

Gameboard

Maths

Circles 4i

## Circles 4i



A circle with centre C has the equation  $x^2+y^2-10x+4y+4=0$ .

#### Part A Find the coordinates of C

By completing the square for x and y find the coordinates of C. Enter the x and y coordinates below.

Enter the x coordinate:

The following symbols may be useful:  $\times$ 

Enter the  $\boldsymbol{y}$  coordinate:

The following symbols may be useful: y

#### Part B Find radius

Find the radius of the circle.

### Part C Find tangent

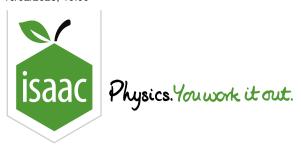
Find the equation of the tangent to the circle at the point P(8,2). Give your answer in the form ax + by + c = 0, where a, b, and c are integers.

The following symbols may be useful: x, y

#### Part D Find area

The circle meets the y axis at Q and the tangent to the circle at P (as in part C) meets the y axis at R. Find the area of triangle PQR.

Used with permission from UCLES, A level, June 2015, Paper 4721, Question 10.



Home Gameboard Maths Radians 2i

## Radians 2i



Figure 1 shows a triangle ABC, and a sector ACD of a circle with centre A. It is given that  $AB=11\,\mathrm{cm}$ ,  $BC=8\,\mathrm{cm}$ , angle  $ABC=0.8\,\mathrm{radians}$  and angle  $DAC=1.7\,\mathrm{radians}$ . The shaded segment is bounded by the line DC and the arc DC.

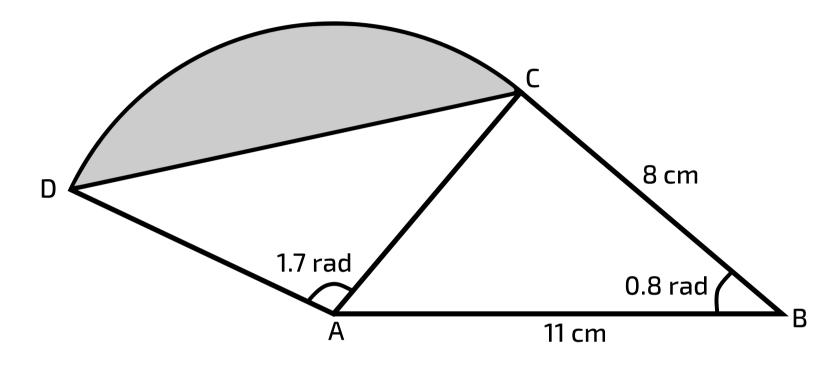


Figure 1: Diagram showing triangle ABC and the sector ACD.

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Calculate the length of AC correct to 3 significant figures.

### Part B Area of segment

Find the area of the shaded segment. Give your answer to 3 significant figures.

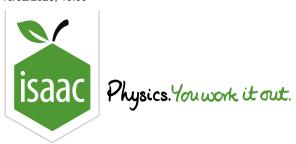
### Part C Perimeter of segment

Find the perimeter of the shaded segment. Give your answer to 3 significant figures.

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Maths

Small Angle Approximations 3ii

## Small Angle Approximations 3ii



### Part A Expression

Use the small angle approximation to write an approximate expression for  $(\cos \theta + 5)(1 + \sin(2\theta))$  in powers of  $\theta$  up to  $\theta^2$ .

The following symbols may be useful: theta

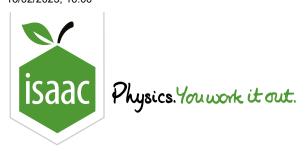
### Part B Approximation

Use your answer from the above part to work out an approximate value for  $(\cos \theta + 5)(1 + \sin(2\theta))$  when  $\theta = 0.075$ . Give your answer to 3 significant figures.

