

DD2459 Software Reliability

Lecture 5

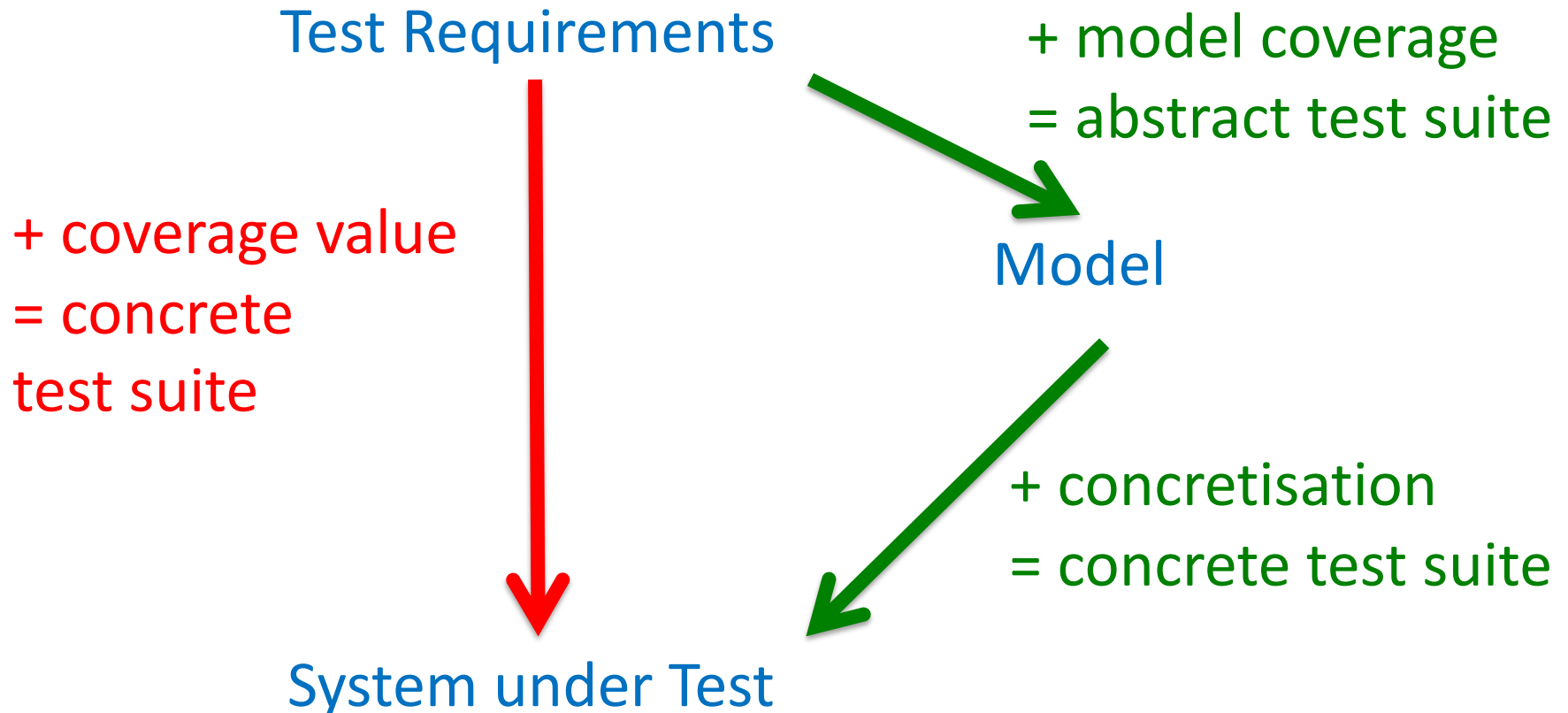
Introduction to Model-Based Testing (MBT)

(see Amman and Offut,
Chapter 2, Section 2.5)

