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[Home](#) [Gameboard](#) [Maths](#) [Calculus](#) [Differentiation](#) [Differentiating Sums and Differences 3](#)

# Differentiating Sums and Differences 3

A Level Further A  
     

## Part A Velocity if $s = ut + bt^2$

A particle is moving in one dimension. Its displacement  $s$  at time  $t$  is given by  $s = ut + bt^2$ , where  $u$  and  $b$  are constants. The velocity  $v$  of the particle at time  $t$  is given by the rate of change of displacement with time, i.e.  $v = \frac{ds}{dt}$ .

Find an expression for the velocity.

The following symbols may be useful:  $b$ ,  $t$ ,  $u$ ,  $v$

## Part B Acceleration if $s = ut + bt^2$

A particle is moving in one dimension. Its displacement  $s$  at time  $t$  is given by  $s = ut + bt^2$ , where  $u$  and  $b$  are constants. The acceleration  $a$  of the particle at time  $t$  is given by the rate of change of velocity with time.

Find an expression for the acceleration.

The following symbols may be useful:  $a$ ,  $b$ ,  $t$ ,  $u$

**Part C**    **Velocity if  $x = \alpha t + \beta t^3$** 

The displacement of a body at time  $t$  is given by  $x = \alpha t + \beta t^3$  where  $\alpha = 4 \text{ m s}^{-1}$  and  $\beta = 5 \text{ m s}^{-3}$ . Use the fact that the velocity is the rate of change of displacement to find the velocity of the body at  $t = 2 \text{ s}$ .

Find the velocity of the body at  $t = 2 \text{ s}$ .

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**Part D**    **Acceleration if  $x = \alpha t + \beta t^3$** 

The displacement of a body at time  $t$  is given by  $x = \alpha t + \beta t^3$  where  $\alpha = 4 \text{ m s}^{-1}$  and  $\beta = 5 \text{ m s}^{-3}$ . Use the fact that the acceleration is the rate of change of velocity to find the acceleration of the body at  $t = 2 \text{ s}$ .

Find the acceleration of the body at  $t = 2 \text{ s}$ .

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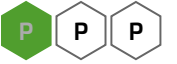


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[Home](#) [Gameboard](#) [Maths](#) [Acceleration f\(t\) 2ii](#)

## Acceleration f(t) 2ii

A Level



A particle  $P$  travels in a straight line. The velocity of  $P$  at time  $t$  seconds after it passes through a fixed point  $A$  is given by  $(0.6t^2 + 3) \text{ m s}^{-1}$ .

### Part A Velocity at $A$

Find the velocity of  $P$  when it passes through  $A$ . Give your answer to 1 significant figure.

---

### Part B Displacement at $t = 1.5$

Find the displacement of  $P$  from  $A$  when  $t = 1.5$ . Give your answer to 3 significant figures.

---

### Part C Velocity at $a = 6$

Find the velocity of  $P$  when it has an acceleration of  $6 \text{ m s}^{-2}$ . Give your answer to 2 significant figures.

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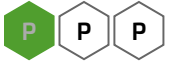


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[Home](#) [Gameboard](#) [Maths](#) [Acceleration f\(t\) 1i](#)

# Acceleration f(t) 1i

A Level



A particle  $P$  moves in a straight line. At time  $t$  s after passing through a point  $O$  of the line the displacement of  $P$  from  $O$  is  $x$  m where  $x = 0.06t^3 - 0.45t^2 - 0.24t$ .

## Part A Velocity of $P$

Find the velocity of  $P$  when  $t = 0$ .

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## Part B Acceleration of $P$

Find the acceleration of  $P$  when  $t = 0$ .

---

## Part C Minimum velocity of $P$

Find the speed of  $P$  when it is at its minimum velocity. Give your answer to 3 significant figures.

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## Part D Positive value of $t$

Find the positive value of  $t$  when the direction of motion of  $P$  changes. Give your answer to 3 significant figures.

