



Physics. *You work it out.*

[Home](#) [Gameboard](#) [Maths](#) [Projectiles: Trajectories 4ii](#)

Projectiles: Trajectories 4ii

A Level



A particle P is projected with speed 40 m s^{-1} at an angle of 35° above the horizontal from a point O.

Part A Magnitude of velocity

For the instant 3 s after projection, calculate the magnitude of the velocity of P. Give your answer to 3 significant figures.

Part B Direction of velocity

For the instant 3 s after projection, calculate the direction of the velocity of P. Give your answer as an angle, in degrees, below the horizontal to 3 significant figures.

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Physics. *You work it out.*[Home](#) [Gameboard](#) [Maths](#) [Projectiles: Trajectories 1i](#)

Projectiles: Trajectories 1i

A Level

A stone is projected horizontally with speed 7 m s^{-1} from a point O on the edge of a vertical cliff. The horizontal and upward vertical displacements of the stone from O at any subsequent time, t seconds, are $x \text{ m}$ and $y \text{ m}$ respectively. Assume that there is no air resistance.

Part A y in terms of x

In this question, use the value $g = 9.8 \text{ m s}^{-2}$ for the acceleration under gravity.

By first expressing x and y in terms of t , find an expression for y in terms of x .

The following symbols may be useful: x , y

Part B Distance between cliff and stone

The stone hits the sea at a point which is 20 m below the level of O.

Find the distance between the foot of the cliff and the point where the stone hits the sea. Give your answer to 3 significant figures.

Part C Speed and direction of motion

Find the speed of the stone immediately before it hits the sea. Give your answer to 2 significant figures.

Find the direction of motion of the stone immediately before it hits the sea. Give your answer as an angle below the horizontal to 3 significant figures.

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Equations

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Projectiles: Trajectories 4i

A Level



A particle is projected with speed 7 m s^{-1} at an angle of elevation of 30° from a point O and moves freely under gravity. The horizontal and vertically upwards displacements of the particle from O at any subsequent time $t \text{ s}$ are $x \text{ m}$ and $y \text{ m}$ respectively.

Part A x & y in terms of t

In this question, use the value $g = 9.8 \text{ m s}^{-2}$ for the acceleration under gravity.

Express x in terms of t . When entering your answer, use fractions and surds rather than decimals.

The following symbols may be useful: $\cos()$, $\sin()$, t , $\tan()$, x

Express y in terms of t . When entering your answer, use fractions rather than decimals.

The following symbols may be useful: $\cos()$, $\sin()$, t , $\tan()$, y

Part B y in terms of x

Hence find the equation, y in terms of x , for the trajectory of the particle.

The following symbols may be useful: x , y

Part C Values of x

Calculate the smaller of two values of x when $y = 0.6$. Give your answer as an exact surd.

Calculate the larger of two values of x when $y = 0.6$. Give your answer as an exact surd.

Part D Direction of motion

Find the direction of motion of the particle when $y = 0.6$ and the particle is rising. Give your answer as an angle from the horizontal and to 3 significant figures.

Adapted with permission from UCLES, A Level, OCR M2, June 2011, Question 5

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Physics. *You work it out.*

[Home](#) [Gameboard](#) [Maths](#) [Parametric Equations 3ii](#)

Parametric Equations 3ii

A Level
P P P

Figure 1 shows the curve with parametric equations

$$x = a \sin \theta, \quad y = a\theta \cos \theta,$$

where a is a positive constant and $-\pi \leq \theta \leq \pi$. The curve meets the positive y -axis at A and the positive x -axis at B.

