

Gameboard

Maths

Vectors: Diagrams and Proof 1i

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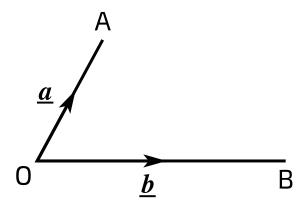


Figure 1: Three points O, A and B, and vectors joining them.

Figure 1 shows points O, A and B, with $\overrightarrow{OA} = \underline{a}$ and $\overrightarrow{OB} = \underline{b}$.

Part A Sketch

Make a sketch of the diagram and mark the points C and D such that $\overrightarrow{OC} = \underline{a} + 2\underline{b}$ and $\overrightarrow{OD} = 2\underline{a} + \underline{b}$. Choose the correct sketch from the 3 options below.

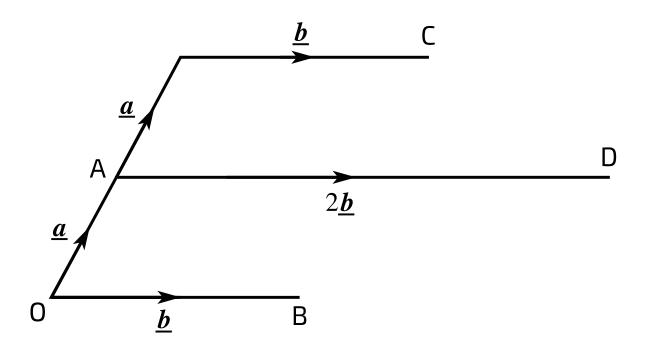


Figure 2: Option A

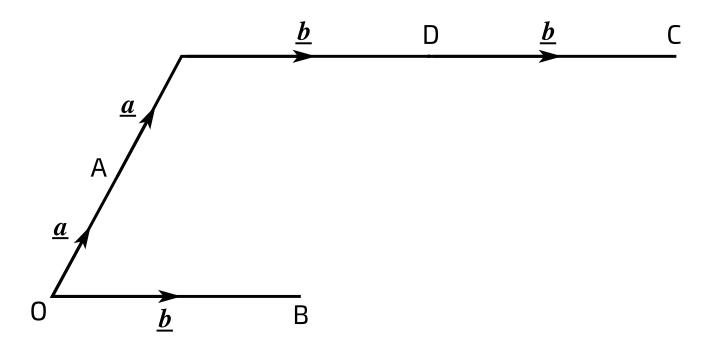


Figure 3: Option B

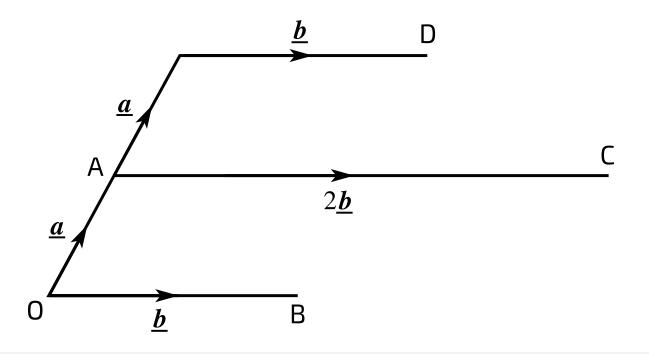


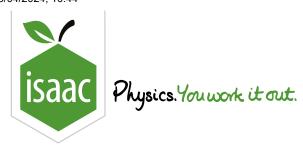
Figure 4: Option C

Vectors: Diagrams and Proof 1i — Isaac Physics Option A Option B Option C Vector \overrightarrow{DC} Part B Express \overrightarrow{DC} in terms of $\underline{\boldsymbol{a}}$ and $\underline{\boldsymbol{b}}$, simplifying your answer. The following symbols may be useful: a, b Part C Proof Prove that ABCD is a parallelogram.

Sides \overrightarrow{AD} and are both equal to Therefore they are parallel and of equal length. Sides \overrightarrow{AB} and are both equal to Therefore they are parallel and of equal length.

The quadrilateral ABCD has two pairs of parallel sides of equal length. Therefore ABCD is a parallelogram.

Items:



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Maths

3D Vectors 2i

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ABCD is a quadrilateral. You are given four pieces of information:

- Relative to a fixed origin O, the position vector of A is $2\underline{\boldsymbol{i}} + 5\underline{\boldsymbol{j}} + 8\underline{\boldsymbol{k}}$.
- Relative to a fixed origin O, the position vector of B is $5\underline{\boldsymbol{i}}+9\underline{\boldsymbol{j}}+8\underline{\boldsymbol{k}}.$
- ullet The vector $ec{BC}=egin{pmatrix} 0 \ 0 \ 5 \end{pmatrix}$.
- ullet The vector $ec{BD}=egin{pmatrix} -3 \ -4 \ 5 \end{pmatrix}$.