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[Home](#) [Gameboard](#) [Maths](#) [Acceleration f\(t\) 3i](#)

# Acceleration f(t) 3i

A Level



A particle starts from rest at the point  $A$  and travels in a straight line. The displacement  $s$  m of the particle from  $A$  at time  $t$  s after leaving  $A$  is given by

$$s = 0.001t^4 - 0.04t^3 + 0.6t^2, \quad \text{for } 0 \leq t \leq 10$$

## Part A Velocity $t = 10$

Find the velocity of the particle when  $t = 10$ .

---

## Part B Velocity $t = 20$

The acceleration of the particle for  $t \geq 10$  is  $(0.8 - 0.08t) \text{ m s}^{-2}$ .

Calculate the velocity of the particle when  $t = 20$ .

---

## Part C Displacement $t = 20$

Find the displacement from  $A$  of the particle when  $t = 20$ . Give your answer to 3 significant figures.

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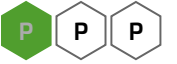


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[Home](#) [Gameboard](#) [Maths](#) [Acceleration f\(t\) 4i](#)

# Acceleration f(t) 4i

A Level



A car is travelling along a straight horizontal road with velocity  $32.5 \text{ m s}^{-1}$ . The driver applies the brakes and the car decelerates at  $(8 - 0.6t) \text{ m s}^{-2}$ , where  $t \text{ s}$  is the time which has elapsed since the brakes were first applied.

## Part A Velocity

Find an expression for the velocity of the car when it is decelerating.

The following symbols may be useful:  $t$

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## Part B Time taken

Find the time taken to bring the car to rest.

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## Part C Distance travelled

Find the total distance travelled by the car whilst it is decelerating.

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[Home](#) [Gameboard](#) [Maths](#) [Calculus and Vectors 1ii](#)

# Calculus and Vectors 1ii

A Level



A particle  $P$  of mass  $0.2 \text{ kg}$  moves on a smooth horizontal plane. Initially it is projected with velocity  $0.8 \text{ m s}^{-1}$  from a fixed point  $O$  towards another fixed point  $A$ . At time  $t \text{ s}$  after projection,  $P$  is  $x \text{ m}$  from  $O$  and is moving with velocity  $v \text{ m s}^{-1}$ , with the direction  $OA$  being positive. A force of  $(1.5t - 1) \text{ N}$  acts on  $P$  in the direction parallel to  $OA$ .

## Part A Expression for $v$

Find an expression for  $v$  in terms of  $t$ .

The following symbols may be useful:  $t$ ,  $v$

## Part B Time when $v = 0.8 \text{ m s}^{-1}$

Find the time (in seconds) when the velocity of  $P$  is next  $0.8 \text{ m s}^{-1}$ .

## Part C Times through $O$

Find the first time when  $P$  subsequently passes through  $O$ .

Find the second time when  $P$  subsequently passes through  $O$ .



## Part D Distance in third second

Find the distance  $P$  travels in the third second of its motion.

