

DD2459 Software Reliability

Lecture 5

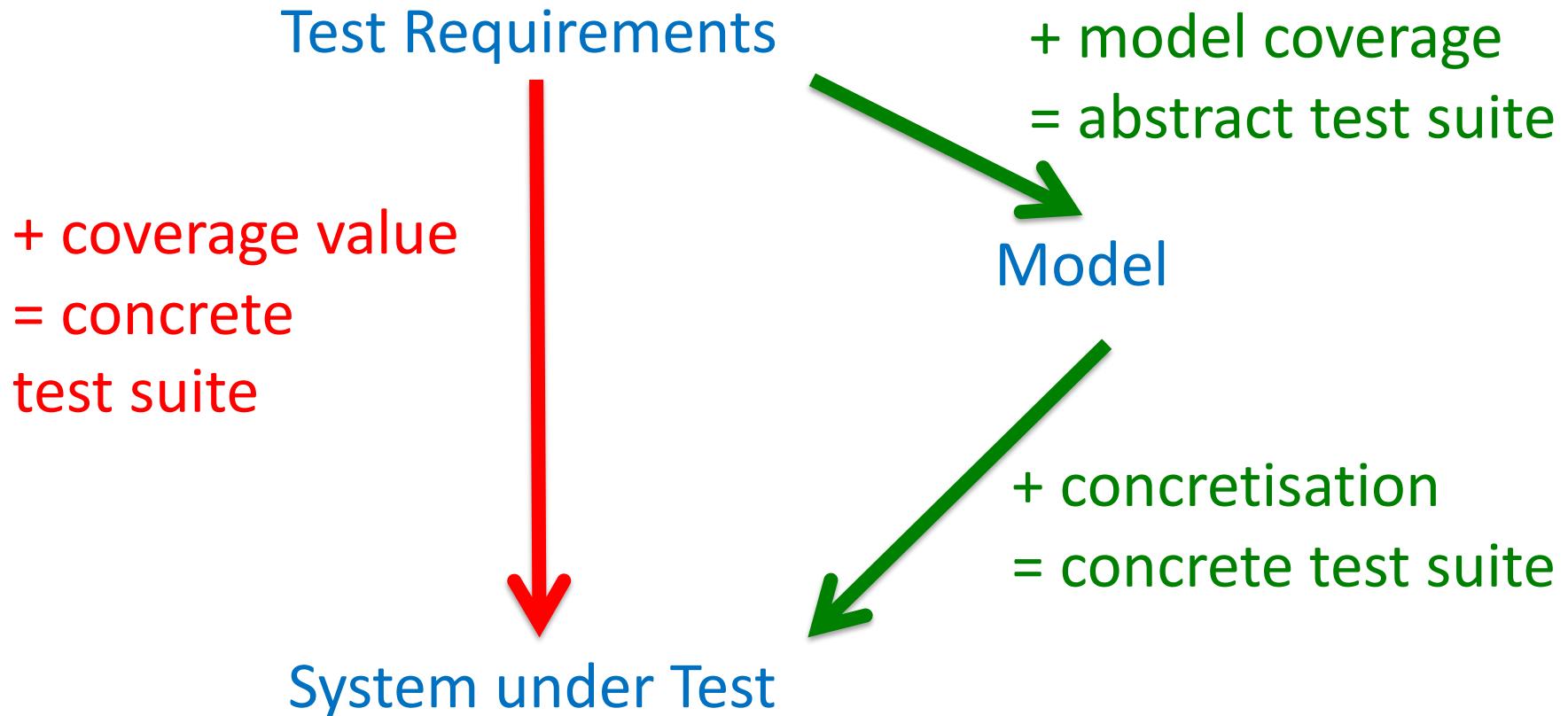
Introduction to
Model-Based Testing (MBT)

(see Amman and Offut,
Chapter 2, Section 2.5)

Part 1. Overview and Principles

What is Model-based Testing?

