LATEX for Discrete Mathematics

Dr. Isaac Griffith

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Symbols

Required Packages: mathtools, amssymb, amsmath Requires: \DeclareMathOperator{\lcm}{lcm} in preamble

Basic Math Operators

- * *
- · \cdot
- + **+**
- ---
- / /
- < <
- > >
- $\bullet \geq \backslash \text{geq}$
- $\bullet \le \setminus \mathtt{leq}$
- \neq \neq
- = =
- $\log x \log x$
- $\max x \max x$
- $\min x \min x$
- $\gcd x \backslash \gcd x$
- lcm x
- $\lim_{h\to 0} \lim_h h \to 0$
- $\sqrt{x} \sqrt{x}$
- $\lfloor x \rfloor$ \lfloor x \rfloor
- $\lceil x \rceil$ \lceil x \rceil
- ... \ldots
- :- \vdots

Sets

- $\mathbb{C} \mathbb{C}$
- $\mathbb{Z} \mathbb{Z}$
- \mathbb{Z}^+ \mathbb{Z}^^{+}
- $\mathbb{N} \mathbb{N}$
- $\mathbb{R} \mathbb{R}$
- $\mathbb{Q} \mathbb{Q}$

Set Theory Operators

- ∪ \cup
- ∩ \cap
- \bullet \times -\times
- \bullet \subset -\subset
- $\bullet \subseteq \setminus \mathtt{subseteq}$
- ⊈ \nsubseteq
- \bullet \supset -\supset
- ⊇ \supseteq
- ⊉ \nsupseteq
- $\bullet \ \in \setminus \mathtt{in}$
- \notin \notin
- \bullet \ -\setminus
- Ø − \varnothing

Logic Operators

 \bullet \land - \setminus land

- V \lor
- ⊕ \oplus
- $\neg \setminus lnot$
- ullet ightarrow \backslash to
- ullet \longleftrightarrow \leftrightarrow
- \vdash $\backslash vdash$
- \models \models
- $\top \text{top}$
- ⊥ \bot
- \bullet \exists \exists
- $\forall \forall$
- \therefore \therefore
- \square square

Function Operators

- ullet $\equiv \setminus equiv$
- o \circ
- ∞ \infty

Big Operators

- V − \bigvee
- ∧ \bigwedge
- ∩ \bigcap
- [] \bigcap
- $\sum \sum$
- ∏ \prod

Relations Operators

- \Box \sqsubset
- \sqsubseteq \sqsubseteq
- □ \sqsubset
- \bullet \supseteq -\sqsubseteq
- ullet $\sim \sim$

- ≺ \prec
- \succ -\succ
- ≼ \preccurlyeq
- \succcurlyeq \succurlyeq

Algorithms

ullet := -\coloneqq

ullet \leftarrow - \gets

Graphs and Trees

- $\deg \deg$

Matrices

• ⊙ - \odot

Constructing Truth Tables and Membership Tables

To create a Truth Table, we simply need to create a table. For example the truth table for $((A \to B) \land \neg B) \to \neg A$ is created as follows:

LATEX Code:

```
1 \begin{center}
2 \begin{tabular}{|c|c|ccc|c|}
3 \hline
4 $A$ & $B$ & $A \to B$ & $\lnot B$ & $(A \to B) \land \not B$ & $\lnot A$ &
5 $((A \to B) \land \lnot B) \to \lnot A$ \\ hline
6 F & F & T & T & T & T & \textbf{T} \\
7 F & T & T & F & F & F & T & \textbf{T} \\
8 T & F & F & T & F & F & F & \textbf{T} \\
9 T & T & T & F & F & F & \textbf{T} \\
1 \end{\text{center}}
```

Results:

A	В	$A \rightarrow B$	$\neg B$	$(A \rightarrow B) \land \not B$	$\neg A$	$((A \to B) \land \neg B) \to \neg A$
F	F	Т	Т	Τ	Т	T
F	T	T	\mathbf{F}	\mathbf{F}	${ m T}$	${f T}$
T	F	F	${ m T}$	\mathbf{F}	\mathbf{F}	${f T}$
T	Т	Γ	\mathbf{F}	\mathbf{F}	\mathbf{F}	${f T}$

Creating Proof Trees

Required Packages

- cancel
- bussproofs

Proof Trees

Proof trees are created using the following commands:

