## Métodos estadísticos y de inferencia causal

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Junio 2019

### Contenidos I

- Diseño de experimentos
  - Simulación de poder
- 2 Inferencia Causal
  - RCT
  - IV CF
  - Matching
  - Diff-in-Diff
  - SCM
- Attrition
  - Manski bounds
  - Lee bounds
- Clasificación
  - Gráficas de heterogeneidad por efectos fijos
  - Clustering & PCA

## Lectura sugerida I

- [AI17a] S. Athey and G.W. Imbens, Chapter 3 the econometrics of randomized experimentsa, Handbook of Field Experiments (Abhijit Vinayak Banerjee and Esther Duflo, eds.), Handbook of Economic Field Experiments, vol. 1, North-Holland, 2017, pp. 73 – 140.
- [AI17b] Susan Athey and Guido W. Imbens, The state of applied econometrics: Causality and policy evaluation, Journal of Economic Perspectives 31 (2017), no. 2, 3–32.
- [AP08] Joshua D. Angrist and Jörn-Steffen Pischke, Mostly harmless econometrics: An empiricist's companion, Princeton University Press, December 2008.

## Dropbox

Los materiales y ésta presentación la pueden encontrar aquí.

Diseño de experimentos

### Simulación de Poder I

Poder estadístico  $(1-\beta)$  es la verosimilitud/probablidad de detectar cierto efecto cuando hay un efecto que detectar.

$$H_0: \theta = 0$$

$$H_1 : \theta \neq 0$$

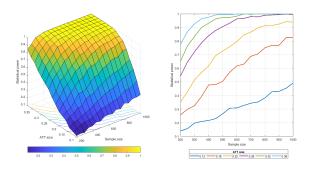
$$1 - \beta = Pr(\text{rechazar } H_0 \mid H_1 \text{ es verdadera})$$

Concluir	Realidad					
	$H_0$ TRUE	$H_0$ FALSE				
$H_0$ TRUE $H_0$ FALSE	$ \begin{array}{ c c }\hline (1-\alpha)\\ \text{Type II: }\alpha \end{array}$	Type I : $\beta$ $(1 - \beta)$				

### Simulación de Poder II

El proceso de simulación de poder identifica 2 etapas:

Método de identificación :  $\mathbb{E}[Y|X] = \theta^{\mathsf{T}}X$ 



Do files: sim\_AB\_FS\_1.do, simulation\_iv.do

Inferencia Causal

#### Obervaciones Potenciales

$$Y_{i} = \begin{cases} Y_{1i} & \text{if } D_{i} = 1 \\ Y_{0i} & \text{if } D_{i} = 0 \end{cases}$$
$$Y_{i} = Y_{0i} + (Y_{1i} - Y_{0i})D_{i}$$

¿Cómo obtenemos efectos de tratamiento promedio - (ATE)?

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$$\mathbb{E}[Y_i \mid D_i = 1, X_i] - \mathbb{E}[Y_i \mid D_i = 0, X_i] = \underbrace{\mathbb{E}[Y_{1i} \mid D_i = 1, X_i] - \mathbb{E}[Y_{0i} \mid D_i = 1, X_i]}_{\text{Bias}} + \underbrace{\mathbb{E}[Y_{0i} \mid D_i = 1, X_i] - \mathbb{E}[Y_{0i} \mid D_i = 0, X_i]}_{\text{Bias}}$$

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Problema fundamental de la inferencia causal

