

2/4

Linked List

Singly Linked List

**Data Structures
C++ for C Coders**

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Self-referenced structures – review

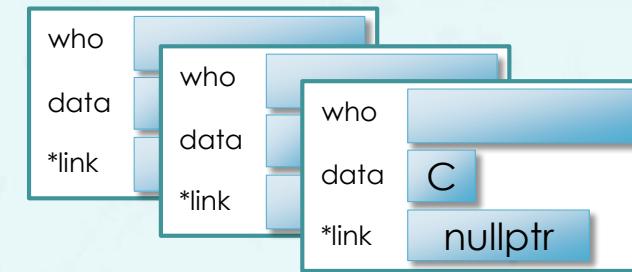
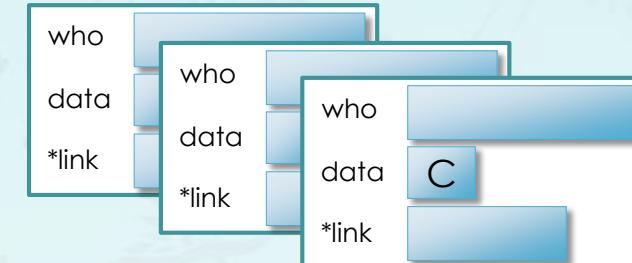
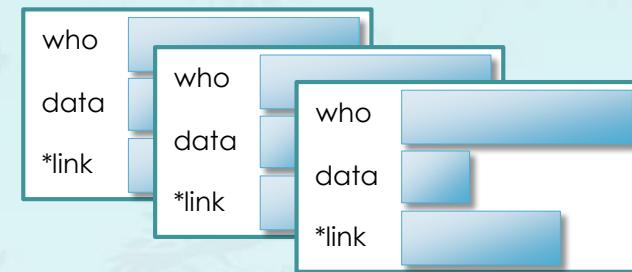
Exercise: Link a, b and c nodes;

```
struct List {  
    string who;  
    char data;  
    List *link;  
};  
  
List a, b, c;  
a.data = 'A';  
b.data = 'B';  
c.data = 'C';  
a.link = b.link = c.link = nullptr;
```

List a, b, c;

a.data = 'A';
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Self-referenced structures – review

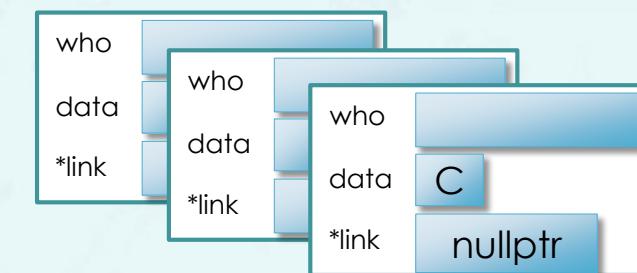
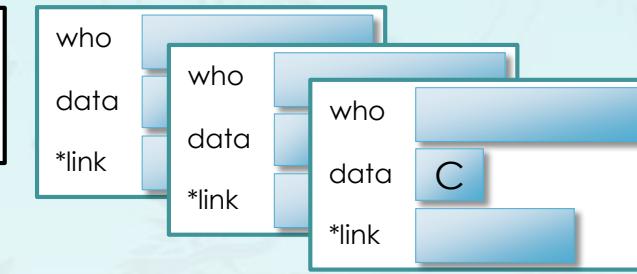
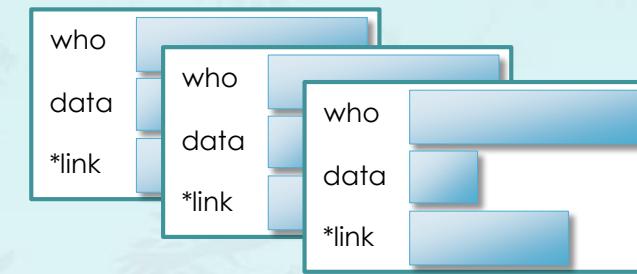
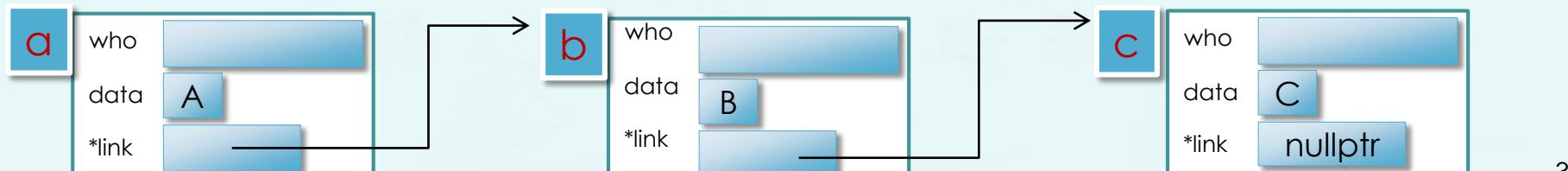
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Self-referenced structures – review