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Functions: Reciprocal Trig 3i

## Functions: Reciprocal Trig 3i



It is given that heta is the acute angle such that  $\sec \theta \sin \theta = 36 \cot \theta$ .

#### Part A Value of $\tan \theta$

Find  $\tan \theta$ .

The following symbols may be useful: cos(), sin(), tan(), theta

### Part B Value of $\tan{(\theta-\frac{\pi}{4})}$

Hence, using an appropriate formula, find the exact value of  $\tan{(\theta-\frac{\pi}{4})}$ .

The following symbols may be useful: pi, theta

### Part C Value of $\tan{(2\theta)}$

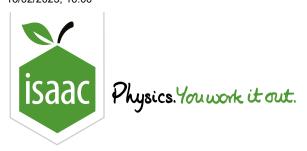
Using an appropriate formula, find the exact value of  $\tan{(2\theta)}$ .

The following symbols may be useful: theta

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Trigonometry: Combined Angles 2i

# Trigonometry: Combined Angles 2i



#### Part A Proof

Use the identity for  $\cos{(A+B)}$  to write  $4\cos{(\theta+60^\circ)}\cos{(\theta+30^\circ)}$  in the form  $p+q\sin{(r\theta)}$ , where  $p,\,q$  ,  $r\in{\mathbb R}$ .

The following symbols may be useful: theta

#### Part B $4\cos 82.5^{\circ}\cos 52.5^{\circ}$

Hence find the exact value of  $4\cos 82.5^{\circ}\cos 52.5^{\circ}$ .

#### Part C Solve

Solve, for  $0^\circ < \theta < 90^\circ$ , the equation  $4\cos\left(\theta + 60^\circ\right)\cos\left(\theta + 30^\circ\right) = 1$ .

Give the smallest solution, in degrees, to three significant figures.

Give the largest solution, in degrees, to three significant figures.

#### 

Given that there are no values of  $\boldsymbol{\theta}$  which satisfy the equation

$$4\cos\left( heta+60^{\circ}
ight)\cos\left( heta+30^{\circ}
ight)=k,$$

determine the set of values of the constant k.

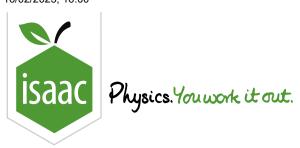
Give one of the bounds, in the form k < a,  $k \le a$ , k > a or  $k \ge a$  where a is an exact value.

The following symbols may be useful:  $\langle , \langle =, \rangle, \rangle = , k$ 

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Trigonometry: Double Angles 2i

## Trigonometry: Double Angles 2i



#### Part A Proof

Simplify  $\sin{(2\theta)} \big( \tan{\theta} + \cot{\theta} \big)$  as far as possible.

The following symbols may be useful: theta

#### Part B Exact Value

Hence find the exact value of  $\tan \frac{\pi}{12} + \tan \frac{\pi}{8} + \cot \frac{\pi}{12} + \cot \frac{\pi}{8}$ .

#### Part C Solve

Using your answer to part A, solve the equation  $\sin{(4\theta)} \left(\tan{\theta} + \cot{\theta}\right) = 1$  for  $0 < \theta < \frac{\pi}{2}$ , to three significant figures, giving your answer in **radians**.

Part D 
$$\left(1-\cos\left(2 heta
ight)
ight)\left( anrac{ heta}{2}+\cotrac{ heta}{2}
ight)^3$$

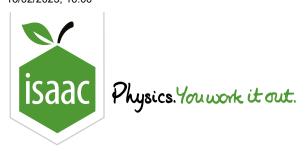
Using you answer to part A, express  $\left(1-\cos\left(2\theta\right)\right)^2\!\left( anrac{ heta}{2}+\cotrac{ heta}{2}
ight)^3$  in terms of  $\sin heta$ .

The following symbols may be useful: theta

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Trigonometry: Combined Angles 4i

# Trigonometry: Combined Angles 4i



### Part A Combined Angles

Express  $4\cos\theta-2\sin\theta$  in the form  $R\cos{(\theta+\alpha)}$ , where R>0 and  $0^{\circ}<\alpha<90^{\circ}$ .

