

# FORMULA STUDENT GERMANY

INTERNATIONAL DESIGN COMPETITION

## Active Rear Wheel Steering

Torben Brockhage, Ignition Racing Team electric  
Philipp Bergmann, Ignition Racing Team electric





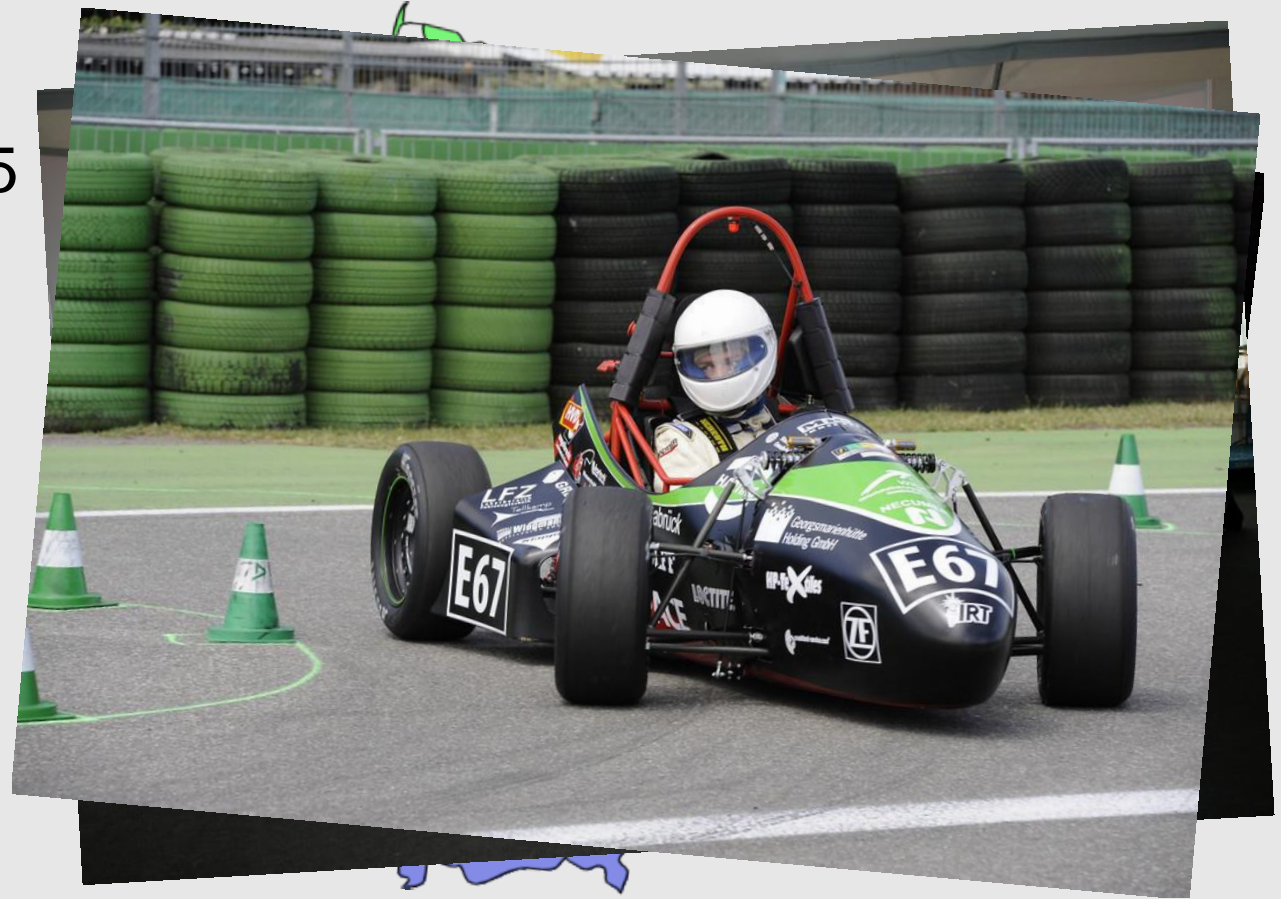
## Structure

- Introduction of the team and the car
- Motivation to develop rear wheel steering
- Mechanical realization
- Electric drivetrain
- Vehicle dynamics and simulation
- Control systems and software
- Results



### Ignition Racing Team electric

- FSE team from the UAS Osnabrück
- 45 active team members in 2014/2015
- First participation FSC 2007
- Since 2011 participation in FSE



### IR15 eXcess

- 5th electric car
- 225 kg overall
- Single motor at rear axle (YASA 750)
- Full-carbon fiber monocoque
- 378 V, 6.6 kWh Lithium-Polymer accumulator
- Only car using Rear Wheel Steering (RWS) at FSG and FSS 2015





## Motivation to develop Rear Wheel Steering

- Improving the lateral dynamics of the car
- Active changes in vehicles performance possible
- System weight is quite low (only 3 kg overall)
- System is easy exchangeable
- Innovation in Formula Student





### First Task: name the system – find cool acronym

4-wheel

cool

steering system

fancy

adaptive

moving

stear4fear

electrical

active

toe correction

rear wheel

mechatronic



## Active Steering System (ASS)



First Task: name the system – find cool acronym

4-wheel

cool

steering system

adaptive

moving

steering

electrical

active

toe correction

rear wheel

mechatronic

got nice  
**ASS**  
Active Steering System (ASS)

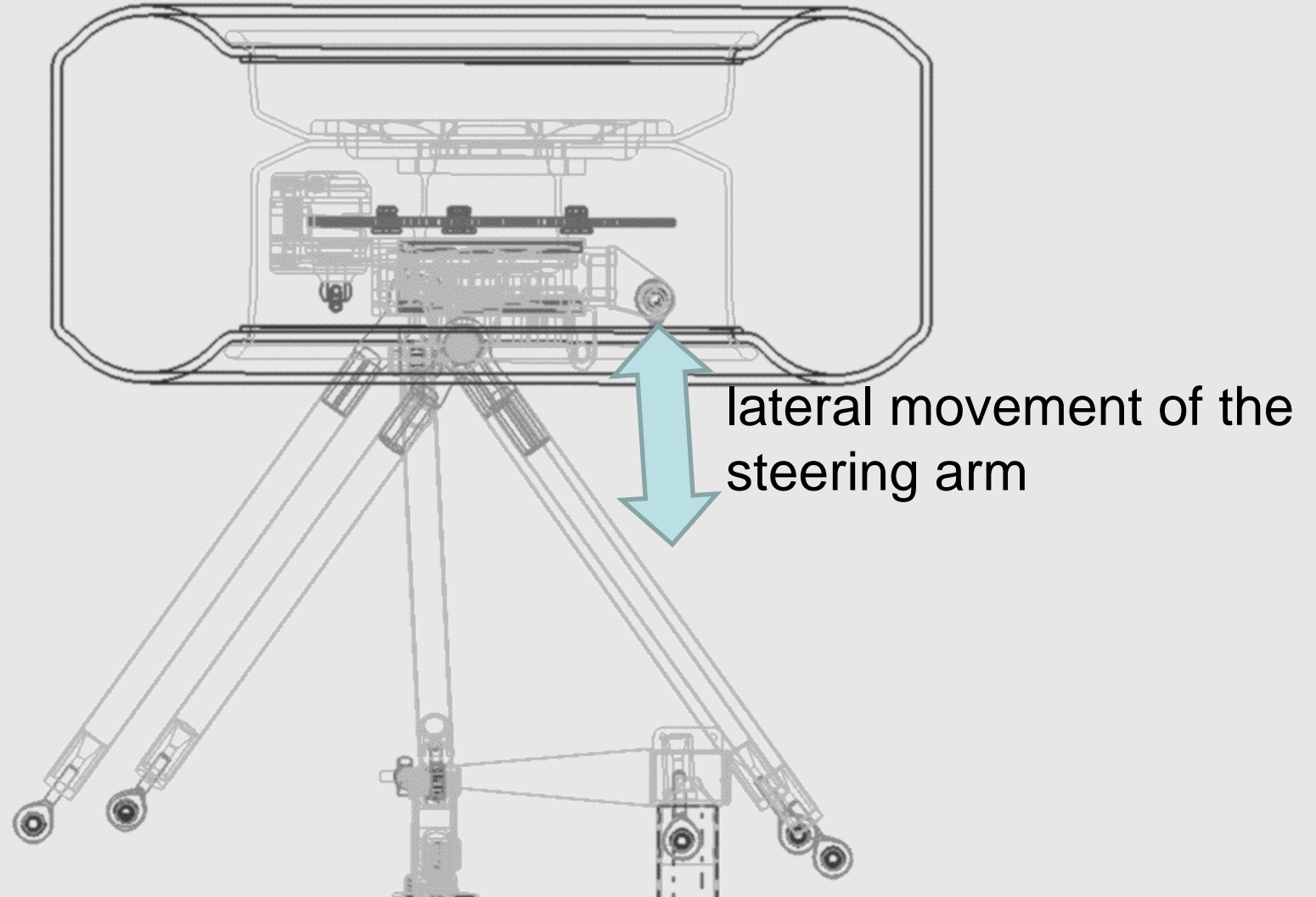


## Concept

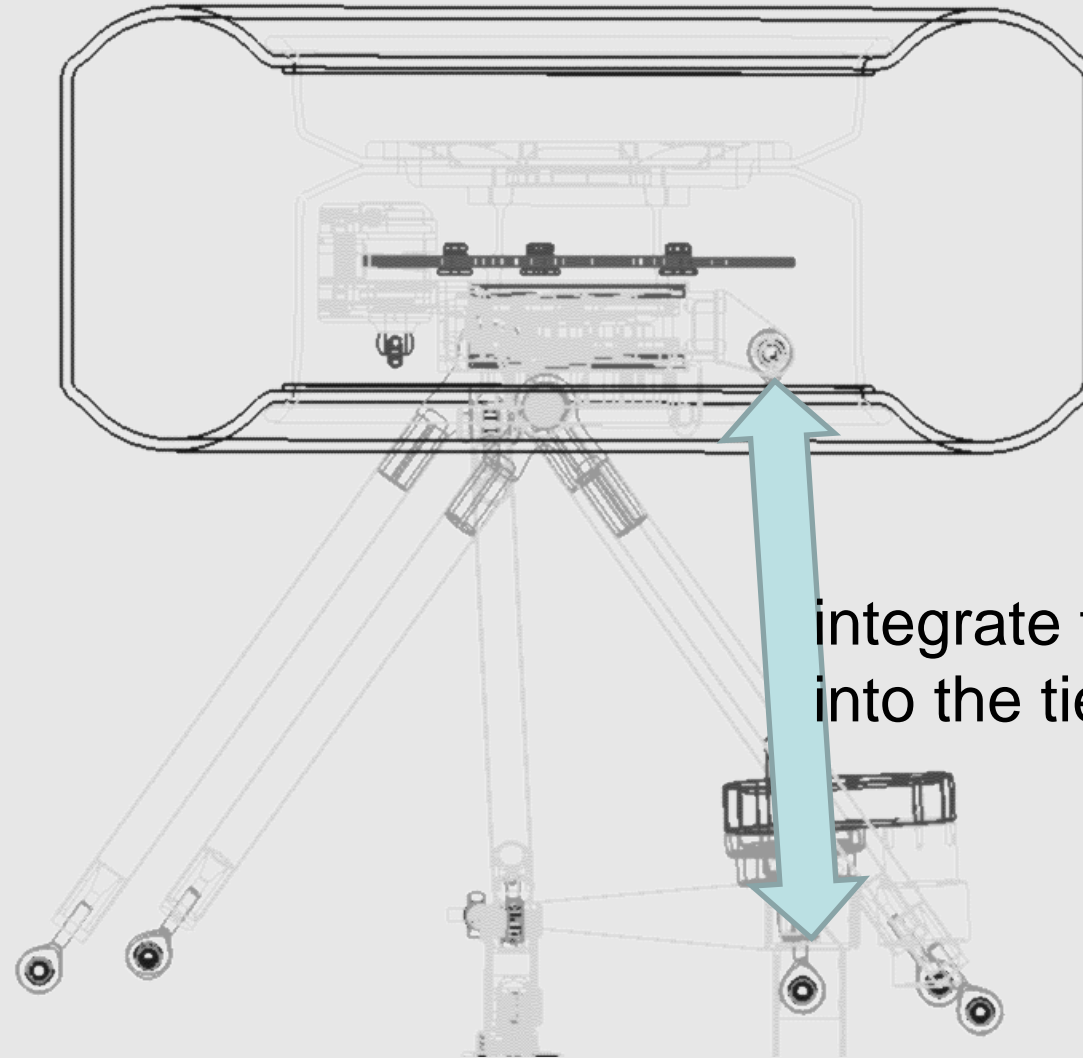
- Goal: actuator steers the rear axle ( $\pm 3^\circ$  allowed)