Part 1. Overview and Principles

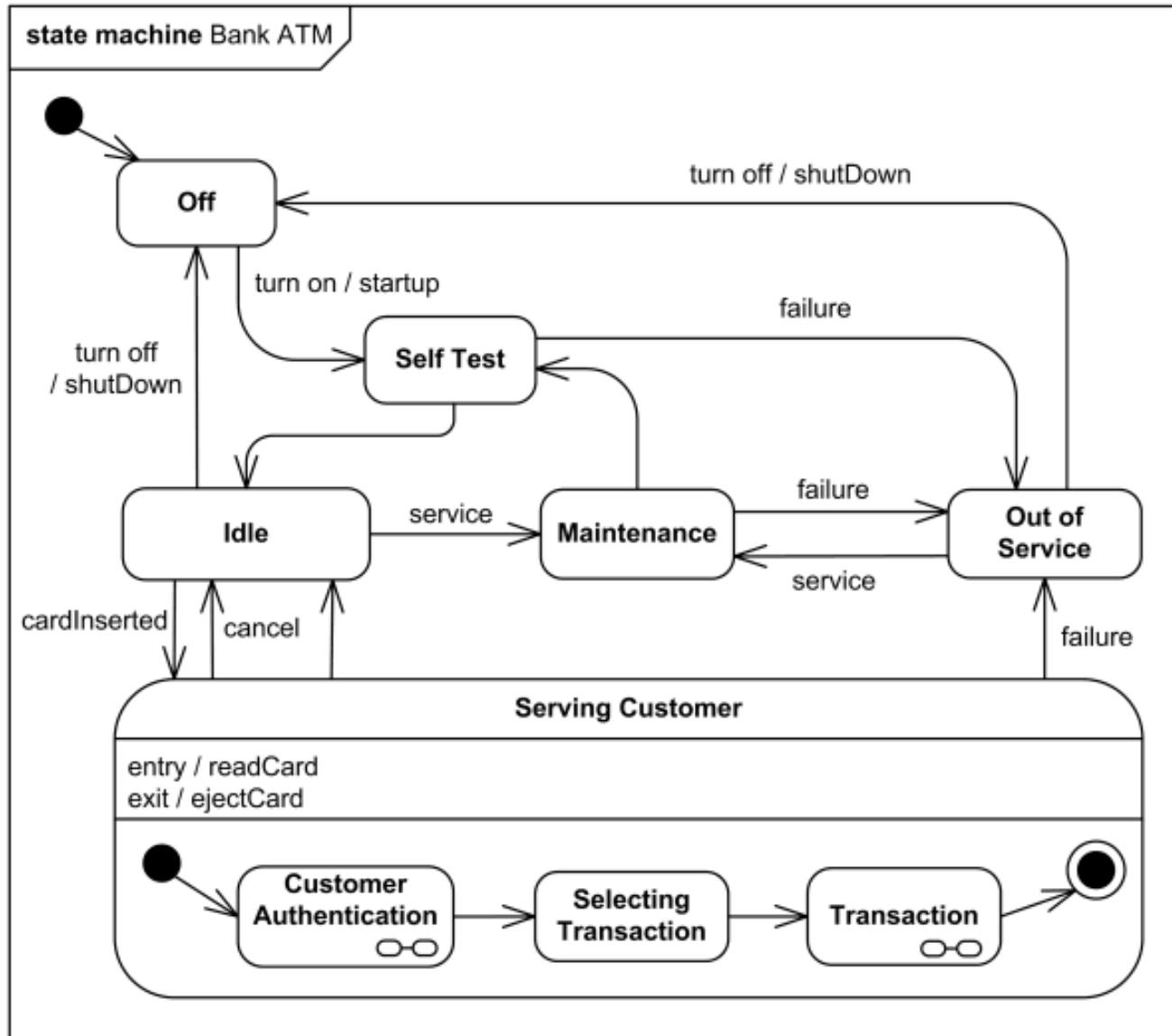
What is Model-based Testing?

Traditional Code Testing vs. Model-based Testing



What models to use?

- To solve the oracle problem we basically need *executable dynamic models*
 - Statecharts
 - Sequence diagrams (use cases)
 - Executable code



ATM Model

MBT Advantages

- Model need only reproduce **some features** of a system under test
- Simplification of code (**abstraction**)
- Select relevant model features! (What to test?)
- **False positives and negatives?**
- Quicker and easier to generate tests
- Use **graph coverage**
- Test generation can be automated
- Tool support (Conformiq, Spec Explorer ...)

Solving the Oracle Problem?

- Model can determine test verdicts
- AKA. conformance testing (a “golden model”)
- Verdict construction can be reduced to equality or membership test.

$$x = y \text{ or } x \in S$$

- Needs exact synchronization between model and code otherwise false positives/negatives
- Difficult with legacy code (no model) and agile development (no time).

Conformance Testing

- **Claim:** There is a sense in which conformance testing just pushes the testing problem elsewhere
- **Why?:** How do we validate the model itself?
 - Simulation?
 - Testing? (systematic simulation?)
 - Formal verification? (too big or complex?)

Model-Based Testing

in practise

1. Take a **system model M** e.g. statechart
2. Take a **coverage model C**, e.g:
 - 2.1 Node coverage
 - 2.2. Edge coverage
3. Construct test cases to reach **x%** coverage of **M**
 - 3.1. Manually
 - 3.2. Constraint solver (**added value of a tool**)
4. **Translate** test cases into scripts, **run, record**, and **compare outcomes with model M**

Leading MBT Tools

We are aware of 30+ MBT tools.

Leading tools at present are:

- Simulink Design Verifier
(visual Simulink model and cause-effect graphs)
- SpecExplorer - 2013
(text ASM model and spec#)
- GraphWalker (visual)
(FSM model and A* algorithm)
- Conformiq (visual)
(UML Statecharts + glass box coverage models)

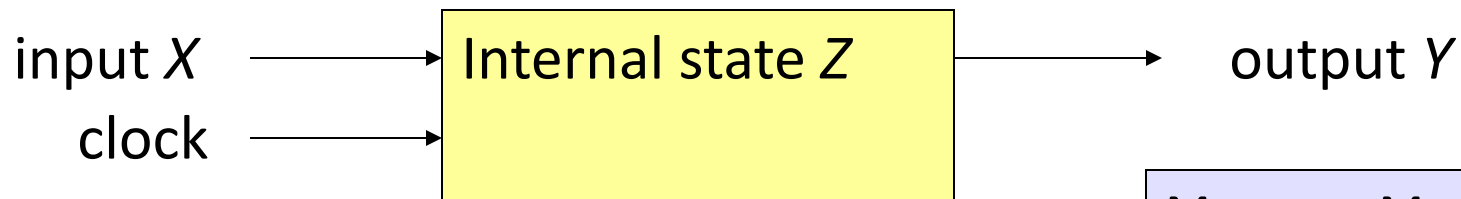
When to use MBT?

