

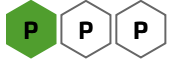


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Expand and Simplify Binomials

Further A



Part A $(x + 1)^4$

Expand and simplify $(x + 1)^4$.

The following symbols may be useful: x

Part B $(z + 2a)^3$

Expand and simplify $(z + 2a)^3$.

The following symbols may be useful: a , z

Part C $(a - b)^5$

Expand and simplify $(a - b)^5$.

The following symbols may be useful: a , b

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Find Coefficients 2

Further A



Without expanding the binomials, find:

Part A Coefficient of x^4y^6

The coefficient of x^4y^6 in the expansion of $(x^2 + 3y^2)^5$.

Part B Coefficient of x^{20}

The coefficient of x^{20} in the expansion of $(x^2 + 3x)^{12}$.

Part C The coefficient of ab^7

The coefficient of ab^7 in the expansion of $(a + \frac{1}{4}b)^8$.

Part D **Constant term**

The constant term in the expansion of $\left(\frac{x^2}{2} - \frac{8}{x}\right)^9$.

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Group and Expand

Further A



Expand $(1 - 2x + 3x^2)^7$ in ascending powers of x as far as x^3 .

The following symbols may be useful: x

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Binomial: All Rational n Zi

A Level



Part A Expansion

Expand $(1 - 4x)^{\frac{1}{4}}$ in ascending powers of x , up to and including the term in x^3 .

The following symbols may be useful: x

Part B Values of a and b

The term of lowest degree in the expansion of

$$(1 + ax)(1 + bx^2)^7 - (1 - 4x)^{\frac{1}{4}}$$

in ascending powers of x is the term x^3 . Find the values of the constants a and b .

What is the value of a ?

The following symbols may be useful: a

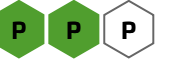
What is the value of b ?

The following symbols may be useful: b



Binomial: All Rational n 1i

A Level



Part A Partial Fractions

Given that $\frac{3x+4}{(1+x)(2+x)^2} \equiv \frac{A}{1+x} + \frac{B}{2+x} + \frac{C}{(2+x)^2}$, find A , B , and C .

Find A .

The following symbols may be useful: A

Find B .

The following symbols may be useful: B

Find C .

The following symbols may be useful: c

Part B Expand

Hence or otherwise expand $\frac{3x+4}{(1+x)(2+x)^2}$ in ascending powers of x , up to and including the term in x^2 .

The following symbols may be useful: x

Part C **Values of x**

State the set of values of x for which the expansion in the above part is valid.

What form does your answer take? Choose from the list below, where a and b are constants and $a < b$, and then find a and/or b .

- ☐ $x < a$
 - ☐ $x \leq a$
 - ☐ $x > a$
 - ☐ $x \geq a$
 - ☐ $a < x < b$
 - ☐ $a \leq x \leq b$
 - ☐ $x < a$ or $x > b$
 - ☐ $x \leq a$ or $x \geq b$
-

Write down the value of a .

Write down the value of b (or if your chosen form has no b , write "n").

The following symbols may be useful: n

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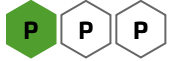
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Maclaurin Series - Binomial

Further A



Part A Expand $(1 + r)^{\frac{1}{3}}$ and find $1.1^{\frac{1}{3}}$ and $9^{\frac{1}{3}}$

Expand $(1 + r)^{\frac{1}{3}}$ up to the term in r^3 .

The following symbols may be useful: r

Hence, using your expansion, find $(1.1)^{\frac{1}{3}}$ to 3 decimal places.

Now, using your expansion again, find $9^{\frac{1}{3}}$ to 2 decimal places.

Part B Electric field on the axis of a charged sheet

The electric field E on the axis of a uniformly charged circular sheet at a distance z from the centre of the sheet is given by

$$E = \frac{\sigma}{2\epsilon_0} \left[1 - \frac{z}{\sqrt{z^2 + a^2}} \right]$$

where σ is the charge per unit area on the sheet and a is the radius of the sheet. Show that in the limit when $z \gg a$ the field on the axis is such that $E \approx \frac{A}{z^2}$ and find A .

The following symbols may be useful: A , a , ϵ_0 , σ , z



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Maclaurin Series - Cos & Sin 1

Further A



Part A Find the cosine of the angle 0.2 rad

Find, using a Maclaurin expansion, the cosine of the angle 0.2 rad, correct to 3 decimal places.

Part B Find the sine of the angle 0.08 rad

Find, using a Maclaurin expansion, the sine of the angle 0.08 rad, correct to 2 significant figures.

Part C Potential energy of mass on pendulum

A pendulum consists of a point mass m suspended on a light string of length l . When the string makes an angle of ϕ to the vertical its potential energy relative to the point where $\phi = 0$ is given by $mgl(1 - \cos \phi)$. Show that for $\phi \ll 1$ the potential energy is given approximately by $A_0\phi^2$ and find an expression for A_0 .

The following symbols may be useful: g , l , m

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Maclaurin Series - ln

Further A



Part A Expand $\ln(1 + z)$ and hence $\ln(2 + 4y)$

(i) Write down the Maclaurin expansion of $\ln(1 + z)$ up to the term in z^3 .

The following symbols may be useful: z

(ii) By re-writing $\ln(2 + 4y)$ in the form $A + \ln(1 + z)$, where A is a constant, find the Maclaurin expansion of $\ln(2 + 4y)$ up to the term in y^3 .

The following symbols may be useful: y , z

Part B Expand $\ln\left(\frac{1+q}{1-q}\right)$

Find the first 4 non-zero terms in the Maclaurin expansion of $\ln\left(\frac{1+q}{1-q}\right)$.

The following symbols may be useful: q

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Maclaurin Series - Exponentials 2

Further A



Part A Expand $Ae^{-\alpha t}$

Expand $Ae^{-\alpha t}$ up to the term in t^2 .

The following symbols may be useful: A, alpha, p, t

Part B Expand $e^p - e^{-p}$

Find the first two non-zero terms in the Maclaurin expansion of $e^p - e^{-p}$.

The following symbols may be useful: A, alpha, p, t

Part C Energy decay in oscillations

A lightly damped oscillatory system has a period T . The total energy of the system at time t is given by $E(t)$. One period later its energy $E(t + T) = E(t)e^{-\gamma T}$.

(i) Find an expression for the fractional change in energy in one cycle.

The following symbols may be useful: T , e , γ

(ii) On the assumption that $\gamma T \ll 1$ find an approximate expression for the fractional change in energy in one cycle.

The following symbols may be useful: T , e , γ