### Concept



### Concept



integrate the actuator  
into the tie rod



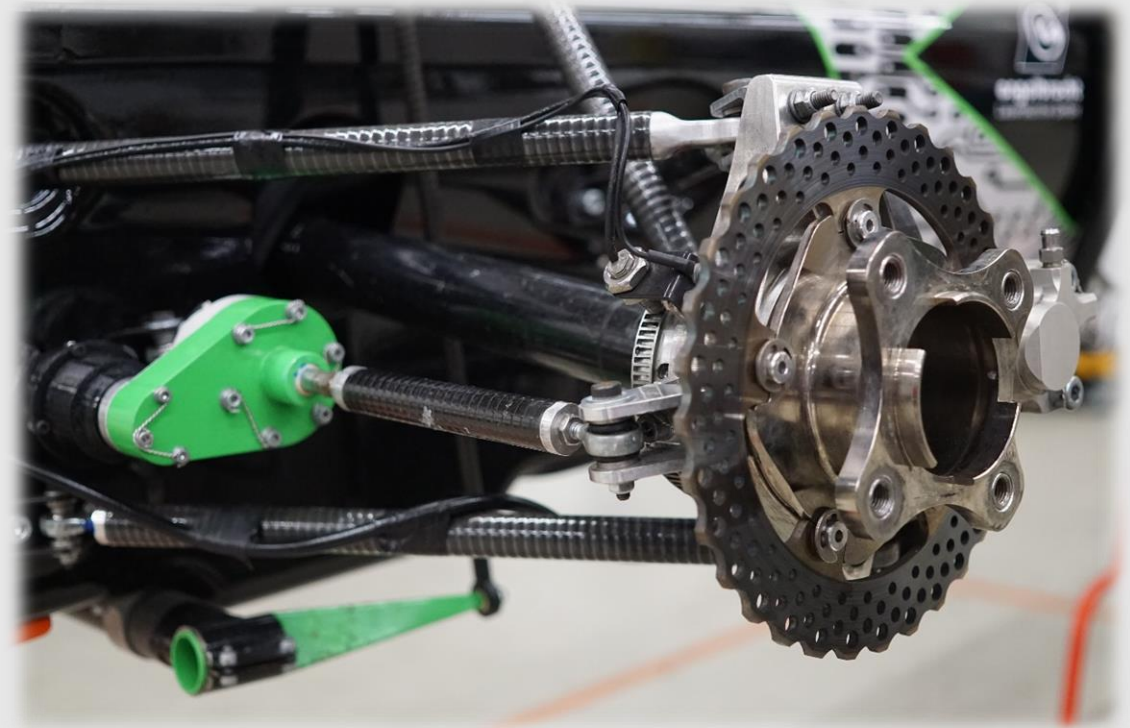
## Concept Decisions

- Goal: actuator steers the rear axle ( $\pm 3^\circ$  allowed)
- One actuator per wheel
- Integrate the actuator into the tie rod
- Driven by electric motor



### Mechanical Requirements

- Transform rotary movement from the motor in linear movement
- Self-locking in case of system failure
- Small weight and small volume
- Fit actuators into the rest of the suspension





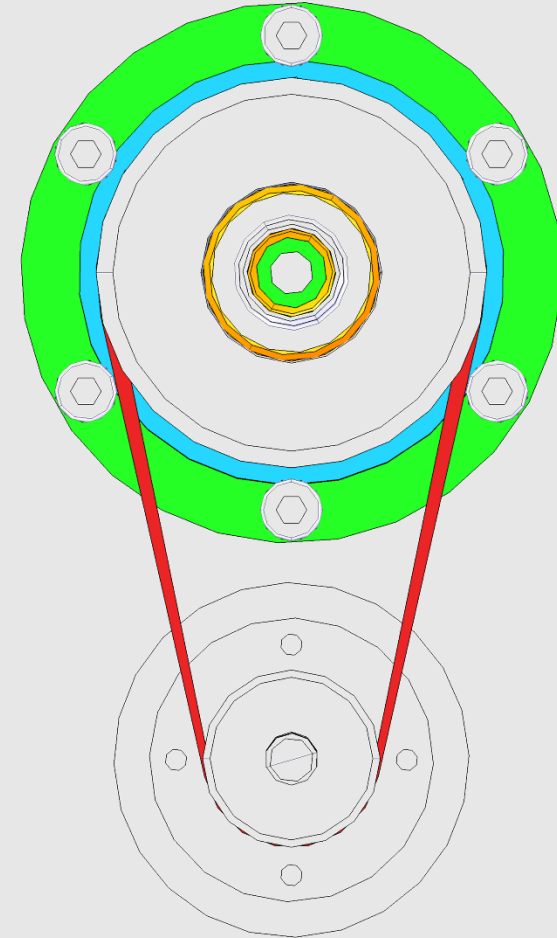
## The Trapezoidal Thread Spindle

- Transform rotary in linear movement
- Small lead angle
  - self-locking
- Special nitriding steel
  - reduced wear
  - constant friction coefficient



### Realization of the Actuator – Belt Drive

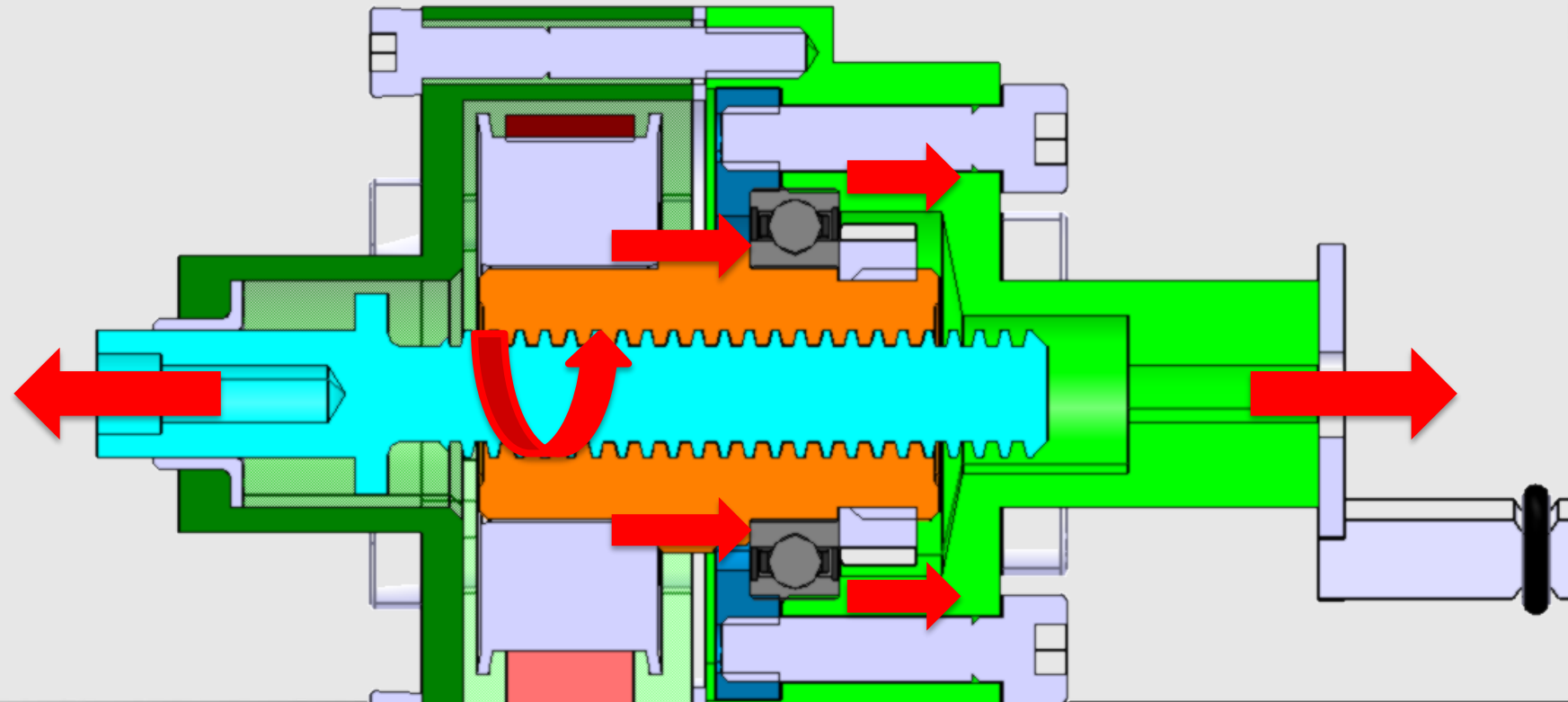
- Transmits the torque from the motor to the spindle nut
- Transmission ratio 1:2
- Decouples the motor from the linear forces





