

Bubble sort: compare 1

A bubble sort algorithm can be programmed in multiple ways. Look at the three versions of the bubble sort algorithm (use the tabs to see each version) and put them in order of efficiency with the **most** efficient first and the **least** efficient last in the list.

Version 1 Version 2 Version 3

```
1  PROCEDURE bubble_sort (items)
2
3      // Initialise the variables
4      num_items = LEN(items)
5
6      // Pass through the array of items n-1 times
7      FOR pass_num = 1 TO num_items - 1
8          // Perform a pass
9          FOR index = 0 TO num_items - 2
10             // Compare items to check if they are out of order
11             IF (items[index] > items[index + 1]) THEN
12                 // Swap the items
13                 temp = items[index]
14                 items[index] = items[index + 1]
15                 items[index + 1] = temp
16             ENDIF
17         NEXT index
18     NEXT pass_num
19 ENDPROCEDURE
```

```

1  PROCEDURE bubble_sort (items)
2
3      // Initialise the variables
4      num_items = LEN(items)
5      swapped = True
6
7      // Repeat while one or more swaps have been made
8      WHILE swapped == True
9          swapped = False
10         // Perform a pass
11         FOR index = 0 TO num_items - 2
12             // Compare items to check if they are out of order
13             IF items[index] > items[index + 1] THEN
14                 // Swap the items
15                 temp = items[index]
16                 items[index] = items[index + 1]
17                 items[index + 1] = temp
18                 swapped = True
19             ENDIF
20         NEXT index
21     ENDWHILE
22 ENDPROCEDURE

```

```

1  PROCEDURE bubble_sort (items)
2
3      // Initialise the variables
4      num_items = LEN(items)
5      swapped = True
6      pass_num = 1
7
8      // Repeat while one or more swaps have been made
9      WHILE swapped == True
10         swapped = False
11         // Perform a pass, reducing the number of comparisons each time
12         FOR index = 0 TO num_items - 1 - pass_num
13             // Compare items to check if they are out of order
14             IF items[index] > items[index + 1] THEN
15                 // Swap the items
16                 temp = items[index]
17                 items[index] = items[index + 1]
18                 items[index + 1] = temp
19                 swapped = True
20             ENDIF
21         NEXT index
22         pass_num = pass_num + 1
23     ENDWHILE
24 ENDPROCEDURE

```

☐ 3, 2, 1

☐ 1, 2, 3

☐ 2, 1, 3

Bubble sort: purpose of temp

Bubble sort moves each item in a list up until it reaches a value that is higher than that item. It then looks at the next item and does the same. Once all of the items have been moved, the collection is sorted.

Consider the pseudocode below.

Pseudocode

```
1  PROCEDURE bubblesort_ascending(data_set)
2      num_items = LEN(data_set)
3      swaps = True
4      WHILE i < (num_items - 2) AND swaps == True
5          swaps = False
6          FOR j = 0 TO (num_items - i - 2)
7              IF (data_set[j] > data_set[j + 1]) THEN
8                  temp = data_set[j]
9                  data_set[j] = data_set[j + 1]
10                 data_set[j + 1] = temp
11                 swaps = True
12             ENDIF
13         NEXT j
14         i = i + 1
15     ENDWHILE
16 ENDPROCEDURE
```

Explain the purpose of the **temp** variable in the algorithm.

- ☐ **temp** is used to store a copy of one of the values that is being swapped.
- ☐ **temp** is used to count the number of comparisons between items.
- ☐ **temp** is used to stop the algorithm when the list is sorted.
- ☐ **temp** is used to store the total number of items in the list.

Bubble sort: maximum swaps

Michael is going to sort an array `items` that holds **5 random numbers** generated using a subroutine that produces random integers. As the numbers are generated at runtime, it is not possible to guess how the unsorted array will look.