- Model-based testing can be conducted as part of model-based development
- Model-based development = describing software using accurate modeling languages e.g. UML

UML Statecharts

- A **UML statechart**, is an object-based variant of Harel's *statechart* language.
- Statecharts overcome limitations of finite state machines, without losing benefits.
- Combine aspects of **Moore** and **Mealy machines**
- New concepts:
 - Hierarchically nested states
 - Orthogonal regions
 - Extended actions
 - History

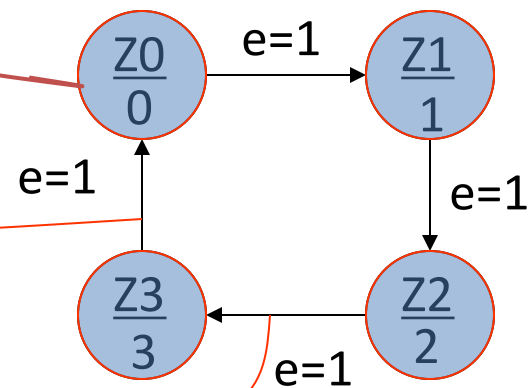
Moore and Mealy Automata



Next state Z^+ computed by function δ
Output computed by function λ

Moore- + Mealy
automata=finite state
machines (FSMs)

- Moore-automata:
 $Y = \lambda(Z); \quad Z^+ = \delta(X, Z)$
- Mealy-automata
 $Y = \lambda(\textcolor{red}{X}, Z); \quad Z^+ = \delta(X, Z)$

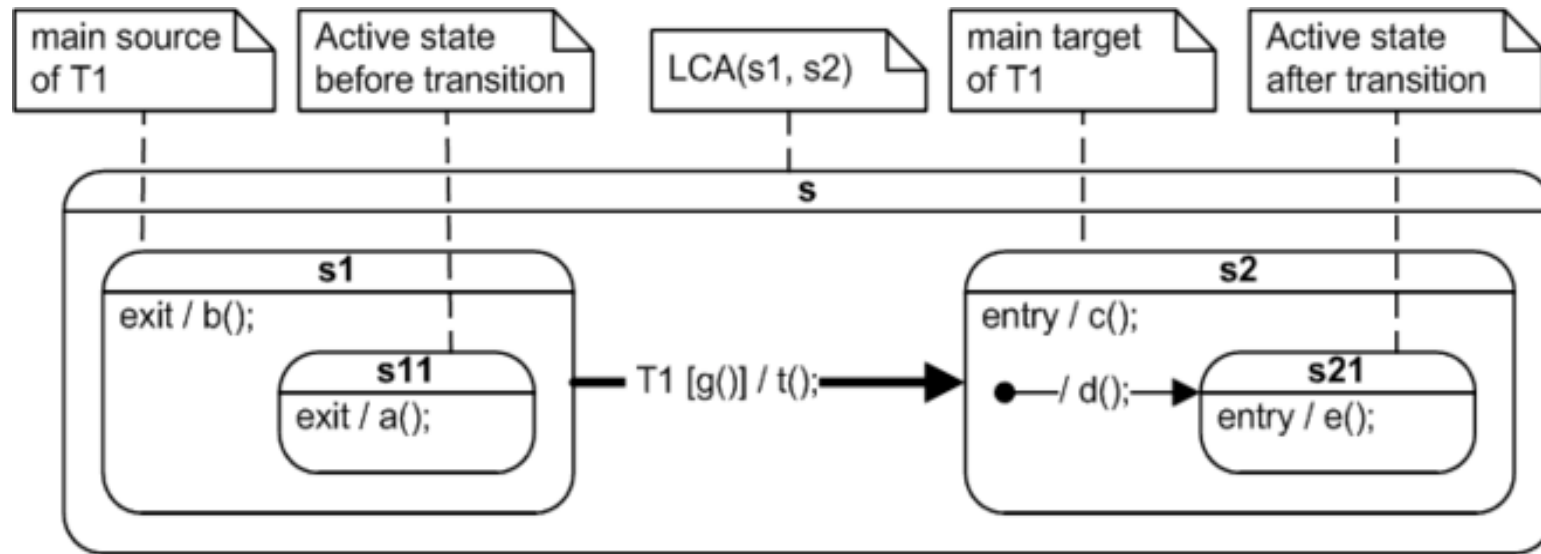


UML 2.4

- Two kinds of state machines.
- **Behavioral state machines** are used to model the behavior of individual entities (e.g., class instances)
- **Protocol state machines** are used to express usage protocols and can be used to specify the legal usage scenarios of classifiers, interfaces, and ports.
- Behavioral state machine is **subclassed** by protocol state machine.