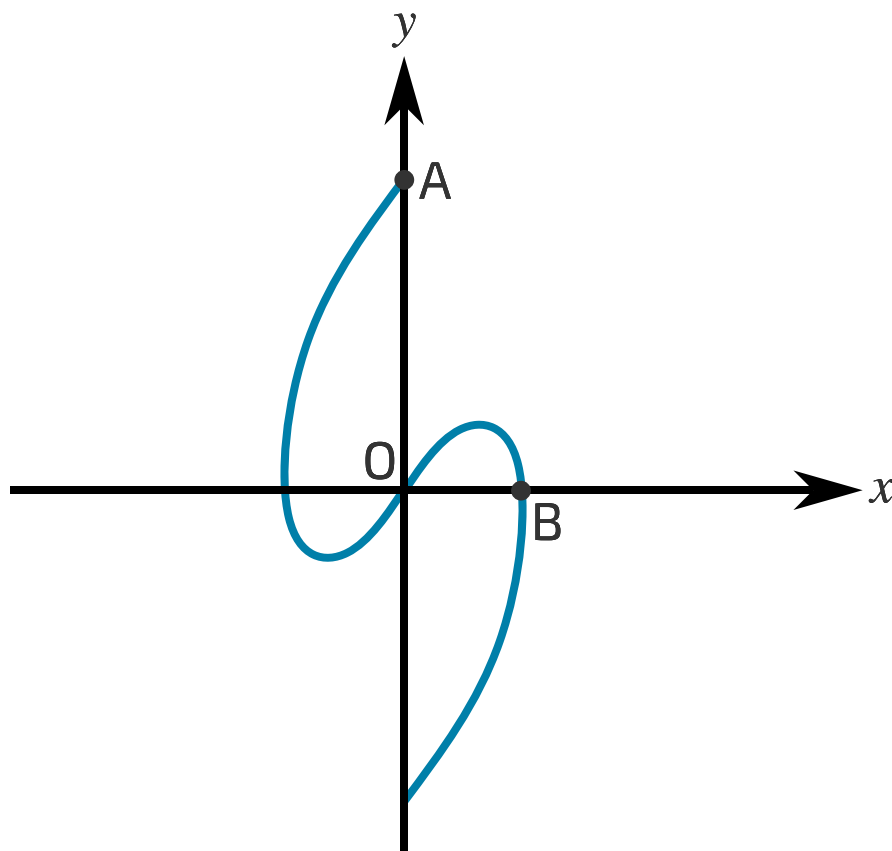


Figure 1: The graph defined by $x = a \sin \theta, y = a\theta \cos \theta$ for $-\pi \leq \theta \leq \pi$.

Part A Points O, A and B

What is the value of θ corresponding to the origin?

$\theta =$

What are the coordinates of A?

(0,)

What are the coordinates of B?

(, 0)

Items:

- $-\pi$

$-\frac{\pi}{2}$

0

$\frac{\pi}{2}$

π

$-2a$

$-\pi a$

$-a$

$-\frac{\pi}{2}a$

a

$\frac{\pi}{2}a$

$2a$

πa

Part B Gradient

Find an expression for $\frac{dy}{dx}$.

The following symbols may be useful: `Derivative(y, x)`, `arccos()`, `arccosec()`, `arccot()`, `arcsec()`, `arcsin()`, `arctan()`, `cos()`, `cosec()`, `cot()`, `sec()`, `sin()`, `tan()`, `theta`, `x`, `y`

Part C Tangent equation

Find the equation for the tangent to the curve at the origin.

The following symbols may be useful: `x`, `y`

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Parametric Equations 1ii

A Level

A curve is defined by the parametric equations

$$x = \sin^2 \theta, y = 4 \sin \theta - \sin^3 \theta$$

where $-\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}$.

Part A Find $\frac{dy}{dx}$

Find an expression for $\frac{dy}{dx}$.

The following symbols may be useful: `Derivative(y, x)`, `arccos()`, `arccosec()`, `arccot()`, `arcsec()`, `arcsin()`, `arctan()`, `cos()`, `cosec()`, `cot()`, `sec()`, `sin()`, `tan()`, `theta`, `x`, `y`

Part B Point on the curve

Find the coordinates of the point on the curve at which the gradient is 2.

Give your answers as exact fractions.

x -coordinate:

y -coordinate:

Part C Stationary points

Drag and drop answers into the boxes below to complete the argument showing that the curve has no stationary points.

If the curve has stationary points, $\frac{dy}{dx}$ at those points. Hence, using the expression for $\frac{dy}{dx}$ found in part A,

$- 3 \sin^2 \theta = 0$

$\Rightarrow \sin \theta = \pm \sqrt{\frac{\text{}}{3}}$

However, $\sin \theta$ obeys the inequality $\leq \sin \theta \leq$ so there is no value of θ that satisfies $\sin \theta = \pm \sqrt{\frac{\text{}}{3}}$. Therefore, there are no stationary points.

Items:

- 2

-1

< 0

= 0

0

> 0

1

2

4

5

6

7

Part D Cartesian equation

Find a cartesian equation of the curve, giving your answer in the form $y^2 = f(x)$.