### A Sectional Drawing of the Actuator

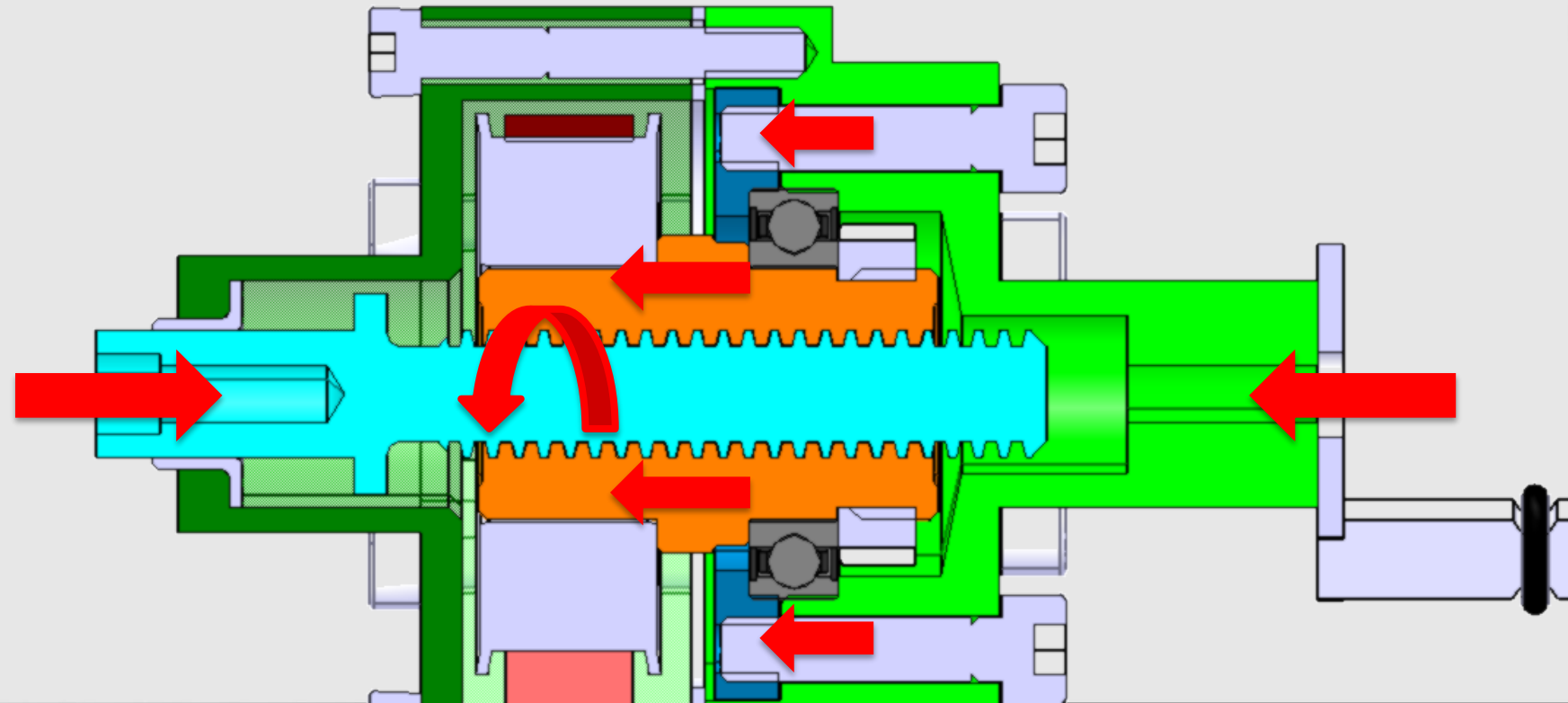
- Axial forces are transferred by deep groove ball bearing





### A Sectional Drawing of the Actuator

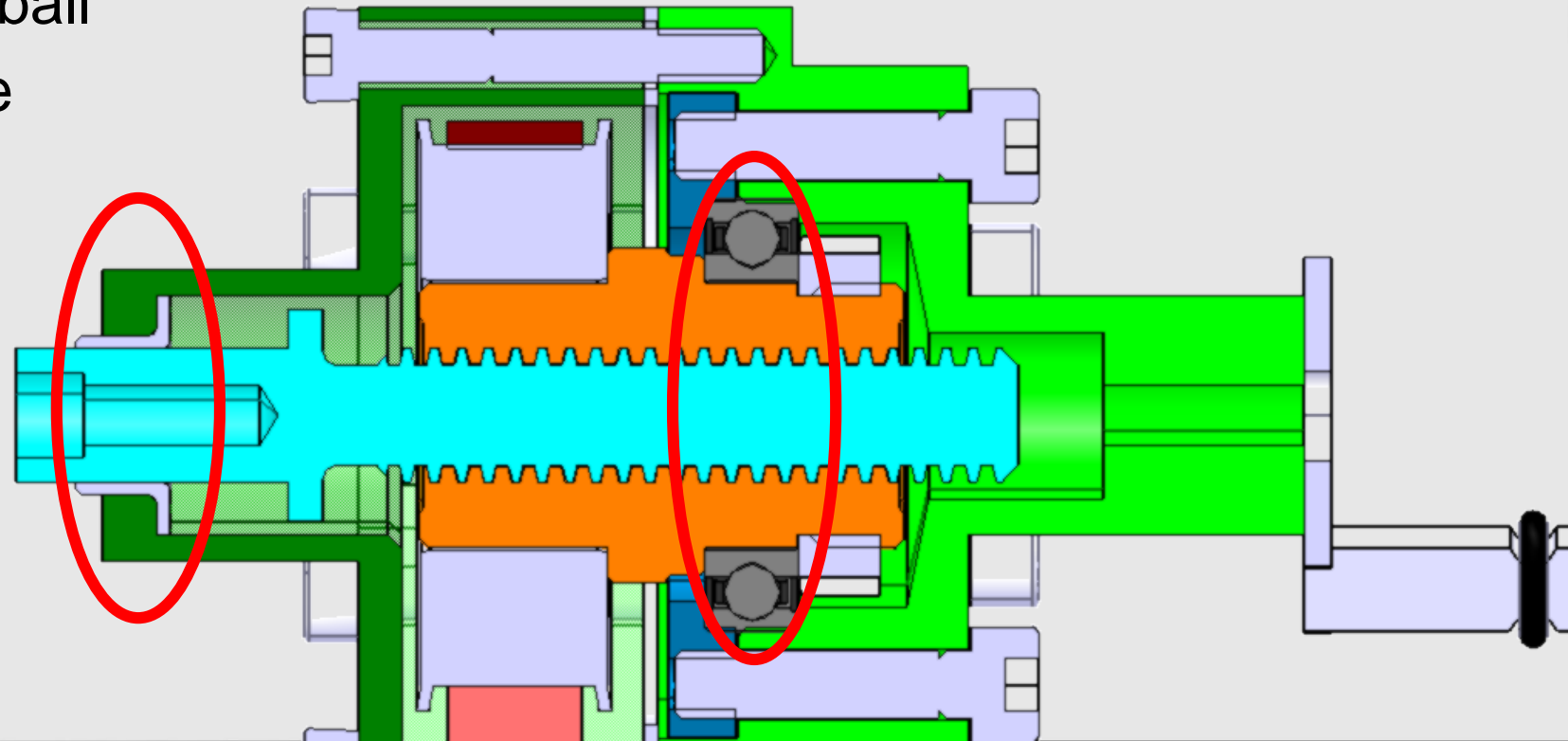
- Axial forces are transferred by deep groove ball bearing





### A Sectional Drawing of the Actuator

- Axial forces are transferred by deep groove ball bearing
- Fixed by locating grooved ball bearing and a floating slide bearing inside the housing
- The spindle transfers the movement to the tie rod







## Electrical Drivetrain

- Max. force in the rear tie rod 1.6kN
  - Simulated in MSC Adams CAR (based on caster, align torque, max. lateral forces and steering arm length)
- Power
  - max. speed :  $1200 \frac{1}{min} \rightarrow$  steer  $3^\circ$  in 0.2 seconds
  - max. torque:

$$M_S = \frac{F_T}{2 * \pi * \eta_S} * \frac{\nabla}{1000} = \frac{1600}{2 * \pi * 0.3} * \frac{2}{1000} = 1.69 Nm$$

→ Power: 187 W mechanical!



## Electrical Drivetrain

- Developed own calculation program
- Includes all relevant data
- Calculates electric parameters based on mechanical parameters

### IRTe Rear Wheel Steering Caluclation

Suspension Data			Mechanical Calculation			eletrical calculation	
Positioning-Force Wheel	1600	N	positioning way:	14,11765	mm	Max. Voltage	29,4 V
Positioning Speed:	35	mm/s	minium positioning speed (0,2s for 80% Travel)	28,23529	mm/s	Nom. Voltage	25,9 V
max .steer angle	3	°	positioning power	56	W	Min. Voltage	21 V
steer angle / positioning way	0,425	deg/mm	spindle nut speed	2100	1/min	Peak Power	476 W
Mechanical Data			spindle nut torque	1,018592	Nm	Peak Current	22,66667 A
spindle gradient	1	mm	spindle nut power	224	W	Energy Comsumption	31,73333 Wh
spindle efficiency	0,25		belt drive torque	0,509296	Nm	Capacity	1,225225 Ah
ratio belt drive	2		belt drive speed	4200	1/min	Req Voltage at Motor for act. Speed	35,68142 V
planet gear ratio	4,8		planet gear torque	0,132629	Nm	motor current	<b>7,847877</b> A
planet gear efficiency	0,8		planet gear speed	20160	1/min	Drop through torque	2321,01 1/min
Motor Data			motor speed	20160	1/min	real voltage	39,7894 V
max. current motor controller	10	A	motor torque	<b>0,132629</b>	Nm	Motor efficiency	85 %
torque constant	0,0169	Nm/A	Motor Power	280	W		
nominal current	2,79	A					
thermic time constant winding	19,3	s					
Kennliniensteigung	17500	1/min/Nm					
RPM factor	565	1/min*V					
Load Data							
Load cycle	0,2						
Load Time	20	min					
Line Series	7						



## Electrical Drivetrain

- Position controlled electric drivetrain
- Motor: Brushless DC Motor, Ø40 mm x 26 mm (170 g)
- Planetary-gearbox: 4,8:1 (118 g)
- Position encoder: 512 position per turn
- Controller: 240 W peak power per side – 10 A, 24 V (170 g)



## Vehicle Dynamics

Reasons to use RWS:

- Velocity pole shifting
- Yaw control
- Side slip angle influence
- Active toe correction
- ... aaannnd it is pretty cool ;-)