- \AxiomC{value} Create an assumption or axiom for which there is nothing before it.
- \UnaryInfC{value} Creates an inference for a single (last defined) result.
- \BinaryInfC{value} Creates an inference for the prior two results.
- \bullet \TrinaryInfC{value} Creates an inference for the prior three results.
- \QuinaryInfC{value} Creates an inference for the prior four results.
- \RightLabel{value} Creates a label (on the right) of the line for an inference

Example

LATEX Code:

Results:

$$\frac{ (P \land Q) \lor (P \land R)) \qquad \frac{P \land Q}{P} \ ^{\{\land E_L\}} \qquad \frac{P \land R}{P} \ ^{\{\land E_L\}} }{P}$$

Creating Graphs and Trees

Required Packages

• tikz

Creating a Simple Graph

LATEX Code:

```
1 \begin{tikzpicture}
2 [node distance={10mm}, main/.style = {draw, circle, line width=0.25mm}]
3
4 \node[main] (1) {};
5 \node[main] (2) [above right of=1] {};
6 \node[main] (3) [below right of=1] {};
7 \node[main] (4) [above right of=3] {};
8
9 \draw [line width=0.25mm] (1) -- (2);
10 \draw [line width=0.25mm] (1) -- (3);
11 \draw [line width=0.25mm] (2) -- (4);
12 \draw [line width=0.25mm] (3) -- (4);
13 \end{tikzpicture}
```

Results:

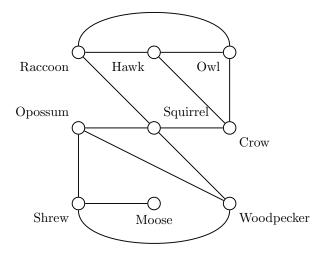


A More Interesting Example

```
begin{tikzpicture}
[node distance={20mm},main/.style = {draw, circle, line width=0.25mm}]

node[main] (1) [label=below left:{Raccoon}] {};
node[main] (2) [label=below left:{Hawk},right of=1] {};
node[main] (3) [label=below left:{Owl},right of=2] {};
```

```
8 \node[main] (4) [label=above left:{Opossum},below of=1] {};
9 \node[main] (5) [label=above right:{Squirrel},right of=4] {};
10 \node[main] (6) [label=below right:{Crow},right of=5] {};
12 \node[main] (7) [label=below left:{Shrew},below of=4] {};
13 \node[main] (8) [label=below:{Moose},right of=7] {};
14 \node[main] (9) [label=below right:{Woodpecker},right of=8] {};
16 \draw [line width=0.25mm] (1) -- (2);
17 \draw [line width=0.25mm] (2) -- (3);
18
19 \draw [line width=0.25mm] (1) -- (5);
20 \draw [line width=0.25mm] (2) -- (6);
21 \draw [line width=0.25mm] (3) -- (6);
23 \draw [line width=0.25mm] (4) -- (5);
24 \draw [line width=0.25mm] (5) -- (6);
^{26} \det [\text{line width=0.25mm}] (4) -- (7);
27 \draw [line width=0.25mm] (4) -- (9);
28 \draw [line width=0.25mm] (5) -- (9);
30 \draw [line width=0.25mm] (7) -- (8);
_{32} \draw [line width=0.25mm] (1) to [out=90, in=90, looseness=.75] (3);
33 \draw [line width=0.25mm] (7) to [out=270, in=270, looseness=.75] (9);
34 \end{tikzpicture}
```



Digraphs

```
1 \begin{tikzpicture}
2 [node distance={20mm}, main/.style = {draw, circle, line width=0.25mm}]
3
4 \node[main] (1) {a};
5 \node[main] (2) [right of=1] {b};
6 \node[main] (3) [right of=2] {c};
7 \node[main] (4) [below of=1] {e};
8 \node[main] (5) [right of=4] {d};
9
10 \draw [->,line width=0.25mm] (1) -- (2);
11 \draw [->,line width=0.25mm] (3) -- (2);
12 \draw [->,line width=0.25mm] (2) -- (5);
```

```
13 \draw [->,line width=0.25mm] (5) -- (3);

14

15 \draw [->,line width=0.25mm] (1) to [out=95, in=175, looseness=5] (1);

16 \draw [->,line width=0.25mm] (1) to [out=30, in=150, looseness=1.25] (3);

17 \draw [->,line width=0.25mm] (3) to [out=85, in=5, looseness=5] (3);

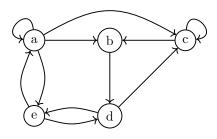
18 \draw [->,line width=0.25mm] (4) to [out=120, in=250, looseness=1.25] (1);

19 \draw [->,line width=0.25mm] (1) to [out=290, in=70, looseness=1.25] (4);

20 \draw [->,line width=0.25mm] (4) to [out=-15, in=195, looseness=1.25] (5);

21 \draw [->,line width=0.25mm] (5) to [out=165, in=15, looseness=1.25] (4);

22 \end{tikzpicture}
```

