



## GRAMMAR-BASED TESTING

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*"A tester has the heart of a developer...*

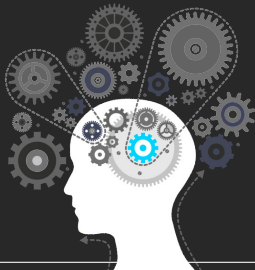
*in a jar on their desk..." – Anonymous*

# Outcomes



After today's lecture you will be able to:

- Understand the use of mutation testing in source code
- Understand several of the Java Mutation operators
- Understand mutation coverage criteria for source code

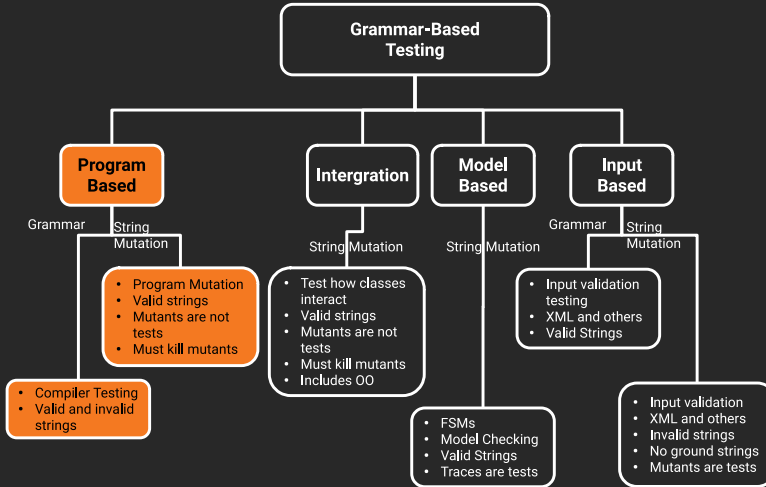


# Applying Syntax-Based Testing



- Syntax-based criteria **originated** with programs and have been used mostly with programs
- **BNF criteria** are most commonly used to test compilers
- **Mutation testing** criteria are most commonly used for unit testing and integration testing of classes

# Instantiating Grammar-Based Testing





- Testing **compilers** is very complicated
  - Millions of **correct** programs!
  - Compilers must recognize and reject **incorrect** programs
- **BNF criteria** can be used to generate programs to test all language features that compilers must process
- This is a very **specialized** application and not discussed in detail



- The original and most widely known application of syntax-based testing is to **modify programs**
- **Operators** modify a **ground string** (program under test) to create **mutant program**
- Mutant programs must compile correctly (**valid strings**)
- Mutants are **not tests**, but used to find tests
- Once mutants are defined, **tests** must be found to cause mutants to fail when executed
- This is called **"Killing Mutants"**

**Definition:** Given a mutant  $m \in M$  for a ground string program  $P$  and a test  $t$ ,  $t$  is said to **kill**  $m$  if and only if the output of  $t$  on  $P$  is different from the output of  $t$  on  $m$ .

- If mutation operators are designed well, the resulting tests will be very powerful
- Different operators must be defined for programming languages and different goals
- Testers can keep adding tests until all mutants have been killed
  - **Dead mutant:** A test case has killed it
  - **Stillborn mutant:** Syntactically illegal
  - **Trivial mutant:** almost every test can kill it
  - **Equivalent mutant:** No test can kill it (same behavior as original)



## Original Method

```
int Min(int A, int B) {  
    int minVal;  
    minVal = A;  
    if (B < A)  
    {  
        minVal = B;  
    }  
    return(minVal);  
} // end Min
```

6 mutants

Each represents a  
separate program

## With Embedded Mutants

```
int Min(int A, int B) {  
    int minVal;  
    minVal = A;  
    Δ1 minVal = B;  
    if (B < A)  
    Δ2 if (B > A)  
    Δ3 if (B < minVal)  
    {  
        minVal = B;  
    Δ4 Bomb();  
    Δ5 minVal = A;  
    Δ6 minVal = failOnZero(B);  
    }  
    return(minVal);  
} // end Min
```