Execution order

- UML specifies that taking a state transition executes the following **actions** in the following **sequence**
 1. **Evaluate the guard condition** associated with the transition and perform the following steps only if the guard evaluates to TRUE.
 2. **Exit** the source state configuration.
 3. **Execute** the actions associated with the transition.
 4. **Enter** the target state configuration.



Taking $T1$ causes the evaluation of guard $g()$;
 Exit of $s11, s1$,
 Action sequence $a(); b(); t(); c(); d();$ and $e();$
 Entry of $s2, s21$
 (assuming guard $g()$ evaluates to $TRUE$)

MS Spec Explorer (Spec#)

Text-based *state machine models*

Class Client {

bool entered;

 Map<Client,Seq<**string**>> unreceivedMsgs;

 [Action] **void** Enter()

 Action of abstract state machine on state entry

requires !entered; { required condition

 entered = true;

 }

```
[Action] void Send(string message)
    requires entered; {
    foreach (Client c in enumof(Client), c != this,
    c.entered)
        c.unreceivedMsgs[this] += Seq{message};
    }
```

A Chat room model

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Lecture 5

Introduction to Model-Based Testing (MBT)

(see Amman and Offut,
Chapter 2, Section 2.5)

Part 2. MBT for ATCG

Model-based Automated Test-Case Generation (ATCG)

- Manual construction of test cases is a difficult, time-consuming and error-prone activity that requires expertise.
- Automated Test-Case Generation (TCG) has been the “holy grail” of testing for some time.
- Is this even possible? If so, how?
- Black/white-box testing
- Want algorithms which generate test cases with a known level of coverage

TCG Technologies

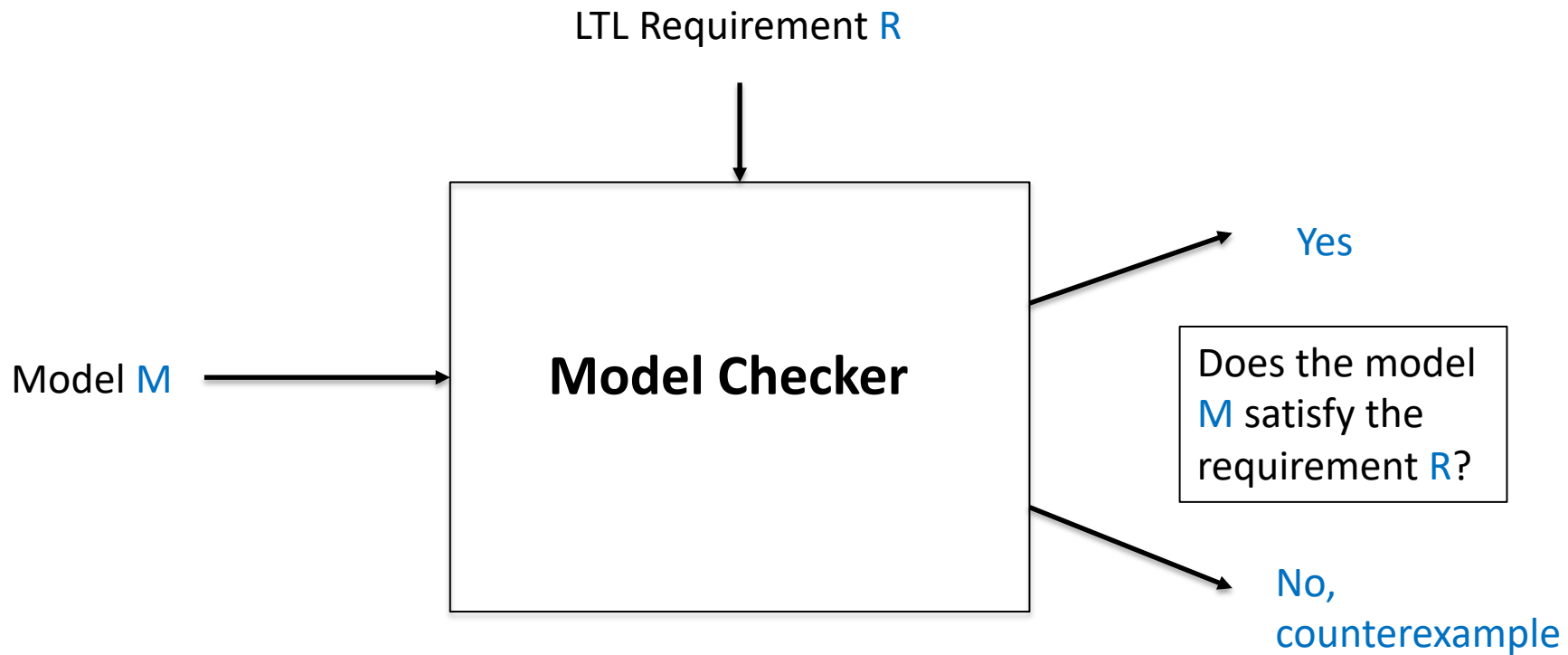
- Model-based test case generation can be done with various **technologies**:

