

<u>Gameboard</u>

Maths Algebra

Manipulation

Writing and Using Algebra 14

### Writing and Using Algebra 14





A postman delivers mail to four houses. House 1 receives 3s letters and t parcels. House 2 receives 7s letters. House 3 receives 5s letters and 2t parcels. House 4 receives t parcels.

#### Part A Write the information as an equation

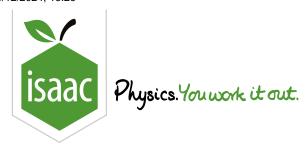
Write an equation for the total number of items the four houses receive, N. Simplify your answer as far as possible.

The following symbols may be useful: N, s, t

#### Part B Write an equation for C

Assuming that the cost to send a letter is  $80 \, \mathrm{pence}$  and the cost to send a parcel is £5.50, write an equation for C, the total cost in pounds to send all the items that were delivered.

The following symbols may be useful: C, s, t



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Maths

Algebra Manipulation

Common Factors 8

### **Common Factors 8**

#### Essential GCSE Maths 15.8



Simplify the following, factorising if possible.

Part A 
$$3x^2 imes 2a imes ax^3$$

$$3x^2 imes 2a imes ax^3$$

The following symbols may be useful: a, x

Part B 
$$7p imes rac{1}{2}x^2 \div rac{p}{4} - 7x$$

$$7p \times \frac{1}{2}x^2 \div \frac{p}{4} - 7x$$

The following symbols may be useful: p, x

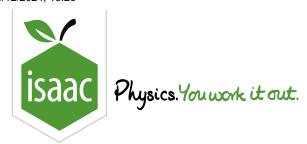
Part C 
$$3c imes \left(rac{1}{2}x
ight)^2 imes 8c^2x + 4c^3$$

$$3c imes \left(rac{1}{2}x
ight)^2 imes 8c^2x + 4c^3$$

The following symbols may be useful: c,  $\,\mathbf{x}$ 

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STEM SMART Double Maths 1 - Algebra, Indices & Straight Lines



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Maths

Algebra

Manipulation

Simplifying Indices

### Simplifying Indices

Pre-Uni Maths for Sciences A2.6



Part A Simplify 
$$(4a^2b^3)^{rac{1}{2}} imes (9ab^2)^{-rac{3}{2}}$$

Simplify 
$$(4a^2b^3)^{rac{1}{2}} imes (9ab^2)^{-rac{3}{2}}$$

The following symbols may be useful: a, b

Part B Simplify 
$$(8p^3q^2)^{\frac{2}{3}}\div\left(rac{2p}{q^{\frac{1}{3}}}
ight)^5$$

Simplify 
$$(8p^3q^2)^{\frac{2}{3}}\div\left(rac{2p}{q^{\frac{1}{3}}}
ight)^5$$

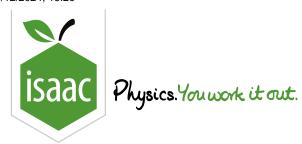
The following symbols may be useful: p, q

Part C Simplify 
$$(10^{-34})^{\frac{1}{2}}(10^{-10})^{\frac{1}{2}}(10^8)^{-\frac{5}{2}}$$

Simplify 
$$(10^{-34})^{\frac{1}{2}}(10^{-10})^{\frac{1}{2}}(10^8)^{-\frac{5}{2}}$$

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# <u>STEM SMART Double Maths 1 - Algebra, Indices & Straight Lines</u>



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Maths

Algebra Manipulation

Simplifying Surds

### Simplifying Surds

Pre-Uni Maths for Sciences A2.3



Simplify the following expressions.

Part A 
$$2\sqrt{20}+\sqrt{45}-5\sqrt{5}$$

Simplify 
$$2\sqrt{20} + \sqrt{45} - 5\sqrt{5}$$

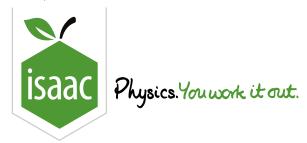
Part B 
$$4(\sqrt{3}+1)(\sqrt{3}-1)-2(2+\sqrt{2})(1+\sqrt{2})$$

Simplify 
$$4(\sqrt{3}+1)(\sqrt{3}-1)-2(2+\sqrt{2})(1+\sqrt{2})$$

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Maths

Algebra Manipulation Rationalisation

### Rationalisation

#### Pre-Uni Maths for Sciences A2.2





Rationalise the denominators of the following expressions.

Part A  $\frac{3\sqrt{6}}{2\sqrt{18}}$ 

$$\frac{3\sqrt{6}}{2\sqrt{18}}$$

Rationalise the denominator of 
$$\frac{3\sqrt{6}}{2\sqrt{18}}.$$

Part B

$$\frac{4-\sqrt{3}}{4+2\sqrt{3}}$$

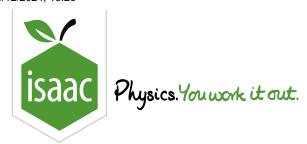
Rationalise the denominator of  $\frac{4-\sqrt{3}}{4+2\sqrt{3}}$ .

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Maths

Algebra Manipulation

Manipulating Algebraic Fractions 1

### **Manipulating Algebraic Fractions 1**



A Level

Pre-Uni Maths for Science A3.1

Rearrange each of the following equations to make the indicated symbol the subject.

