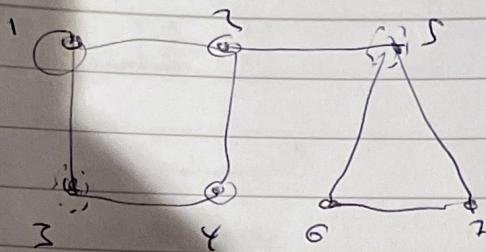


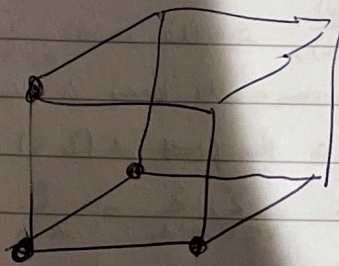
COMBINATORICS



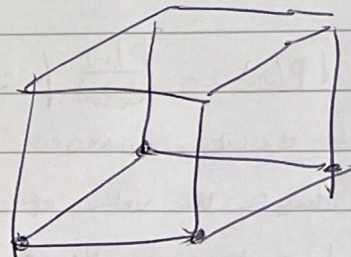
$\{3\}$ is boundary

boundary of $\{1,2,4\}$ is $\{3,5\}$

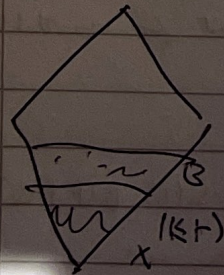
$|A| = 4$ is Q_3



Ball $|b(A)| = 3$



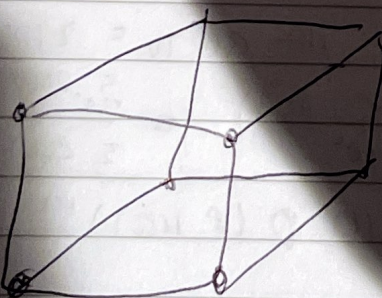
sub cube $|b(A)| = 4$



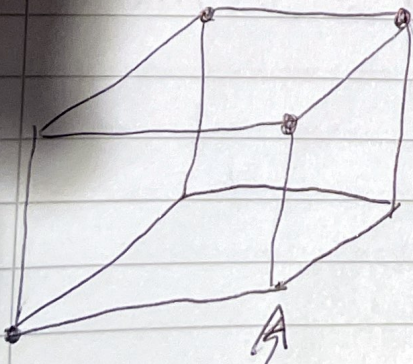
A

Q_4

in sections

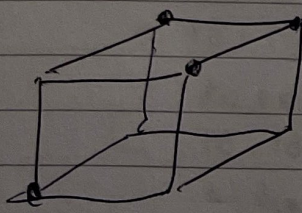
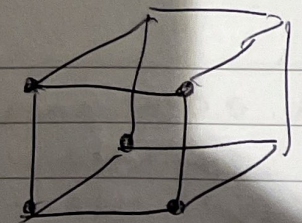


$\leftarrow A_+^{(10)} = A_+$



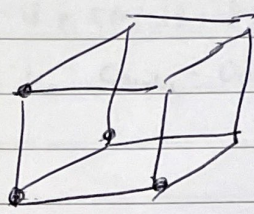
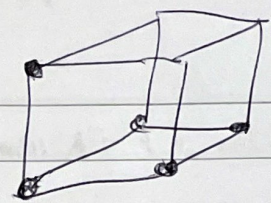
$\leftarrow A_-^{(10)} = A_-$

$i \uparrow$



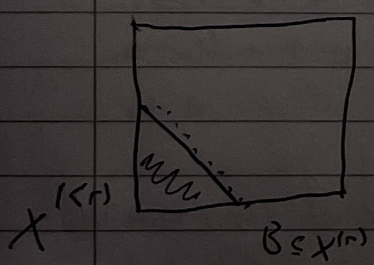
A

C_i



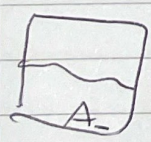
$C_i(A)$

$|C_i(A)| = |A|$. $C_i(A)$ "looks more like" a Hamming ball than A does.



Harper's isoperimetric inequality

Proof of Harper



A