$$\mathbb{E}[Y_{0i} \mid D_i = 1, X_i]$$

# $RCT: \{Y_i\} \perp (D_i \mid X_i)$

Table 1: Treatment Effects

	Months after treatment							
		Same	e day settlen	nent	l	2 months	5 months	Long run
	Pha	se 1	Phase 2		Phase 1/2			
			OLS				OLS	
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
Control (constant)	0.060***	0.034***	0.11***	0.10***	0.094***	0.15***	0.39***	0.45***
Calculator	(0.013) 0.051** (0.022)	(0.011) 0.019 (0.019)	(0.030) 0.047** (0.021)	(0.030) 0.0077 (0.019)	(0.026) 0.018 (0.014)	(0.043) 0.0035 (0.021)	(0.039) -0.0069 (0.024)	(0.049) -0.0025 (0.025)
Conciliator	0.054***	0.033*	(0.021)	(0.013)	0.016	-0.0028 (0.023)	-0.030 (0.028)	-0.053 (0.036)
Emp present (EP)	(0.010)	0.14***		0.14* (0.072)	0.14***	0.11**	0.094*	0.070 (0.050)
Calculator#EP		0.16** (0.079)		0.16* (0.089)	0.16***	0.18***	0.16**	0.14**
Conciliator#EP		0.16** (0.074)		(,	0.16** (0.071)	0.21*** (0.079)	0.27*** (0.075)	0.20** (0.078)
Observations R-squared	1074 0.0072	1074 0.12	1092 0.051	1092 0.11	2166 0.13	2166 0.12	2166 0.11	2166 0.087
Court dummies	NO	NO	YES	YES	YES	YES	YES	YES
DepVarMean InteractionVarMean	0.0	0.18	0.	20	0.15	0.19 0.18	0.32	0.43
Calc=Conc Calc#EP=Conc#EP	0.88	0.53 0.98	-	- -	$0.94 \\ 1.00$	0.82 0.58	$0.79 \\ 0.68$	$0.40 \\ 0.085$

## IV - corrigiendo la endogeneidad

Consideremos un modelo  $y_i = X_i \beta + \epsilon_i$ 

$$\hat{\beta}_{OLS} = (X'X)^{-1}X'y = (X'X)^{-1}X'(X\beta\epsilon) = \beta + (X'X)^{-1}X'\epsilon$$

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#### Variables instrumentales Z

- Primera etapa fuerte :  $X_i = Z_i \gamma + \nu_i$
- Restricción de exclusión : Z'e = 0

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#### $\overline{\text{Variables instrumentales } Z}$

• Primera etapa fuerte :  $X_i = Z_i \gamma + \nu_i$ 

 $\bullet$ Restricción de exclusión :  $\ensuremath{\ensuremath{Z^\prime} e} = 0$ 

$$\hat{\beta}_{IV} = (Z'X)^{-1}Z'y \to \beta$$

#### Estimación - 2SLS

(i) 
$$X = Z\gamma + \nu$$

$$\hat{\gamma} = (Z'Z)^{-1}Z'X$$

$$\hat{X} = X\hat{\gamma} = \underbrace{Z(Z'Z)^{-1}Z'}_{P_Z}X$$

(ii) 
$$y = \hat{X}\beta + \epsilon$$

$$\hat{\beta}_{2SLS} = (X'P_ZX)^{-1}X'P_Zy = \hat{\beta}_{GMM}$$

• Lluvia

• Lluvia - no funcionó

- Lluvia no funcionó
- Distancia a la junta

- Lluvia no funcionó
- o Distancia a la junta no funcionó

#### Control function I

Es un método de dos etapas generalizado, pues explota la estructura de la variable endógena - por lo que obtenemos residuos generalizados.

$$\begin{array}{ll} y=X\beta+\epsilon & \quad \text{Ec. estructural} \\ X=Z\gamma+\nu & \quad \text{Primera etapa} \\ \mathbb{E}[Z'\nu]=0 & \quad \text{Ortogonalidad} \\ \epsilon=\nu\rho+u & \quad \mathbb{E}[\nu u]=0 & \quad \text{Residuo generalizado} \end{array}$$

De la última ecuación:  $\rho = \mathbb{E}[\nu\nu']^{-1}\mathbb{E}[\nu\epsilon]$  y notemos que

$$\{\epsilon,\nu\}\perp Z \Longrightarrow u\perp Z$$

$$\therefore u \perp X$$

Entonces,

CF

$$y = X\beta + \nu\rho + u$$

#### Control function II

- En el modelo lineal básico con coeficientes constantes, donde las VEE aparecen linealmente, y donde uso formas reducidas lineales, CF es lo mismo que 2SLS. Pero el primero proporciona una prueba simple y robusta de la hipótesis nula de que X es exógena :  $\rho=0$
- Quando exploto características especiales de la VEE, por ejemplo, reconozco que es una variable binaria, CF es probablemente más eficiente que 2SLS pero, en términos de consistencia, el enfoque de CF suele ser menos robusto que el de IV.
- ⑤ En modelos con múltiples funciones no lineales de VEE, el enfoque CF maneja parsimoniosamente la endogeneidad y proporciona pruebas de exogeneidad simples.

