * (o + p);  
Δ2 a *= m * (o + p);
```

## 8 UOI – Unary Operator Insertion:

Each unary operator (arithmetic `+`, arithmetic `-`, conditional `!`, logical `~`) is inserted in front of each expression of the correct type

Examples:

```
a = m * (o + p);  
Δ1 a = m * -(o + p);  
Δ2 a = -(m * (o + p));
```



# Mutation Operators for Java (5)

## 9 UOD – Unary Operator Deletion:

Each unary operator (arithmetic +, arithmetic -, conditional !, logical ~) is deleted.

Examples:

```
if !(X <= Y && !Z)
Δ1 if !(X > Y && !Z)
Δ2 if !(X < Y && Z)
```

## 10 SVR – Scalar Variable Replacement:

Each variable reference is replaced by every other variable of the appropriate type that is declared in the current scope.

Examples:

```
a = m * (o + p);
Δ1 a = o * (o + p);
Δ2 a = m * (m + p);
Δ3 a = m * (o + o);
Δ4 p = m * (o + p);
```





# Mutation Operators for Java (6)

- ⑪ BSR – Bomb Statement Replacement:  
Each statement is replaced by a special Bomb() function

Examples:

```
a = m * (o + p);
```

**Δ1** Bomb() // Raises exception when reached



# Summary: Subsuming Other Criteria

- Mutation is widely considered the **strongest** test criterion
  - and most **expensive**!
  - By far the most test requirements (each mutant)
  - Usually the most tests
- Mutation **subsumes** other criteria by including specific mutation operators
- Subsumption can only be defined for **weak mutation** - other criteria only impose local requirements
  - Node coverage, Edge coverage, Clause coverage
  - General active clause coverage: **Yes-Requirement on single tests**
  - Correlated active clause coverage: **No-Requirement**



**Are there any questions?**