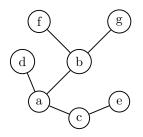


A Simple Tree

LATEX Code:

```
1 \begin{tikzpicture}
2 [node distance={15mm}, main/.style = {draw, circle, line width=0.25mm}]
3
4 \node[main] (1) {b};
5 \node[main] (2) [left of=1] {d};
6 \node[main] (3) [below left of=1] {a};
7 \node[main] (4) [above left of=1] {f};
8 \node[main] (5) [above right of=1] {g};
9 \node[main] (6) [below of=1] {c};
10 \node[main] (7) [below right of=1] {e};
11
12 \draw [line width=0.25mm] (1) -- (4);
13 \draw [line width=0.25mm] (1) -- (5);
14 \draw [line width=0.25mm] (3) -- (2);
16 \draw [line width=0.25mm] (3) -- (6);
17 \draw [line width=0.25mm] (6) -- (7);
18
19 \end{tikzpicture}
```

Results:



A Basic Rooted Tree

```
1 \begin{tikzpicture}
```

```
[every node/.style = {shape=circle, draw, line width=0.25mm, align=center}]

node {a}

child {node {b}

child {node {f}}

child {node {g}} edge from parent [line width=0.25mm]}

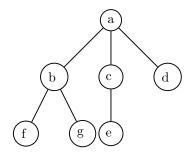
child {node {c}

child {node {c}}

child {node {e}} edge from parent [line width=0.25mm]}

child {node {d}} edge from parent [line width=0.25mm]};

end{tikzpicture}
```



A Simple Binary Tree

LATEX Code:

```
begin{tikzpicture}
[every node/.style = {shape=circle, draw, line width=0.25mm, align=center}]

node {c}

child {node {a}

child {node {b}

child {node {f}}

child {node {f}}

child {node {g}} edge from parent [line width=0.25mm]}

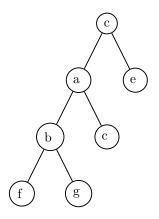
child {node {c}} edge from parent [line width=0.25mm]}

child {node {e} edge from parent [line width=0.25mm]};

child {node {e} edge from parent [line width=0.25mm]};

end{tikzpicture}
```

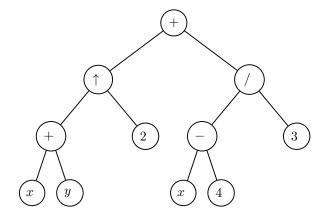
Results:



Binary Tree Example

```
1 \begin{tikzpicture}
2 [
3 level 1/.style = {sibling distance = 4 cm},
4 level 2/.style = {sibling distance = 2.5cm},
```

```
level 3/.style = {sibling distance = 1cm},
    every node/.style = {shape=circle, draw, line width=0.25mm, align=center}
7 ]
8 \node {$+$}
      child {node {$\uparrow$}
9
        child {node {$+$}
10
          child {node {$x$}}
11
          child {node {$y$}}}
12
        child {node {$2$}}
        edge from parent [line width=0.25mm]}
14
15
      child {node {$/$}
        child {node {$-$}
16
          child {node {$x$}}
17
          child {node {$4$}}}
18
        child {node {$3$}}
19
      edge from parent [line width=0.25mm]};
20
22 \end{tikzpicture}
```



Writing Algorithms with Pseudocode

Required Packages

- algorithm
- algorithment algorithment algorithment without option "noend"

