

1/30/23 Sorting

regular #s have a natural total order

partial order - complex #s

Bogo sort random  $O(n) = n!$

Selection sort - look for smallest item over & over  $n^2 = O(n)$

Insertion Sort - start w/ tiny list of length 1, continue checking array of items & insert them where needed  
 $n^2 = O(n)$

Binary Search - fastest,  
 $-n \log(n)$

Bubble Sort - look @ elements & swap  $n^2$   
- items bubble up

CRAM

Memory is 100x slower than CPU (cache is fast)

Cache affinity

Merge Sort - 2 lists, take two elements, compare, into 1 list, cut in  $1/2$ , do exact same thing, it creates "runs" of 4.  $n \log n$

Shell sort  $O(n^{\frac{5}{3}})$

- rly weird

- faster than quick sort when  $n$  small

$n \log n$   
merge sort

heap sort

quick sort (average case)  
smallest constant

Quick Sort

- pick #, average of 3 items this is pivot

- people pick different pivot algorithms

- 3 arrays of whats smaller, equal & bigger

- sort smaller & larger using the same algorithm of either

Heapsort  $n^3$   
- fastest

## Heaps

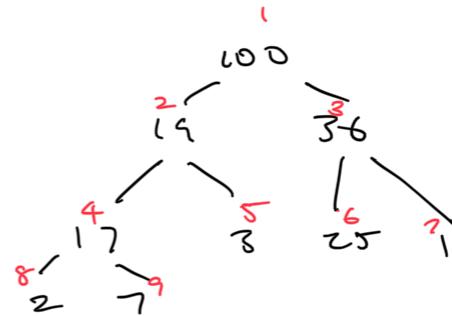
- many kinds
- a binary tree
- 1 node = heap
- parent node is  $>$  than leaves
- can have 0, 1, or 2 child

$n \log n$

- not recursive

Build heap  $n \log n$

- start @ last element



left child is always  $i * 2$

right is  $(i * 2) + 1$

merge sort works for magnetic tape storage bc you can't jump back & forth, just need 3 tapes, assuming you don't have RAM  
using comparisons, smallest is  $n \log n$

Radix sort (kinda  $n \log n$ )

- look @ lowest digit
- doesn't use comparison