HW3 Q7,8

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Question 7

a) Here we code the function to implement SGD with mini-batches:

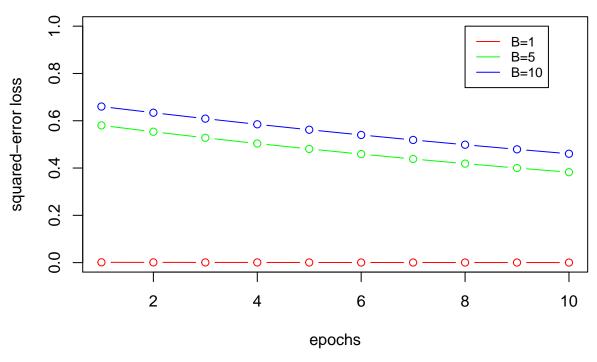
```
stochastic_gd <- function(X,y,epsilon,batch_size,epochs){</pre>
  #' Function written as per required inputs and outputs
  \#' Oparam X: matrix, data-set of input variable values of size N*n
  #' Cparam y: vector of responses for each given set of input variable values, size N*1
  #' Oparam epsilon: numeric, value for the learning rate at each step
  #' @param B: batch size, number of observations to use at each step when computing gradient
  #' @param epochs: integer (positive), number of passes through the entire data-set
  #' Creturn squared_loss: matrix, of squared error loss values, one for each step, size epochs*N/B
  B<-batch_size
  #print(B)
  N < -dim(X)[1]
  #print(N)
  n < -dim(X)[2]
  #print(n)
  #indices<-seq(1,N/B,length.out=N)</pre>
  #print(indices)
  beta<-matrix(0,nrow=n,ncol=1)</pre>
  squared_loss<-matrix(NA,nrow=epochs,ncol=N/B)</pre>
  # loss_0<-1/N*t(y)%*%y
  # squared_loss[1,]<-rep(loss_0,N/B)</pre>
  for (j in 1:epochs){
    loss < -c(rep(0, N/B))
    for (i in 1:(N/B)){
      start < -(i-1)*B+1
      #print(start)
      end<-start+B-1
      #print(end)
      predictors<-as.matrix(X[start:end,])</pre>
      response <- y [start:end]
      if (B==1){
        gradient<-2/N*(as.matrix(predictors)%*%(response-t(as.matrix(predictors))%*%beta))</pre>
        #print(gradient)
        #print(dim(gradient))
        beta <- beta + epsilon * gradient
        #print(beta)
        #print(dim(beta))
```

```
loss_iter<-1/N*(response-t(as.matrix(predictors))%*%beta)^2</pre>
        #print(dim(loss_iter))
        loss[i] <-loss_iter</pre>
      }
      else{
        gradient<-2/N*(t(as.matrix(predictors))%*%(response-as.matrix(predictors)%*%beta))</pre>
        #print(gradient)
        #print(dim(gradient))
        beta<-beta+epsilon*gradient
        #print(beta)
        #print(dim(beta))
        loss_iter<-1/N*(t(response-as.matrix(predictors)%*%beta)%*%(response-as.matrix(predictors)%*%be
        #print(dim(loss iter))
        loss[i]<-loss_iter</pre>
    }
    squared_loss[j,]<-loss
  #print(loss)
  #print(squared_loss)
return(squared_loss)
```

Here we generate the data to test the function

```
set.seed(2021)
sigma < -0.01
X \leftarrow mvrnorm(n=100, mu=rep(0,10), Sigma=diag(rep(1,10)))
a_star<-mvrnorm(n=1, mu=rep(0,10), Sigma=diag(rep(1,10)))
delta<-mvrnorm(n=1, mu=rep(0,100),Sigma=diag(rep(sigma^2,100)))</pre>
y<-X%*%a_star+delta
result_1<-stochastic_gd(X,y,0.01,1,10)
result_5<-stochastic_gd(X,y,0.01,5,10)
result_10<-stochastic_gd(X,y,0.01,10,10)
epochs <-1:10
loss_epochs_1<-result_1[,dim(result_1)[2]]</pre>
loss_epochs_5<-result_5[,dim(result_5)[2]]</pre>
loss_epochs_10<-result_5[,dim(result_10)[2]]</pre>
plot(x=epochs,y=loss_epochs_1,type="b",col="red",ylim=(c(0,1)),ylab="squared-error loss",main="Simulate
points(x=epochs,y=loss_epochs_5,type="b",col="blue")
points(x=epochs,y=loss_epochs_10,type="b",col="green")
legend(8,1, legend=c("B=1", "B=5", "B=10"),
       col=c("red", "green", "blue"), lty=1, cex=0.8)
```

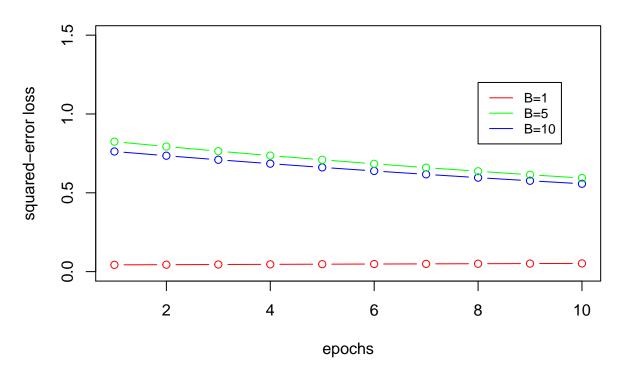
Simulated Data (sigma=0.01)



Here we change the value of sigma

```
set.seed(2021)
sigma < -1
X<-mvrnorm(n=100, mu=rep(0,10),Sigma=diag(rep(1,10)))</pre>
a_star<-mvrnorm(n=1, mu=rep(0,10),Sigma=diag(rep(1,10)))
delta<-mvrnorm(n=1, mu=rep(0,100),Sigma=diag(rep(sigma^2,100)))
y<-X%*%a_star+delta
result_1<-stochastic_gd(X,y,0.01,1,10)</pre>
result_5<-stochastic_gd(X,y,0.01,5,10)
result_10<-stochastic_gd(X,y,0.01,10,10)
epochs <-1:10
loss_epochs_1<-result_1[,dim(result_1)[2]]</pre>
loss_epochs_5<-result_5[,dim(result_5)[2]]</pre>
loss_epochs_10<-result_5[,dim(result_10)[2]]</pre>
plot(x=epochs,y=loss_epochs_1,type="b",col="red",ylim=c(0,1.5),ylab="squared-error loss", main="Simulat
points(x=epochs,y=loss_epochs_5,type="b",col="blue")
points(x=epochs,y=loss_epochs_10,type="b",col="green")
legend(8,1.2, legend=c("B=1", "B=5", "B=10"),
       col=c("red", "green", "blue"), lty=1, cex=0.8)
```

Simulated Data (sigma=1)



Question 8