Find the vector \overrightarrow{AB} . Give your answer in the form (x,y,z) with the commas and without the spaces.

Find the vector \vec{CD} . Give your answer in the form (x,y,z) with the commas and without the spaces.

${\bf Part \ C} \qquad {\bf Finding} \ AD$

Find the vector \overrightarrow{AD} . Give your answer in the form (x,y,z) with the commas and without the spaces.

Part D Type of quadrilateral

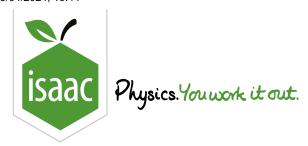
The shape $ABCD$ lies in a plane. What type of quadrilateral is $ABCD$?	
	A parallelogram
	A rectangle
	An irregular quadrilateral
	A square
	A kite
	A trapezium
	A rhombus

Created for isaacphysics.org by Jonathan Waugh

Gameboard:

STEM SMART Double Maths 15 - Trigonometry, Vectors &

Kinematics Revision



Home

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Maths

Constant Acceleration 2i

Constant Acceleration 2i



A stone is released from rest on a bridge and falls vertically into a lake. The stone has velocity $14\,\mathrm{m\,s^{-1}}$ when it enters the lake.

Part A Distance fallen

Calculate the distance the stone falls before it enters the lake.

Part B Time on entering the lake

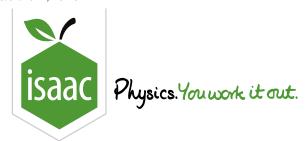
Calculate the time after its release when it enters the lake. Give your answer to 3 significant figures.

Part C Acceleration

The lake is $15\,\mathrm{m}$ deep and the stone has velocity $20\,\mathrm{m\,s^{-1}}$ immediately before it reaches the bed of the lake.

Given that there is no sudden change in the velocity of the stone when it enters the lake, find the acceleration of the stone while it is falling through the lake. Give your answer to 2 significant figures.

Used with permission from UCLES, A Level, June 2016, OCR M1, Question 1



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Maths

Kinematics Graphs

Kinematics Graphs



A man drives a car on a horizontal straight road. At t=0 where the time t is in seconds, the car runs out of petrol. At this instant the car is running at $12\,\mathrm{m\,s^{-1}}$. The car decelerates uniformly, coming to rest when t=8. The man then walks back along the road at $0.7\,\mathrm{m\,s^{-1}}$ until he reaches a petrol station a distance of $420\,\mathrm{m}$ from his car. After his arrival at the petrol station it takes him $250\,\mathrm{s}$ to obtain a can of petrol. He is then given a lift back to his car on a motorcycle. The motorcycle starts from rest and accelerates uniformly until its speed is $20\,\mathrm{m\,s^{-1}}$; it then decelerates uniformly, coming to rest at the stationary car at time t=T.

Part A (t,v) graph

Sketch the shape of the (t, v) graph for the man for $0 \le t \le T$. [Your sketch need not be drawn to scale yet numerical values should be shown].

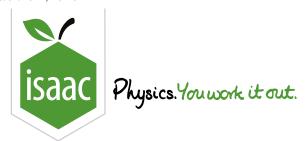
To see an example sketch, answer the following question: What is the largest positive value of v on the graph?

Part B Finding deceleration

Find the deceleration of the car for 0 < t < 8.

${\bf Part \ C} \qquad {\bf Finding} \ T$

Find the value of T.



<u>Gameboard</u>

Maths

Projectiles: General 3ii

Projectiles: General 3ii



A golfer hits a ball from a point O on horizontal ground with a velocity of $55\,\mathrm{m\,s^{-1}}$ at an angle of $20\,^\circ$ above the horizontal. The ball first hits the ground at a point A and the time of flight is t seconds. Assume that there is no air resistance.

Part A Value of t

Calculate the value of t to 3 significant figures.

Part B Distance OA

Calculate the distance OA to 3 significant figures.

Part C Speed of motion

Calculate the speed of motion of the ball $2.6\,\mathrm{s}$ after the golfer hits the ball. Give your answer to 3 significant figures.

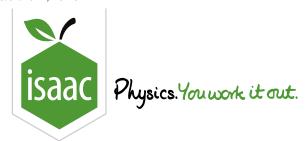
Part D Direction of motion

Calculate the direction of motion of the ball $2.60\,\mathrm{s}$ after the golfer hits the ball. Give your answer, measured below the horizontal, to 3 significant figures.