### Control function III

	Months after treatment									
	Same day settlement						5 months	Long run	Same da	
	Pha	se 1	Pha	ise 2		Phase 1/2				
	OLS					OLS C				
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	
Control (constant)	0.060***	0.034***	0.11***	0.10***	0.094***	0.15***	0.39***	0.45***	0.053	
	(0.013)	(0.011)	(0.030)	(0.030)	(0.026)	(0.043)	(0.039)	(0.049)	(0.040)	
Calculator	0.051**	0.019	0.047**	0.0077	0.018	0.0035	-0.0069	-0.0025	0.0084	
	(0.022)	(0.019)	(0.021)	(0.019)	(0.014)	(0.021)	(0.024)	(0.025)	(0.014)	
Conciliator	0.054***	0.033*			0.016	-0.0028	-0.030	-0.053	0.023	
	(0.019)	(0.018)			(0.019)	(0.023)	(0.028)	(0.036)	(0.019)	
Emp present (EP)		0.14***		0.14*	0.14***	0.11**	0.094*	0.070	0.47**	
		(0.050)		(0.072)	(0.041)	(0.046)	(0.048)	(0.050)	(0.21)	
Calculator#EP		0.16**		0.16*	0.16***	0.18***	0.16**	0.14**	0.16***	
		(0.079)		(0.089)	(0.056)	(0.061)	(0.064)	(0.061)	(0.054)	
Conciliator#EP		0.16**			0.16**	0.21***	0.27***	0.20**	0.17**	
		(0.074)			(0.071)	(0.079)	(0.075)	(0.078)	(0.074)	
Control Function									-0.19	
									(0.12)	
Observations	1074	1074	1092	1092	2166	2166	2166	2166	2166	
R-squared	0.0072	0.12	0.051	0.11	0.13	0.12	0.11	0.087	0.135	
Court dummies	NO	NO	YES	YES	YES	YES	YES	YES	YES	
DepVarMean	0.0	95	0.20		0.15	0.19	0.32	0.43	0.15	
Interaction Var Mean		0.18					0.18			
Calc=Conc	0.88	0.53	-	-	0.94	0.82	0.79	0.40	0.47	
Calc#EP=Conc#EP	-	0.98	-	-	1.00	0.58	0.68	0.085	0.91	

Do files: treatment\_effects.do, treatment\_effects\_IV\_CF.do

### Matching

Recordemos el problema fundamental de inferencia causal:  $\mathbb{E}[Y_{0i} \mid D_i = 1, X_i]$ ?

## Supongamos: strong ignorability

 $CIA: (Y_i|X) \perp D_i$ 

$$(I_i|A) \perp D_i$$

Overlap :  $0 < e(x) := \mathbb{E}[D_i \mid X_i = x] < 1$  para todo x en el soporte de X

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$$0 < e(x) := \mathbb{E}[D_i \mid X_i = x] < 1$$
 para todo  $x$  en el soporte de  $X$ 

Sea

$$m(i) = \operatorname{argmin}_{j:D_j \neq D_i} ||X_i - X_j||$$

$$\begin{split} \hat{Y}_i(0) &= \begin{cases} Y_i^{obs} & \text{si } D_i = 0 \\ Y_{m(i)}^{obs} & \text{si } D_i = 1 \end{cases} & \hat{Y}_i(1) &= \begin{cases} Y_{m(i)}^{obs} & \text{si } D_i = 0 \\ Y_i^{obs} & \text{si } D_i = 1 \end{cases} \\ \hat{X}_i(0) &= \begin{cases} X_i^{obs} & \text{si } D_i = 0 \\ X_{m(i)}^{obs} & \text{si } D_i = 1 \end{cases} & \hat{X}_i(1) &= \begin{cases} X_{m(i)}^{obs} & \text{si } D_i = 0 \\ X_i^{obs} & \text{si } D_i = 1 \end{cases} \end{split}$$

