

$hist[i] \sim X, \text{ for } 0 \leq i \leq maxVal$
Therefore, $Supp[X] = \{0, 1, 2, 3 \dots, maxVal\}$.

Let $n = \text{total number of pixels in the image, which means}$

$$\sum_{i=0}^{maxVal} hist[i] = n$$

$Mean[X]$ is the average pixel value in the image.

Since $Mean[Y] = \sum_{y \in Supp[Y]} y * p(y)$, where $p(y) = \text{the probability of } y$,

Therefore, $\mu = Mean[X] = \sum_{i=0}^{maxVal} i * p(i)$, where $p(i) = \frac{hist[i]}{n}$

and, $\sigma^2 = Var[X] = \sum_{i=0}^{maxVal} (i - \mu)^2 * p(i)$, where $p(i) = \frac{hist[i]}{n}$

$gaussian(i, \mu, \sigma^2) \in [0, 1)$ since it is a normalized probability function

Assuming Mean and Var are calculated correctly then

$$\sum_{i=0}^{maxVal} gaussian(i, \mu, \sigma^2) \text{ should approach } 1.$$

With the professor's histogram, the above summation adds up to 0.97, which is expected.

However, since $gaussian(i, \mu, \sigma^2) \in [0, 1)$, all $Gval[i]$ in the program will truncate to 0. To fix this, each $Gval[i]$ must be scaled by n to represent the number of values $hist[i]$ in n .

Therefore, $Gval[i] = n * gaussian(i, \mu, \sigma^2)$