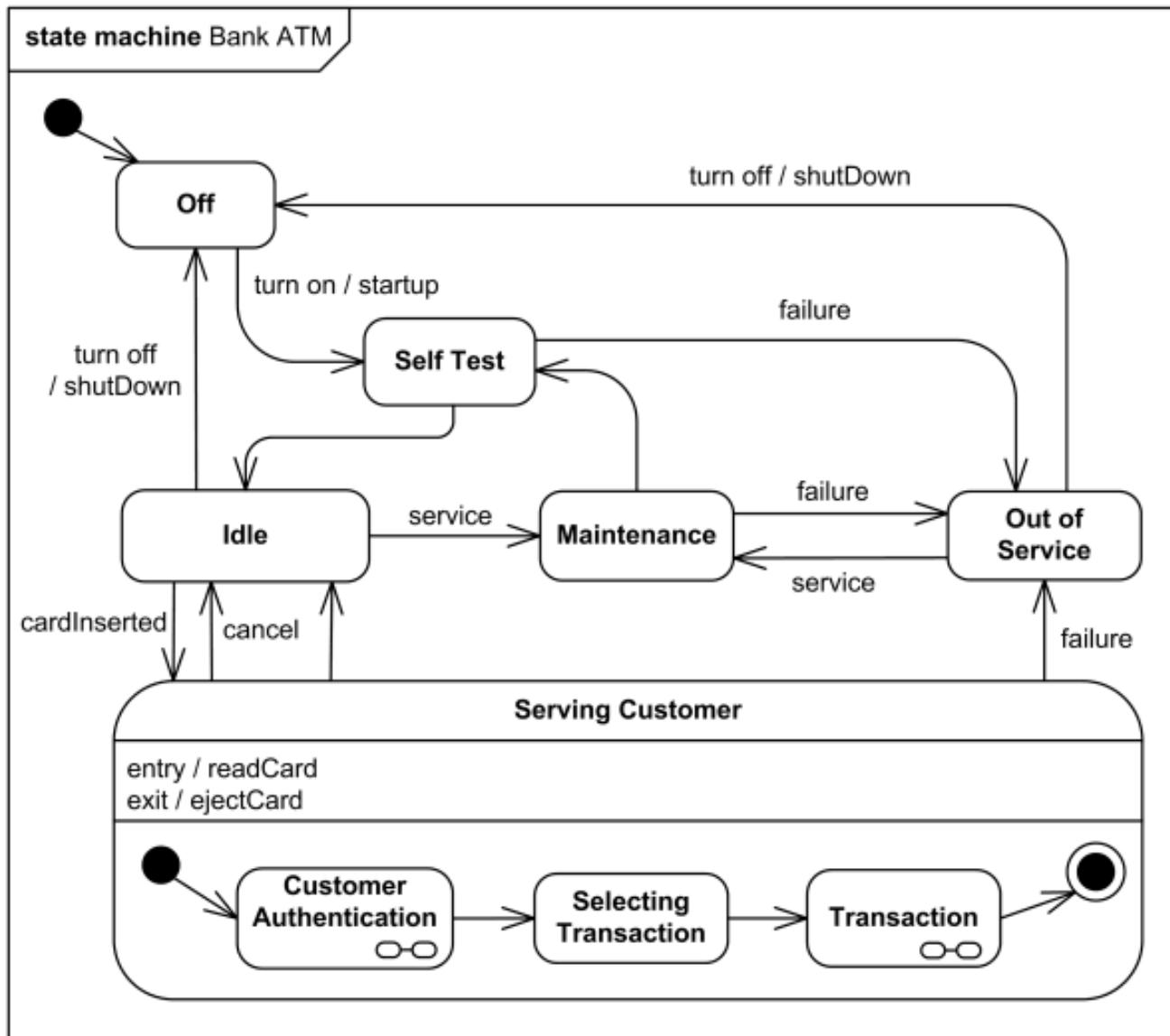
Traditional Code Testing vs. Model-based Testing



What models to use?

- To solve the oracle problem we basically need **executable *dynamic models***
 - Statecharts
 - Sequence diagrams (use cases)
 - Executable code

ATM Model



MBT Advantages

- Model need only reproduce **some features** of a system under test
- Simplification of code (**abstraction**)
- Select relevant model features! (What to test?)
- **False positives and negatives?**
- Quicker and easier to generate tests
- Use **graph coverage**
- Test generation can be automated
- Tool support (Conformiq, Spec Explorer ...)

Solving the Oracle Problem?

- Model can determine **test verdicts**
- AKA. **conformance testing** (a “golden model”)
- Verdict construction can be reduced to **equality** or **membership test**.

$$x = y \text{ or } x \in S$$

- Needs exact **synchronization** between model and code otherwise **false positives/negatives**
- Difficult with legacy code (no model) and agile development (no time).

Conformance Testing

- **Claim:** There is a sense in which conformance testing just pushes the testing problem elsewhere
- **Why?:** How do we validate the model itself?
 - Simulation?
 - Testing? (systematic simulation?)
 - Formal verification? (too big or complex?)

Model-Based Testing in practise

1. Take a **system model M** e.g. statechart
2. Take a **coverage model C**, e.g:
 - 2.1 Node coverage
 - 2.2. Edge coverage
3. Construct test cases to reach **x%** coverage of M
 - 3.1. Manually
 - 3.2. Constraint solver (**added value of a tool**)
4. **Translate** test cases into scripts, **run**, **record**, and **compare outcomes with model M**

Leading MBT Tools

We are aware of 30+ MBT tools.

Leading tools at present are:

- Simulink Design Verifier
(visual Simulink model and cause-effect graphs)
- SpecExplorer - 2013
(text ASM model and spec#)
- GraphWalker (visual)
(FSM model and A* algorithm)
- Conformiq (visual)
(UML Statecharts + glass box coverage models)

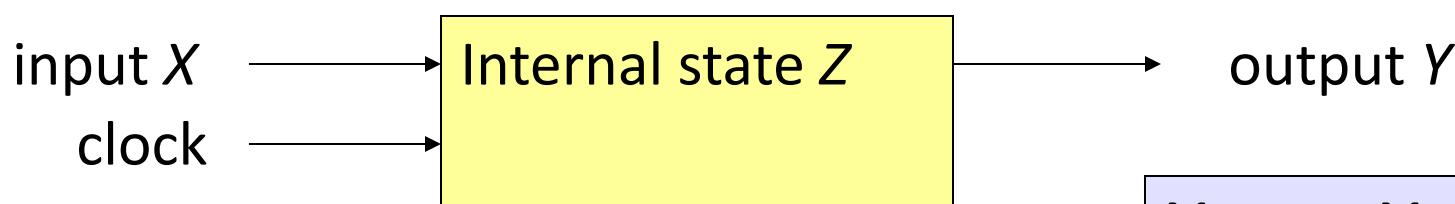
When to use MBT?