Give the exact value of R.

The following symbols may be useful: R

Give the value of  $\alpha$  to three significant figures.

#### Part B $4\cos\theta - 2\sin\theta = 3$

Hence solve the equation  $4\cos\theta-2\sin\theta=3$  for  $0^\circ<\theta<360^\circ$ , giving your answers in degrees to three significant figures.

Give the smallest solution.

Give the largest solution.

Part C  $25-(4\cos\theta-2\sin\theta)^2$ 

Using your answer to part A, determine the greatest and least values of

$$25-(4\cos\theta-2\sin\theta)^2$$

as  $\theta$  varies, and, in each case, find the smallest positive value of  $\theta$  for which that value occurs, giving your answers in degrees, to three significant figures.

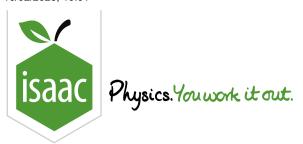
Give the smallest value of  $\theta$  which corresponds to the maximum value.

Give the smallest value of  $\theta$  which corresponds to the minimum value.

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Functions Graph Sketching

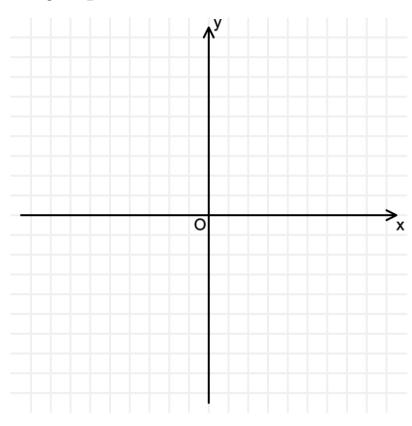
Sketching Inverse Trigonometric Functions

# **Sketching Inverse Trigonometric Functions**



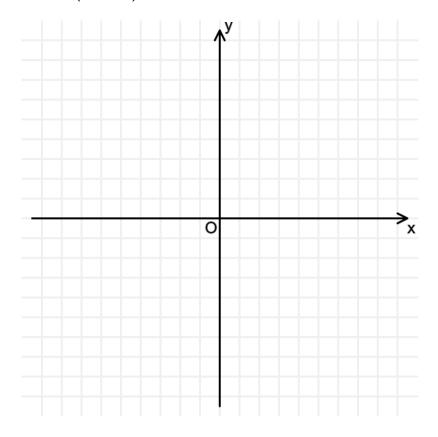
Part A Sketch  $\arcsin \frac{x}{3} + \frac{\pi}{2}$ 

Sketch the graph of  $y = \arcsin rac{x}{3} + rac{\pi}{2}.$ 



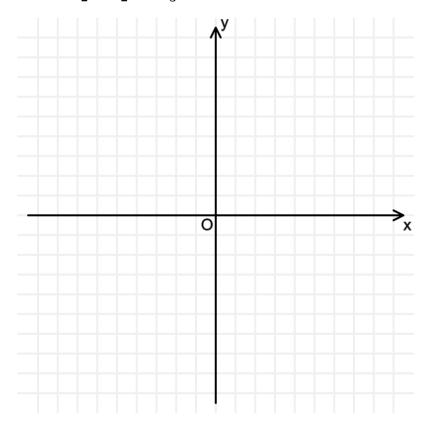
### Part B Sketch $2\arctan{(x-1)}$

Sketch the graph of  $y = 2 \arctan(x - 1)$ .



# Part C Sketch $\arccos\left(-\frac{x}{2} + \frac{1}{2}\right) - \frac{\pi}{3}$

Sketch the graph of  $y=\arccos{\left(-\frac{x}{2}+\frac{1}{2}\right)}-\frac{\pi}{3}.$ 



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