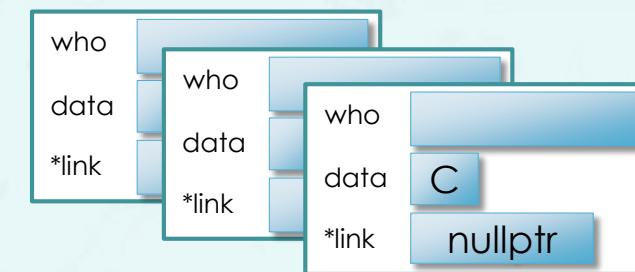
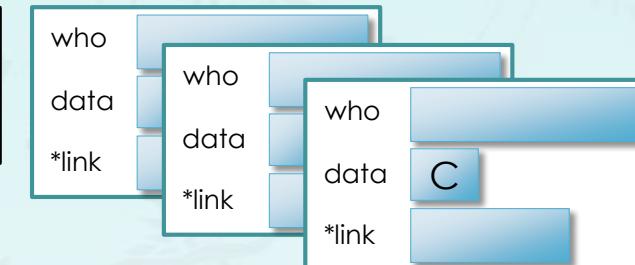
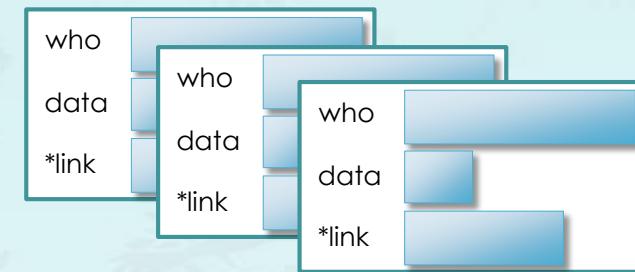
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```
struct List {  
    string who;  
    char data;  
    List *link;  
};  
  
List a, b, c;  
List *p, *q, *r;
```

List a, b, c;

a.data = 'A';
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c.data = 'C';

a.link = b.link = c.link = nullptr;

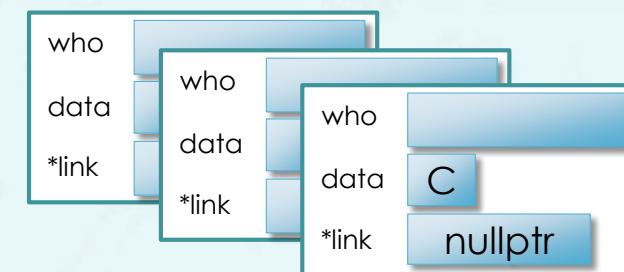
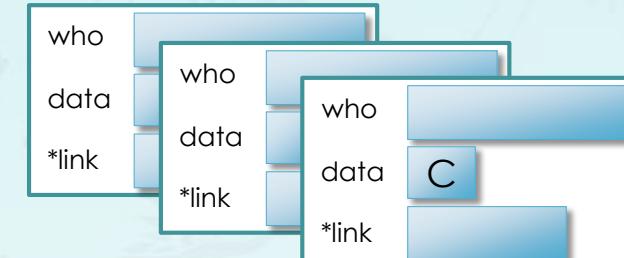
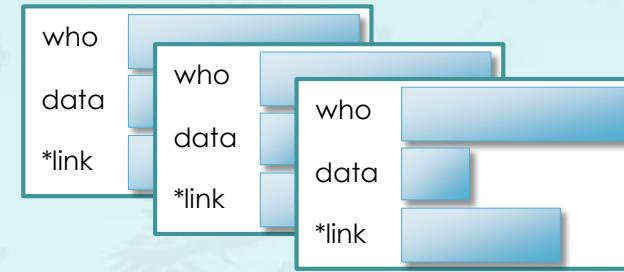


Self-referenced structures – review

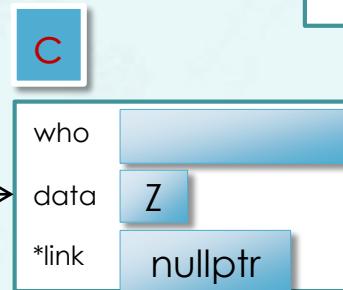
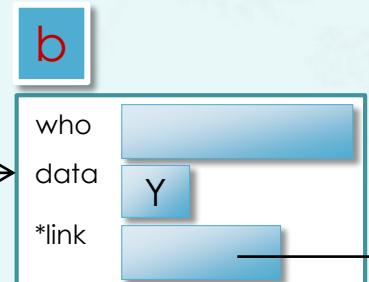
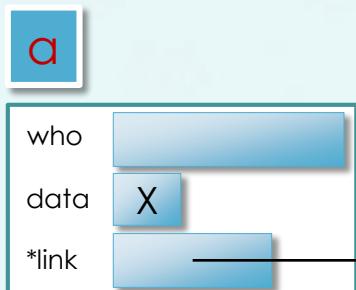


Exercise: Link a, b and c nodes;

```
struct List {  
    string who;  
    char data;  
    List *link;  
};  
  
List a, b, c;  
List *p, *q, *r;
```

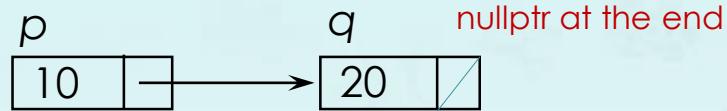


- (1) Let each p, q, and r points to a, b, and c;
- (2) Store each 'X', 'Y', and 'Z' in data
- (3) Connect them using p, q and r as shown below:



Linked List

TASK: Code a function that returns the head of following linked list.