El estimador de matching está dado por:

$$\hat{\tau} = \frac{1}{N} \sum_{i} \hat{Y}_{i}(1) - \hat{Y}_{i}(0)$$

### Matching

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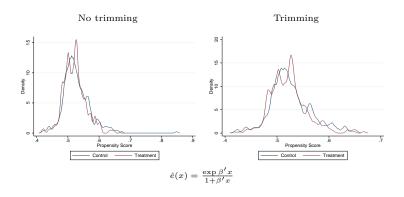
El estimador de matching está dado por:

$$\hat{\tau} = \frac{1}{N} \sum_{i} \hat{Y}_i(1) - \hat{Y}_i(0)$$

Se puede mejorar el sezgo de este estimador usando regresión lineal para ajustar el sezgo asociado con diferencias entre  $\hat{X}_i(0)$  y  $\hat{X}_i(1)$ .

### Estimación I

(I) 'Verificar' overlap - Trimming procedure



### Estimación II

#### (II) Balance

Table 2: Balance

	Control	Treatment	p-value
Entitlement by law	60234.96	57567.95	0.62
	(3400.38)	(4098.63)	
Public lawyer	0.08	0.09	0.77
	(0.01)	(0.01)	
Woman	0.45	0.45	0.86
	(0.02)	(0.03)	
At will worker	0.07	0.06	0.44
	(0.01)	(0.01)	
Tenure	3.82	3.47	0.29
	(0.25)	(0.22)	
Daily wage	535.31	514.78	0.7
	(32.76)	(40.85)	
Weekly hours	58.5	56.79	0.12
	(0.81)	(0.73)	
Observations	416	377	

### Estimación III

#### (III) 'Evaluar' CIA

Table 3: Pseudo-treatment effect

Pseudo treatment effect. Nearest-neighbor matching						
	Phase 1/2					
	Entitlement	Daily wage	Tenure			
	(1)	(2)	(3)			
ATE	28.3 (1162.4)	-2.3 (11)	-0.2 (.2)			
% ATE	0.05	-0.43	-5.22			
Baseline mean	60342.9	536.2	3.8			
Obs		377				
Obs HD		415				
Bias adjustment	YES	YES YES				
Matches	[1-3]	[1-3]	[1-3]			

### Estimación IV

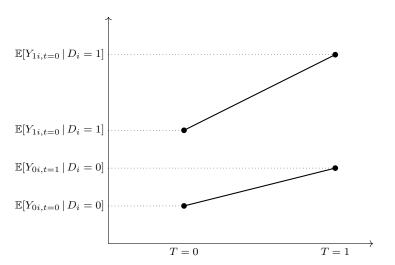
(III) Análisis

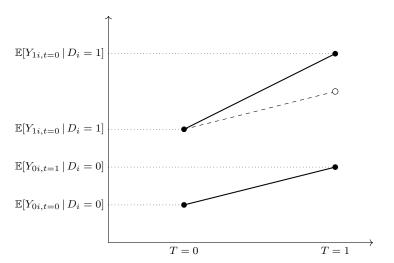
Table 4: Matching

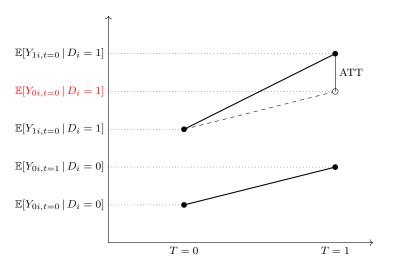
	Treatment	effect. Nea	rest-neigh	bor matchi	ng			
	Phase 1/2							
		Variable	PSM					
	(1)	(2)	(3)	(4)	(5)	(6)		
ATE	2580 (1939)	3536** (1715)	3242* (1934)	3939** (1725)	3698* (1900)	3995** (1554)		
% ATE	34	47	43	52	49	53		
Baseline mean Obs Obs HD	7598 377 415							
Bias adjustment Matches	NO [1-1]	NO [1-3]	YES [1-1]	YES [1-3]	[1-1]	- [1-3]		