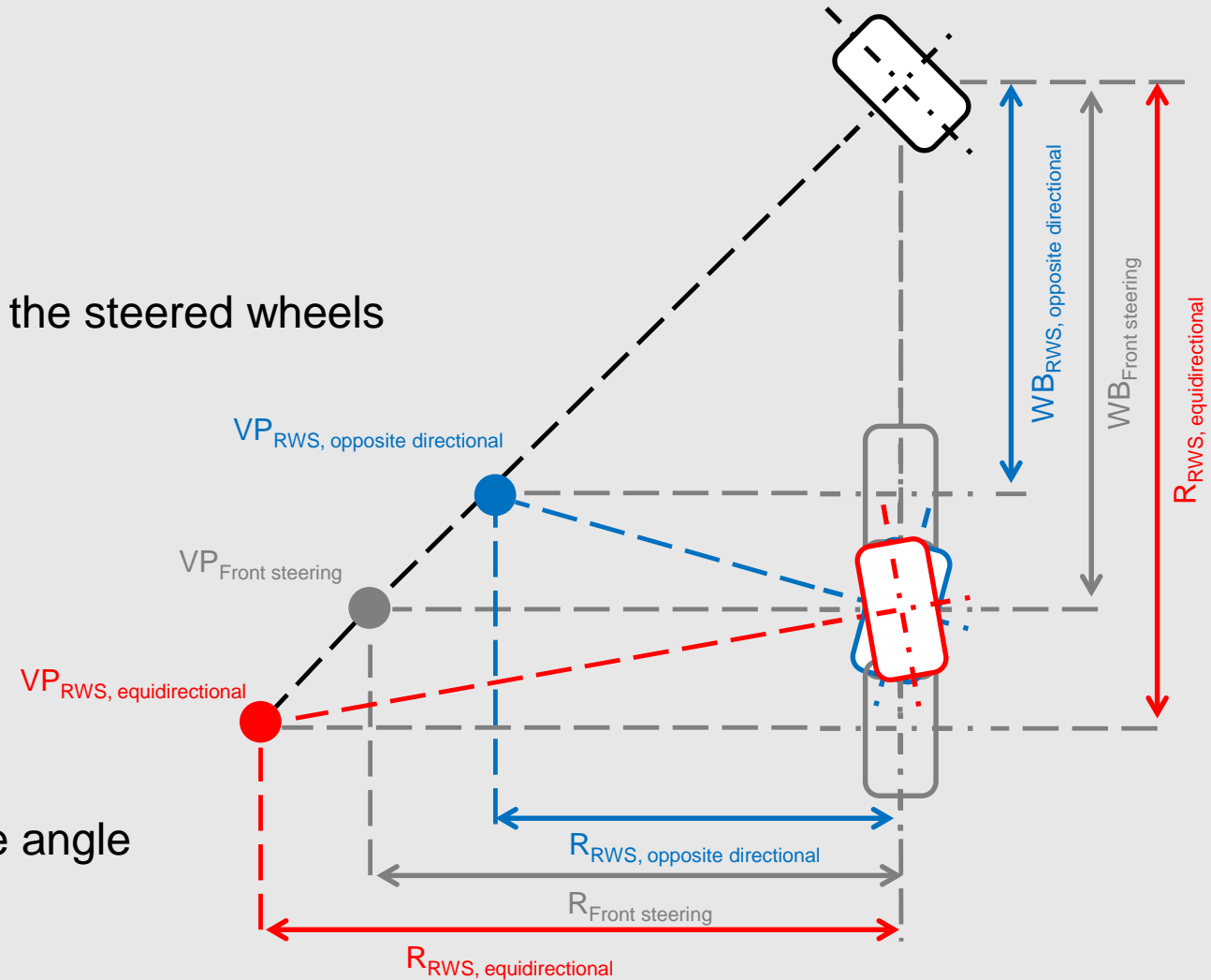


Mitschke, Wallentowitz;  
Dynamik der Kraftfahrzeuge

### Vehicle Dynamics

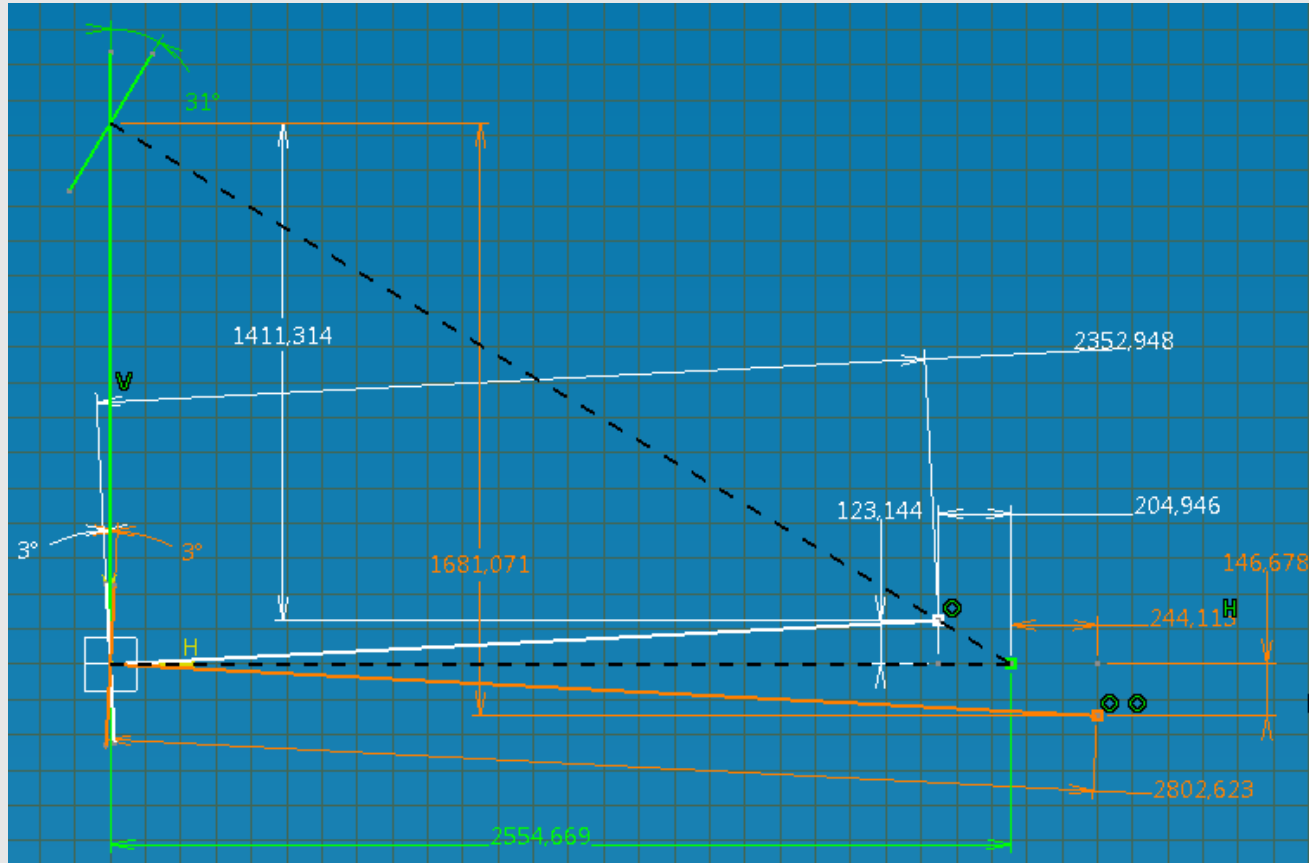
#### Velocity Pole Shifting:

- RWS creates a virtual wheelbase
- VP: intersection of the lines based orthogonally on the steered wheels
- Steering inversely:
  - VP moves towards the front axle
  - WB and turning cycle are reduced
- Steering accordantly
  - VP moves behind the rear axle
  - WB and turning cycle are increased
- No VP when front and rear wheels steer with same angle  
→ Vehicle moves parallel



### Vehicle Dynamics

#### Velocity Pole Shifting:

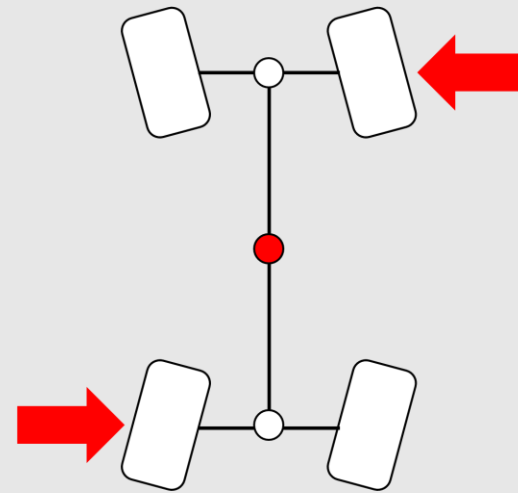


Steering	Accordantly	Inversely	Neutral
Wheelbase [mm]	1681	1411	1535
Turning cycle radius [mm]	2802	2352	2554

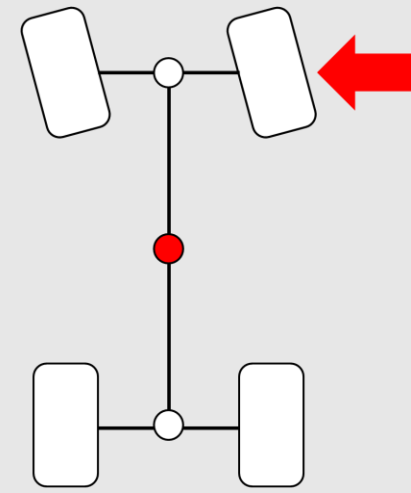
### Vehicle Dynamics

#### Yaw control:

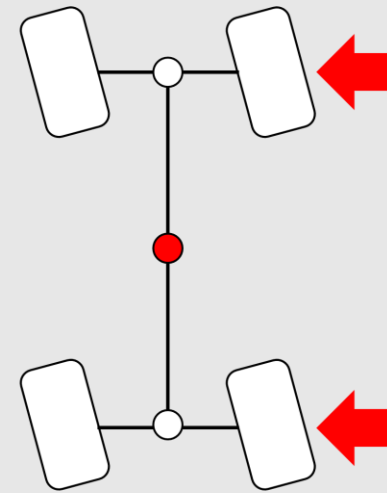
- RWS creates and supports lateral forces on the rear tires
- Inversely:
  - Improvement of yaw moment
  - Higher lateral acceleration
- Accordantly:
  - Weakening of the yaw moment
  - Improvement of understeering



Opposite directional steering angle  
Increased yawing moment



Conventional



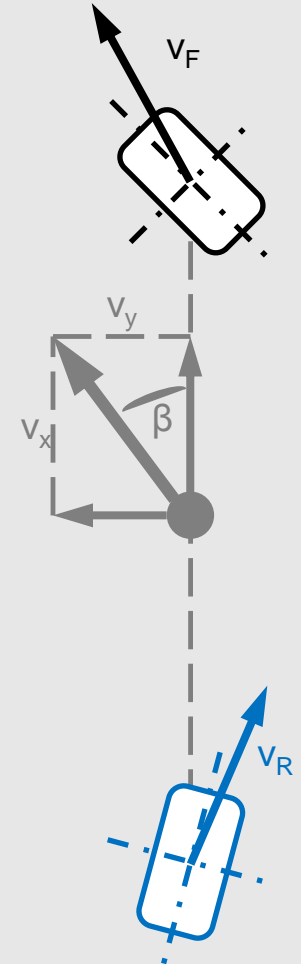
Equidirectional steering angle  
Decreased yawing moment



### Vehicle Dynamics

#### Side slip angle influence:

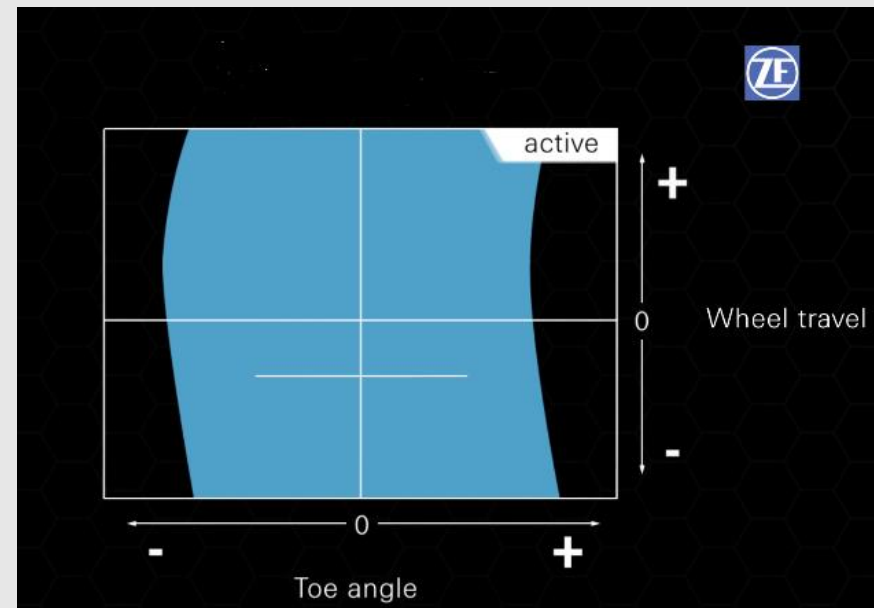
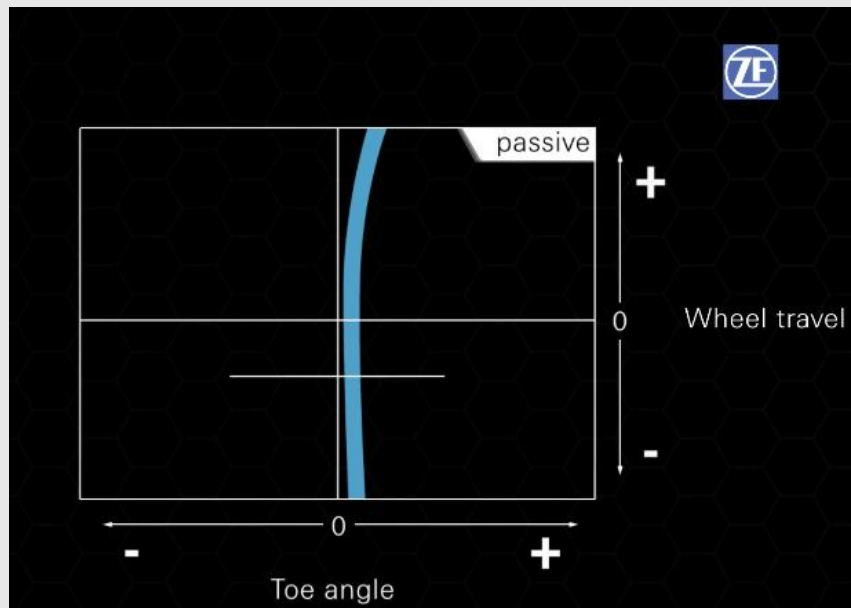
- Describes the orientation of the car and its velocity
- Effects caused by using RWS:
  - Rear axle is immediately taken into account of the vehicle's movement → lateral forces on tires
  - $\beta$  will decrease
  - RWS systems can improve the vehicle stability during over- or understeering situations