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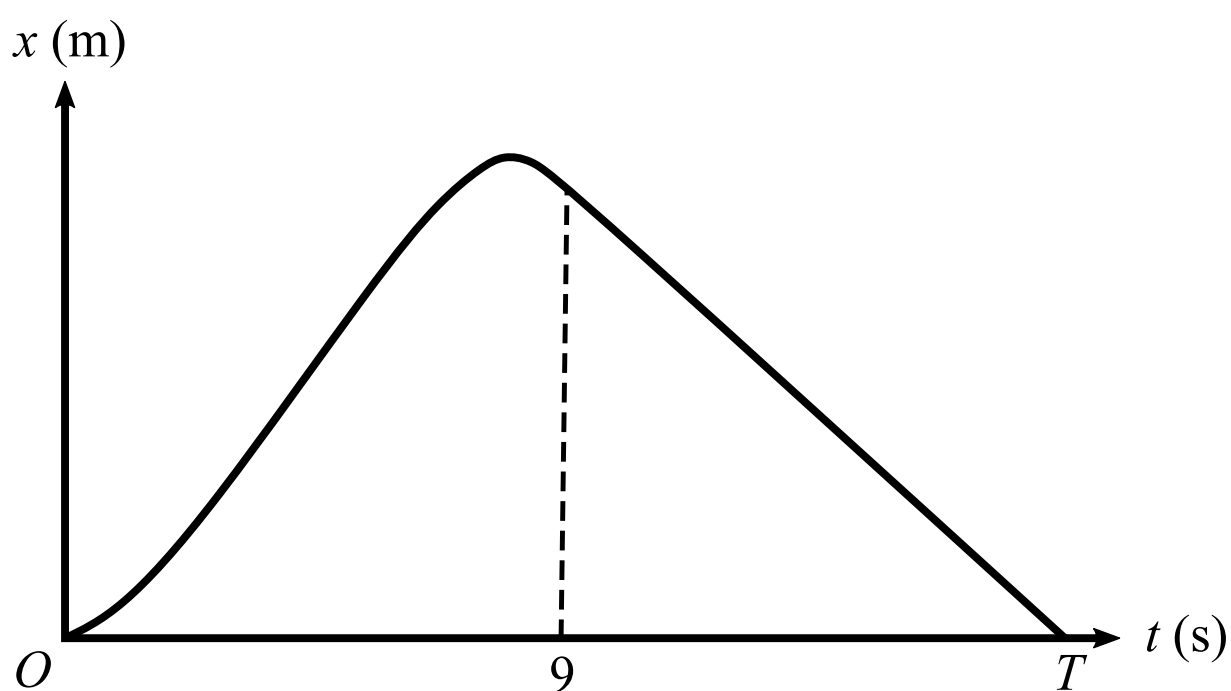


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[Home](#) [Gameboard](#) [Maths](#) [General Kinematics 1ii](#)

# General Kinematics 1ii

A Level



**Figure 1:** Distance-time graph showing the motion of the particle between  $A$  and  $B$ .

A particle travels along a straight line from a point  $A$  to a point  $B$  and then returns to  $A$  along the same straight line. During the first 9 s of the motion the displacement  $x$  m of the particle from  $A$  at time  $t$  s is given by  $x = t^2 - \frac{1}{12}t^3$ . The particle then travels at a constant speed of  $2\frac{1}{4} \text{ m s}^{-1}$  until it reaches  $A$  at time  $t = T$ .

## Part A Velocity expression

Find an expression for the velocity of the particle during the first 9 s of its motion.

The following symbols may be useful:  $t$

## Part B Time and distance

Find the time it takes the particle to reach  $B$ .

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Find the distance  $AB$  in metres.

---

## Part C Time taken

Find the value of  $T$ .