Do files: settlement\_conciliator\_matching.do

### DiD - Parallel Worlds





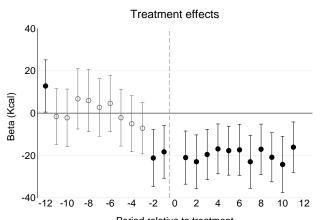


## Impuesto a bebidas azucaradas

Regresión DiD con FE:

$$C_{it}^{k} = \alpha_i + \gamma_t + \sum_{j=-12}^{12} \beta_k T_i \times I(t=j) + \nu_{it}$$

donde  $T_i = 1$  si i está en el grupo más expuesto



## Synthetic Control Methods (SCM) I

Sean  $(y_{tn}^0, y_{tn}^1)$  las observaciones potenciales para la unidad n al tiempo t.

$$y_{tn} = D_{tn}y_{tn}^1 + (1 - D_{tn})y_{tn}^0$$
,  $D_{tn} = \begin{cases} 1 & \text{if } t \ge T_0, n = 0\\ 0 & \text{otherwise} \end{cases}$ 

El efecto de tratamiento es :  $\tau_{tn} \equiv y_{tn}^1 - y_{tn}^0$ El supuesto clave en SCM es:

Existen pesos  $\beta_n \in [0,1]$  para  $n=1,\ldots,N$  tales que

$$y_{t0}^{0} = \sum_{n=1}^{N} \beta_n y_{tn}^{0}$$

para t = 1..., T; y los pesos suman uno:  $\sum_{n=1}^{N} \beta_n = 1$ .

El estimador en  $t = T_0, \dots, T$  está dado por:

$$\tau_t = y_{t0}^1 - \sum_{n=1}^N \beta_n y_{t0}^0$$

## Synthetic Control Methods (SCM) II

Denotando por  $x_t \equiv (y_{t1}, \dots, y_{tN})^\mathsf{T}$  a el vector de las observaciones para los controles. Podemos considerar el modelo de regresión

$$y_{t0} = \beta^{\mathsf{T}} x_t + u_{t0} \qquad t = 1, \dots, T_0$$
 (1)

y la estimación por lo tanto está dada por:

$$\min \sum_{t=1}^{T_0} (y_{t0} - \beta^\mathsf{T} x_t)^2 \tag{2}$$

s.t.

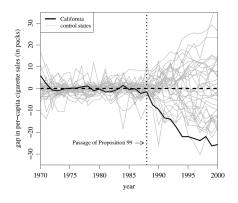
$$||\beta||_1 = 1$$
  
$$\beta_i \ge 0 \quad i = 1, \dots, n$$

# ¿Inferencia?

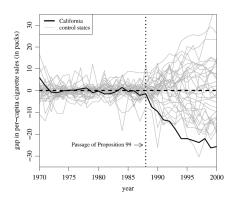
El principal problema con esta metodología es la dificultad para conducir **inferencia**, es decir, hay poco o ningún conocimiento sobre la distribución asintótica del estimador SCM, o su **intervalo de confianza**.

- (i) Enfoques de población finita: Supuesto de que las unidades de tratamiento se asignan aleatoriamente y usan placebos, pruebas de permutación o alguna variante que explota la estructura de datos del panel, para realizar inferencia, que son llamados
- (ii) Enfoques asintóticos: Los supuestos clave hacen que el número de individuos o períodos de tiempo tienden a infinito.