1. *graph search,*
2. *constraint solving*
3. *theorem proving*
4. *model checking,*

We will focus on **model checking**

Model Checking

- A **model checker** is a tool which takes as input
 - An automaton model M
 - A logical formula ϕ
- If ϕ is a **true statement** about all possible behaviors of M then the model checker **confirms** it (**proof**)
- If ϕ is a **false statement** about M the model checker constructs a **counterexample** (a **simulation sequence**)
- A counterexample to ϕ satisfies $\neg\phi$
- A **simulation sequence** can be executed as a **test case**

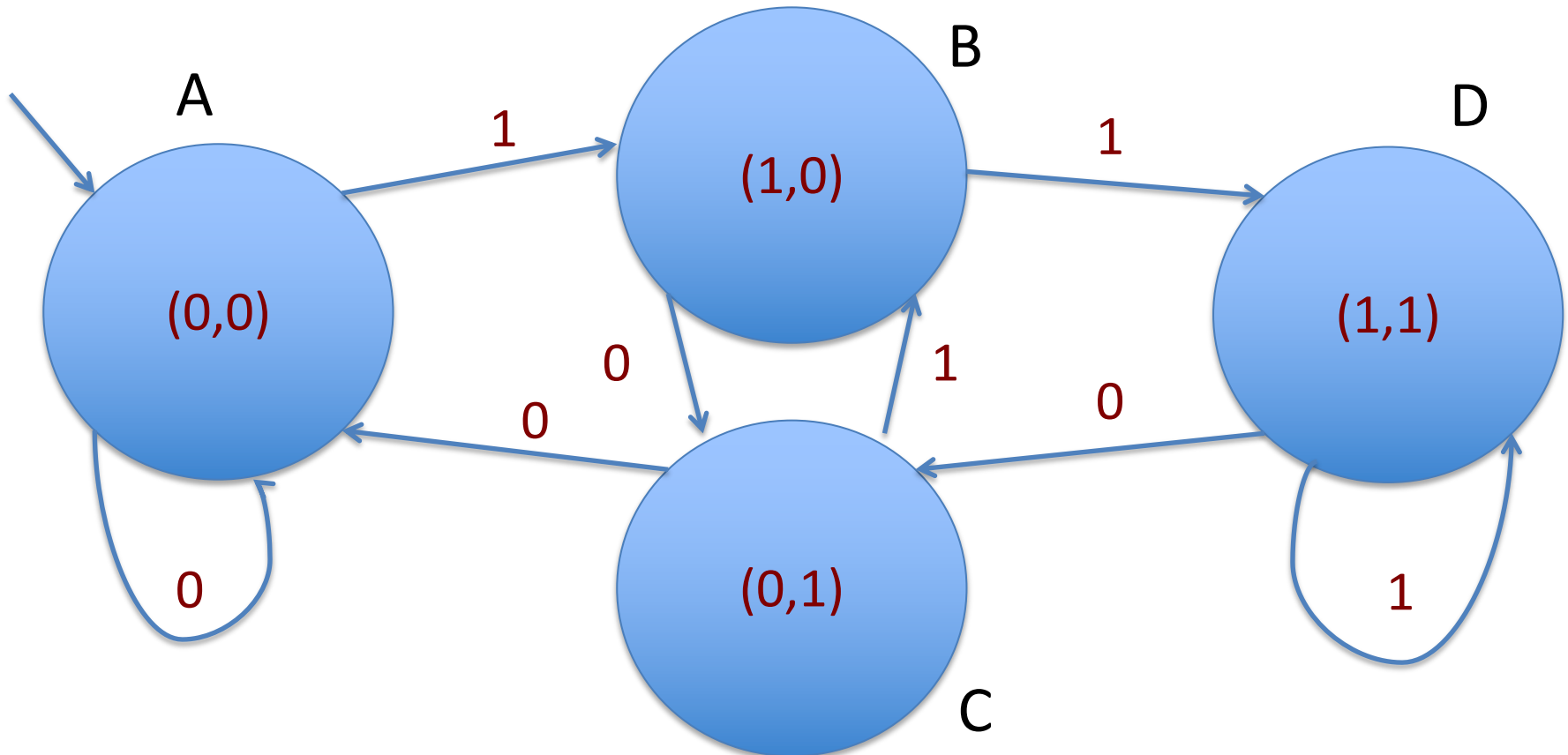


Recall from Lecture 4,

A **counterexample** is a trace that satisfies $\neg R$

Example: Two Bit Shift Register as a Moore Automaton

- $Q = \{A, B, C, D\}$, $\Sigma = \{0,1\}$, $q_0=A$,
- output = (Bit1, Bit2) i.e. “shift right”



