

LITERATURE REVIEW: — Dynamic Massive Parallel Computation Model for Graph Problems —

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1 Introduction

Big data and data analytics have become increasingly popular over the years, with the growing volume and variety of available data, and cheaper and more powerful computational processing. However, traditional data mining algorithms are becoming insufficient when performing computation on massive amounts of data, so parallel computing is introduced to increase the available computation power and to speed up application processing [1]. Parallel computing is a type of computing architecture where applications, computations, or processes are executed simultaneously. It basically breaks a larger task into several very similar smaller tasks so that they can be run independently at the same time, and their results are later combined upon completion. Parallel computing is widely used in various fields, such as climate prediction, fluid dynamics, and cryptology, in order to resolve their needs for speed.

One of the most popular models of parallel computing is the Massive Parallel Computation (MPC) model, which is seen as the canonical model for dealing with large scale data nowadays. It consists of machines with a large number of processors performing a set of coordinated tasks in synchronism [6]. And the main objective in the analysis of algorithms in the MPC model is to solve a problem with constant number of rounds while minimizing the amount of communication performed per round [5].

Although the MPC model is able to process massive amounts of data, it takes up large volumes of resources during computation. Also, because the datasets in the real world evolve continuously instead of being static, algorithms and models are forced to be re-executed after small modifications occur to the data, which leads to excessive processing time and resource requirements. As a result, researches of dynamic algorithms in traditional computing models are greatly promoted, since they are able to adjust and maintain solutions to given problems throughout input data modifications by performing only limited computation.

In this project, I aim to implement and test the dynamic algorithm in the Dynamic Massive Parallel Computation (DMPC) model by Italiano et al. [9] on some alternative

graph-theoretic problems, such as the 2-CYCLE conjecture and the maximal independent set.

2 Literature Review

The concept of MPC is extensively studied in recent years. However, there exists a very important bottleneck in designing efficient MPC algorithms for graph problems when the space per machine is much smaller than the number of vertices n - it requires $\Omega(\log k)$ rounds to find a vertex at distance k from a given vertex [4]. For example, based on the 2-CYCLE conjecture, even distinguishing a graph consisting of single cycle of length n from 2 cycles of size $n/2$ requires $\Omega(\log n)$ rounds [10] [11]. Another one of the graph problem in the MPC model is the minimum spanning tree, which was recently proved to be solved in $O(\log n)$ rounds using an overall space of $\tilde{O}(n^{1+\epsilon})$ for some constant $\epsilon < 1$ [3].

It took almost 10 years for researchers to overcome the $O(\log n)$ barrier for computing approximate matching problems, and only very recently did Ghaffari and Uitto [8] implement an algorithm that can compute a $(1+\epsilon)$ -approximate matching in $\tilde{O}(\sqrt{\log \Delta})$ rounds using sub-linear memory, where Δ is the maximum degree in the graph. Under the same memory assumption, Andoni et al. [2] showed that connected components was able to be run in $\tilde{O}(\log D)$ rounds, where D is the diameter of the graph. In addition, the computation of maximal independent set can be solved by the algorithm in [8] also in $\tilde{O}(\sqrt{\log \Delta})$ rounds. And this result is now improved by himself to simple $O(\log \log \Delta)$ round with $\tilde{O}(n)$ memory per machine [7].

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