```
struct Node {  
    int data;  
    Node* next;  
};  
using pNode = Node*;
```

Write a function that creates a node and returns **pNode**.

```
pNode newNode(int val) {  
    pNode node = (pNode)malloc(sizeof(Node));  
    node->data = val;  
    node->next = nullptr;  
    return node;  
}
```

C

```
pNode newNode(int val) {  
    pNode node = new Node;  
    node->data = val;  
    node->next = nullptr;  
    return node;  
}
```

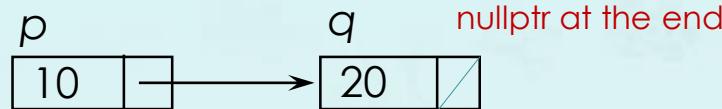
C++

```
pNode node = new Node {0, nullptr};
```

C++

Linked List

TASK: Code a function that returns the head of following linked list.



```
struct Node {  
    int data;  
    Node* next;  
};  
using pNode = Node*;
```

```
pNode newList2(int a, int b) {  
    pNode p = new Node {a, nullptr};  
    pNode q = new Node {b, nullptr};  
    p->next = q;  
    return p;  
}
```

```
pNode newList2(int a, int b) {  
    pNode q = new Node {b, nullptr};  
    pNode p = new Node {a, q};  
    return p;  
}
```

```
pNode newList2(int a, int b) {  
    pNode q = new Node {b, nullptr};  
    return new Node {a, q};  
}
```

Linked List – find()

main에서 영향을 주고 싶다면
pNode를 이중 포인터로 받와야한다.
그래도 pNode x = list를 해서 copy한 다음에
하는 것을 추천

pNode find(pNode list, int val)

while (list != nullptr) {

}

이렇게 해도 됨
여기 함수에서 사용하는 list는
main에 list에 영향을 주지 않음

list

이게 맞는것

```
pNode find(pNode list, int val)
if (empty(list)) return nullptr;

pNode x = list
while (x != nullptr) {
    if (x->data == val) return x;
    x = x->next;
}
return x;
```

무엇이 맞을까요?

```
pNode x = list;
for(;x!=nullptr; x = x->next)
if(x->data == val) return x;
x = x->next;
return x;
```

이렇게 해도됨

```
pNode find(pNode list, int val)
if(empty(list)) return nullptr;
```

```
pNode x = list
while (x-> next != nullptr) {
}
return x;
```

```
bool empty(pNode list)
return list == nullptr;
```

show_all() => 여기서 이걸 쓰면 아주 좋음
list == nullptr 이 맞으면 true
틀리면 false를 바로 return

이렇게 하면 첫번째 element는 건너뜀

8

Linked List – **pop_front()**

TASK: Code a function that deletes the first node and returns the new first node.

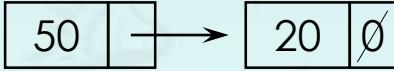
list



(before)

앞에 있는 head를 없애고
head를 그 뒤로

list



(after)

```
pNode pop_front(pNode list)
```

```
if (empty(list)) return list;  
  
list = list->next;  
return list;
```

What's wrong?

```
pNode pop_front(pNode list)
```

```
if (empty(list)) return list;  
  
pNode x = list;  
list = list->next;  
delete x;  
return list;
```

Linked List – **push_front()**

TASK: Code a function that add a node at the beginning of the list.

- If the list is empty, the new node becomes the head node.

list



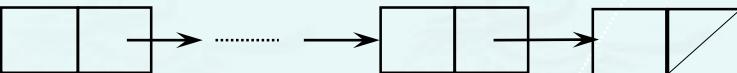
list



node



list



```
pNode push_front(pNode list, int val)
```

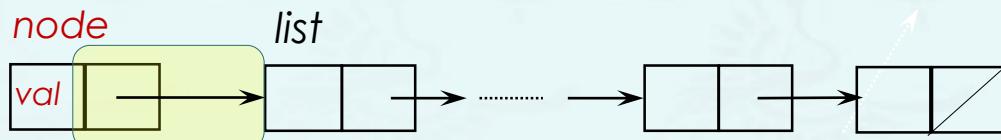
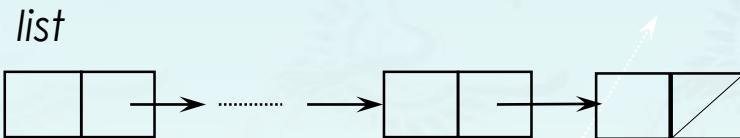
```
if (empty(list))  
    return new Node{val, nullptr};
```

```
pNode node = new Node{val, nullptr};
```

Linked List – **push_front()**

TASK: Code a function that add a node at the beginning of the list.

- If the list is empty, the new node becomes the head node.