- Model-based testing can be conducted as part of model-based development
- Model-based development = describing software using accurate modeling languages e.g. UML

UML Statecharts

- A **UML statechart**, is an object-based variant of Harel's *statechart* language.
- Statecharts overcome limitations of finite state machines, without losing benefits.
- Combine aspects of **Moore** and **Mealy** machines
- New concepts:
 - Hierarchically nested states
 - Orthogonal regions
 - Extended actions
 - History

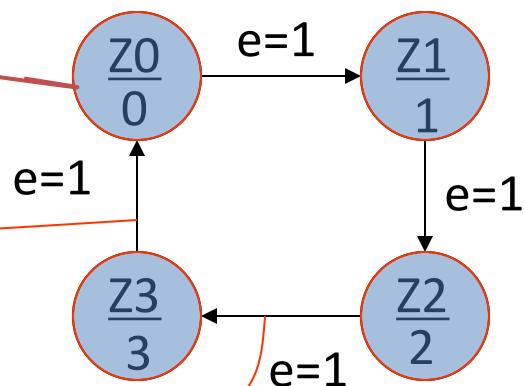
Moore and Mealy Automata



Next state Z^+ computed by function δ
Output computed by function λ

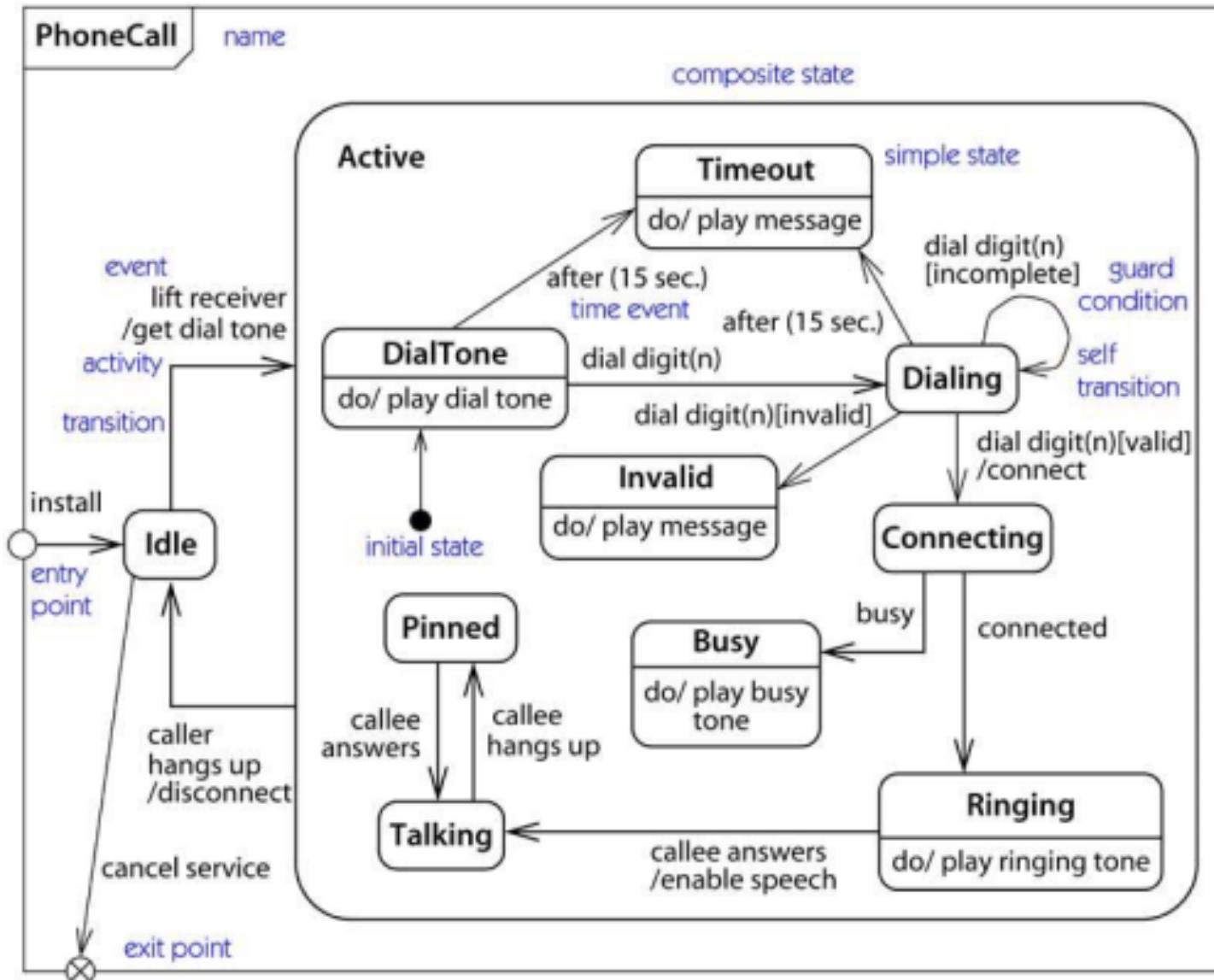
Moore- + Mealy
automata=finite state
machines (FSMs)

- Moore-automata:
 $Y = \lambda (Z); Z^+ = \delta (X, Z)$
- Mealy-automata
 $Y = \lambda (X, Z); Z^+ = \delta (X, Z)$



