

Comparing summed probability distributions of shoreline and radiocarbon dates from the Mesolithic Skagerrak coast of Norway

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1 Introduction

Population size is regarded as an important driver of cultural variation, and is of critical importance to our understanding of past human societies (e.g. French et al., 2021; Shennan, 2000). The frequency distribution of radiocarbon dates has been used extensively as one proxy for past relative population sizes (e.g. Crema, 2022; French et al., 2021), including in Norwegian Stone Age archaeology (Bergsvik et al., 2021; Jørgensen et al., 2020; Lundström et al., 2021; Nielsen, 2021; Nielsen et al., 2019; Solheim, 2020; Solheim and Persson, 2018; see also Persson, 2009). The potentially immense value of insights into past population dynamics, combined with the ubiquity of radiocarbon dates and the relative ease with which these can now be processed within what has been termed a dates as data methodology has undoubtedly contributed to the popularity of the approach. Several limitations and forms of criticism have, however, been directed at these procedures. Some of the objections are of a methodological nature, while others pertain to the underlying logic and the degree to which there is likely to be a direct connection between the frequency of ^{14}C -dates and population dynamics (Carleton and Groucutt, 2021; Torfing, 2015). What appears to be agreed upon by practitioners and critics alike is that radiocarbon dates are best analysed in this manner when compared and contrasted to other proxies for past population dynamics and other variables that might impact these (Bergsvik et al., 2021; French, 2016; Palmisano et al., 2021, 2017). This paper reports on and begins to unpack the relationship between two measures that have been linked to relative population size in the context of the Mesolithic Skagerrak coast in south-eastern Norway, namely summed probability distribution of calibrated radiocarbon dates and the summed probability distribution of shoreline dated sites (hereafter RSPD and SSPD, respectively).

2 Background

Large parts of the post-glacial landscape of Northern Scandinavia is characterised by dramatic isostatic uplift that has led to a net sea-level fall throughout the Holocene, despite eustatic sea-level rise (e.g. Mörner, 1979). As coastal foragers appear to have predominantly settled on or close to the contemporaneous shoreline, this can be utilised to assign an approximate date to the sites. This is done by coupling the present-day altitude of the sites with reconstructions of past shoreline displacement – a method known as shoreline dating. This is not least useful for dating the large number of surveyed sites in the region where other temporal data that often follow with an excavation are not available, such as radiocarbon dates or typological indicators in artefact inventories.

The frequency of shoreline dated sites has also been compared to RSPDs in the past (Solheim and Persson, 2018; Tallavaara and Pesonen, 2020). However, this has been done by finding point estimates of shoreline dates that are then aggregated in somewhat arbitrary bins of 200 or 500 years. This therefore does not take into account the uncertainty in the distance between the sites and the contemporaneous shoreline, nor the impact the variability in the rate of sea-level change has on the precision of the dates that can be achieved with the method. In a recent study, Roalkvam (2023a) has presented a probabilistic method for shoreline dating that takes these parameters into account, thus setting the stage for a more refined investigation of the relationship between frequency of ^{14}C -dates and shoreline dated sites. The parametrisation of the method

was based on simulating the distance between sites with ^{14}C -dates and the prehistoric shoreline along the Skagerrak coast in the region between Horten municipality in the northeast to Arendal municipality in the southwest (see map in Figure 1). The results of the analysis indicates that the sites tend to have been located close to the shoreline until just after 4000 BCE when a few sites become more withdrawn from the shoreline, followed by a clear break around 2500 BCE, at which point shoreline dating appears to lose its utility. Thus, this geographical and temporal limit are also used for this study.

This paper is decidedly exploratory. While some speculative thoughts concerning the relationship between the variables outlined above underlie the analysis, these could not be instantiated as concrete hypotheses. The data have thus been explored using a set of standard models to begin to unpick patterns and grasp the relationship between the variables. Furthermore, the dates as data approach is dependent on there being a direct link between the past generation of material that ultimately become ^{14}C samples, and population size. The sum of shoreline dated sites, on the other hand, is determined by site frequency, and if used as a proxy for population size is therefore dependent on there being a connection between site count and population size. If a comparison of these proxies do not, or only partially correspond, it is thus an open question what factors have impacted either distribution to cause this discrepancy, and which measure, if any, reflects true population dynamics. The issue will therefore initially demand an open and exploratory approach where a multitude of explanatory and confounding effects can be drawn on to suggest explanations of any observed pattern.