### Vehicle Dynamics

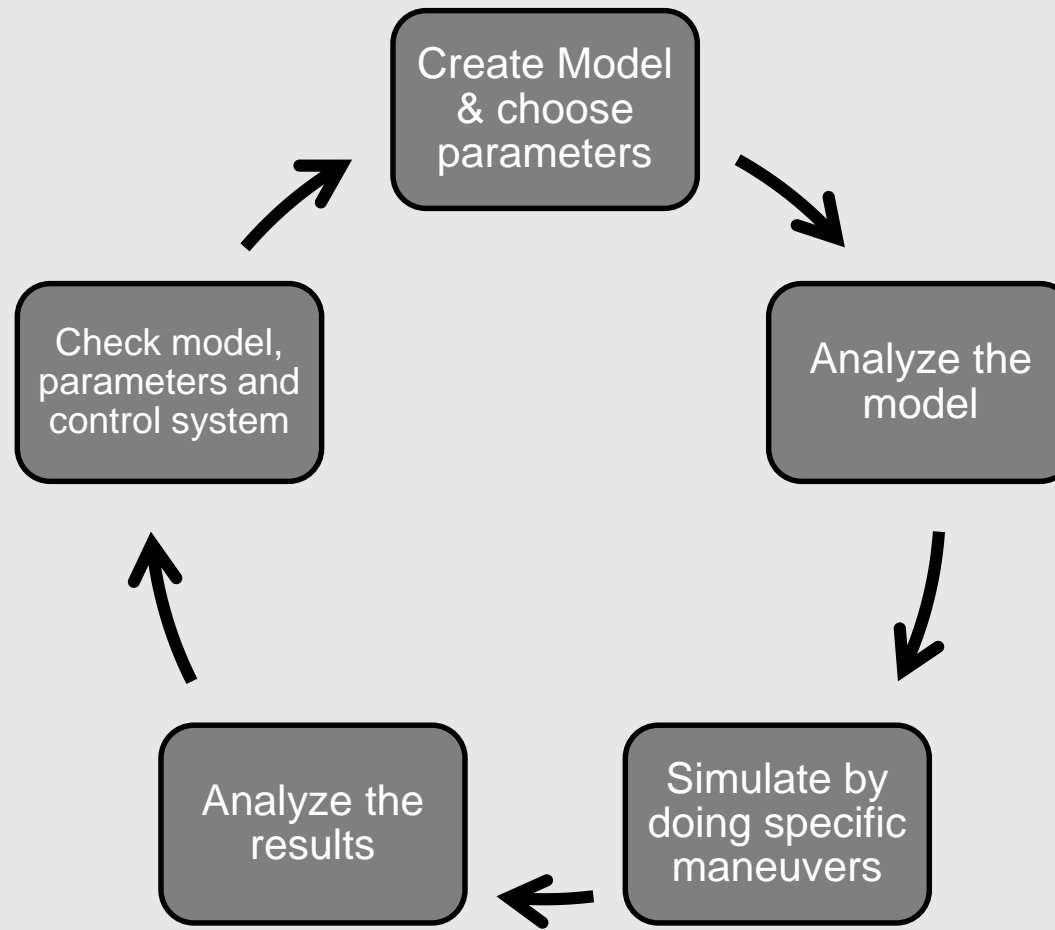
#### Active toe correction

- Passive feature → new degree of freedom while developing the kinematics



© ZF Friedrichshafen AG

### Simulation





## Simulation

- Linear one track model modified to rear wheel steering as a LTI state space system

$$\begin{bmatrix} \dot{\beta} \\ \ddot{\psi} \end{bmatrix} = \begin{bmatrix} -\frac{c_f+c_r}{mv} & -\left(1 + \frac{c_f l_f - c_r l_r}{mv^2}\right) \\ -\frac{l_f^2 c_f + l_r^2 c_r}{Jv} & -\frac{c_f l_f - c_r l_r}{J} \end{bmatrix} \begin{bmatrix} \beta \\ \dot{\psi} \end{bmatrix} + \begin{bmatrix} \frac{c_f}{mv} & \frac{c_r}{mv} \\ \frac{l_f c_f}{J} & -\frac{l_r c_r}{J} \end{bmatrix} \begin{bmatrix} \delta_f \\ \delta_r \end{bmatrix} \quad \underline{Y} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} \beta \\ \dot{\psi} \end{bmatrix}$$

- Simulation using MATLAB script + Simulink model → fast and effective
- Parameters were chosen simplified and based on literature values

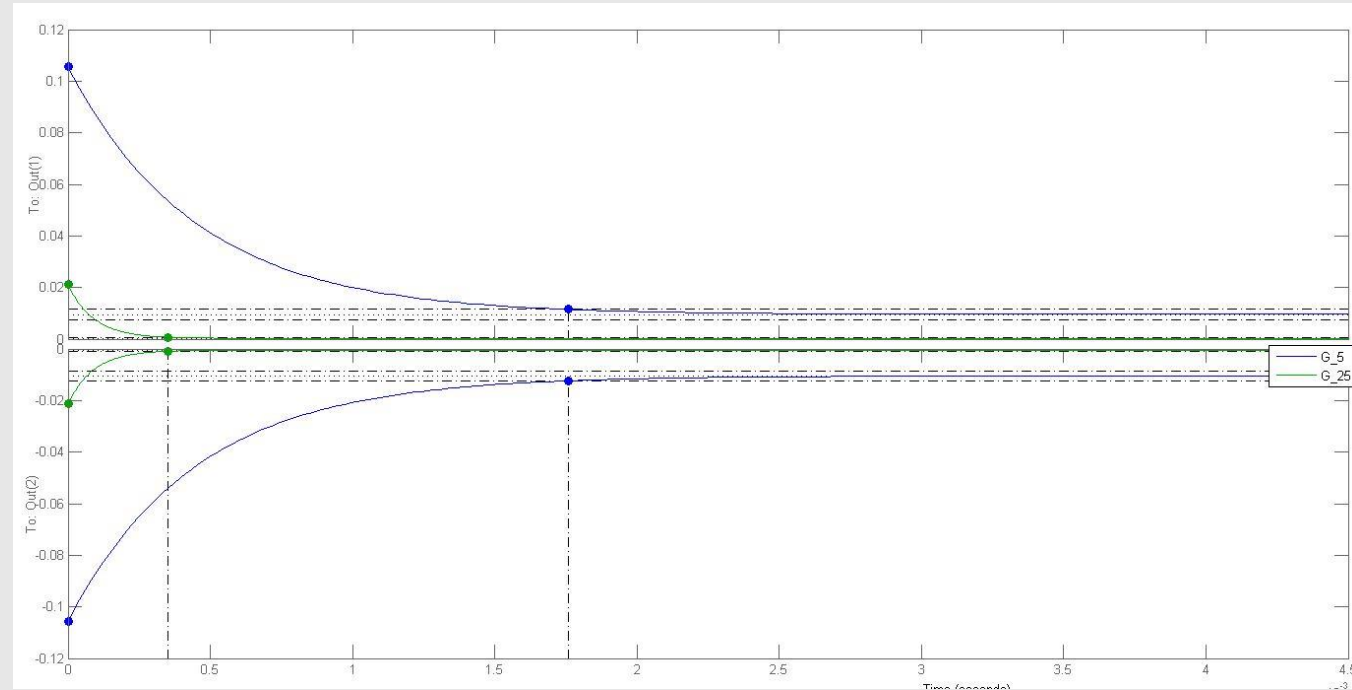


### Simulation

Modell analysis:

- MIMO system
- PTD1 behavior
- Most important characteristic: step response

→ level of the required dynamics of the drivetrain

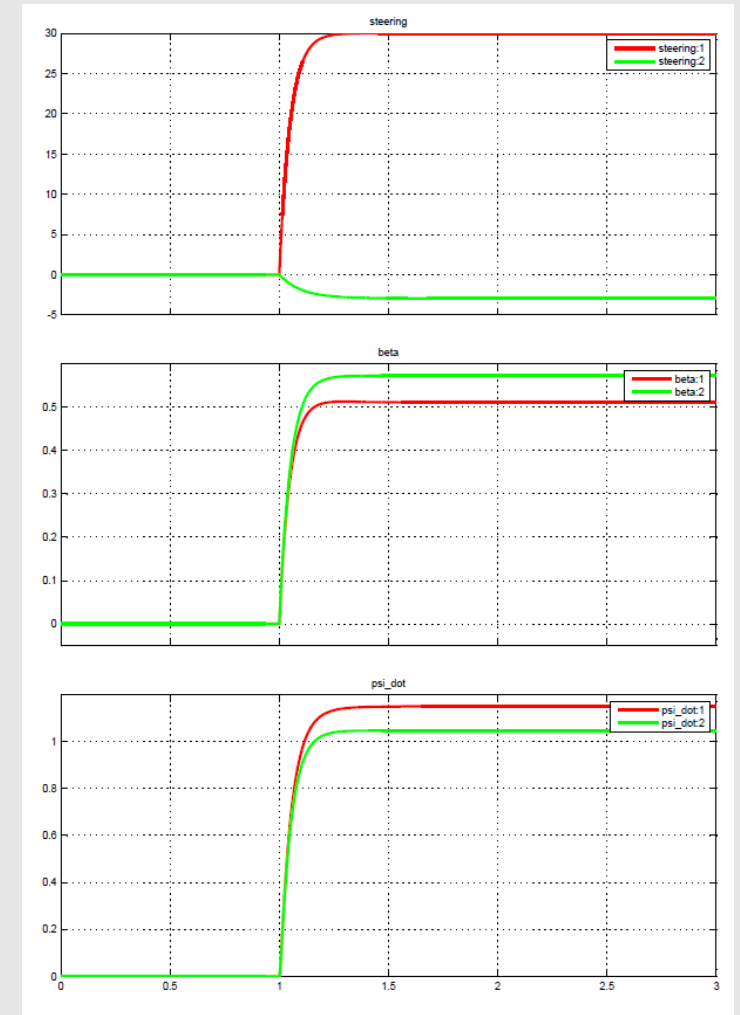


Step responses at 5 & 25  $\frac{m}{s}$

### Simulation

#### Results:

- Proof of theory:
  - Improving of yaw rate at low speeds & weakening at high speeds
  - Side slip angle is reduced
  - Vehicle remains stable
- Basic idea how the control system needs to work
- Changing point of rear steering direction at  $11 \frac{m}{s}$