Replace one variable  
with another

Replaces operator

Immediate runtime  
failure ... if reached

Immediate runtime  
failure if B == 0, else  
does nothing

**Mutation Coverage (MC)**: For each  $m \in M$ , TR contains exactly one requirement, to kill  $m$ .

- The RIPR model from Chapter 2:
  - **Reachability**: The test causes the **faulty statement** to be reached (in mutation – the **mutated** statement)
  - **Infection**: The test causes the faulty statement to result in an **incorrect state**
  - **Propagation**: The incorrect state **propagates** to incorrect output
  - **Revealability**: The tester must **observe** part of the incorrect output
- The RIPR model leads to **two variants** of mutation coverage...

# Syntax-Based Coverage Criteria



**Strongly Killing Mutants:** Given a mutant  $m \in M$  for a program  $P$  and a test  $t$ ,  $t$  is said to **strongly kill**  $m$  iff the **output** of  $t$  on  $P$  is different from the output of  $t$  on  $m$

**Weakly Killing Mutants:** Given a mutant  $m \in M$  that modifies a location  $l$  in a program  $P$ , and a test  $t$ ,  $t$  is said to **weakly kill**  $m$  iff the **state** of the execution of  $P$  on  $t$  is different from the state of the execution of  $m$  on  $t$  immediately after  $l$

- Weakly killing satisfies **reachability** and **infection**, but not **propagation**

**Weak Mutation Coverage (WMC):** For each  $m \in M$ , TR contains exactly one requirement, to weakly kill  $m$ .

- “Weak mutation” is so named because it is **easier to kill** mutants under this assumption
- Weak mutation also requires **less analysis**
- A few mutants can be killed under weak mutation but not under strong mutation (**no propagation**)
- Studies have found that test sets that weakly kill all mutants also strongly kill most mutants

# Weak Mutation Example



Mutant 1 in the Min() example is:

```
minVal = A;  
Δ1 minVal = B;  
if (B < A)  
    minVal = B;
```

- The complete test specification to kill mutant 1:
  - **Reachability**: `true` // Always get to that statement
  - **Infection**:  $A \neq B$
  - **Propagation**:  $(B < A) = \text{false}$  // skip the next assignment
  - **Full Test Specification**:  
 $\text{true} \wedge (A \neq B) \wedge ((B < A) = \text{false})$   
 $\equiv (A \neq B) \wedge (B \geq A)$   
 $\equiv (B > A)$
  - Weakly kill mutant 1, but not strongly?

# Equivalent Mutation Example



Mutant 3 in the Min() example is equivalent:

```
minVal = A;  
if (B < A)  
Δ3 if(B < minVal)
```

- The infection condition is “**(B < A) != (B < minVal)**”
- However, the previous statement was “**minVal = A**”
  - Substituting, we get: “**(B < A) != (B < A)**”
  - This is a logical **contradiction**!
- **Thus no input can kill this mutant**

# Strong Versus Weak Mutation



```
1  boolean isEven(int X)
2  {
3      if (X < 0)
4          X = 0 - X;
5      if ((double) (X / 2) == ((double) X) / 2.0)
6          return true;
7      else
8          return false;
9  }
```