2.1 Population dynamics and summed probabilities

To what degree the radiocarbon record is determined by past population numbers might vary both geographically and chronologically, based on variation in investigatory and taphonomic factors (Bluhm and Surovell, 2019; Surovell et al., 2009), as well as cultural processes within prehistoric populations. One example of the latter is the difference that might exist between farmer and forager populations, where Freeman et al. (2018) have suggested that an increased per capita energy consumption introduced with farming means that ^{14}C -dates should not be weighted equally when making relative population estimates across such populations. Similarly, while site counts have also been invoked for the analysis of past population dynamics, these are likely to be impacted by factors such as land-use and mobility patterns, and settlement nucleation and dispersion (Palmisano et al., 2017). However, these could be considered theoretical issues that have implications for how fluctuations in these proxies should be interpreted, and possibly weighted differently according some criteria. Before any such fluctuations are given any substantive interpretation, however, there are a host of methodological issues that have to be considered.

The most critical of these follow from the fact that the summation of the probabilities associated with the dates for the SPDs is not a statistically coherent procedure. This is because the summed probabilities can no longer be seen as probabilities, but rather represent the combination of events and uncertainties, making the two indistinguishable, and rendering the interpretation of the resulting sum difficult (Blackwell and Buck, 2003; Crema, 2022). As Timpson et al. (2021, p. 2) put it: ‘the SPD is not *the* single best explanation of the data, nor even *a* explanation of the data, but rather a conflation of many possible explanations simultaneously, each of which is mired by the artefacts inherited from the calibration wiggles.’ The SPD is not a model. It is the combined representation of a range of possible explanations for the data – the frequency of dated events combined with the variable uncertainty associated with these (Carleton and Groucutt, 2021). This means that an SPD cannot be directly analysed to draw inferences on population dynamics, nor can it be directly compared to other time-series data (Carleton et al., 2018; Timpson et al., 2021). While this problem can never be entirely resolved, a range of approaches have been developed in an attempt to work around this issue.

The most commonly applied of these is a null-hypothesis significance testing approach by means of Monte Carlo simulation, as introduced by Shennan et al. (2013) and later expanded upon by Timpson et al. (2013). This works by comparing the observed RSPD with a series of simulated RSPDs, generated from a null-model. These null-models are typically a uniform, exponential or logistic distribution. These are chosen *a priori* with reference to common long-term population dynamics and are typically parametrised by fitting the models by means of regression or maximum likelihood estimation (MLE). The result from these simulations are then

used to create a 95% critical envelope representing the null model. The proportion of the observed RSPD that falls outside this envelope is then used to estimate a global p-value indicating whether the null model can be rejected. In the case that it can, the portions of the observed RSPD that falls outside this envelope can subsequently be interpreted as representing potentially meaningful demographic events, relative to the null model. However, care has to be taken in how these are interpreted. First, this follows from the fact that 5% of the deviations from the critical envelope can be expected to be random, and there is no way to know which deviations this pertains to. Secondly, a for example exponential null model fit to the data is only one of an infinite set of exponential models with different growth rates that could be used. While a model fit by means of MLE will likely have a reasonable growth rate, and by extension exclude many other exponential fits as likely to explain the data, this can be difficult to determine. Finally, the p-value only indicates whether or not the null-model as a whole can be rejected as an explanation of the data, and does not provide statistical justification for interpreting local deviations themselves as meaningful demographic signals, as has often been the case (see review by Crema, 2022; Timpson et al., 2021).