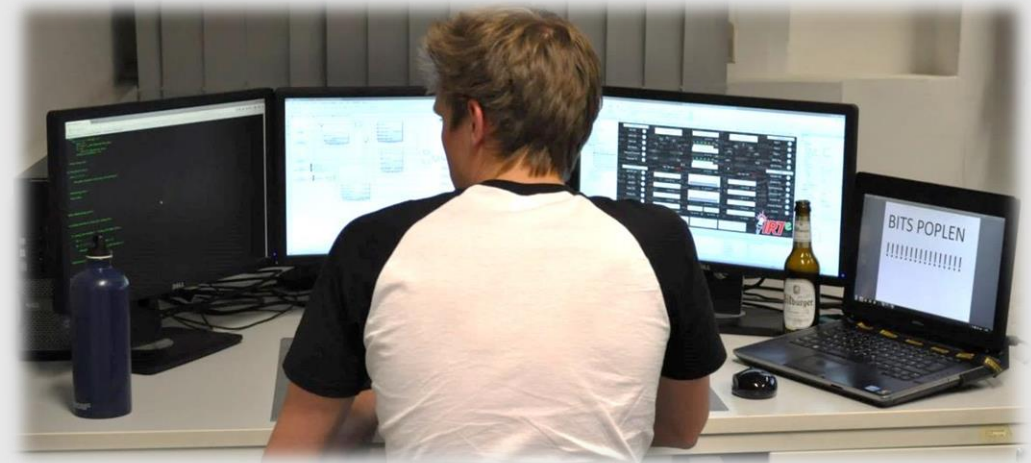


ABS - No ABS

### Control System and Software

Main tasks:

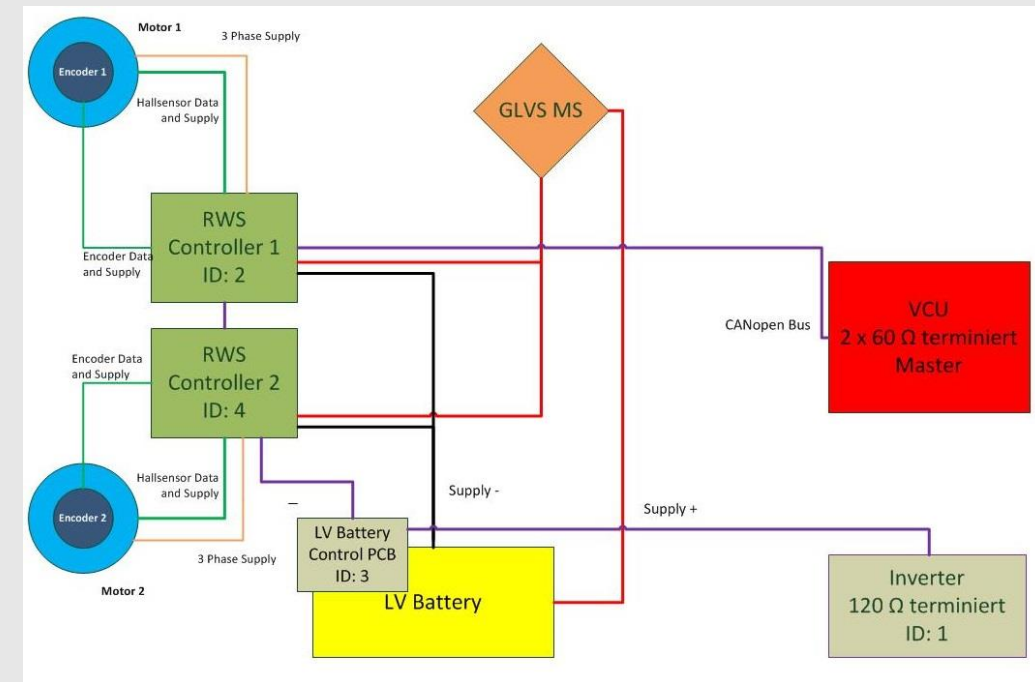
- Parametrization drivetrain
- Communication
- Develop control system
- Implementation into main software
- Start up and visualization
- Data analysis and improvement



## Control system and software

Drivetrain + communication:

- Fit values like max. acceleration, speed, PID tuning, operation mode to the requirements
- Two actuators → twice parametrization
- CANopen bus @ 1mbit/s
- Triggered signals to remain functionality
- Choose necessary messages wisely







## Control system and software

### Control systems

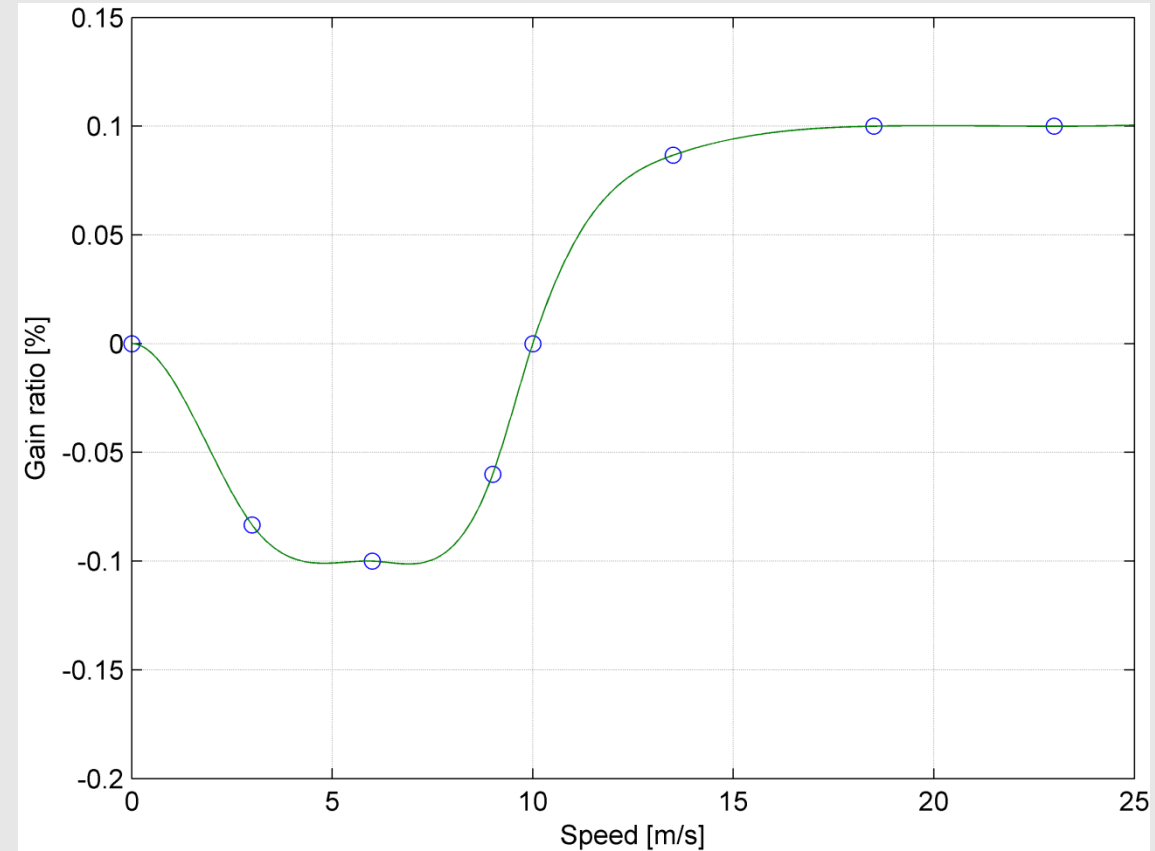
- Review on project targets: reliability, reproducibility, easy handling, stability
- Main question: open or closed loop control

	Advantages	Disadvantages
<b>Open Loop</b>	<ul style="list-style-type: none"><li>• React immediately</li><li>• Reproducible</li><li>• Stable</li></ul>	<ul style="list-style-type: none"><li>• No elimination of external influences</li><li>• Target will not always be reached</li><li>• Accuracy depends on model</li></ul>
<b>Closed loop</b>	<ul style="list-style-type: none"><li>• Elimination of external influences</li><li>• Target will be reached</li></ul>	<ul style="list-style-type: none"><li>• May be instable</li><li>• Might react slow</li><li>• Hardly reproducible</li></ul>

## Control system and software

### Controller:

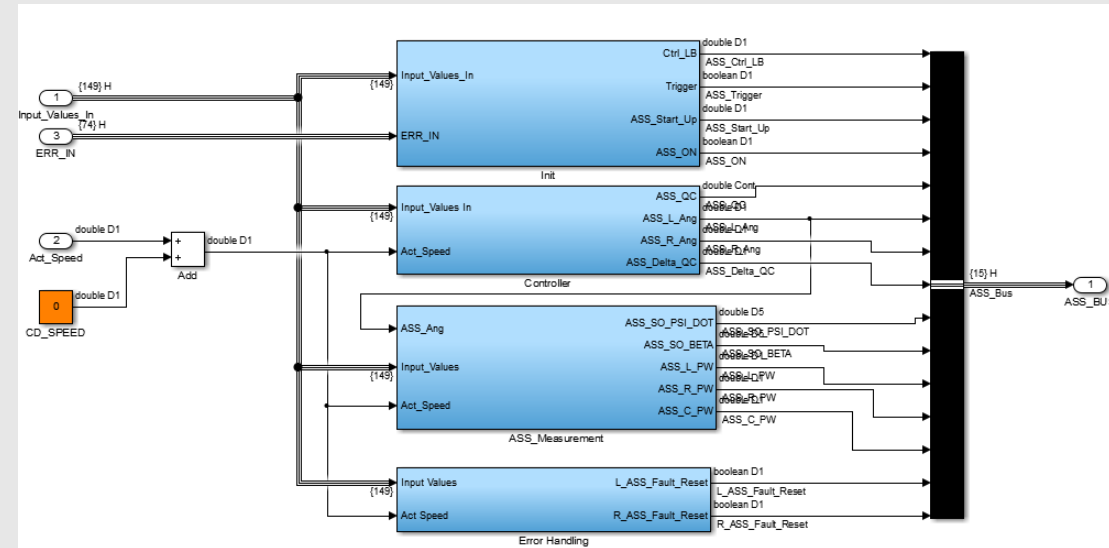
- Basis nonlinear factor, based current vehicle speed for front steering angle
- Created from simulation results
- Using cubic spline interpolation
- Further influence by:
  - Desired driver acceleration
  - Motor current
  - Security checks