Binary Search

```
1 \begin{algorithm}[H]
2 \begin{algorithmic}
  \caption{Binary Search Algorithm}
4 \Procedure{binarySearch}{$x, a_1, a_2, \ldots, a_n, Loc$}
    \State $i \coloneqq 1$
    \State $j \coloneqq n$
    \While{$i < j$}
      \State $m \coloneqq \lfloor(i + j) / 2\rfloor$
9
10
      \If {$x > a_m$}
        \ \State $i \coloneqq m + 1$
11
12
        \State $j \coloneqq m$
13
      \EndIf
14
15
    \EndWhile
16
```

```
17 \If{$x = a_i$}
18 \State $Loc \coloneqq i$
19 \Else
20 \State $Loc \coloneqq 0$
21 \EndIf
22 \EndProcedure
23 \end{algorithmic}
24 \end{algorithm}
```

Algorithm 1 Binary Search Algorithm

```
procedure BINARYSEARCH(x, a_1, a_2, \dots, a_n, Loc)
i \coloneqq 1
j \coloneqq n
while i < j do
m \coloneqq \lfloor (i+j)/2 \rfloor
if x > a_m then
i \coloneqq m+1
else
j \coloneqq m
if x = a_i then
Loc \coloneqq i
else
Loc \coloneqq 0
```

Bubble Sort

LATEX Code:

```
1 \begin{algorithm}[H]
  \caption{Bubble Sort Algorithm}
  \begin{algorithmic}
  \Procedure{bubbleSort}{$a_1, a_2, \ldots, a_n$}
    \For{si \gets 1$ \text{textbf}{to} $n - 1$}
       \For{j \ gets 1$ \text{textbf}{to}  n - i}}
         \If { a_j > a_{j+1} } 
           \state $a_j \leq a_j \leq a_{j+1}
         \EndIf
       \EndFor
10
    \EndFor
11
12 \EndProcedure
^{13} \setminus end\{algorithmic\}
14 \end{algorithm}
```

Results:

Algorithm 2 Bubble Sort Algorithm

```
\begin{array}{l} \textbf{procedure} \ \texttt{BUBBLESORT}(a_1, a_2, \dots, a_n) \\ \textbf{for} \ i \leftarrow 1 \ \textbf{to} \ n-1 \ \textbf{do} \\ \textbf{for} \ j \leftarrow 1 \ \textbf{to} \ n-i \ \textbf{do} \\ \textbf{if} \ a_j > a_{j+1} \ \textbf{then} \\ a_j \leftrightarrow a_{j+1} \end{array}
```

Circuit Diagrams

Required Packages

 \bullet tikz

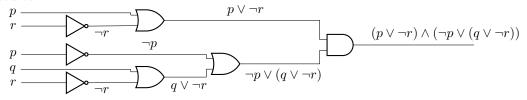
- circuitikz
- tkz-euclide
- Required Tikz Libraries: calc, positioning, intersections, quotes, decorations.markings, matrix, backgrounds

Example

LATEX Code:

```
\begin{tikzpicture}
      \ctikzset{
            logic ports=ieee,
            logic ports/scale=0.5,
      % Logic ports
10 \node[not port] (NOTa) at (0,0){};
11 \node[not port] (NOTb) at (0,-0.75){};
12 \setminus node[not port] (NOTc) at (0,-1.5){};
13 \setminus node[or port] (ORa) at (2,0.15){};
14 \node[or port] (ORb) at (2,-1.35){};
15 \node[or port] (ORc) at (4,-1){};
16 \node[and port] (ANDa) at (7,-0.5){};
17
18 % Connections
20 \draw (ANDa.out) -- ++(3.0,0)node[near end,above]{\true \node \no
21 \land (\lnot p \lor (q \lor \lnot r))$};
22 \draw (ORc.out) -| node[near start,below]{\frac{1}{n} p \lor (q \lor \lnot r)$}(ANDa.in 2);
23 \draw (ORa.out) - | node[near start,above] {$p \lor \lnot r$}(ANDa.in 1);
^{24} \draw (NOTb.out) -| node[near start,above]{^{1} not p$}(ORc.in 1);
^{25} \ (ORb.out) -| node[near start,below]{$q \lor \lnot r$}(ORc.in 2);
^{26} \draw (NOTc.out) -- node[near start,below]{$\lnot r$}(ORb.in 2);
27 \draw (NOTa.out) -- node[near start,below]{$\lnot r$}(ORa.in 2);
28 \draw (NOTa.in 1) -- ++(-1.0,0)node[left]{$r$};
29 \draw (NOTb.in 1) -- ++(-1.0,0)node[left]{$p$};
30 \draw (NOTc.in 1) -- ++(-1.0,0) node [left] {$r$};
^{31} \draw (-1.45,0.35) node[left]{$p$} -| (ORa.in 1);
32 \draw (-1.45,-1.15) node[left]{$q$} -| (ORb.in 1);
34 \end{tikzpicture}
```