```
pNode push_front(pNode list, int val)
if (empty(list))
    return new Node{val, nullptr};
pNode node = new Node{val, nullptr};  
list  
node->next = list;
return node;
```

Linked List – push_back()

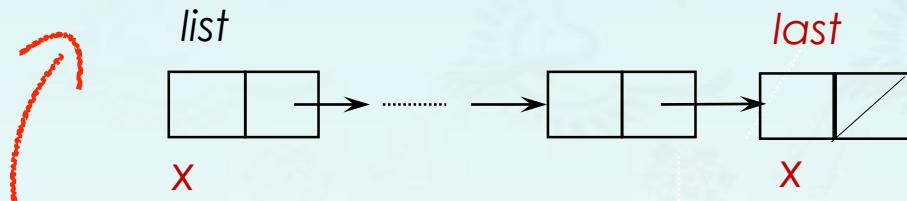
TASK: Code a function that appends a node at the end of the list.

- If the list is empty, the new node becomes the head node.



while 문이 끝나면 return x; 는 결국 nullptr를 return 해 줄 수 밖에 없는 것이다.

그럼 어떻게? -> 미리 앞의 것이 nullptr이라면 그전 것을 return



pNode last(pNode list)

```
pNode x = list;  
while (x != nullptr)  
    x = x->next;  
return x'
```

```
pNode push_back(pNode list, int val)  
if (empty(list))  
    return new Node{val, nullptr};
```

pNode last(pNode list)

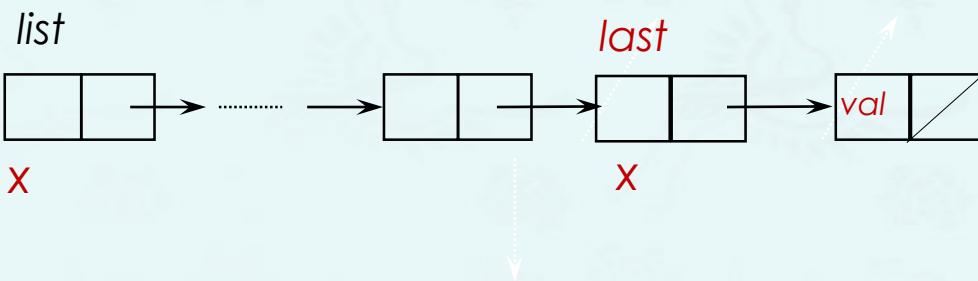
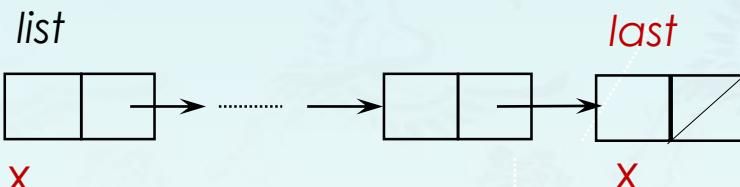
```
pNode x = list;  
while (x->next != nullptr)  
    x = x->next;  
return x;
```

Q: Which one is correct?

Linked List – **push_back()**

TASK: Code a function that appends a node at the end of the list.

- If the list is empty, the new node becomes the head node.



```
pNode push_back(pNode list, int val)
```

```
if (empty(list))
    return new Node{val, nullptr};

pNode x = last(list);
x->next = new Node{val, nullptr};
return x;

return list;
```

```
pNode last(pNode list)
```

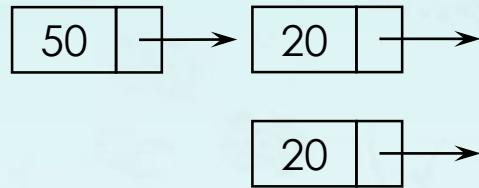
```
pNode x = list;
while (x->next != nullptr)
    x = x->next;
return x;
```

Linked List – **pop()**

TASK: Code a function that deletes a node with a value specified.

- If the first node(or **head**) is the one to delete, then just invoke **pop_front()**.
- As observed below, we must to know **the pointer x** which is stored in the **previous node** of node x.

list

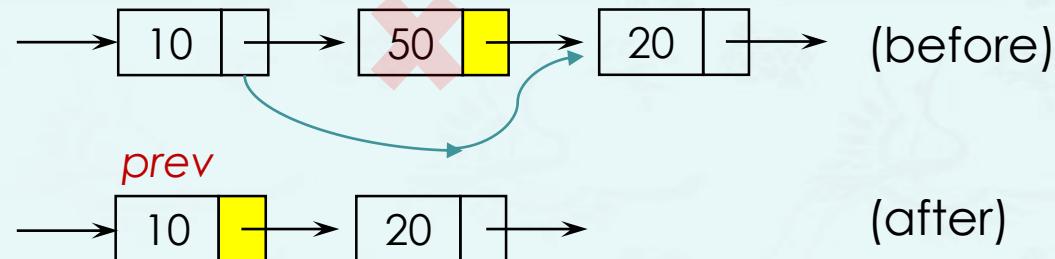


(before)

(after)

prev

curr