### Control system and software

#### Implementation:

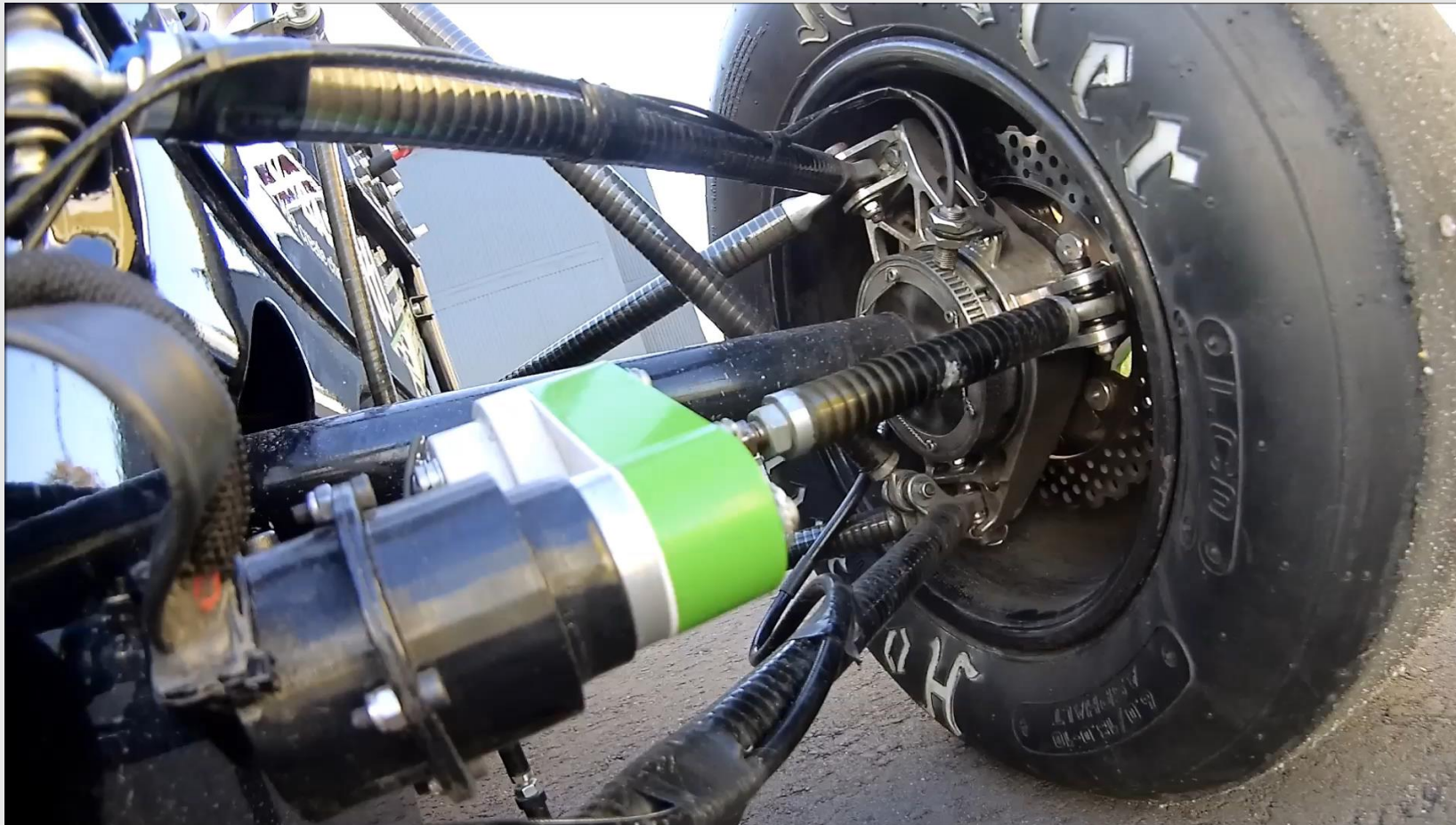
- VCU: dSPACE MicroAutoBox II → Simulink
- Initialization by using last motor positions saved in VCU's flash storage
- Error detection by motor controllers, driver resettable at very low speeds and no steering
- Power measurement to shut down when LV battery is empty
- dSPACE ControlDesk for fast parameter optimizing



# FORMULA STUDENT GERMANY

INTERNATIONAL DESIGN COMPETITION

VIDEO 😊







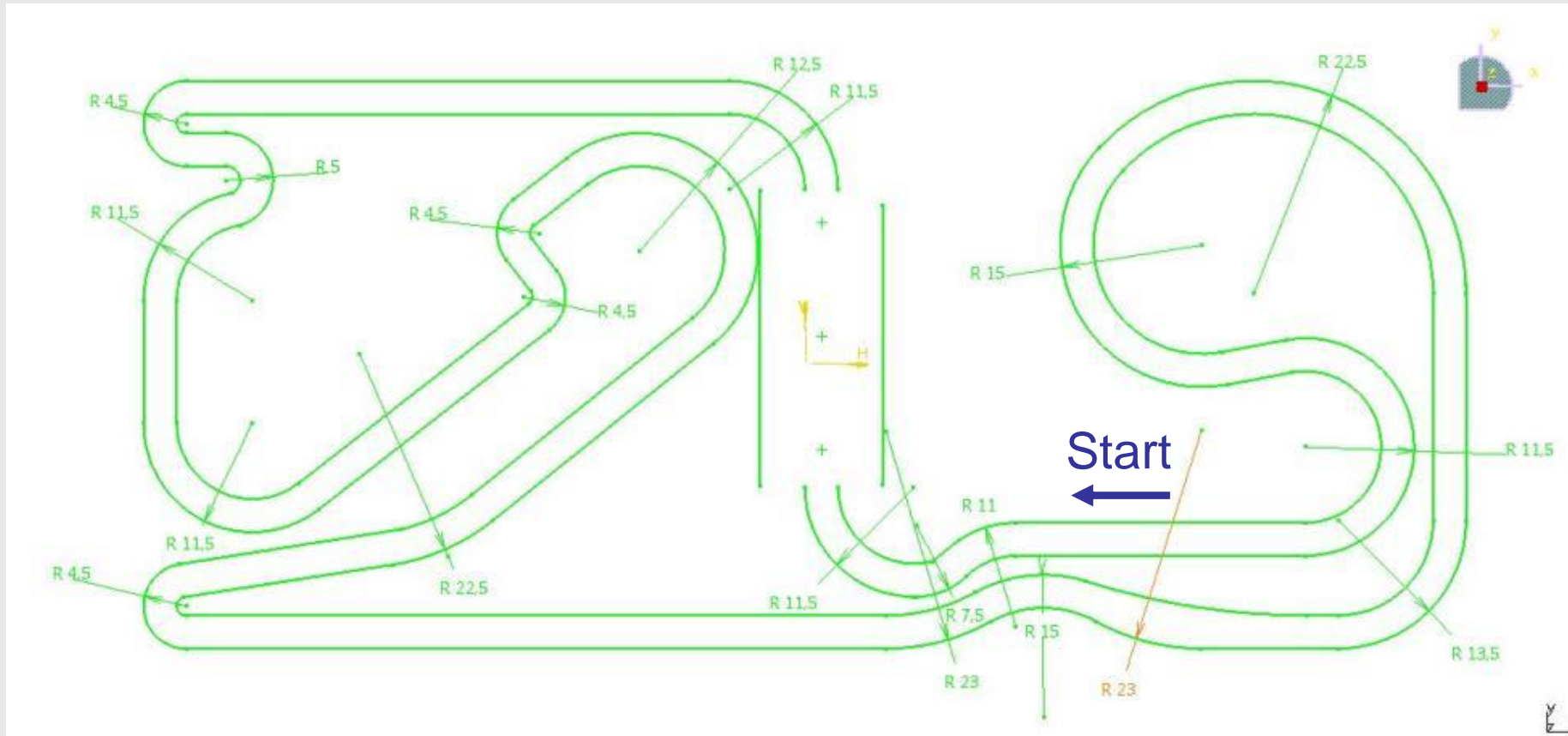
## Testing

- Unfortunately we had several problems ... only 150 km before FSG
- But, pretty amazing results!
- Setup:
  - Hoosier LC0 at 14 psi
  - Very rough, dry surface
  - 1200 Nm
  - Max. Power 55kW → Endurance Test
  - Focus: Laptimes!



### Testing

Track (length: 670m)