Results:

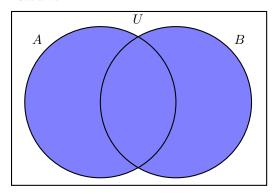


Venn Diagrams

Set Union

```
1 \begin{tikzpicture}
2
3 % Set A
```

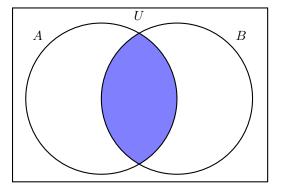
```
4 \node [circle,
      fill=blue!50,
       minimum size = 4cm,
      label=\{135:\$A\$\}\] (A) at (0,0)\{\};
9 % Set B
10 \node [circle,
      fill=blue!50,
11
      minimum size = 4 cm,
12
      label=\{45:\$B\$\}\] (B) at (2,0)\{\};
13
14
^{15} \draw[black,thick] (-2.35,-2.2) rectangle (4.4,2.4);
16
17 % Circles outline
18 \draw[black,thick] (0,0) circle(2cm);
19 \draw[black,thick] (2,0) circle(2cm);
21 % Union text label
22 \node[black] at (1,2.2) {$U$};
23
24 \end{tikzpicture}
```



Set Intersection

```
1 \begin{tikzpicture}[thick,
       set/.style = {circle,
minimum size = 4cm,
           color=black}]
6 \text{ } \text{draw[black,thick] } (-2.35,-2.2) \text{ rectangle } (4.4,2.4);
8 % Set A
9 \node[set,label={135:$A$}] (A) at (0,0) {};
11 % Set B
12 \node[set,label={45:$B$}] (B) at (2,0) {};
13
14 % Intersection
15 \begin{scope}
       \clip (0,0) circle(2cm);
16
17
       \clip (2,0) circle(2cm);
       \fill[blue!50](0,0) circle(2cm);
18
19 \end{scope}
21 % Circles outline
22 \draw (0,0) circle(2cm);
23 \draw (2,0) circle(2cm);
```

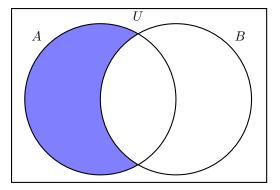
```
24
25 \node[black] at (1,2.2) {$U$};
26
27 \end{tikzpicture}
```



Set Difference

LATEX Code

Results

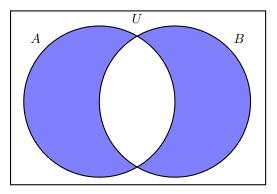


Symmetric Difference

LATEX Code

```
\begin{tikzpicture}[thick,
      set/.style = {circle,
          minimum size = 4cm}]
5 \draw[black,thick] (-2.35,-2.2) rectangle (4.4,2.4);
7 % Set A
8 \node[set,fill=blue!50,label={135:$A$}] (A) at (0,0) {};
node[set,fill=blue!50,label={45:$B$}] (B) at (2,0) {};
13 % Intersection
14 \begin{scope}
      \clip (0,0) circle(2cm);
15
      \clip (2,0) circle(2cm);
16
      \fill[white](0,0) circle(2cm);
18 \end{scope}
19
20 % Circles outline
21 \draw (0,0) circle(2cm);
22 \draw (2,0) circle(2cm);
24 \node[black] at (1,2.2) {$U$};
25
27 \end{tikzpicture}
```

