

<u>Gameboard</u>

Maths

Calculus

Integration

Integration by Substitution 1

Integration by Substitution 1





Part A Integrate $\sin(c\theta)$

Find $\int \sin(c\theta) d\theta$, where c is a constant.

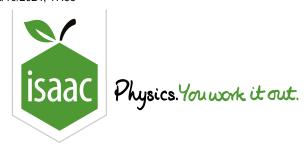
The following symbols may be useful: C, c, k, theta

Part B Integrate $\mathrm{e}^{\alpha v}$

Find $\int e^{\alpha v} dv$, where α is a constant.

The following symbols may be useful: alpha, e, k, v

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<u>Gameboard</u>

Maths

Calculus Integration

Integration by Substitution 2

Integration by Substitution 2

Pre-Uni Maths for Sciences K3.2



Part A Integrate $(bv+c)^2$

Find $\int (bv+c)^2 dv$, where b and c are constants.

The following symbols may be useful: b, c, k, v

Part B Integrate $a(y-b)^3$

Find $\int_0^b a(y-b)^3 dy$, where a and b are constants.

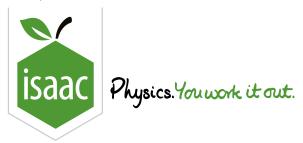
The following symbols may be useful: a, b

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Gameboard:

STEM SMART Single Maths 35 - Integration by

Substitution



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Maths

Integration: General 4ii

Integration: General 4ii



Part A Integrate $(4-3x)^7$

Find
$$\int (4-3x)^7 dx$$
.

The following symbols may be useful: c, x

Part B Integrate
$$(4-3x)^{-1}$$

Find
$$\int (4-3x)^{-1} dx$$
.

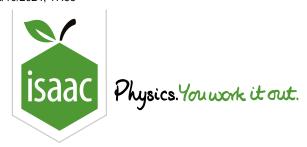
The following symbols may be useful: c, x

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Gameboard:

STEM SMART Single Maths 35 - Integration by

<u>Substitution</u>



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Maths

Integration by Substitution 5ii

Integration by Substitution 5ii



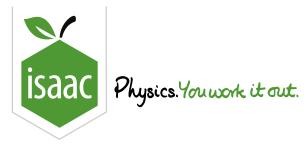
Use the substitution u=2x-5 to find the exact value of $\int_{\frac{5}{2}}^3 (4x-8)(2x-5)^7 \mathrm{d}x$.

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Gameboard:

STEM SMART Single Maths 35 - Integration by

Substitution



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Maths

Integration by Substitution 5i

Integration by Substitution 5i



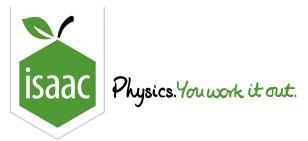
Use the substitution u=2x+1 to evaluate $\int_0^{rac{1}{2}} rac{4x-1}{(2x+1)^5} \mathrm{d}x.$

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Gameboard:

STEM SMART Single Maths 35 - Integration by

Substitution



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Maths

Integration by Substitution 4ii

Integration by Substitution 4ii

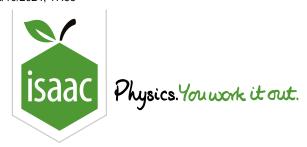


Use the substitution
$$u=\sqrt{x+2}$$
 to find the exact value of $\int_{-1}^7 \frac{x^2}{\sqrt{x+2}} \mathrm{d}x$.

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Maths

Integration by Substitution 4i

Integration by Substitution 4i

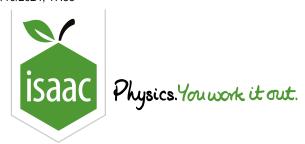


Use the substitution $u=1+\sqrt{x}$ to find the exact value of $\int_4^9 \frac{1}{1+\sqrt{x}} \mathrm{d}x$ in the form $a+b\ln(c)$, where a,b, and c are positive constants to be found.

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<u>Gameboard</u>

Maths

Calculus Integration

Integration by Substitution 3

Integration by Substitution 3

Pre-Uni Maths for Sciences K3.3



Part A Integrate $\frac{3}{(z+1)^2}$

Find
$$\int_0^2 \frac{3}{(z+1)^2} \, \mathrm{d}z.$$

Part B Integrate $\frac{e^{-\alpha x}}{(1+e^{-\alpha x})^4}$

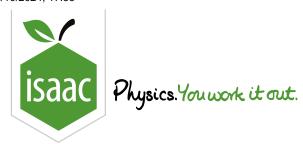
Find $\int \frac{\mathrm{e}^{-\alpha x}}{(1+\mathrm{e}^{-\alpha x})^4}\,\mathrm{d}x$, where lpha is a constant.

The following symbols may be useful: C, alpha, c, e, k, x

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Gameboard:

<u>STEM SMART Single Maths 35 - Integration by</u> Substitution



<u>Gameboard</u>

Maths

Integration by Substitution 2i

Integration by Substitution 2i



In this question, I denotes the definite integral $\int_2^5 \frac{5-x}{2+\sqrt{x-1}} \mathrm{d}x$. The value of I can be found using two different methods.

Part A Substitution

Show that the substitution $u=\sqrt{x-1}$ transforms I to $\int_1^2 \left(4u-2u^2\right)\!\mathrm{d}u$ and hence find the exact value of I

The following symbols may be useful: I

Part B Rationalisation

Simplify as far as possible $\Big(2+\sqrt{x-1}\Big)\Big(2-\sqrt{x-1}\Big)$.

The following symbols may be useful: x

By first multiplying the numerator and denominator of $\frac{5-x}{2+\sqrt{x-1}}$ by $2-\sqrt{x-1}$, find the exact value of I.

The following symbols may be useful: I

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