```
pNode pop(pNode list, int val)
```

```
if (list->data == val)  
    return pop_front(list);
```

```
pNode curr = list;  
pNode prev = nullptr;  
while (curr != nullptr) {
```

```
}
```

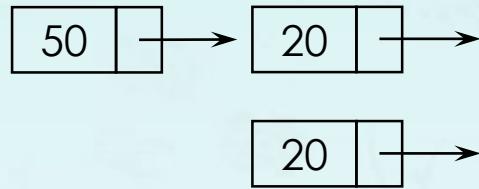
```
return list;
```

Linked List – **pop()**

TASK: Code a function that deletes a node with a value specified.

- If the first node(or **head**) is the one to delete, then just invoke **pop_front()**.
- As observed below, we must to know **the pointer x** which is stored in the **previous node** of node x.

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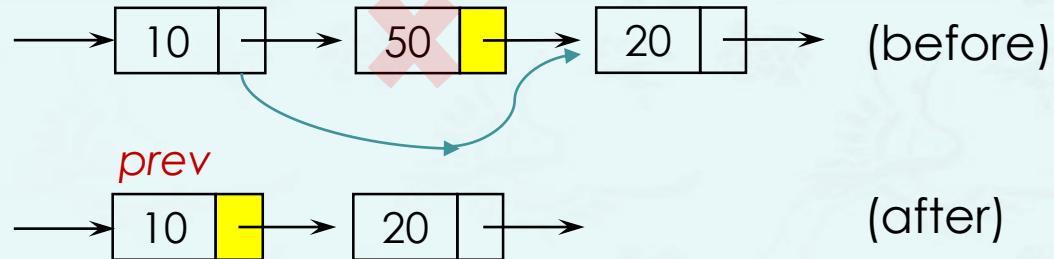


(before)

(after)

prev

curr



(before)

(after)

```
pNode pop(pNode list, int val)
```

```
if (list->data == val)  
    return pop_front(list);
```

```
pNode curr = list;  
pNode prev = nullptr;  
while (curr != nullptr) {  
    if (curr->data == val) {
```

```
}
```

```
}  
return list;
```

Linked List – insert()

TASK: Code a function that inserts a node(5) **at a node position x** specified by a value(7).

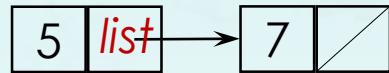
- If the first node(or **head**) is the position, then just invoke **push_front()**.
- As observed below, we must to know **the pointer x** which is stored in the **previous node** of node x.

list



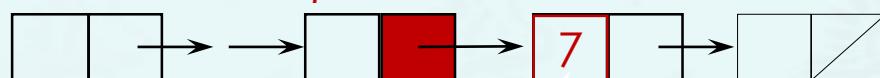
(before)

node



(after)

list



(before)

list



(after)

```
pNode insert(pNode list, int val, int x)
```

```
if (list->data == x)
```

```
pNode curr = list;
```

```
pNode prev = nullptr;
```

```
while (curr != nullptr) {  
    if (curr->data == x) {
```

```
        pNode node = new Node{val, prev->next};
```

```
        prev = curr;
```

```
        curr = curr->next;
```

```
}
```

```
return list;
```

Linked List

❖ resizing array vs. linked list

Tradeoffs. Can implement a stack with either resizing array or linked list; client can use interchangeably. Which one is better?

Linked-list implementation

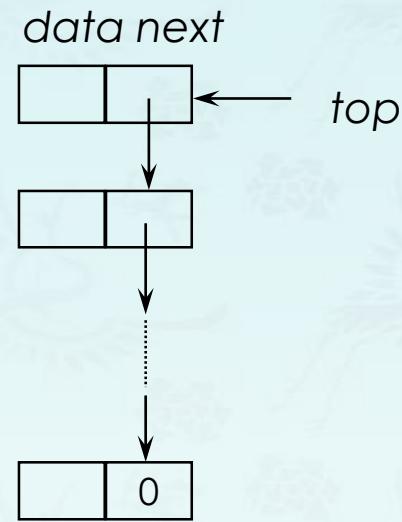
- Every operation takes constant time in the worst case.
- Uses extra time and space to deal with the links.

Resizing-array implementation

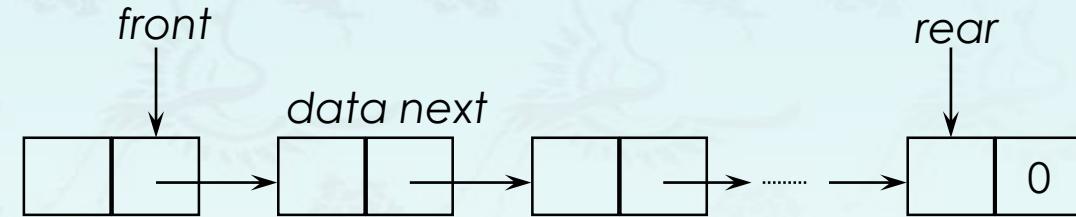
- Every operation takes constant amortized time.
- Less waste space

Linked List

Using linked lists, **stacks** and **queues** facilitate easy insertion and deletion of nodes.



(a) linked stack



(b) linked queue

Polynomials

❖ Polynomials representation

$$A(x) = a_{m-1}x^{e_{m-1}} + \cdots + a_0x^{e_0}$$

a_i = nonzero coefficients

e_i = nonnegative integer exponents such as

$e_{m-1} > e_{m-2} > \dots > e_0 \geq 0$

❖ We may draw a **poly node** as

coef	expo	next
------	------	------

❖ Type definition