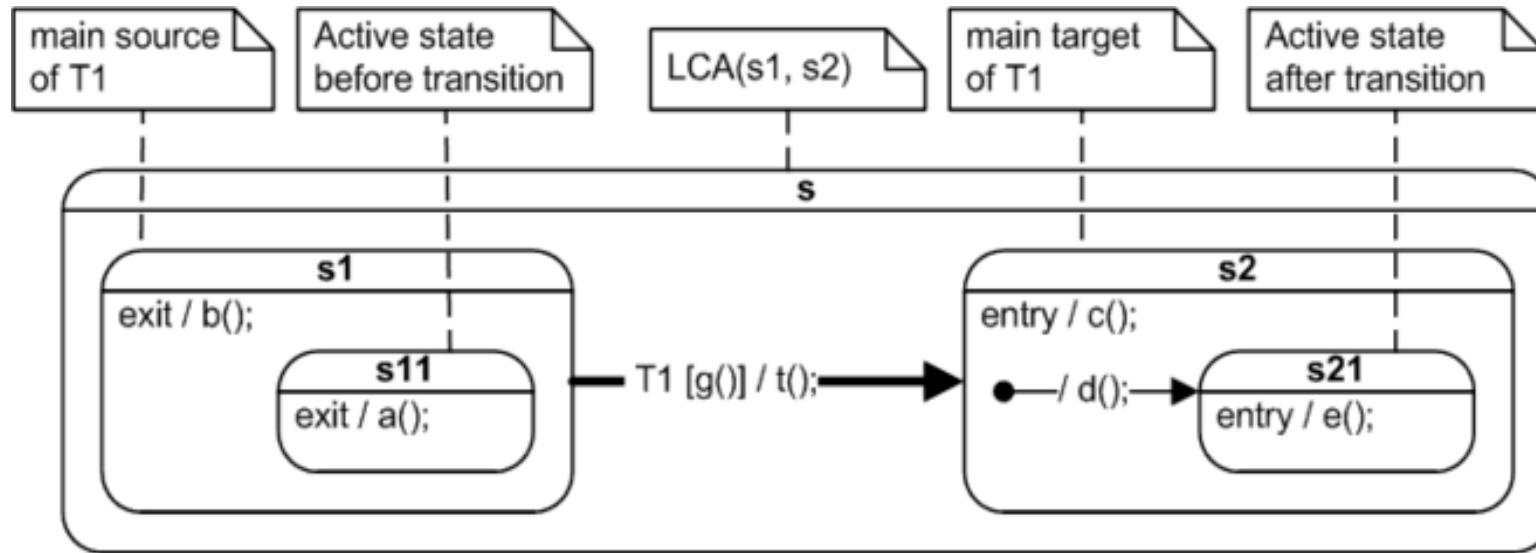
UML 2.4

- Two kinds of state machines.
- **Behavioral state machines** are used to model the behavior of individual entities (e.g., class instances)
- **Protocol state machines** are used to express usage protocols and can be used to specify the legal usage scenarios of classifiers, interfaces, and ports.
- Behavioral state machine is **subclassed** by protocol state machine.



Execution order

- UML specifies that taking a state transition executes the following **actions** in the following sequence
 1. **Evaluate the guard condition** associated with the transition and perform the following steps only if the guard evaluates to TRUE.
 2. **Exit** the source state configuration.
 3. **Execute** the actions associated with the transition.
 4. **Enter** the target state configuration.



Taking **T1** causes the evaluation of guard **g()**;
 Exit of **s11**, **s1**,
 Action sequence **a();** **b();** **t();** **c();** **d();** and **e();**
 Entry of **s2**, **s21**
 (assuming guard **g()** evaluates to **TRUE**)

MS Spec Explorer (Spec#)

Text-based *state machine models*

Class Client {

bool entered;

Map<Client,Seq<**string**>> unreceivedMsgs;

[Action] **void** Enter()

Action of abstract state machine on state entry

requires !entered; { **required condition**

 entered = true;

}

```
[Action] void Send(string message)  
    requires entered; {  
        foreach (Client c in enumof(Client), c != this,  
            c.entered)  
            c.unreceivedMsgs[this] += Seq{message};  
    }
```

A Chat room model

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Lecture 5

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Chapter 2, Section 2.5)

Part 2. MBT for ATCG

Model-based Automated Test-Case Generation (ATCG)

- Manual construction of test cases is a difficult, time-consuming and error-prone activity that requires expertise.
- Automated Test-Case Generation (TCG) has been the “holy grail” of testing for some time.
- Is this even possible? If so, how?
- Black/white-box testing
- Want algorithms which generate test cases with a known level of coverage