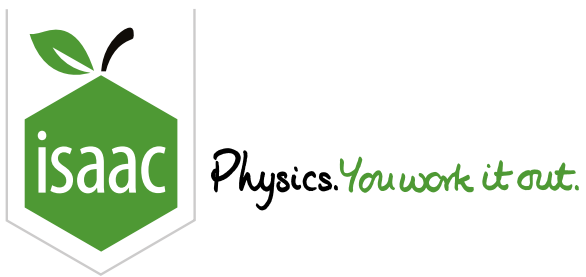
The following symbols may be useful: x, y

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[Home](#) [Gameboard](#) [Maths](#) [Parametric Equations 2i](#)

Parametric Equations 2i



A curve has parametric equations

$$x = \frac{1}{t+1}, y = t - 1.$$

The line $y = 3x$ intersects the curve at two points.

Part A Value of t

Show that the value of t at one of these points is -2 and find the value of t at the other point.

The following symbols may be useful: t

Part B Normal

Find the equation of the normal to the curve at the point for which $t = -2$, giving your answer in the form $y = f(x)$.

The following symbols may be useful: x , y

Part C Value of t

Find the value of t at the point where this normal meets the curve again.

The following symbols may be useful: t

Part D Cartesian Equation

Find a cartesian equation of the curve, giving your answer in the form $y = f(x)$.

The following symbols may be useful: x , y

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Parametric Integration 1

A Level



The curve C has parametric equations

$$x = 2t^2 - 3 \quad y = t(4 - t^2)$$

The curve crosses the x -axis at the points A and B and the region R is enclosed by the loop of the curve, as shown in **Figure 1**.