# ¿Inferencia?



## ¡Inferencia!



## **RWP**

### Theorem

La región de confianza para el estimador SCM está dada por:

$$B\left(\hat{\tau}_t, \mathbf{r}||x_t|| + \sigma z_{(1-\alpha/2)}\right)$$

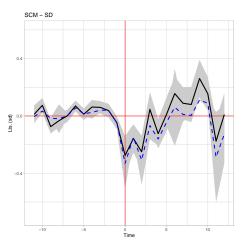
$$donde \; \mathsf{r} = \frac{||\nabla R_{T_0}(\hat{\beta})|| + \sqrt{||\nabla R_{T_0}(\hat{\beta})||^2 - 2|\Omega_{\hat{\beta}}| \left(R_{T_0}(\hat{\beta}) - T_0^{-1}\chi_{1-\alpha}\right)}}{|\Omega_{\hat{\beta}}|}$$

## SCM con datos panel

Explotamos la estructura de panel y las múltiples unidades tratadas.

## SCM con datos panel

Explotamos la estructura de panel y las múltiples unidades tratadas.



Rscript: SCM\_synth.R

Attrition

### Manski bounds I

- Ningún supuesto sobre el mecanismo de selección
- La variable dependiente necesita estar acotada
- NA imputados de acuerdo al mínimo y máximo valor posible
- Cotas no informativas :(

## Manski bounds II

Sea  $S_i$  una dummy identificando a los 'no-attriters'.

$$_{i}E[Y_{1i} \mid S_{i} = 0 | D_{i} = 1]$$
 $E[Y_{0i} \mid S_{i} = 0, D_{i} = 0]?$ 

Worst-case scenario :  $E[Y_{1i} \mid S_i = 0 \mid D_i = 1] = 0$  y  $E[Y_{0i} \mid S_i = 0, D_i = 0] = 1$ 

$$MB^{L} = P(S_{i} = 1 \mid D_{i} = 1)E(Y_{i} \mid D_{i} = 1, S_{i} = 1)$$
$$- [P(S_{i} = 1 \mid D_{i} = 0)E(Y_{i} \mid D_{i} = 0, S_{i} = 1) + P(S_{i} = 0 \mid D_{i} = 0)]$$

análogamente:

$$MB^{U} = P(S_{i} = 1 \mid D_{i} = 1)E(Y_{i} \mid D_{i} = 1, S_{i} = 1) + P(S_{i} = 0 \mid D_{i} = 1)$$
$$-P(S_{i} = 1 \mid D_{i} = 0)E(Y_{i} \mid D_{i} = 0, S_{i} = 1)$$

## Lee bounds I

- RAT :  $(Y_i, S_i) \perp D_i$
- Monotonicidad :  $Pr(S_1 \ge S_0) = 1$ Asignación de tratamiento sólo afecta *attrition* en una dirección solamente.

El objetivo es encontrar cotas

$$LB^{L} \leq \mathbb{E}[Y_1 - Y_0 \mid S_0 = 1, S_1 = 1] \leq LB^{U}$$

### Lee bounds II

### <u>Theorem</u>

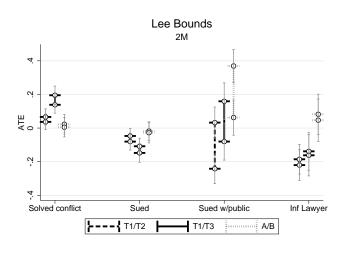
Bajo RAT, monotonicidad y 
$$PR(S = 1 \mid D = 0) \neq 0$$
  

$$LB^{L} = \mathbb{E}[Y \mid D = 1, S = 1, Y \leq F^{-1}(1 - p)] - \mathbb{E}[Y \mid D = 0, S = 1]$$

$$LB^{U} = \mathbb{E}[Y \mid D = 1, S = 1, Y \geq F^{-1}(p)] - \mathbb{E}[Y \mid D = 0, S = 1]$$

$$donde \ p = \frac{Pr(S = 1 \mid D = 1) - Pr(S = 1 \mid D = 0)}{Pr(S = 1 \mid D = 1)}.$$