Results



Plotting Functions

You will need to use the tikz library: shapes.geometric

Domain and Range

```
begin{tikzpicture}

node[ellipse,

draw = black,

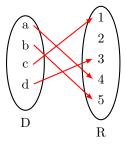
thick,

text = white,

minimum width = 1cm,

minimum height = 2.5cm] (A) at (0,0) {};
```

```
\node[ellipse,
       draw = black,
11
       thick,
       minimum width = 1cm,
       minimum height = 3cm] (B) at (2,0) {};
13
14
     \node[anchor=north] at ([yshift=-2pt]A.south) {D};
     \node[anchor=north] at ([yshift=-2pt]B.south) {R};
16
17
     \node[anchor=north] at ([yshift=-2pt]A.north) (a) {a};
18
     \node[anchor=north] at ([yshift=-2pt]a.south) (b) {b};
19
     \node[anchor=north] at ([yshift=-2pt]b.south) (c) {c};
20
     \node[anchor=north] at ([yshift=-2pt]c.south) (d) {d};
21
     \label{local_node} $$ \node[anchor=north] at ([yshift=-2pt]B.north) (r1) {1};
22
     \node[anchor=north] at ([yshift=-2pt]r1.south) (r2) {2};
\node[anchor=north] at ([yshift=-2pt]r2.south) (r3) {3};
23
24
     \node[anchor=north] at ([yshift=-2pt]r3.south) (r4) {4};
25
26
     \node[anchor=north]
27
28
       at ([yshift=-2pt]r4.south) (r5) {5};
29
     \draw[-latex, thick, red] (a.east) -- (r4.west) {};
30
     \draw[-latex, thick, red] (b.east) -- (r5.west) {};
31
     \draw[-latex, thick, red] (c.east) -- (r1.west) {};
\draw[-latex, thick, red] (d.east) -- (r3.west) {};
32
34 \end{tikzpicture}
```



Plotting the Floor Function LATEX Code

```
begin{tikzpicture}

tkzInit[xmin = -3, xmax = 3, ymin = -3, ymax = 2]

tkzDrawXY[color=black,thick]

tkzLabelXY[text=black,fill=none]

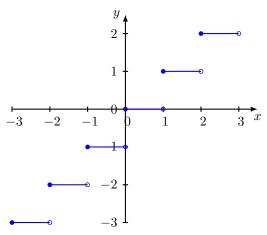
foreach \a in {-3,...,2}{

    \draw[blue,thick] (\a, \a) -- (\a + 1, \a);

    \node [circle, draw, thick, fill, line width = .5pt, color = blue, inner sep = 0pt, minimum size = 3pt] (ca) at (\a, \a) {};

node [circle, draw, thick, fill=none, line width = .5pt, color = blue, inner sep = 0pt, minimum size = 3pt] (ca) at (\a + 1, \a) {};

end{tikzpicture}
```



Matrices

Required Packages

• amsmath

Result:

$$\mathbf{A} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 1 & 0 \end{bmatrix}, \quad \mathbf{B} = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \end{bmatrix}$$

Code Listings

Required Packages

- xcolor if you want color listings
- lstlistings

Customizing

Codestyle and Colors

Colors and styles can be set in the preamble (after \documentclass{...} but before \begin{document}

```
1 2 % You can setup colors if you included the xcolor package
3 4 \definecolor{name}{rgb}{r,g,b}
```

Customization Options

- backgroundcolor colour for the background. External color or xcolor package needed.
- commentstyle style of comments in source language.
- basicstyle font size/family/etc. for source (e.g. basicstyle=\ttfamily\small)
- keywordstyle style of keywords in source language (e.g. keywordstyle=\color{red})
- numberstyle style used for line-numbers
- numbersep distance of line-numbers from the code
- stringstyle style of strings in source language
- showspaces emphasize spaces in code (true/false)
- showstringspaces emphasize spaces in strings (true/false)
- showtabs emphasize tabulators in code (true/false)
- numbers position of line numbers (left/right/none, i.e. no line numbers)
- prebreak displaying mark on the end of breaking line (e.g. prebreak=\raisebox{0ex}[0ex][0ex][\text{\ensuremath{\hookleftarrow}}})
- captionpos position of caption (t/b)
- frame showing frame outside code (none/leftline/topline/bottomline/lines/single/shadowbox)
- breakwhitespace sets if automatic breaks should only happen at whitespaces
- breaklines automatic line-breaking
- keepspaces keep spaces in the code, useful for indetation
- tabsize default tabsize
- escapeinside specify characters to escape from source code to LATEX (e.g. escapeinside={\%*}{**}})
- rule color - Specify the colour of the frame-box

Supported Languages

• ABAP	• C	• csh	• Haskell
• ACSL	• C++	• Delphi	• HTML
• Ada	• Caml	• Eiffel	• IDL
• Algol	• CIL	• Elan	\bullet inform
• Ant	• Clean	• erlang	• Java
• Assembler	• Cobol	• Euphoria	• JVMIS
• Awk	• Comal 80	• Fortran	• ksh
• bash	• command.com	• GCL	• Lingo
• Basic	• Comsol	• Gnuplot	• Lisp