```
struct Poly {  
    double coef;  
    double expo;  
    Poly* next;  
};  
using pPoly = Poly*;
```

Polynomials

❖ Example:

$$a \rightarrow [3 \ | \ 14 \ | \ \square] \rightarrow [2 \ | \ 8 \ | \ \square] \rightarrow [1 \ | \ 0 \ | \ 0]$$

(a) $3x^{14} + 2x^8 + 1$

$$b \rightarrow [8 \ | \ 14 \ | \ \square] \rightarrow [-3 \ | \ 10 \ | \ \square] \rightarrow [10 \ | \ 6 \ | \ 0]$$

(b) $8x^{14} + 3x^{10} + 10x^6$

Q: How to add two polynomials? $c = a + b$

Polynomials

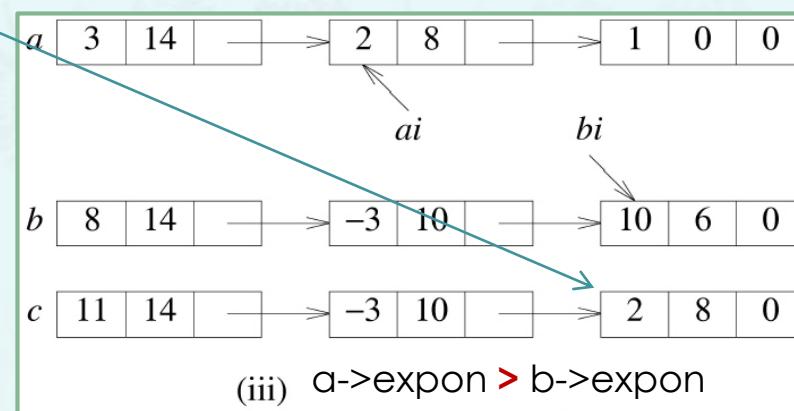
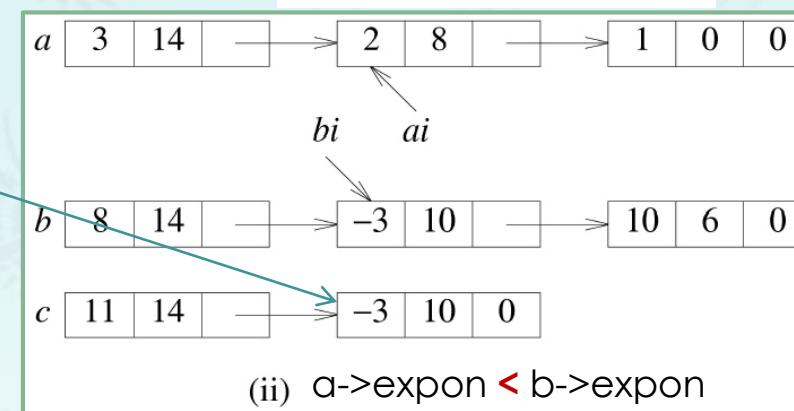
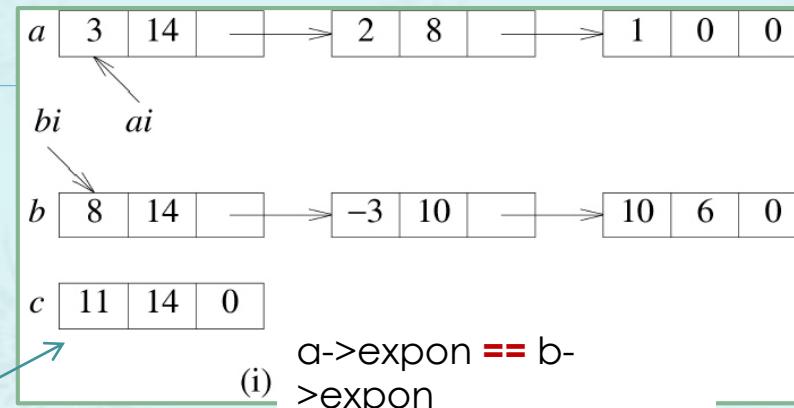
Q: How to add two polynomials?

$$a = 3x^{14} + 2x^8 + 1$$

$$b = 8x^{14} - 3x^{10} + 10x^6$$

$$c = a + b$$

$$= \mathbf{11x^{14} - 3x^{10} + 2x^8 + 10x^6 + 1}$$



Doubly Linked lists

- ❖ **Doubly linked list:** each node contains, besides the **next**-node link, a second link field pointing to the **previous** node in the sequence. The two links may be called **forward** and **backward**, or **next** and **prev(ious)**.



- ❖ **Type definition**