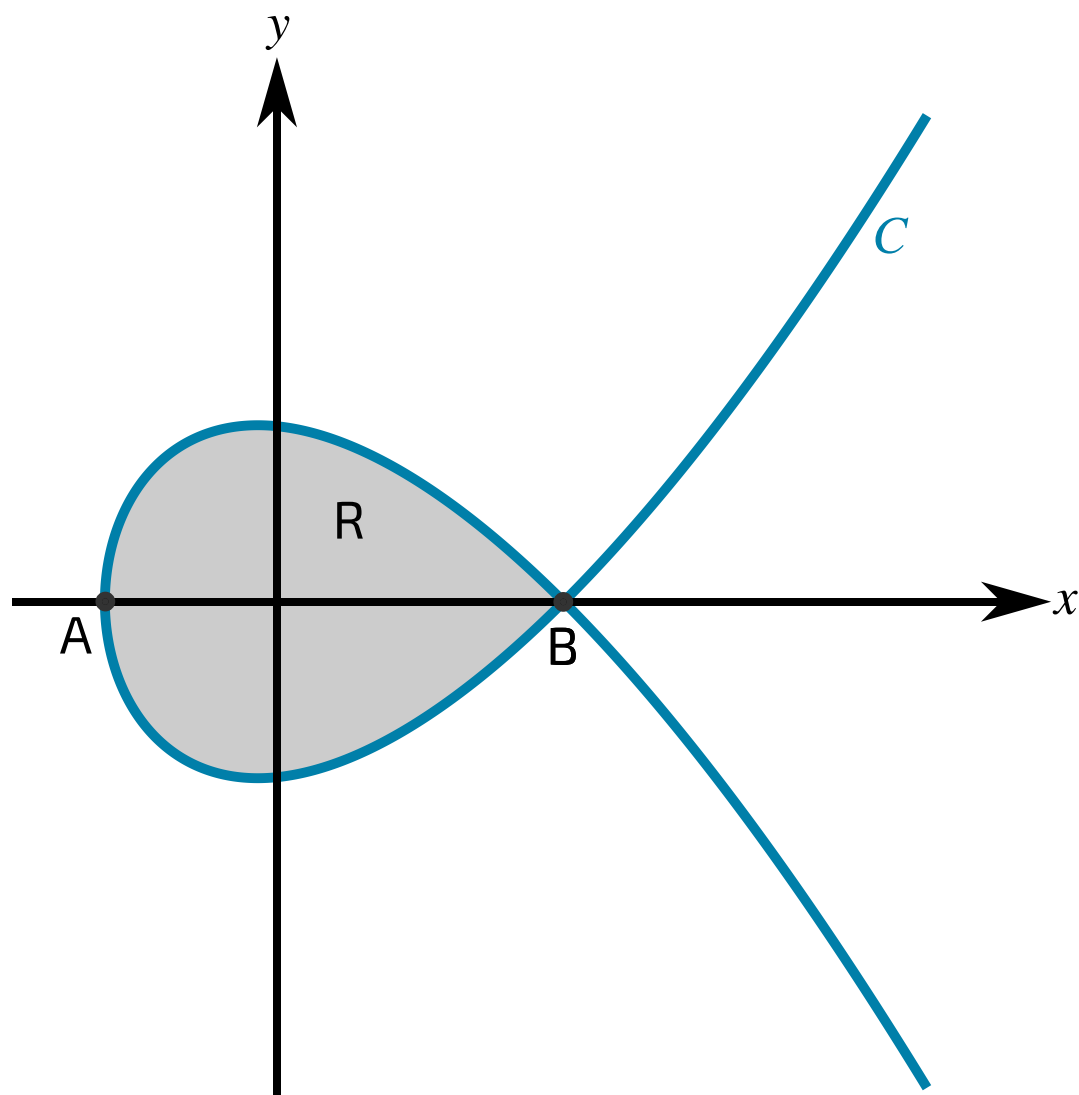


Figure 1: A graph of the curve C .

Part A Point A

Find the x -coordinate of the point A.

Part B Point B

Find the x -coordinate of the point B.

Part C Area of R

The region R is enclosed by the loop of the curve, as shown in **Figure 1**. Find the exact value of the area of R .

Created for isaacphysics.org by Matthew Rihan

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Parametric Equations 4i

A Level



A curve has parametric equations

$$x = 2 \sin t, \quad y = \cos 2t + 2 \sin t$$

for $-\frac{\pi}{2} \leq t \leq \frac{\pi}{2}$.

Part A Derivative

Find $\frac{dy}{dx}$ as a function of t .

The following symbols may be useful: `Derivative(y, x)`, `cos()`, `cosec()`, `cot()`, `sec()`, `sin()`, `t`, `tan()`, `x`, `y`

Part B Coordinates

Find the (x, y) coordinates of the stationary point.

If a value is not a whole number, enter the value as a decimal.

(,)

Part C Equation

Find the Cartesian equation of the curve.

The following symbols may be useful: x , y

Part D Range

Find the range of values that x can take.

Construct your answer from the items below.

Items:

- <

>

x

$< x <$

$\leq x \leq$

$> x$ **or** $x >$

$\geq x$ **or** $x \geq$

\leq

\geq

-2

-1

0

1

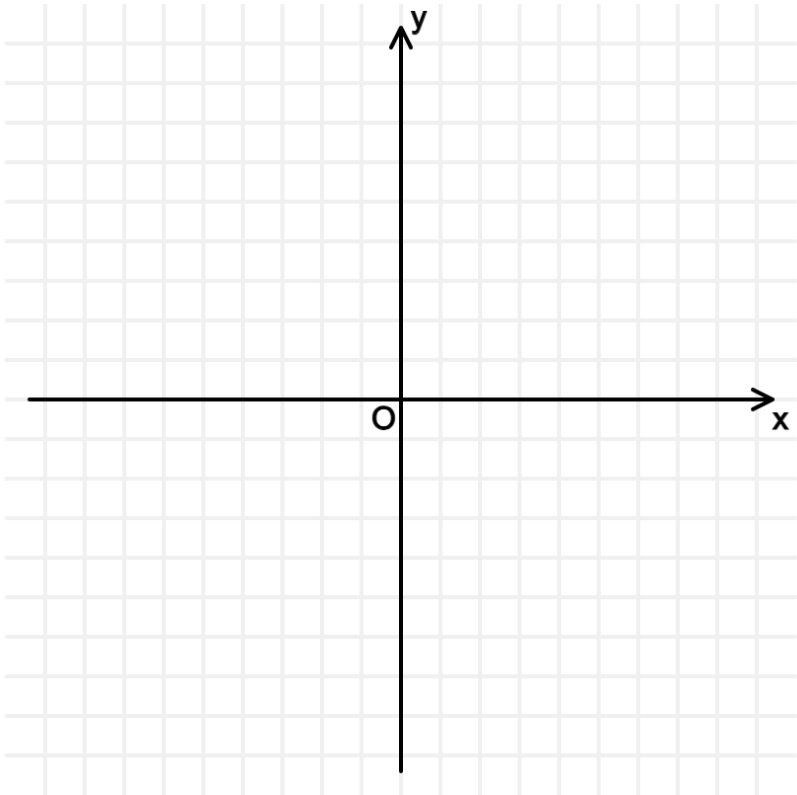
2

3

4

Part E Sketch

Hence sketch the curve.



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