Part A Find 
$$b$$
 if  $\frac{1}{4a} - \frac{c}{3b} = 1$ 

Make 
$$b$$
 the subject of the equation  $\frac{1}{4a} - \frac{c}{3b} = 1$ .

The following symbols may be useful: a, b, c

Part B Find 
$$q$$
 if  $p=rac{2}{q^2}+rac{3}{r}$ 

Consider the equation  $p=\frac{2}{q^2}+\frac{3}{r}$ . Show that if you make q the subject of this equation it can be written in the form  $q=\pm S$  and find an expression for S.

The following symbols may be useful: s, p, r

Part C Find x if  $\frac{1}{x^2} - \frac{a}{z^2} = b$ 

Consider the equation  $\frac{1}{x^2} - \frac{a}{z^2} = b$ . Show that if you make x the subject of this equation it can be written in the form  $x = \pm Y$  and find an expression for Y.

The following symbols may be useful: Y,  $\, a$ ,  $\, b$ ,  $\, z$ 

Part D Find 
$$m$$
 if  $\frac{m}{a} + \frac{n}{b} = c$ 

Make m the subject of the equation  $\frac{m}{a} + \frac{n}{b} = c$ .

The following symbols may be useful: a, b, c, m, n

Part E Find 
$$s$$
 if  $\frac{2}{r}-\frac{5}{s}=6$ 

Make s the subject of the equation  $\frac{2}{r} - \frac{5}{s} = 6$ .

The following symbols may be useful: r, s

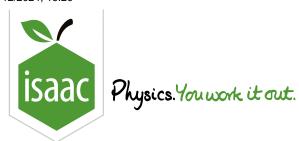
Part F Find 
$$r$$
 if  $\frac{1}{p} = \frac{1}{q} + \frac{1}{r}$ 

Make r the subject of  $\frac{1}{p}=\frac{1}{q}+\frac{1}{r}.$ 

The following symbols may be useful: p, q, r

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## STEM SMART Double Maths 1 - Algebra, Indices & Straight Lines



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Maths

Straight Lines: Coordinates and Lengths 2i

### Straight Lines: Coordinates and Lengths 2i



The points $A,B,$ and $C$ have coordinates $(5,1),(p,7),$ and $(8,2)$ respectively.			
Part A Possible values of $p$			
Given that the distance between the points $A$ and $B$ is twice the distance between points $A$ and $C$ , calculate the possible values of $p$ .			
Enter the possible coordinates of $B$ .			

#### 

Given also that the line passing through A and B has equation y=3x-14, find the coordinates of the midpoint of AB.

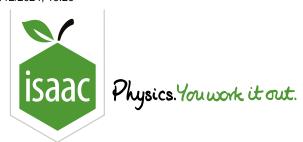
Enter the x and y coordinates below. If a value is not a whole number, enter the value as a decimal.

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STEM SMART Double Maths 1 - Algebra, Indices & Straight Lines



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Maths

Straight Lines: Coordinates and Lengths 1ii

### Straight Lines: Coordinates and Lengths 1ii



#### Part A Find coordinate

The line segment joining the points (-2,7) and (-4,p) has gradient 4. Find the value of p.

The following symbols may be useful: p

#### Part B Find coordinates and midpoint

The line segment joining the points (-2,7) and (6,q) has midpoint (m,5). Find m and q.

Enter the values of m and q. If a value is not a whole number, enter the value as a decimal.

$$m = \bigcap$$

$$q = \bigcap$$

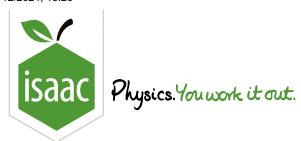
#### Part C Find coordinate from length

The line segment joining the points (-2,7) and (d,3) has length  $2\sqrt{13}$ . Find the two possible values of d. Enter the greatest possible value of d.

The following symbols may be useful: d

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## STEM SMART Double Maths 1 - Algebra, Indices & Straight Lines



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Maths

Straight lines: gradients and normals 2i

## Straight lines: gradients and normals 2i



A is the point (2,7) and B is the point (-1,-2).

#### Part A Equation of line

Find the equation of the line through A parallel to the line y=4x-5, giving your answer in the form y=mx+c.

The following symbols may be useful: x, y

### Part B Length of AB

Calculate the length of AB, giving your answer in simplified surd form.

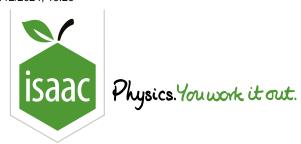
### Part C Find equation of line

Find the equation of the line which passes through the midpoint of AB, and which is perpendicular to AB. Give your answer in the form ax + by + c = 0, where a, b, and c are integers.

The following symbols may be useful: x, y

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## STEM SMART Double Maths 1 - Algebra, Indices & Straight Lines



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Maths

Algebra Manipulation

Lorentz Transform 1

### **Lorentz Transform 1**

#### Pre-Uni Maths for Sciences B4.7



Consider the following equations

$$w_x = rac{c\cos heta - v}{1 - rac{v\cos heta}{c}}$$

$$w_y = rac{c\sin heta}{\gamma\left(1-rac{v\cos heta}{c}
ight)}$$

where 
$$\gamma=rac{1}{\sqrt{1-rac{v^2}{c^2}}}.$$

Find an expression for  $w=\sqrt{w_x^2+w_y^2}$  in terms of one of either v, c or  $\theta$ .

The following symbols may be useful: c, cos(), sin(), tan(), theta, v, w

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