```
struct Node {  
    int      data;  
    Node*   prev;  
    Node*   next;  
};  
using pNode = Node*;
```

Q. Array vs. Singly linked list vs. Doubly linked list, Why?

Doubly Linked lists

Q. Array vs. Singly linked list vs. Doubly linked list, Why?

Advantages of linked list:

- Dynamic structure (Memory Allocated at run-time)
- Have more than one data type.
- Re-arrange of linked list is easy (Insertion-Deletion).
- **It doesn't waste memory.**

Disadvantages of linked list:

- In linked list, if we want to access any node it is difficult.
- **It uses more memory.**

Advantages of doubly linked list:

- A doubly linked list can be **traversed in both directions** (forward and backward). A singly linked list can only be traversed in one direction.
- Most operations are $O(1)$ instead of $O(n)$.

Pointer Linked – **Lab**

```
#include <iostream>
using namespace std;
class Node {
public:
    char ch;
    Node* next;
};

int main( ) {
    Node* p = nullptr, *q = nullptr;
    char ch;
    while (cin.get(ch) && ch != '\n') {
        p = new Node;
        p->ch = ch;
        p->next = q;
        q = p;
    }
    while (p != nullptr) {
        cout.put(p->ch);
        p = p->next;
    }
    cout << endl;
}
```

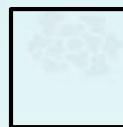
Pointer Linked – Lab

```
#include <iostream>
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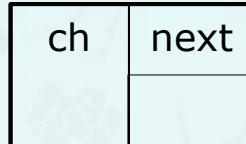
int main( ) {
    Node* p = nullptr, *q = nullptr;
    char ch;
    while (cin.get(ch) && ch != '\n') {
        p = new Node;
        p->ch = ch;
        p->next = q;
        q = p;
    }
    while (p != nullptr) {
        cout.put(p->ch);
        p = p->next;
    }
    cout << endl;
}
```

Assuming the input A, B, C, D to this program, what would be the data structure after the input?

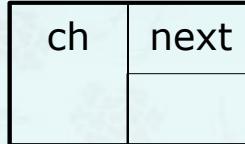
Draw a figure to represent the data structure in memory. Use a mnemonic memory address to represent each node such as A2, B5, C1, ..., etc.



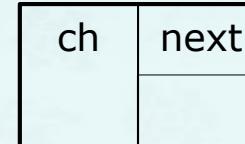
p
D3



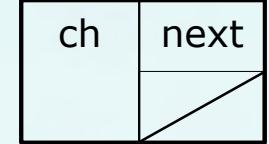
C1



B5



A2



q

What is missing in the figure?

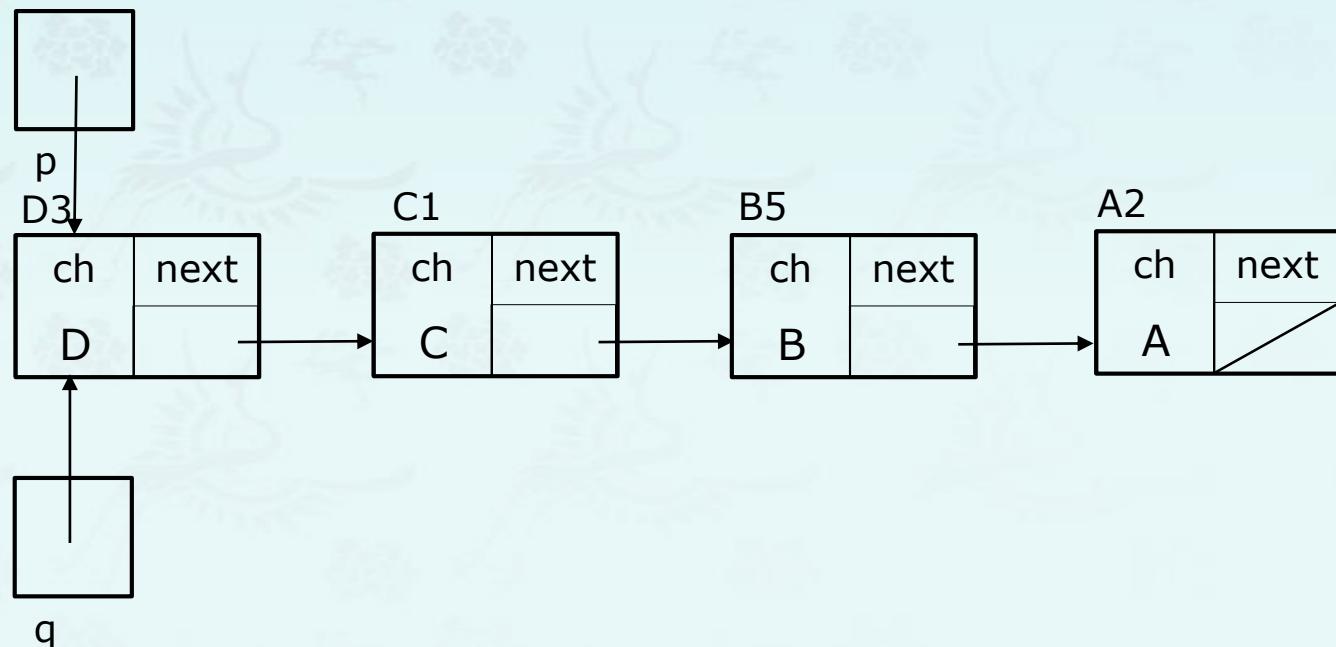
Pointer Linked