2-Bit Shift Reg in NuSMV

using .smv format

```
MODULE main
VAR
  -- system outputs
  Bit1 : boolean; -- Boolean variable
  Bit2 : boolean;
  state : {A, B, C, D}; -- scalar variable

IVAR
  -- system inputs
  input : boolean;

ASSIGN
  init(state) := A;
  init(Bit1) := 0;
  init(Bit2) := 0;
```

```
next(state) := case
    state = A & input = 1 : B;
    state = B & input = 0 : C;
    state = B & input = 1 : D;
    state = C & input = 0 : A;
    state = C & input = 1 : B;
    state = D & input = 0 : C;
    TRUE : state;
esac;
```

```
next(Bit1) := case lab 3 esac;
next(Bit2) := case lab 3 esac;
```

Linear Temporal Logic LTL in .smv format

- Use temporal logic to express automaton requirements
- **Boolean variables**
- $A, B, \dots, X, Y, \dots \text{MyVar}, \text{etc.}$
- **Boolean operators**
- $! (\phi), (\phi \ \& \ \theta), (\phi \ | \ \theta), (\phi \ \rightarrow \ \theta), \dots$
- **Temporal (time) operators**
- $F (\phi)$ (**sometime** in the future ϕ)
- $G (\phi)$ (**always** in the future ϕ)
- $(\phi \ U \ \theta)$ (ϕ holds **until** θ holds)
- $X (\phi)$ (**next** ϕ holds)
- Write $X^n(\phi)$ for $X(X(\dots X(\phi) \))$ (ϕ **holds in n steps**)

Examples of LTL

Right now it is Wednesday

Wednesday

Tomorrow is Wednesday

X (Wednesday)

(A) Thursday (always) immediately follows Wednesday

G(Wednesday \rightarrow X (Thursday))

(A) Saturday (always) follows Wednesday

G(Wednesday \rightarrow F(Saturday))

Yesterday was Wednesday

G(Wednesday \leftrightarrow X (Thursday)) & Thursday

- Exercise: define the sequence of days precisely, i.e. just one solution
- Question: are there any English statements you can't make in LTL?
- Question: what use cases can you express in LTL?

Basic Identities

It makes sense to say that

$$G(\varphi) = \varphi \ \& \ X(\varphi) \ \& \ X(X(\varphi)) \ \& \ \dots$$

or

$$G(\varphi) = \bigwedge_{i \geq 0} X^i(\varphi)$$

Also

$$F(\varphi) = \varphi \mid X(\varphi) \mid X(X(\varphi)) \mid \dots$$

$$F(\varphi) = \bigvee_{i \geq 0} X^i(\varphi)$$

Useful Logical Identities for LTL

- Boolean identities

$$\begin{aligned} \neg(\neg(\phi)) &\Leftrightarrow \phi, & \neg(\phi \mid \psi) &\Leftrightarrow (\neg\phi \ \& \ \neg\psi) , \\ (\phi \rightarrow \psi) &\Leftrightarrow (\neg(\phi) \mid \psi) \text{ etc.} \end{aligned}$$

- LTL identities

$$\begin{aligned} \neg(G(\neg(\phi))) &\Leftrightarrow F(\phi) \\ \neg(X(\phi)) &\Leftrightarrow X(\neg(\phi)) \\ G(\phi \ \& \ \psi) &\Leftrightarrow G(\phi) \ \& \ G(\psi) \\ G(\phi) &\Leftrightarrow \phi \ \& \ X(G(\phi)) \\ G(G(\phi)) &\Leftrightarrow G(\phi) \end{aligned}$$

- Exercise: using these identities, prove:

$$\begin{aligned} \neg(F(\neg(\phi))) &\Leftrightarrow G(\phi) \\ F(\phi \mid \psi) &\Leftrightarrow F(\phi) \mid F(\psi) \\ F(\phi) &\Leftrightarrow \phi \mid X(F(\phi)) \end{aligned}$$

- Remark TCG usually involves **negating formulas**, so its useful to understand what a negation means

LTL Specifications

.smv format

LTLSPEC

```
G( Bit1 <-> (X Bit2) )
```

```
-- always the value of Bit1 now equals the  
-- value of Bit2 in the next time step  
-- This is obviously TRUE!
```

```
G( Bit1 <-> (X Bit1) )
```

```
-- always the value of Bit1 now equals the  
-- value of Bit1 in the next time step  
-- This is obviously FALSE!
```

NuSMV Output Example

```
-- specification G( Bit1 <=> (X Bit2) )  
-- is true  
-- specification G( Bit1 <=> (X Bit1) )  
-- is false  
-- as demonstrated by the following execution  
sequence
```

Trace Description: LTL Counterexample

Trace Type: Counterexample

```
-> State: 1.1 <-
```

```
state = A Bit1 = false Bit2 = false
```

```
-> Input: 1.2 <-
```

```
input = 1
```

```
-> State 1.2 <-
```

```
state = B Bit1 = true Bit2 = false
```


Automated Glass-box TCG

- We can use a model checker to generate counterexamples to formulas (i.e. test cases) with **specific structural properties**.
- This is done by inspecting the **graph structure** of the automaton
- i.e. **white/glass box testing**
- “**Most**” use of model checkers concerns this.