Used with permission from UCLES, A Level, June 2017, OCR M2, Question 2

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STEM SMART Double Maths 15 - Trigonometry, Vectors & Kinematics Revision



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Maths

Applying Trigonometry

Applying Trigonometry



A rower attempts to row across a river from a place A where the banks of the river are straight and parallel. They wish to reach a point B which is directly opposite to A on the other bank (i.e. on a line perpendicular to the bank at point A).

They start to row towards B, keeping the boat aligned in a direction parallel to $\underline{\bm{j}}$, but discover that there is a current flowing in a direction $\underline{\bm{i}}$ parallel to the banks, such that their resultant travel is along a vector $\underline{\bm{v}} = \underline{\bm{i}} + 4 \bm{j}$.

Part A Speed of the rower

Find the magnitude of vector v.

The following symbols may be useful: v

Part B Angle between \underline{v} and \underline{i}

Find the angle between vectors $\underline{\boldsymbol{v}}$ and $\underline{\boldsymbol{i}}$. Give your answer to no more than 3 s.f.

Part C Direction of travel

If they are to arrive at B, but can adjust their rowing speed to cross to the other bank in the same time that it would take if there were no current, in what direction should they actually row? Give your answer as a vector in terms of the unit vectors i and j.

The following symbols may be useful: i, j, v_row

What is the angle between $\underline{\boldsymbol{v}}$ and \boldsymbol{j} ? Give your answer to no more than 3 s.f.

Part D A tower in the distance

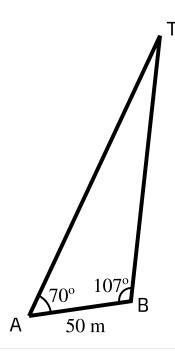


Figure 1: The tower, and points A and B.

Some walkers see a tower, T, in the distance and want to know how far away it is. They take a bearing from point A and walk for $50\,\mathrm{m}$ in a straight line before taking another bearing from point B. They find that the angle TAB is $70\,^\circ$ and angle TBA is $107\,^\circ$ (see **Figure 1**).

Find the distance of the tower from A. Give your answer to 3 s.f.

Part E Distance from C

They continue walking in the same direction for another $100\,\mathrm{m}$ to a point C, so that AC is $150\,\mathrm{m}$. What is the distance of the tower from C? Give your answer to $3\,\mathrm{s.f.}$

Part F Shortest distance from A to C

Find the shortest distance of the walkers from the tower as they walk from A to C. Give your answer to 3 s.f.

Part G Area swept out

D is the point on AC such that TD is the shortest distance of the walkers from the tower.

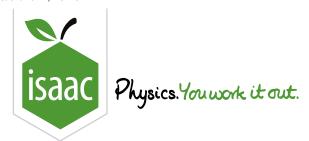
Find the area of ground represented by the triangle ATD. Give your answer in ${
m km}^2$ and to 3 s.f.

Adapted with permission from SAW 2017 and UCLES, A Level, January 2009, Paper 4722, Question 5.

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Maths

Trigonometry: Double Angles 4i

Trigonometry: Double Angles 4i



Part A Proof

By first expanding $\cos(2\theta + \theta)$, rewrite $\cos 3\theta$ in terms of $\cos \theta$.

The following symbols may be useful: cos(), theta

Part B $\cos 6\theta$

Hence write $\cos 6\theta$ in terms of $\cos \theta$.

The following symbols may be useful: cos(), theta

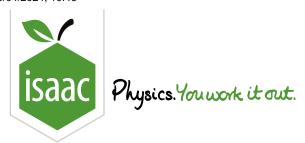
Part C The equation $1+\cos 6\theta=18\cos^2 \theta$

Give the smallest positive solution to the equation

$$1 + \cos 6\theta = 18\cos^2 \theta$$

in degrees.

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Maths

Trigonometry: Combined Angles 4ii

Trigonometry: Combined Angles 4ii



Part A Combined Angles

Express $8\sin\theta - 6\cos\theta$ in the form $R\sin(\theta - \alpha)$, where R > 0 and $0^\circ < \alpha < 90^\circ$.

Give the value of R.

The following symbols may be useful: R

Give the value of α to three significant figures.

Part B Solve

Hence solve, for $0^{\circ} < \theta < 360^{\circ}$, the equation $8\sin\theta - 6\cos\theta = 9$, giving your answers in degrees to three significant figures.

Give the smallest solution.

Give the largest solution.

Part C Maximum Value

Hence find the greatest possible value of

$$32\sin x - 24\cos x - (16\sin y - 12\cos y)$$

as the angles \boldsymbol{x} and \boldsymbol{y} vary.

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