```
#include <iostream>
using namespace std;
class Node {
public:
    char ch;
    Node* next;
};

int main( ) {
    Node* p = nullptr, *q = nullptr;
    char ch;
    while (cin.get(ch) && ch != '\n') {
        p = new Node;
        p->ch = ch;
        p->next = q;
        q = p;
    }
    while (p != nullptr) {
        cout.put(p->ch);
        p = p->next;
    }
    cout << endl;
}
```

Assuming the input A, B, C, D to this program, what would be the data structure after the input?

Draw a figure to represent the data structure in memory. Use a mnemonic memory address to represent each node such as A2, B5, C1, ..., etc.



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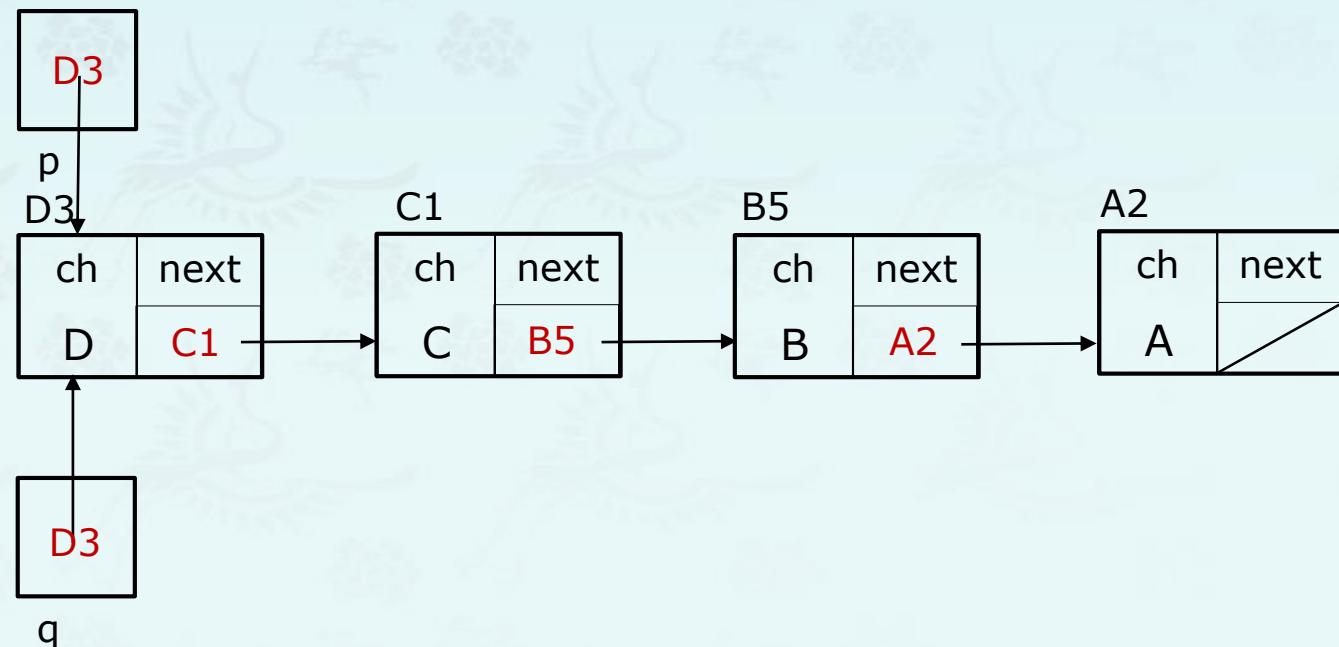
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After executing the while loop,
What is the output?
What are the values of p and q?