Test Requirements

Trap Properties

- Recall a test requirement is a *requirement that can be satisfied by one or more test cases*
- Basic idea is to capture each test requirement as an LTL formula known as a “trap property”

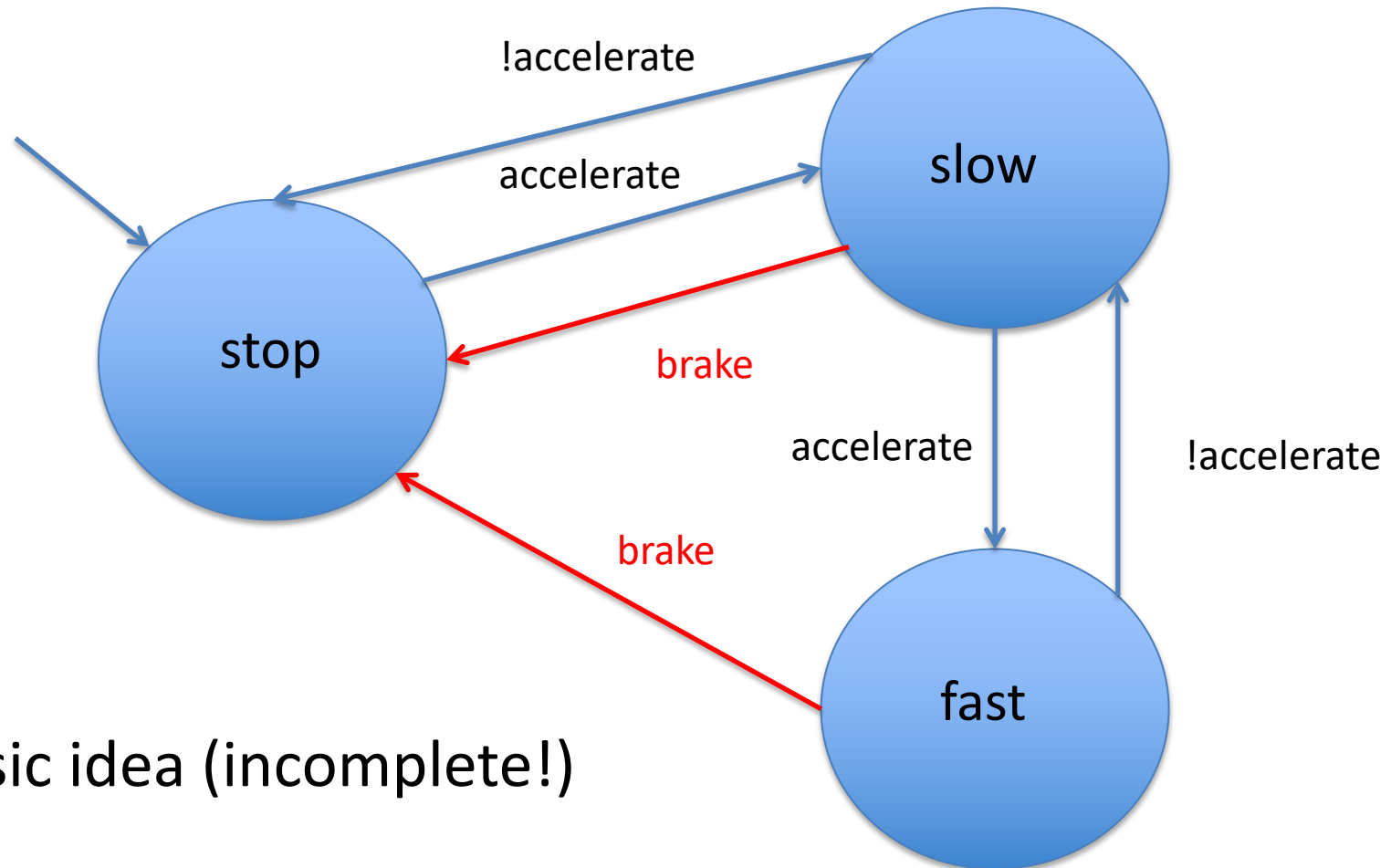
Example Suppose the test requirement is “*cover state D of shift register*”

Trap property is $G(\neg (state = D))$

This formula is *False* and any counterexample must be a path that goes through state D.

Case Study:

Car Controller Model (CC)



Basic idea (incomplete!)

```
MODULE main
VAR
    state: {stop, slow, fast};
    -- velocity states

IVAR
    accelerate: boolean; -- gas pedal
    brake: boolean; -- brake pedal

ASSIGN
    Init(state) := stop;

    Next(state) := case
        accelerate & !brake & state = stop : slow;
        accelerate & !brake & state = slow : fast;
        !accelerate & !brake & state = fast : slow;
        !accelerate & !brake & state = slow: stop;
        brake: stop;
        TRUE: state;
    esac;
```

Trap properties for Structural Coverage Models

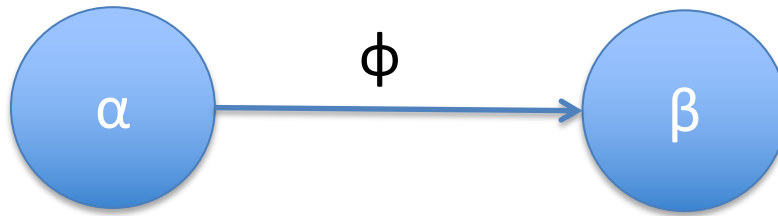
- Let's use NuSMV to automatically construct test suites that satisfy the different **glass box coverage models** introduced in Lecture 2.
- Examples:
 - Node coverage NC
 - Edge coverage EC
 - Condition coverage PC
- How to interpret these concepts?