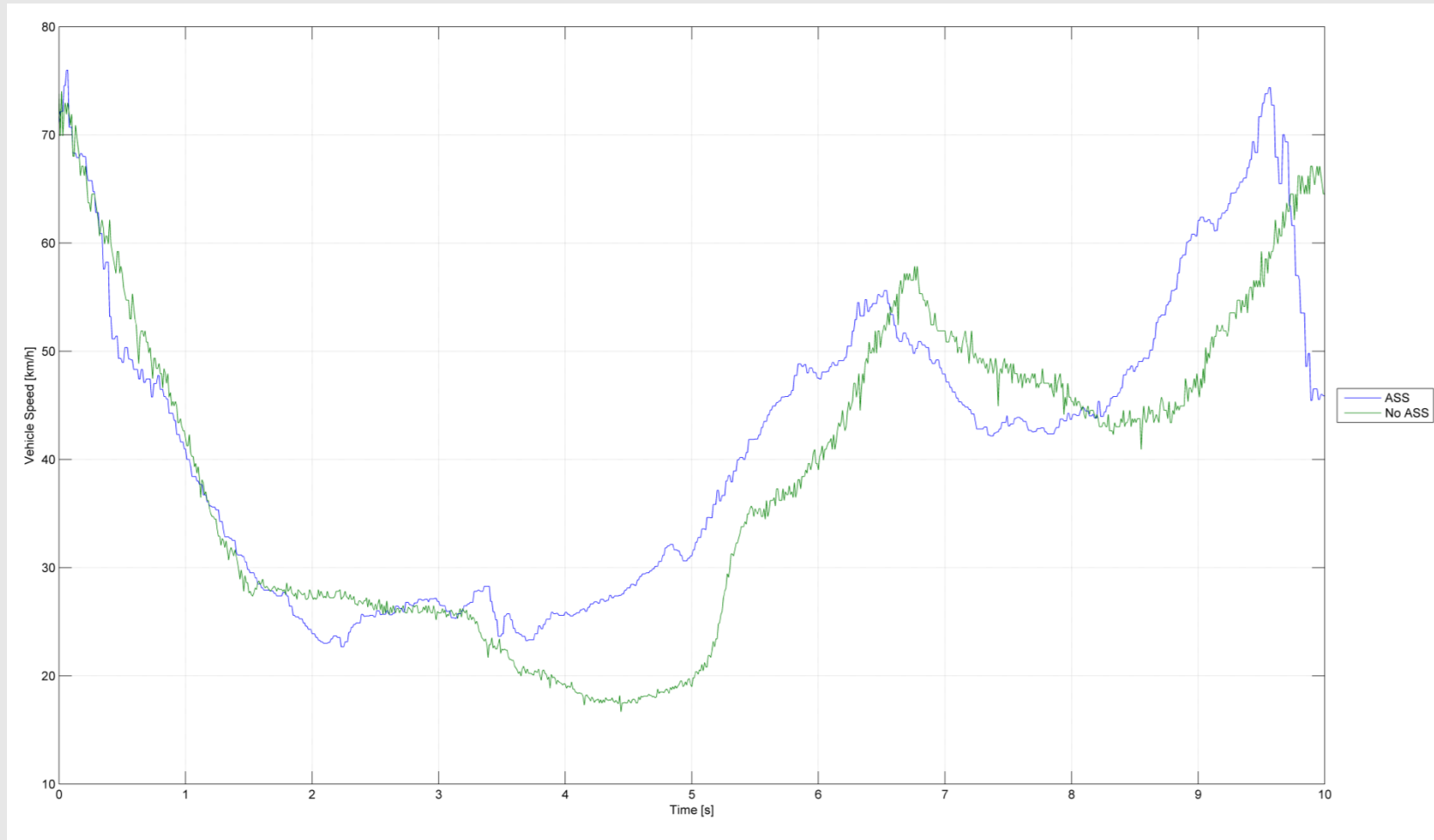


## Testing

### Overall results:

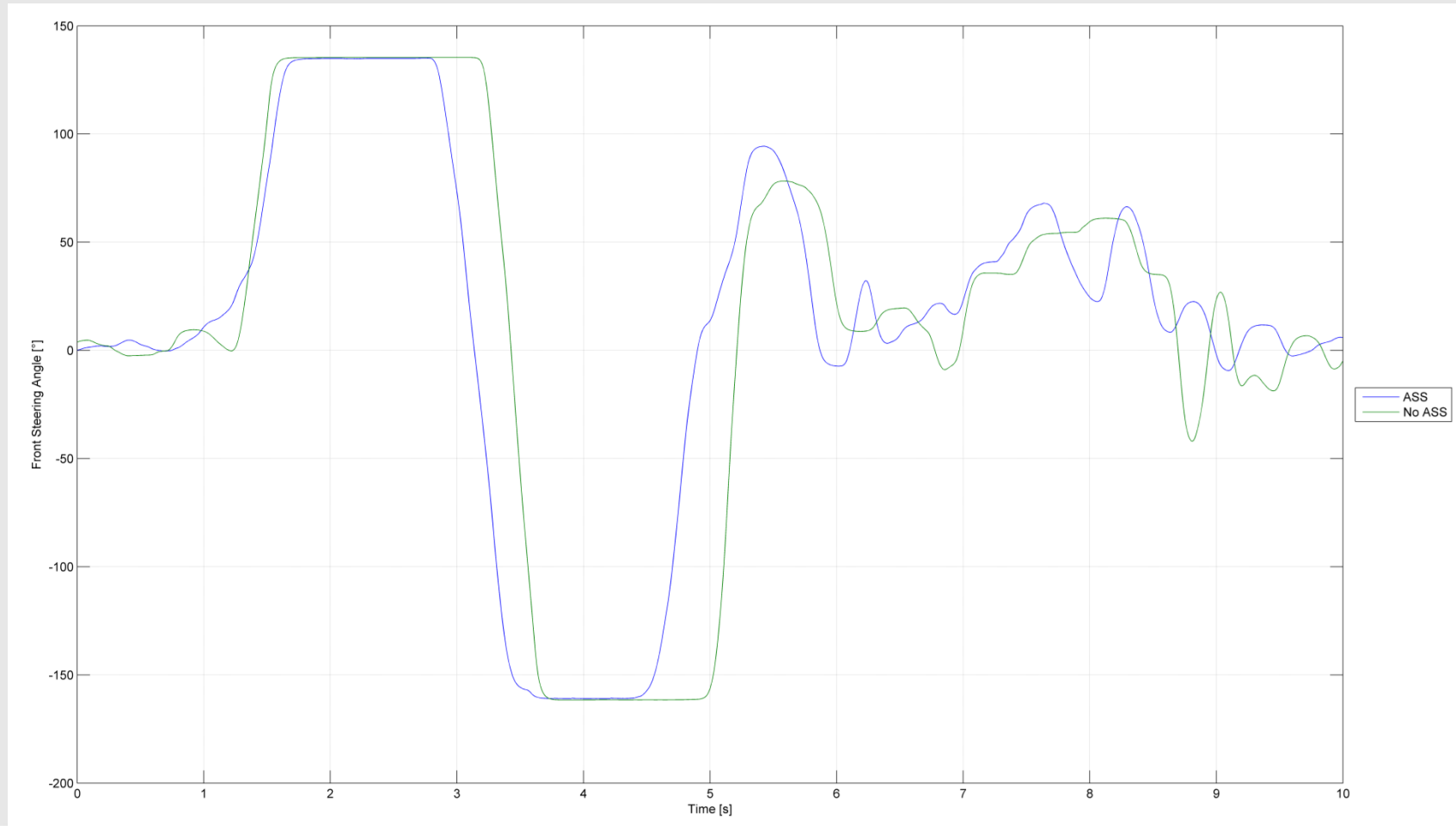
- Laptimes improved up to 1 s
  - Avg. speed using RWS:  $50.51 \frac{km}{h}$
  - Avg. speed without RWS:  $48.54 \frac{km}{h}$
- Vehicle corners recognizable faster
- Driver feedback:
  - Less steering forces
  - Handling is easier
  - Acclimatization is very necessary

### Testing

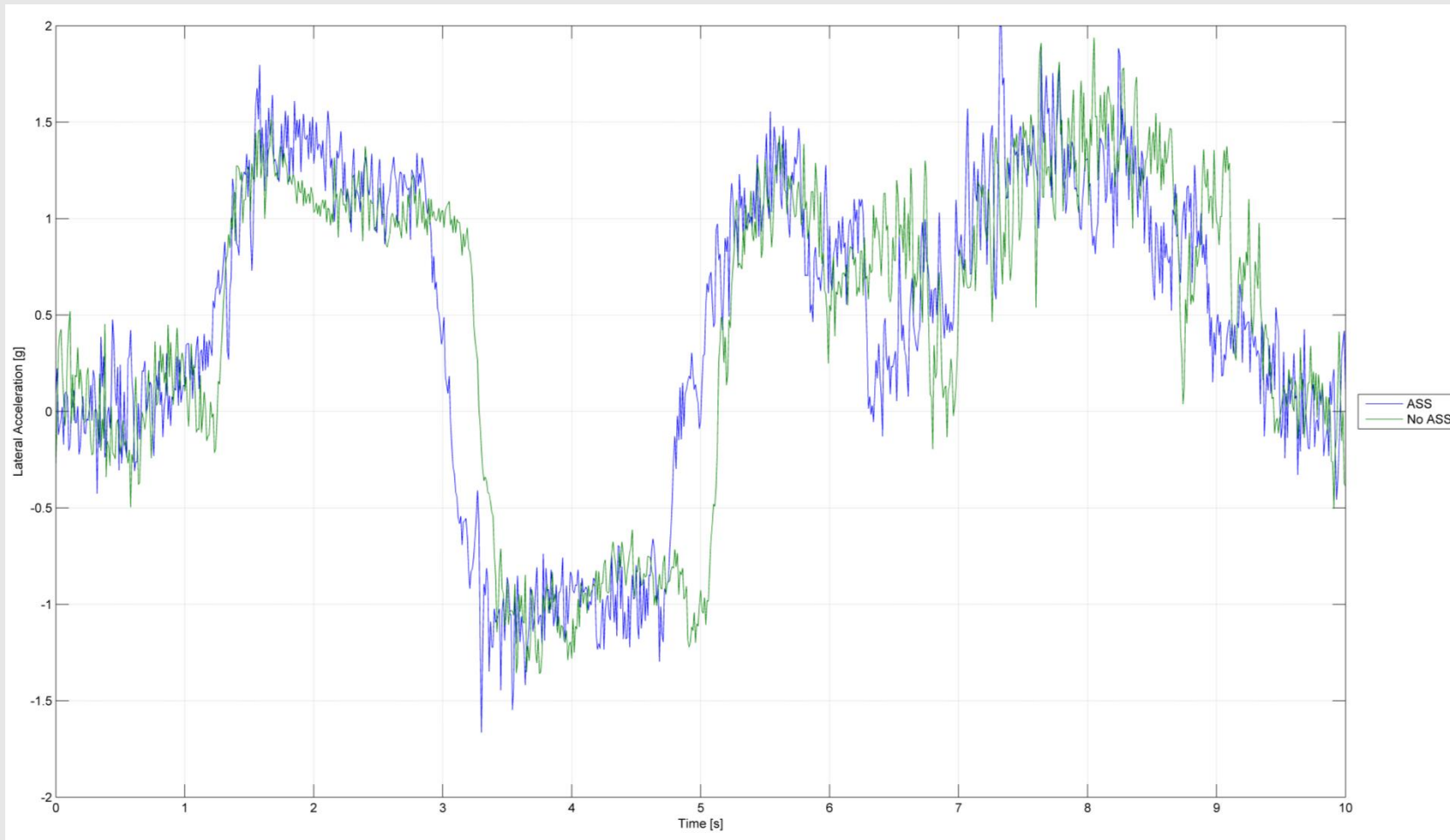




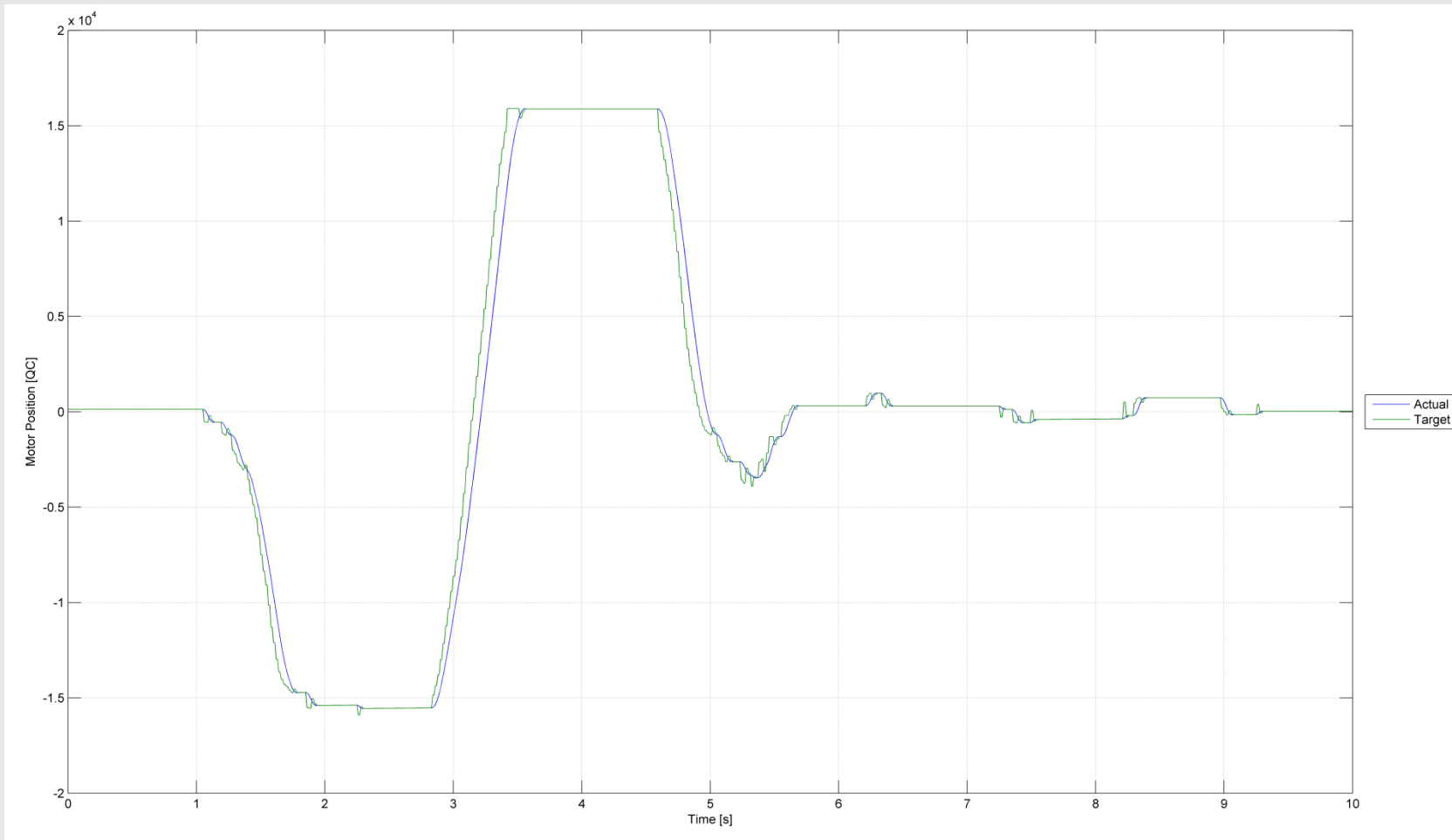
### Testing



### Testing



### Testing





## Resume

- Managed to reach all project targets!
- Increased the vehicle performance a lot and measurable
- A large amount of testing time is necessary
  - Optimize the control systems
  - Driver – car interaction
- Possible future prospects:
  - Reduce weight ;-)
  - Implement a closed loop control system
  - Compare it to 2 wheel driven torque vectoring





Thanks for your attention!

Feel free to ask Questions

