## Returns to Education

January 13, 2019

## Markets in Education

#### Education is a unique marketplace:

- It is not perfectly competitive (e.g. large fixed costs, imperfect information);
- Spillovers or externalities are quite common;
- Supply is often local(ish);
- Education is highly differentiated, both vertically (age) and horizontally (different quality/classes for individuals who are the same age);
- The quality of your education (might) depend on the characteristics of other consumers (i.e. your peers).

That means that we can use economic tools to answer questions about education policy, but we need to go beyond the simplest models of perfect competition. Although plenty of policy-makers and commentators focus on trying to get the market more toward their perfect competition ideal.

- Simple economic model:
  - An individual's utility depends on their consumption: u(c)
  - Their consumption depends on their wage:  $p \cdot c \leq w$
  - Their wage depends on their eduction: w = w(e)
- One of the earliest (and most important) questions in the economic of eduction: what are the returns to eduction?
  - For now, we will focus on the individual returns to eduction as opposed to the social returns to eduction.
- What do we mean by the "returns to eduction?"
- Why do we care about the individual returns to eduction?



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## Estimating the Individual Returns to Eduction

Let's suppose that you ran an OLS regression:

$$In(Y_i) = \beta_0 + \beta_1 Education_i + \epsilon_i$$
 (1)

- Does  $\beta_1$  define the individual returns to education?
- If not, is  $\beta_1$  larger or smaller than the returns to eduction?



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• Let's assume that an individual's outcome  $Y_i$  is a function of her years of education  $(Ed_i)$  and ability  $(Ability_i)$ 

$$Y_i = \beta_0 + \beta_1 E d_i + \beta_2 Ability_i + \epsilon$$
 (2)

• What happens if we just estimate our original model, omitting ability?

$$Y_i = \gamma_0 + \gamma_1 E d_i + \mu \tag{3}$$

• Using our formula for a regression coefficient  $E(\hat{\gamma}_1) = \frac{cov(Y, Ed_i)}{var(Ed_i)}$ , and substituting  $\alpha + \beta_1 Ed_i + \beta_2 Ability_i + \epsilon$  for  $Y_i$ , we get:

$$E(\hat{\gamma}_1) = \frac{cov(\alpha + \beta_1 Ed_i + \beta_2 Ability_i + \epsilon, Ed_i)}{var(Ed_i)}$$
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$$= \frac{cov(\beta_0, Ed_i)}{var(Ed_i)} + \beta_1 + \beta_2 \frac{cov(Ability_i, Ed_i)}{var(Ed_i)} + \frac{cov(\epsilon, Ed_i)}{var(Ed_i)}$$
(5)

- The first term is zero since  $\beta_0$  is a constant and the last term is also zero given the main OLS assumptions ( $cov(\epsilon, X_i) = 0$ )
- This leaves us with the omitted variable bias formula:

$$E(\hat{\gamma}_1) = +\beta_1 + \beta_2 \frac{cov(Ability_i, Ed_i)}{var(Ed_i)}$$
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- Note that the last term  $\frac{cov(Ability_i, Ed_i)}{var(Ed_i)}$  is the coefficient from a
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- There are (roughly) six approaches to estimating the returns:
  - Bound the returns to education
  - Selection-on-observables
  - Structural models
  - 4 Twin studies
  - Quasi-experimental evidence
  - ® Random Control Trials (RCTs)



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