The array is to be sorted into ascending order using the version of the bubble sort algorithm shown in pseudocode below:

Pseudocode

```
1  PROCEDURE bubble_sort(items)
2      // Initialise variables
3      num_items = LEN(items)
4      temp = 0
5      pass_number = 1
6      swapped = True
7
8      // Continue while swaps have been made and there are more passes to
9      evaluate
10     WHILE swapped == True AND pass_number <= num_items - 1
11         swapped = False
12         FOR index = 0 TO num_items - 2
13             // Check if items are out of order
14             IF (items[index] > items[index + 1]) THEN
15                 // Swap items
16                 temp = items[index]
17                 items[index] = items[index + 1]
18                 items[index + 1] = temp
19                 swapped = True
20             ENDIF
21             pass_number = pass_number + 1
22         NEXT index
23     ENDWHILE
ENDPROCEDURE
```

What is the **maximum** number of swaps that might be carried out?

What is the **maximum** number of passes that might be performed?

Bubble sort: trace 3

Geraint is using the **bubble sort** algorithm to put their list of top five countries to visit into alphabetical order, from A to Z.

Using the **countries** list below, fill in the blanks to show the order of the countries after **each pass of the bubble sort algorithm**, using a new row for each pass. The algorithm will pass over the entire list four times.

countries				
Laos	Egypt	Peru	Fiji	Cuba
<div></div>	<div></div>	<div></div>	<div></div>	<div></div>
<div></div>	<div></div>	<div></div>	<div></div>	<div></div>
<div></div>	<div></div>	<div></div>	<div></div>	<div></div>
<div></div>	<div></div>	<div></div>	<div></div>	<div></div>

Items:

Cuba

Egypt

Fiji

Laos

Peru

Insertion: complete algorithm

The **insertion sort** algorithm works by building up a sorted sublist, one item at a time. To do that, one by one the items in the list are examined and inserted into the correct position in the sorted sublist. The sorted sublist grows until the whole list is sorted.

The following pseudocode subroutine is an implementation of the insertion sort algorithm. There is a block of code missing.

Drag and drop the statements into the correct order to complete the missing part of the code. Make sure that you **indent** the statements as appropriate.

Pseudocode

```
1  PROCEDURE insertion_sort (items)
2      num_items = LEN(items)
3      FOR index = 1 TO num_items - 1
4          item_to_insert = items[index]
5          previous = index - 1
6          >>>> [missing block of code] <<<<
7      NEXT index
8  ENDPROCEDURE
```

Available items

WHILE previous >= 0 AND items[previous] > item_to_insert

previous = previous - 1

items[previous + 1] = item_to_insert

items[previous + 1] = items[previous]

ENDWHILE

Insertion: trace 2



Pam is a teacher. She wants to sort her students test scores so that the highest score appears at the start of the list.

She uses an **insertion sort** to sort the data.

Drag and drop the lines into the correct order to show the state of the list of scores as the data is progressively sorted (i.e. as each item is correctly positioned).

The initial order of the list is: 43, 74, 64, 68, 49, 70

Available items

74, 64, 43, 68, 49, 70

74, 68, 64, 43, 49, 70

74, 70, 68, 64, 49, 43

74, 68, 64, 49, 43, 70

74, 43, 64, 68, 49, 70

Insertion: trace 4

Geraint is using the **insertion sort** algorithm to put their list of top five countries to visit into alphabetical order, from A to Z.

countries				
Peru	Laos	Fiji	Egypt	Cuba

The insertion sort algorithm has been started on the list below. In the first row, the first item is highlighted to show it is in the sorted sublist and the unsorted sublist contains the remaining items.

In the second row, the first pass has completed and the sorted sublist now contains two items, which are highlighted.

Fill in the blanks to show the order of the countries at the end of each pass when performing an **insertion sort**. Use a new row for each pass.

countries				
Peru	Laos	Fiji	Egypt	Cuba
Laos	Peru	Fiji	Egypt	Cuba
<div></div>	<div></div>	<div></div>	<div></div>	<div></div>
<div></div>	<div></div>	<div></div>	<div></div>	<div></div>
<div></div>	<div></div>	<div></div>	<div></div>	<div></div>

Items:

CubaEgyptFijiLaosPeru

Merge sort: trace 6

You have been given some playing cards that have not been sorted:

Original order

9

6

7

7

2

2

10

10

6

9

4

7

5

5

8

8

Drag and drop the cards provided to show the order they would be in at the **end** of each **step** of a **merge sort**.

For this part of the question, you just need to show the **splitting** part of the algorithm.