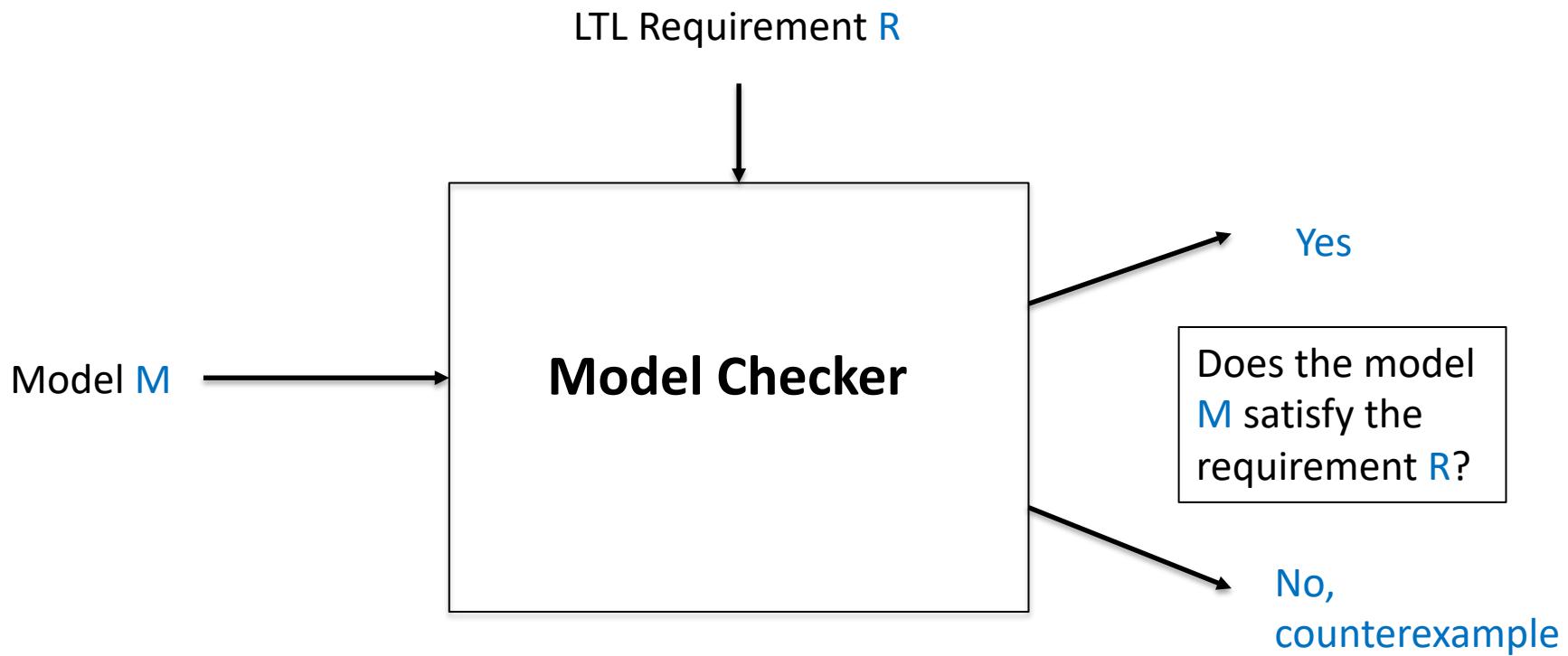
TCG Technologies

- Model-based test case generation can be done with various **technologies**:
 1. *graph search*,
 2. *constraint solving*
 3. *theorem proving*
 4. *model checking*,

We will focus on **model checking**

Model Checking

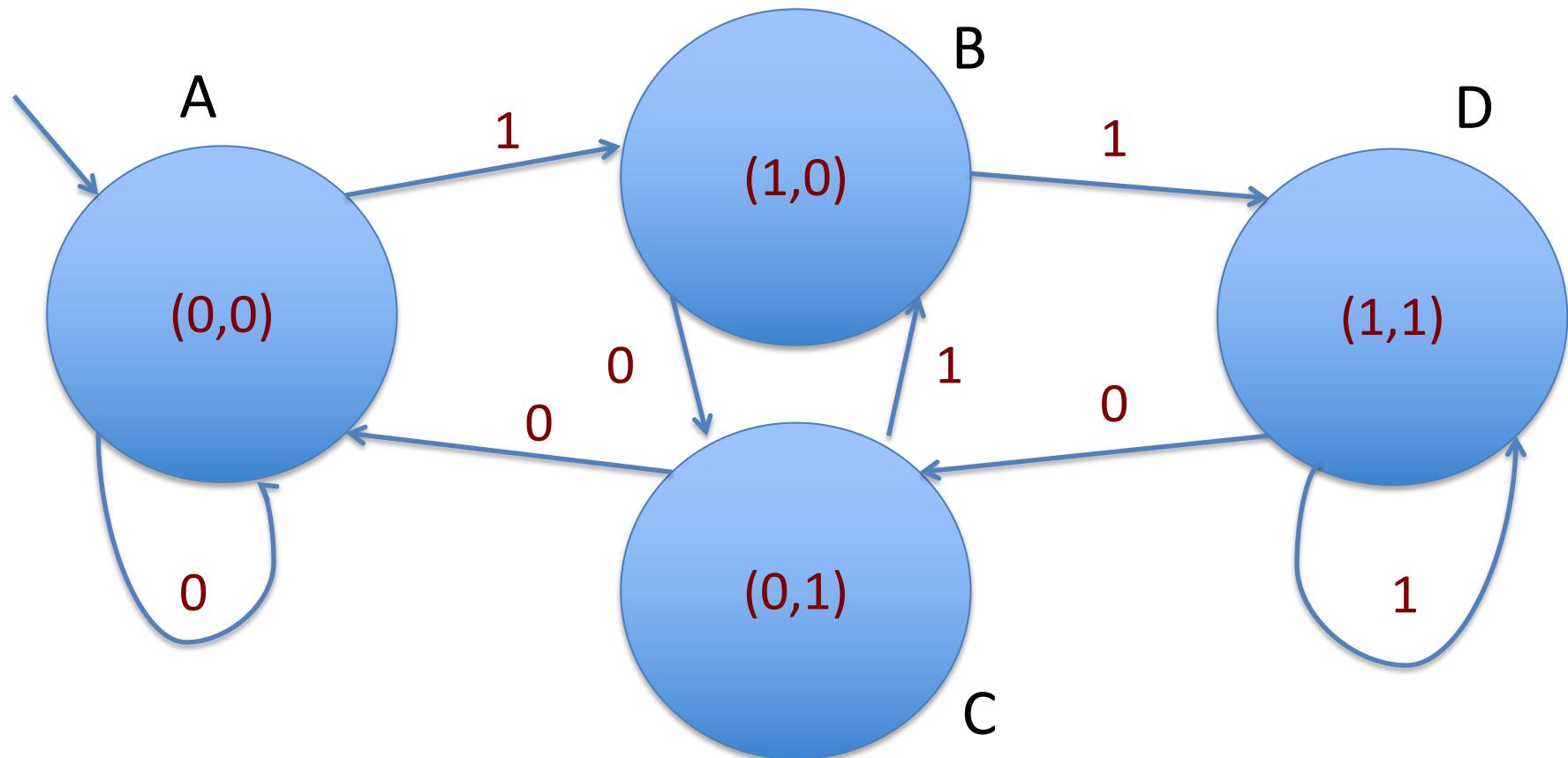
- A **model checker** is a tool which takes as input
 - An automaton model M
 - A logical formula ϕ
- If ϕ is a **true statement** about all possible behaviors of M then the model checker **confirms** it (**proof**)
- If ϕ is a **false statement** about M the model checker constructs a **counterexample** (**a simulation sequence**)
- A counterexample to ϕ satisfies $!\phi$
- A **simulation sequence** can be executed as a **test case**