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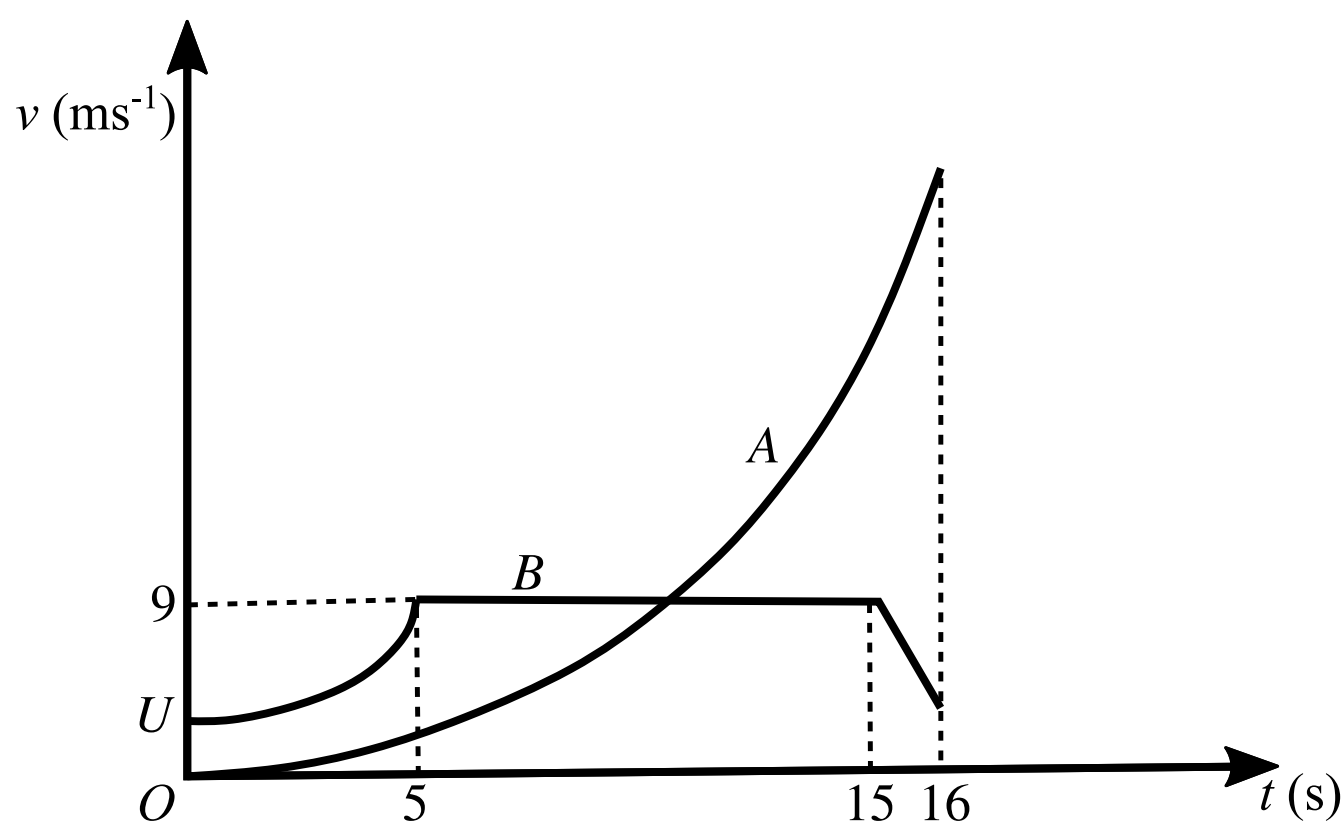


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[Home](#) [Gameboard](#) [Maths](#) [Kinematics & Calculus](#)

# Kinematics & Calculus

A Level



**Figure 1:** Velocity-time graph of the motion of two particles  $A$  and  $B$  along the same straight line.

The diagram shows the  $(t, v)$  graphs for two particles  $A$  and  $B$  which move on the same straight line. The units of  $v$  and  $t$  are  $\text{m s}^{-1}$  and  $\text{s}$  respectively. Both particles are at the point  $S$  on the line when  $t = 0$ . The particle  $A$  is initially at rest, and moves with acceleration  $0.18t \text{ m s}^{-2}$  until the two particles collide when  $t = 16 \text{ s}$ . The initial velocity of  $B$  is  $U \text{ m s}^{-1}$  and  $B$  has variable acceleration for the first five seconds of its motion. For the next ten seconds of its motion  $B$  has a constant velocity of  $9 \text{ m s}^{-1}$ ; finally  $B$  moves with constant deceleration for one second before it collides with  $A$ .

## Part A $t$ for same velocity

Calculate the value of  $t$  at which the two particles have the same velocity.

**Part B** Calculate  $U$ 

For  $0 \leq t \leq 5$  the distance of  $B$  from  $S$  is  $(Ut + 0.08t^3)$  m.

Calculate  $U$ .

---

**Part C** Distance from  $S$ 

Calculate how far  $B$  is from  $S$  when  $t = 5$  s.

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**Part D**  $v_B$  when  $t = 16$  s

Calculate the velocity of  $B$  when  $t = 16$  s.

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