• Oberon-2 • Promela • SHELXL • Logo • OCL • PSTricks • Simula • make • SPARQL • Mathematica • Octave • Python • Matlab • Oz • R • SQL • Mercury • Pascal • Reduce • tcl • MetaPost • Perl • Rexx • TeX • PHP • Miranda • RSL • VBScript • PL/I • Mizar • Ruby Verilog • ML • Plasm • S • VHDL • VRML • Modula-2 • PostScript • SAS • MuPAD • POV • Scilab • XML

• sh

• XSLT

Haskell Examples:

• NASTRAN

Linear Search

LATEX Code:

```
\begin{lstlisting}[language=Haskel1]
linSearch :: Eq a => [a] -> Int -> a -> Int
linSearch [] _ _ = 0
linSearch (y:ys) i x =
    if x == y then i
    else linSearch ys (i + 1) x
\end{lstlisting}
```

• Prolog

Results:

```
1 linSearch :: Eq a => [a] -> Int -> a -> Int
2 linSearch [] _ _ = 0
3 linSearch (y:ys) i x =
4     if x == y then i
6     else linSearch ys (i + 1) x
```

Binary Search

```
\begin{lstlisting}[language=Haskel1]
binSearch :: (Ord a) => [a] -> a -> Int -> Int -> Int
binSearch arr x lo hi
   | hi < lo = -1
   | pivot > x = binSearch arr x lo (mid - 1)
   | pivot < x = binSearch arr x (mid + 1) hi
   | otherwise = mid
   where
    mid = lo + (hi - lo) 'div' 2
    pivot = arr!!mid
\end{lstlisting}</pre>
```

```
binSearch :: (Ord a) => [a] -> a -> Int -> Int
binSearch arr x lo hi
   | hi < lo = -1
   | pivot > x = binSearch arr x lo (mid - 1)
   | pivot < x = binSearch arr x (mid + 1) hi
   | otherwise = mid
   where
   mid = lo + (hi - lo) 'div' 2
   pivot = arr!!mid</pre>
```

Merge Sort

LATEX Code:

```
\begin{lstlisting}[language=Haskell]
merge :: (Ord a) => [a] -> [a] -> [a]
merge [] [] = []
merge [] ys = ys
merge xs [] = xs
merge allX@(x:xs) allY@(y:ys)
 | x > y
          = y : merge allX ys
  | otherwise = x : merge xs allY
sort :: (Ord a) => [a] -> [a]
sort [] = []
sort [a] = [a]
sort [a,b]
 | a > b
            = [b, a]
  | otherwise = [a, b]
sort list =
  let split = splitAt(length list 'div' 2) list
     firstHalf = sort (fst split)
      secondHalf = sort (snd split)
  in merge firstHalf secondHalf
\end{lstlisting}
```

Results:

```
1 merge :: (Ord a) => [a] -> [a] -> [a]
2 merge [] [] = []
3 merge [] ys = ys
4 merge xs [] = xs
5 merge allX@(x:xs) allY@(y:ys)
6 \mid x > y = y : merge all X ys
    | otherwise = x : merge xs allY
9 sort :: (Ord a) => [a] -> [a]
10 sort [] = []
11 sort [a] = [a]
12 sort [a,b]
                = [b, a]
    | a > b
otherwise = [a, b]
15 sort list =
let split = splitAt(length list 'div' 2) list
    firstHalf = sort (fst split)
secondHalf = sort (snd split)
17
18
in merge firstHalf secondHalf
```

Quick Sort

LATEX Code:

```
\begin{lstlisting}[language=Haskel1]
quickSort :: Ord a => [a] -> [a]
quickSort [] = []
quickSort (pivot:xs) =
   quickSort [y | y <- xs, y < pivot]
   ++ [pivot]
   ++ quicksort [y | y <- xs, y >= pivot]
\end{lstlisting}
```

Results:

```
quickSort :: Ord a => [a] -> [a]
quickSort [] = []
quickSort (pivot:xs) =
quickSort [y | y <- xs, y < pivot]
++ [pivot]
++ quickSort [y | y <- xs, y >= pivot]
```