Recall from Lecture 4,
A **counterexample** is a trace that satisfies $\neg R$

Example: Two Bit Shift Register as a Moore Automaton

- $Q = \{A, B, C, D\}$, $\Sigma = \{0,1\}$, $q_0=A$,
- output = (Bit1, Bit2) i.e. “shift right”



2-Bit Shift Reg in NuSMV using .smv format

```
MODULE main
VAR
-- system outputs
  Bit1 : boolean; -- Boolean variable
  Bit2 : boolean;
  state : {A, B, C, D}; -- scalar variable

IVAR
-- system inputs
  input : boolean;

ASSIGN
  init(state) := A;
  init(Bit1) := 0;
  init(Bit2) := 0;
```

```
next(state) := case
    state = A & input = 1 : B;
    state = B & input = 0 : C;
    state = B & input = 1 : D;
    state = C & input = 0 : A;
    state = C & input = 1 : B;
    state = D & input = 0 : C;
    TRUE : state;
esac;

next(Bit1) := case lab 3 esac;
next(Bit2) := case lab 3 esac;
```

Linear Temporal Logic LTL

in .smv format

- Use temporal logic to express automaton requirements
- Boolean variables
 - A, B, ..., X, Y, ... MyVar, etc.
- Boolean operators
 - $!(\phi)$, $(\phi \ \& \ \theta)$, $(\phi \mid \theta)$, $(\phi \rightarrow \theta)$,...
- Temporal (time) operators
 - $F(\phi)$ (sometime in the future ϕ)
 - $G(\phi)$ (always in the future ϕ)
 - $(\phi \ U \ \theta)$ (ϕ holds until θ holds)
 - $X(\phi)$ (next ϕ holds)
 - Write $X^n(\phi)$ for $X(X(\dots X(\phi) \dots))$ (ϕ holds in n steps)

Examples of LTL

Right now it is Wednesday

Wednesday

Tomorrow is Wednesday

X (Wednesday)

(A) Thursday (always) immediately follows Wednesday

G(Wednesday -> X (Thursday))

(A) Saturday (always) follows Wednesday

G(Wednesday -> F(Saturday))

Yesterday was Wednesday

G(Wednesday <-> X (Thursday)) & Thursday

- Exercise: define the sequence of days precisely, i.e. just one solution
- Question: are there any English statements you can't make in LTL?
- Question: what use cases can you express in LTL?

Basic Identities

It makes sense to say that

$$G(\varphi) = \varphi \quad \& \quad X(\varphi) \quad \& \quad X(X(\varphi)) \quad \& \quad \dots$$

or

$$G(\varphi) = \bigwedge_{i \geq 0} X^i(\varphi)$$

Also

$$F(\varphi) = \varphi \quad | \quad X(\varphi) \quad | \quad X(X(\varphi)) \quad \dots$$

$$F(\varphi) = \bigvee_{i \geq 0} X^i(\varphi)$$

Useful Logical Identities for LTL

- Boolean identities

$$\begin{aligned} ! (! (\phi)) &\Leftrightarrow \phi, & ! (\phi \mid \phi) &\Leftrightarrow (!\phi \ \& \ !\phi) , \\ (\phi \rightarrow \phi) &\Leftrightarrow (! (\phi) \mid \phi) \text{ etc.} \end{aligned}$$

- LTL identities

$$\begin{aligned} ! (G (! (\phi))) &\Leftrightarrow F (\phi) \\ ! (X (\phi)) &\Leftrightarrow X (! (\phi)) \\ G (\phi \ \& \ \phi) &\Leftrightarrow G (\phi) \& G (\phi) \\ G (\phi) &\Leftrightarrow \phi \ \& \ X (G (\phi)) \\ G (G (\phi)) &\Leftrightarrow G (\phi) \end{aligned}$$

- Exercise: using these identities, prove:

$$\begin{aligned} ! (F (! (\phi))) &\Leftrightarrow G (\phi) \\ F (\phi \mid \phi) &\Leftrightarrow F (\phi) \mid F (\phi) \\ F (\phi) &\Leftrightarrow \phi \mid X (F (\phi)) \end{aligned}$$

- Remark TCG usually involves **negating formulas**, so its useful to understand what a negation means