Reachability:  $X < 0$

Infection:  $X \neq 0$

( $X = -6$ ) will kill  
mutant 4 under  
weak mutation

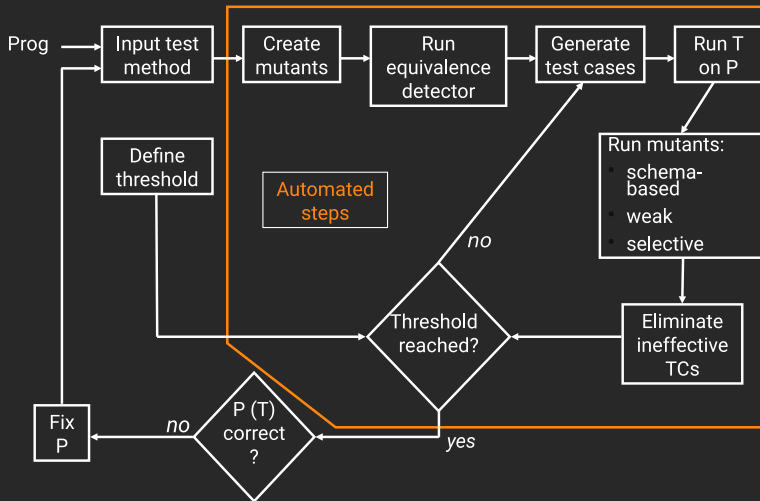
Propagation:

$((\text{double}) ((0 - X)/2) == ((\text{double}) 0 - X) / 2.0)$   
 $!= ((\text{double}) (0 / 2) == ((\text{double}) 0) / 2.0)$

That is,  $X$  is not even ...

Thus ( $X = -6$ ) does not kill the mutant under  
strong mutation

# Testing Programs with Mutation





## Fundamental Premise of Mutation Testing

If the software contains a fault, there will usually be a set of mutants that can only be killed by a test case that also detects that fault.

- This is not an absolute!
- The mutants guide the tester to an effective set of tests
- A very challenging problem:
  - Find a **fault** and a set of **mutation-adequate tests** that do **not** find the fault
- Of course, this depends on the mutation operators...

- At the **method level**, mutation operators for different programming languages are similar
- Mutation operators do one of **two things**:
  - Mimic typical programmer **mistakes** (incorrect variable name)
  - Encourage common test **heuristics** (cause expressions to be 0)
- Researchers design lots of operators, then experimentally **select** the most useful

## Effective Mutation Operators

If tests that are created specifically to kill mutants created by a collection of mutation operators  $O = o_1, o_2, \dots$  also kill mutants created by all remaining mutation operators with very high probability, then  $O$  defines an **effective** set of mutation operators.

# Mutation Operators for Java



1. **ABS** – Absolute Value Insertion
2. **AOR** – Arithmetic Operator Replacement
3. **ROR** – Relational Operator Replacement
4. **COR** – Conditional Operator Replacement
5. **SOR** – Shift Operator Replacement
6. **LOR** – Logical Operator Replacement
7. **ASR** – Assignment Operator Replacement
8. **UOI** – Unary Operator Insertion
9. **UOD** – Unary Operator Deletion
10. **SVR** – Scalar Variable Replacement
11. **BSR** – Bomb Statement Replacement

1. **ABS – Absolute Value Insertion:** Each arithmetic expression (and subexpression) is modified by the functions `abs()`, `negAbs()`, and `failOnZero()`

Examples:

```
a = m * (o + p);
```

```
Δ1 a = abs(m * (o + p));
```

```
Δ2 a = m * abs((o + p));
```

```
Δ3 a = failOnZero(m * (o + p));
```

2. **AOR – Arithmetic Operator Replacement:** Each occurrence of one of the arithmetic operators `+`, `-`, `*`, `/`, and `%` is replaced by each of the other operators. In addition, each is replaced by the special mutation operators `leftOp` and `rightOp`

Examples:

```
a = m * (o + p);
```

```
Δ1 a = m + (o + p);
```

```
Δ2 a = m * (o * p);
```

```
Δ3 a = m leftOp (o + p);
```

# Mutation Operators for Java (2)



- 3. ROR – Relational Operator Replacement:** Each occurrence of one of the relation operators ( $<$ ,  $\leq$ ,  $>$ ,  $\geq$ ,  $=$ ,  $\neq$ ) is replaced by each of the other operators and by `falseOp` and `trueOp`