Splitting

Step 1

group 1

group 2

Step 2

group 1

group 2

group 3

group 4

Step 3

group 1

group 2

group 3

group 4

group 5

group 6

group 7

group 8

Items:

9

6

7

7

2

2

10

10

6

9

4

7

5

5

8

8

You have been given some playing cards that have not been sorted:

Original order

9

6

7

7

2

2

10

10

6

9

4

7

5

5

8

8

Drag and drop the cards provided to show the order they would be in at the **end** of each **step** of a **merge sort**.

For this part of the question, you just need to show the **merging** part of the algorithm. You will need to use your answer from part 1 of the question to help you.

Merging

Step 4

group 1

group 2

group 3

group 4

Step 5

group 1

group 2

Step 6

Sorted cards

Items:

9

6

7

7

2

2

10

10

6

9

4

7

5

5

8

8

Merge sort: trace 4

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You have been given some playing cards that have not been sorted:

4
♠ ♠
♠ ♠
7

8
♠ ♠
♠ ♠
♠ ♠
8

5
♠ ♠
♠ ♠
♠
5

2
♠
♠
2

10
♠ ♠
♠ ♠
♠ ♠
♠ ♠
10

Apply a **merge** sort to sort the cards from the lowest to highest value.

The first three steps of splitting the data have been completed for you:

	Group 1	Group 2
Step 1	<div><div>4 ♠ ♠ ♠ ♠ 7</div><div>8 ♠ ♠ ♠ ♠ ♠ ♠ 8</div><div>5 ♠ ♠ ♠ ♠ ♠ 5</div></div>	<div><div>2 ♠ ♠ 2</div><div>10 ♠ ♠ ♠ ♠ ♠ ♠ ♠ ♠ 10</div></div>

	Group 1	Group 2	Group 3
Step 2	<div><div>4 ♠ ♠ ♠ ♠ 7</div><div>8 ♠ ♠ ♠ ♠ ♠ ♠ 8</div></div>	<div><div>5 ♠ ♠ ♠ ♠ ♠ 5</div><div>2 ♠ ♠ 2</div></div>	<div><div>10 ♠ ♠ ♠ ♠ ♠ ♠ ♠ ♠ 10</div></div>

	Group 1	Group 2	Group 3	Group 4	Group 5
Step 3	<div><div>4 ♠ ♠ ♠ ♠ 7</div></div>	<div><div>8 ♠ ♠ ♠ ♠ ♠ ♠ 8</div></div>	<div><div>5 ♠ ♠ ♠ ♠ ♠ 5</div></div>	<div><div>2 ♠ ♠ 2</div></div>	<div><div>10 ♠ ♠ ♠ ♠ ♠ ♠ ♠ ♠ 10</div></div>

Drag and drop the cards provided at the bottom of the question into the correct positions to show the **merge** steps of the algorithm:

	Group 1	Group 2	Group 3
Step 4	<div><div></div><div></div></div>	<div><div></div><div></div></div>	<div><div></div></div>

	Group 1	Group 2
Step 5	<div> <div></div> <div></div> <div></div> <div></div> </div>	<div> <div></div> </div>

	Sorted group
Step 6	<div> <div></div> <div></div> <div></div> <div></div> <div></div> </div>

Items:

4

♠

♠

♠

7

8

♠

♠

♠

♠

8

5

♠

♠

♠

5

2

♠

♠

2

10

♠

♠

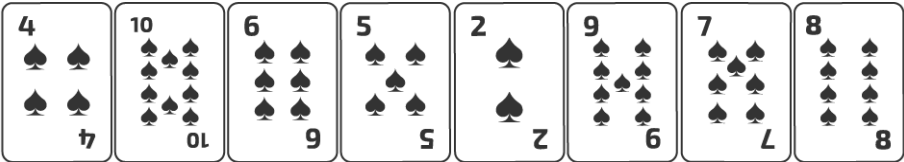
♠

♠

10

Merge sort: trace 5

You have been given some playing cards that have not been sorted:



Drag the lines of cards below into the correct order to show how **each** stage of a merge sort would be performed to sort the the data from lowest to highest.

Available items

4

10

6

5

2

9

7

8

4

5

6

10

2

7

8

9

4

10

6

5

2

9

7

8

2

4

5

6

7

8

9

10

4

10

6

5

2

9

7

8

4

10

6

5

2

9

7

8

4

10

5

6

2

9

7

8