LTL Specifications

.smv format

LTLSPEC

```
G( Bit1 <-> (X Bit2) )  
-- always the value of Bit1 now equals the  
-- value of Bit2 in the next time step  
-- This is obviously TRUE!
```

```
G( Bit1 <-> (X Bit1) )  
-- always the value of Bit1 now equals the  
-- value of Bit1 in the next time step  
-- This is obviously FALSE!
```

NuSMV Output Example

```
-- specification G( Bit1 <-> (X Bit2) )
-- is true
-- specification G( Bit1 <-> (X Bit1) )
-- is false
-- as demonstrated by the following execution
sequence
Trace Description: LTL Counterexample
Trace Type: Counterexample
-> State: 1.1 <-
state = A Bit1 = false Bit2 = false
-> Input: 1.2 <-
input = 1
-> State 1.2 <-
state = B Bit1 = true Bit2 = false
```

Automated Glass-box TCG

- We can use a model checker to generate counterexamples to formulas (i.e. test cases) with specific structural properties.
- This is done by inspecting the graph structure of the automaton
- i.e. white/glass box testing
- “Most” use of model checkers concerns this.

Test Requirements

Trap Properties

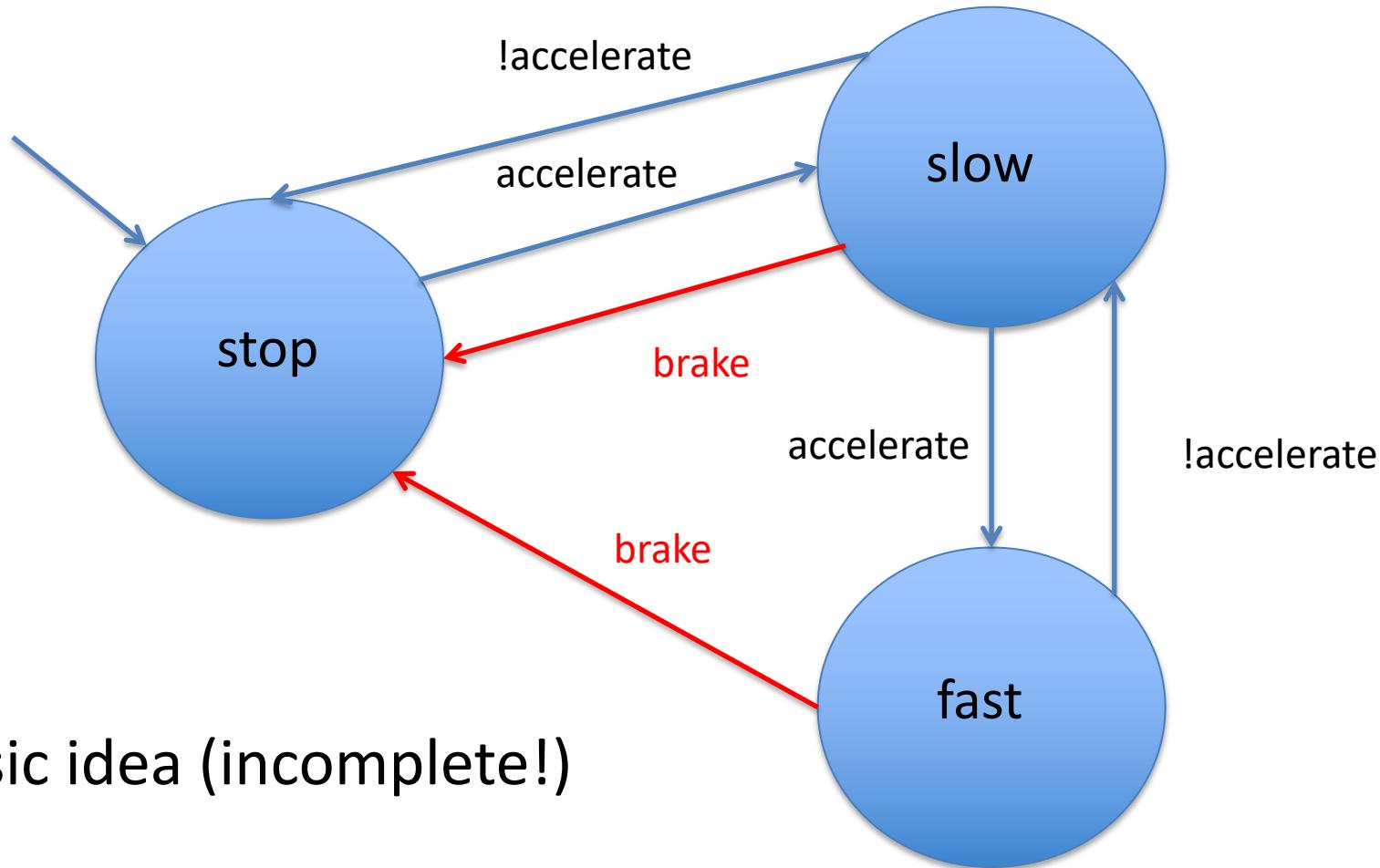
- Recall a test requirement is a *requirement that can be satisfied by one or more test cases*
- Basic idea is to capture each test requirement as an LTL formula known as a “**trap property**”

Example Suppose the test requirement is “*cover state D of shift register*”

Trap property is $G(\neg(state = D))$

This formula is **False** and any counterexample must be a path that goes through state **D**.