## Lee bounds III



Do files: plot\_lee\_bounds.do

## Clasificación

## Calificación de abogados

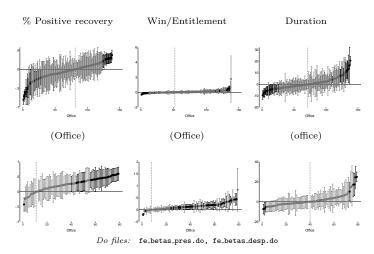
Table 5: Predicciones

	Outcome	Judge ruling prediction		End mode prediction		Payment prediction		Total	
	Lawyer	Lawyer	Calc	Lawyer	Calc	Lawyer	Calc	Lawyer	Calc
1	12.8%	44.4%	27.8%	61.1%	55.6%	19.5%	19.5%	34.5%	34.3%
2	11.2%	62.5%	68.8%	87.5%	62.5%	0%	12.8%	40.3%	48%
3	15.2%	56.3%	62.5%	62.5%	62.5%	22.7%	17.3%	39.2%	47.4%
4	35.2%	45.5%	50%	36.4%	77.3%	15.3%	18.8%	33.1%	48.7%
5	5.6%	33.3%	75%	33.3%	62.5%	9.9%	19.8%	20.5%	52.4%
6	9.6%	60%	70%	70%	65%	0%	18.6%	34.9%	51.2%
7	16%	50%	55.6%	55.6%	72.2%	13.9%	13.9%	33.9%	47.2%
8	13.6%	54.5%	77.3%	86.4%	72.7%	21.4%	21.4%	44%	57.1%

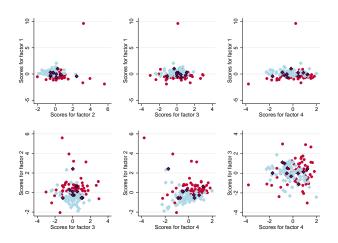
Do files: lawyer\_dataset.do, lawyer\_dataset\_predicc.do, cleaning\_base\_calidad.do, calif\_abogados\_pagos.do

# Heterogeneidad - FE I

Figure 2: Heterogeneous outcome graphs



# Clusters: Buenos/Malos



Do files: lawyer\_dataset\_collapsed.do, cluster\_analysis.do

Gracias:)

### Instalación de OSRM

- (1) Install Node.js 8.11.3 LTS (or current)
- (2) Extract the file osrm\_Release.zip (link from my Dropbox). This is the latest OSRM Windows build.
- (3) Copy the file mexico-latest.osm.pbf in the osrm\_Release folder.
- (4) Open Node.js command prompt
  - Change directory to the osrm\_Release folder cd ~/osrm\_Release
  - Extracting the road network<sup>1</sup> osrm-extract mexico-latest.osm.pbf osrm-contract mexico-latest.osm.pbf

This previous steps only need to be done once. This sets the road network for Mexico.

- You can also download the road network files here. (Extract and copy in the osrm-Release folder.
- (5) Install R package osrm (Version I'm using is Package osrm version 3.0.2

<sup>&</sup>lt;sup>1</sup>If instead you want MLD use osrm-partition and osrm-customize instead of osrm-contract.

### Instalación de OSRM I

In order to launch OSRM as a local instance the following steps are needed.

- Change directory to the osrm\_Release folder in Node.js command prompt cd ~/osrm\_Release
- Set the local OSRM instance osrm-routed --max-table-size=1500 mexico-latest.osrm
- In R, run the script:

```
1 # PACKAGES
2 library (tidyverse) # data wrangling
3 library (stringr) # work with strings
4 library (sf)
              # geospatial
5 library (geosphere) # calculate distances
6 library(haven) # read/write .dta (Stata)
7 library (here) # use relative filepaths
8 library (osrm)
               # calculate road distances
9 library (assertthat)
2 # old spatial packages since osrm works with those
3 library(sp) #spatial objects; used by rgdal
6 # Read in data set
7 dataset = read_dta(here::here("folder", "dta.dta"))
0 # Convert to SpatialPointsDataFrame for use with osrmTable
1 dataset_spdf <- dataset %>% as('Spatial')
```