Node Coverage for CC

- Want a path that visits each node
- Simple approach: write 1 trap property per node
- General form:
- $G(\neg (state = \langle state_name \rangle))$
- Counterexamples satisfy:
- $F(state = \langle state_name \rangle)$
- Example:
$$G(\neg (state = stop));$$
- Clearly this will give redundant test cases, but method is still linear in state-space size.
- Lab Exercise 3: define the remaining 2 trap formulas for car controller

Edge coverage for CC

- Want to traverse each edge between any pair of nodes



- General form $G(\text{state} = \alpha \ \& \ \phi) \rightarrow X(\text{!}(\text{state} = \beta))$
- Counterexample satisfies $F(\text{state} = \alpha \ \& \ \phi \ \& \ X(\text{state} = \beta))$
- Example:

$G(\text{state}=\text{stop} \ \& \ \text{accelerate} \rightarrow$
 $X(\text{!}(\text{state}=\text{slow}))$

- Lab Exercise 3:** define the remaining 5 trap formulas for car controller

Requirements-based TCG

- Can we also perform requirements-based test case generation?
- Want to test the requirements are fulfilled rather than explore structure of the code.
- Can look at **negation of a requirement**

Car Controller

LTL requirements

1. Whenever the brake is activated, car has to stop quickly

$G(\text{brake} \rightarrow X(\text{state}=\text{stop}))$

2. When accelerating and not braking, velocity has to increase gradually

$G(!\text{brake} \ \& \ \text{accelerate} \ \& \ \text{state}=\text{stop} \rightarrow$
 $X(\text{state}=\text{slow}))$

$G(!\text{brake} \ \& \ \text{accelerate} \ \& \ \text{state}=\text{slow} \rightarrow$
 $X(\text{state}=\text{fast}))$

3. When not accelerating and not braking, velocity has to decrease gradually

$G(!\text{brake} \ \& \ !\text{accelerate} \ \& \ \text{state}=\text{fast} \rightarrow$
 $X(\text{state}=\text{slow}))$

$G(!\text{brake} \ \& \ \text{accelerate} \ \& \ \text{state}=\text{slow} \rightarrow$
 $X(\text{state}=\text{stop}))$

Safety Requirements

- A **safety requirement** describes a behavior that may not occur on any path.
- “*Something bad never happens*”
- To verify, all execution paths must be checked exhaustively
- Safety properties usually have the form $G ! \phi$ where ϕ defines the “*bad thing*”
- Counterexamples (**test cases**) are **finite**

Liveness Requirements

- A **liveness requirement** describes a behavior that must hold on all execution paths
- “Something good eventually happens”
- **Safety does not imply liveness**
- **Liveness does not imply safety**
- Liveness properties often have the form
$$F(\theta) \text{ or } G(\phi \rightarrow X^n \theta) \text{ or } G(\phi \rightarrow F\theta)$$
where θ describes the “good” thing and ϕ is some **precondition** needed for it to occur.
- Counterexamples may be **finite** or **infinite** (why?)

TCG for Model-Based Requirements Testing

- Suppose we have an LTL requirement ϕ
- Feed into NuSMV an FSM model A of the SUT, together with the **negated formula** $!\phi$
- Choose any counterexample (a behaviour b) (there should be lots if A is a correct model and ϕ is a correct requirement).
- b satisfies $!\phi$ i.e. b is an example of **correct behavior**
- Feed the **inputs** of b into the SUT and observe the output
- If output from the SUT matches b then **pass** else **fail**

Car Controller Examples

(1) $F(\text{brake} \ \& \ X \ !(\text{velocity}=\text{stop}))$

(2) $F(!\text{brake} \ \& \ \text{accelerate} \ \& \ \text{velocity}=\text{stop} \rightarrow X(\text{velocity}=\text{slow}))$

Concluding Remarks

- Model-based testing has created a lot of interest and opened up new questions
- Tools market is emerging
- What is best modeling language?
- Automated TCG is possible using off-the-shelf tools, e.g. model checkers
- New technologies such as machine learning avoid manual model construction.

Lecture 5 Summary

- MBT uses a model of code for test construction
- Model can be text or graphics
- Graph coverage can be re-used for model coverage
- Models help solve oracle problem (conformance testing)
- Tools allow automated test generation as path traversal in a model.
- ATCG based on *model checking, graph search, constraint solving or theorem proving*