

Localization Lab

MAHALANOBIS THRESHOLD

We need to set the threshold for the Mahalanobis distance (`mahaThreshold`), using the Matlab “`chi2inv`” function. The function $x = \text{chi2inv}(p, nu)$ returns the inverse cumulative distribution function (*icdf*) of the chi-square distribution with degrees of freedom nu , evaluated at the probability values in p .

Knowing that the Mahalanobis distance is obtained by the formula:

$$d^2 = (Y_k - \hat{Y}_{k+1/k})^T (C_k \cdot P_{k+1/k} \cdot C_k^T + Q_\gamma)^{-1} (Y_k - \hat{Y}_{k+1/k})$$

where $C(k) \cdot P(k+1/k) \cdot C(k)^T$ is the covariance matrix of Y^\wedge and Q_γ is the covariance matrix of Y ; so the distance between Y and Y^\wedge is evaluated keeping into account the respective variances.

The shape of the Chi-Square distribution depends on the dimension of the vector $(Y - Y^\wedge)$, which in our case has dimension 2; this will be the value of the degree of freedom that we will consider.

We have also set the p value at 0.95 since the magnets that we are going to detect are likely to be the real one.