Examples:

```
if (X <= Y)
```

**Δ1** `if (X > Y)`

**Δ2** `if (X < Y)`

**Δ3** `if (X falseOp Y) // always returns false`

- 4. COR – Conditional Operator Replacement:** Each occurrence of one of the logical operators (and - `&&`, or - `||`, and with no conditional evaluation - `&`, or with no conditional evaluation - `|`, not equivalent - `^`) is replaced by each of the other operators; in addition, each is replaced by `falseOp`, `trueOp`, `leftOp`, and `rightOp`

Examples:

```
if (X <= Y && a > 0)
```

**Δ1** `if (X <= Y || a > 0)`

**Δ2** `if (X <= Y leftOp a > 0) // returns result of left clause`

# Mutation Operators for Java (3)



5. **SOR – Shift Operator Replacement:** Each occurrence of one of the shift operators `<<`, `>>`, and `>>>` is replaced by each of the other operators. In addition, each is replaced by the special mutation operator `leftOp`

Examples:

```
byte b = (byte) 16;  
b = b >> 2;  
Δ1 b = b << 2;  
Δ2 b = b leftOp 2; // result if b
```

6. **LOR – Logical Operator Replacement:** Each occurrence of one of the logical operators (bitwise and - `&`, bitwise or - `|`, exclusive or - `^`) is replaced by each of the other operators; in addition, each is replaced by `leftOp` and `rightOp`

Examples:

```
int a = 60; int b = 13;  
int c = a & b;  
Δ1 int c = a | b;  
Δ2 int c = a rightOp b; // result is b
```

- 7. ASR – Assignment Operator Replacement:** Each occurrence of one of the assignment operators (`=`, `+=`, `-=`, `*=`, `/=`, `%=`, `&=`, `|=`, `^=`, `<<=`, `>>=`, `>>>=`) is replaced by each of the other operators

Examples:

```
a = m * (o + p);
```

```
Δ1 a += m * (o + p);
```

```
Δ2 a *= m * (o + p);
```

- 8. UOI – Unary Operator Insertion:** Each unary operator (arithmetic `+`, arithmetic `-`, conditional `!`, logical `~`) is inserted in front of each expression of the correct type

Examples:

```
a = m * (o + p);
```

```
Δ1 a = m * -(o + p);
```

```
Δ2 a = -(m * (o + p));
```

# Mutation Operators for Java (5)



9. **UOD – Unary Operator Deletion:** Each unary operator (arithmetic +, arithmetic -, conditional !, logical ~) is deleted.

Examples:

```
if !(X <= Y && !Z)
```

**Δ1** if !(X > Y && !Z)

**Δ2** if !(X < Y && Z)

10. **SVR – Scalar Variable Replacement:** Each variable reference is replaced by every other variable of the appropriate type that is declared in the current scope.

Examples:

```
a = m * (o + p);
```

**Δ1** a = o \* (o + p);

**Δ2** a = m \* (m + p);

**Δ3** a = m \* (o + o);

**Δ4** p = m \* (o + p);





## 11. BSR – Bomb Statement Replacement: Each statement is replaced by a special Bomb() function

Examples:

```
a = m * (o + p);
```

```
Δ1 Bomb() // Raises exception when reached
```

# Summary: Subsuming Other Criteria



- Mutation is widely considered the **strongest** test criterion
  - and most **expensive!**
  - By far the most test requirements (each mutant)
  - Usually the most tests
- Mutation **subsumes** other criteria by including specific mutation operators
- Subsumption can only be defined for **weak mutation** - other criteria only impose local requirements
  - Node coverage, Edge coverage, Clause coverage
  - General active clause coverage: **Yes-Requirement on single tests**
  - Correlated active clause coverage: **No-Requirement**

# For Next Time



Idaho State  
University

Computer  
Science

- Review the Reading
- Review this Lecture
- Come to Class





**Are there any questions?**