### Instalación de OSRM II

```
4 # Use OSRM's server
5 options (osrm.server = "http://router.project-osrm.org/")
6 # NOTE: above uses OSRM's server. If we try one with more than 10,000 queries:
8 # We get the error:
9 # OSRM returned an error:
_0 \mid \# Error: The public OSRM API does not allow results with a number of durations
_{
m 1} | \# higher than 10000. Ask for fewer durations or use your own server and set
      its
2 # --max-table-size option.
4 # Now try it on a local server to avoid the 10,000 guery limit:
5 # First follow the instructions here to install and build the OSRM server:
6 # https://datawookie.netlify.com/blog/2017/09/building-a-local-osrm-instance/
7 # or:
8 # https://github.com/Project-OSRM/osrm-backend/wiki/Running-OSRM
0 # Once the local server is running:
1 options (osrm.server = "http://localhost:5000/")
2 #Compute distances
distances <- osrmTable(src = src, dst = dst)
4 #Check the function osrmViaroute for pairwise comparisons.
```

./Rscripts/geocode.R

### Instalación de OSRM III

```
\Users\xps-seira\Dropbox\repos\osrm\osrm-backend>osrm-routed
osrm-routed <base.osrm> [<options>]:
Options:
  -υ [ --version ]
                                         Show version
  -h [ --help 1
                                         Show this help message
  -1 [ --verbosity ] arg (=INFO)
                                         Log verbosity level: NONE, ERROR,
                                         WARNING, INFO, DEBUG
  --trial [=arg(=1)]
                                         Quit after initialization
Configuration:
  -i [ --ip ] arg (=0.0.0.0)
                                        IP address
  -p [ --port 1 arg (=5000)
                                        TCP/IP port
  <u>-t [ --threads ] arg (=4)</u>
                                         Number of threads to use
  -s [ --shared-memoru ] [=arg(=1)] (=0)
                                         Load data from shared memoru
  -a [ --algorithm ] arg (=CH)
                                         Algorithm to use for the data. Can be
                                         CH, CoreCH, MLD.
  --max-viaroute-size arg (=500)
                                         Max. locations supported in viaroute
                                         queru
  --max-trip-size arg (=100)
                                         Max. locations supported in trip queru
  --max-table-size arg (=100)
                                         Max. locations supported in distance
                                         table queru
  --max-matching-size arg (=100)
                                         Max. locations supported in map
                                         matching query
                                         Max. results supported in nearest queru
  --max-nearest-size arg (=100)
  --max-alternatives arg (=3)
                                         Max. number of alternatives supported
                                         in the MLD route query
  --max-matching-radius arg (=5)
                                         Max. radius size supported in map
                                         matching queru
```

#### Recursos

- Github repo: https://github.com/Project-OSRM/osrm-backend
- Build using docker on Windows: https://phabi.ch/2020/05/06/run-osrm-in-docker-on-windows/

De regreso a los instrumentos.

## Definición de grupo expuesto

Definir un grupo de tratamiento / control puro. Lo haremos eligiendo una partición óptima de la distribución total del gasto sujeto a impuestos, ya que es probable que los grandes gastadores sean más sensibles a un cambio de precio en SD, por lo que los definiremos como el grupo de tratamiento.

$$\begin{aligned} & \underset{H,L}{\min} & & \sum_{t=-12}^{-2} |\beta_t| \\ & \text{s.t} & \\ & & (\beta_t)_{-12 \leq t \leq 12} = \operatorname{argmin} \left\{ \left( y_{it} - \sum_{k=-12}^{12} \alpha_k \mathbbm{1}(t=k) - \sum_{k=-12}^{12} \beta_k \mathbbm{1}(i=T,k=t) + \gamma \mathbbm{1}(i=T) - \lambda_i \right)^2 \right\} \\ & & T = \mathbbm{1}(x_i \geq H) \\ & & C = \mathbbm{1}(x_i \leq L) \\ & & \min(x_i) < L < H < \max(x_i) \end{aligned}$$

De regreso a DiD