Case Study: Car Controller Model (CC)



Basic idea (incomplete!)

```
MODULE main
VAR
  state: {stop, slow, fast};
  -- velocity states

IVAR
  accelerate: boolean; -- gas pedal
  brake: boolean; -- brake pedal

ASSIGN
  Init(state) := stop;

  Next(state) := case
    accelerate & !brake & state = stop : slow;
    accelerate & !brake & state = slow : fast;
    !accelerate & !brake & state = fast : slow;
    !accelerate & !brake & state = slow: stop;
    brake: stop;
    TRUE: state;
  esac;
```

Trap properties for Structural Coverage Models

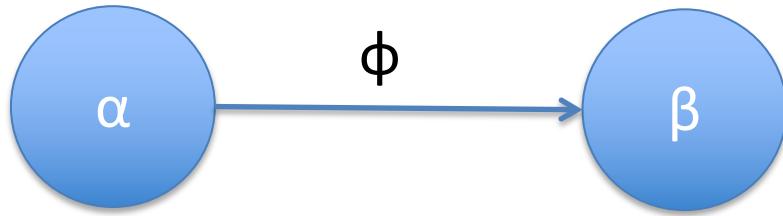
- Let's use NuSMV to automatically construct test suites that satisfy the different **glass box coverage models** introduced in Lecture 2.
- Examples:
 - Node coverage NC
 - Edge coverage EC
 - Condition coverage PC
- How to interpret these concepts?

Node Coverage for CC

- Want a path that visits each node
- Simple approach: write 1 trap property per node
- General form:
- $G(\neg(state = \langle state_name \rangle))$
- Counterexamples satisfy:
- $F(state = \langle state_name \rangle)$
- Example:
$$G(\neg(state = stop));$$
- Clearly this will give redundant test cases, but method is still linear in state-space size.
- Lab Exercise 3: define the remaining 2 trap formulas for car controller

Edge coverage for CC

- Want to traverse each edge between any pair of nodes



- General form $G(\text{state} = \alpha \ \& \ \phi) \rightarrow X(\text{!}(\text{state} = \beta))$
- Counterexample satisfies $F(\text{state} = \alpha \ \& \ \phi \ \& \ X(\text{state} = \beta))$
- Example:
$$G(\text{state} = \text{stop} \ \& \ \text{accelerate} \rightarrow X(\text{!}(\text{state} = \text{slow})))$$
- Lab Exercise 3: define the remaining 5 trap formulas for car controller

Requirements-based TCG

- Can we also perform requirements-based test case generation?
- Want to test the requirements are fulfilled rather than explore structure of the code.
- Can look at **negation of a requirement**

Car Controller

LTL requirements

1. Whenever the brake is activated, car has to stop quickly

$G(\text{brake} \rightarrow X(\text{state}=\text{stop}))$

2. When accelerating and not braking, velocity has to increase gradually

$G(\neg \text{brake} \ \& \ \text{accelerate} \ \& \ \text{state}=\text{stop} \rightarrow X(\text{state}=\text{slow}))$

$G(\neg \text{brake} \ \& \ \text{accelerate} \ \& \ \text{state}=\text{slow} \rightarrow X(\text{state}=\text{fast}))$

3. When not accelerating and not braking, velocity has to decrease gradually

$G(\neg \text{brake} \ \& \ \neg \text{accelerate} \ \& \ \text{state}=\text{fast} \rightarrow X(\text{state}=\text{slow}))$

$G(\neg \text{brake} \ \& \ \text{accelerate} \ \& \ \text{state}=\text{slow} \rightarrow X(\text{state}=\text{stop}))$

Safety Requirements

- A **safety requirement** describes a behavior that may not occur on any path.
- “*Something bad never happens*”
- To verify, all execution paths must be checked exhaustively
- Safety properties usually have the form $G !\phi$ where ϕ defines the “*bad thing*”
- Counterexamples (**test cases**) are finite

Liveness Requirements

- A **liveness requirement** describes a behavior that must hold on all execution paths
- “Something good eventually happens”
- Safety does not imply liveness
- Liveness does not imply safety
- Liveness properties often have the form
 $F(\theta)$ or $G(\phi \rightarrow x^n \theta)$ or $G(\phi \rightarrow F\theta)$
where θ describes the “good” thing and ϕ is some **precondition** needed for it to occur.
- Counterexamples may be **finite** or **infinite** (why?)

TCG for Model-Based Requirements Testing

- Suppose we have an LTL requirement ϕ
- Feed into NuSMV an FSM model A of the SUT, together with the **negated formula** $!\phi$
- Choose any counterexample (a behaviour b) (there should be lots if A is a correct model and ϕ is a correct requirement).
- b satisfies $!! \phi$ i.e. b is an example of **correct behavior**
- Feed the **inputs** of b into the SUT and observe the output
- If output from the SUT matches b then **pass** else **fail**

Car Controller Examples

- (1) $F(\text{brake} \And \text{X } !(\text{velocity}=\text{stop}))$
- (2) $F(\text{!brake} \And \text{accelerate} \And \text{velocity}=\text{stop} \rightarrow \text{X}(\text{velocity}=\text{slow}))$

Concluding Remarks

- Model-based testing has created a lot of interest and opened up new questions
- Tools market is emerging
- What is best modeling language?
- Automated TCG is possible using off-the-shelf tools, e.g. model checkers
- New technologies such as machine learning avoid manual model construction.

Lecture 5 Summary

- MBT uses a model of code for test construction
- Model can be text or graphics
- Graph coverage can be re-used for model coverage
- Models help solve oracle problem (conformance testing)
- Tools allow automated test generation as path traversal in a model.
- ATCG based on *model checking, graph search, constraint solving or theorem proving*