

$$1. \nabla^2 \mathcal{I}(r) = - \frac{6\pi\eta a}{k_B T}$$

$$\nabla^2 \mathcal{I}(r) = \frac{1}{r^2} \frac{d}{dr} \left( r^2 \frac{d\mathcal{I}}{dr} \right) + \frac{1}{r^2 \sin\theta} \frac{d}{d\theta} \left( \sin\theta \frac{d\mathcal{I}}{d\theta} \right) + \frac{1}{r^2 \sin\theta} \frac{d^2 \mathcal{I}}{d\varphi^2}$$

→ Ya que  $\mathcal{I}(r)$  solo depende de  $r$ , se puede eliminar lo que tenga  $\theta$  y  $\varphi$

$$= \frac{1}{r^2} \frac{d}{dr} \left( r^2 \frac{d\mathcal{I}}{dr} \right) = - \frac{6\pi\eta a}{k_B T}$$

$$= \frac{1}{r^2} \left( 2r \frac{d\mathcal{I}}{dr} + r^2 \frac{d^2 \mathcal{I}}{dr^2} \right) = - \frac{6\pi\eta a}{k_B T}$$

$$= \frac{d^2 \mathcal{I}}{dr^2} + \frac{2d\mathcal{I}}{r dr} = - \frac{6\pi\eta a}{k_B T}$$

$$= \frac{d^2 \mathcal{I}}{dr^2} + \frac{2d\mathcal{I}}{r dr} + \frac{6\pi\eta a}{k_B T} = 0$$