2.2 Model comparison and continuous piece-wise linear models

The procedure outlined above represent the standard approach when modelling population dynamics in archaeology. This can be helpful for determining whether the population behaviour has followed the trajectories of standard theoretical models, and is a useful first step here as few assumptions concerning the behaviour and overall development of number of shoreline dated sites over time could be made. However, standard models frequently used to evaluate RSPDs are consistently being rejected in the literature, and deviations from these rejected null-models do not in themselves allow for any interpretations of the deviations, nor a subsequent direct analysis of the SPDs themselves. As a result, and by improving on Goldberg et al. (2016), Timpson et al. (2021) have recently suggested an alternative framework for modelling past population dynamics by use of RSPDs, published with the accompanying R package *ADMUR*. This involves fitting continuous piece-wise linear (CPL) models in addition to the standard models to the data, subjecting these to a procedure of model comparison, and finally evaluating the best model using a goodness-of-fit test in line with the Monte Carlo approach outlined above. The benefit of the CPL models is that these define discrete linear periods of development between hinge points that mark points in time in which the trajectory of the population proxy changes direction, thus allowing for the identification of key events with a conservative description of population dynamics between these. The approach thus also provides a clearer inferential justification for a further analysis and substantive interpretation of the identified best model. Following the evaluation of standard models as outlined above, the data were therefore subsequently subjected to the approach presented by Timpson et al. (2021).

3 Methods and data

Sites surveyed by means of test-pitting between Horten and Arendal were initially retrieved from the national heritage database Askeladden (Norwegian Directorate for Cultural Heritage, 2018), totalling at 1299 records. The records were then manually reviewed and given a quality score based on the criteria in Table 1, indicating the degree to which the spatial location and extent of the sites is believed to be represented in the geometries available in the database (see also Roalkvam, 2020). All sites with a quality score of 4 or worse were excluded from further analysis. Any sites situated at elevations that result in a shoreline date earlier than 9469 BCE were then excluded. This marks the latest start-date among the employed displacement curves, and no sites are yet verifiably older than around 9300 BCE (Glørstad, 2016). Data on excavated sites was originally compiled for Roalkvam (2023a) and has been compared with site data as listed in Damlien et al. (2021) and Nielsen et al. (2019). Only excavated sites with available spatial data in Askeladden or local databases at the Museum of Cultural History of the University of Oslo were included in the analysis. The 102 excavated sites in the dataset without relevant ^{14}C -dates and that were originally shoreline dated in the reports were included in the SSPD along with the retained surveyed sites. This gave a total of shoreline dated sites in the final SSPD.

Table 1: Quality scoring of site records of surveyed sites retrieved from the national heritage database Askeladden. The scoring system was first used in Roalkvam (2020).

Definition	Quality	Count
Site delineated by use of a GNSS-device, or a securely georeferenced record. Extensive database entry.	1	353
Secure spatial data. Slight disturbance of the site or somewhat lacking database record.	2	340
Secure spatial data. Damaged site, such as outskirts of a quarry, and/or very limited database entry.	3	148
Surveyed by archaeologists. However, the database entry is extremely limited/unclear, the site geometry is only given as a point or small automatically generated circle, and/or finds are from the topsoil of a field.	4	165
Likely site but uncertain spatial information. Typical example is recurring stray finds in a field or other larger area.	5	124
Single stray find or unverified claims/suggestions of possible site.	6	169

The borders of the municipalities within which the shoreline dated sites are located were used to limit the radiocarbon sample. Radiocarbon dates were taken from Roalkvam (2023a) and (solheim?). Dates done on food crusts were then excluded due the issue of marine reservoir effects (Nielsen et al., 2019, p. 83), resulting in a final total of ^{14}C -dates. Following both from the point made by Freeman et al. (2018) concerning the comparison of radiocarbon dates from populations with different economic modes, as noted above, and from the fact that shoreline dating appears less reliable after 4000 BCE and appears to loose its utility c. 2500 BCE, the Mesolithic is the main focus of this analysis. Consequently, probabilities falling later than 2500 BCE were excluded from the analysis. Probabilities falling after 4000 BCE and the first, possible small-scale introduction of agriculture in south-eastern Norway were retained to account for edge-effects, but these results should be treated with care for the reasons noted above.

All analyses done in this study were performed using the R programming language (R Core Team, 2020). Underlying data and programming code used for the paper is available in a version-controlled online repository at X. This is structured as a research compendium following Marwick et al. (2018), to allow for reproducibility of the results (see also Marwick, 2017). Analysis of the ^{14}C -dates were done using the R package *rcarbon* (Crema and Bevan, 2021). The R package *shoredat* was used for performing and handling the shoreline dating of sites (Roalkvam, 2023b). Finally, the package *ADMUR* (Timpson et al., 2021) was used for model comparison.

3.1 Summed probability of calibrated radiocarbon dates

To account for investigatory bias that can result from variable sampling intensity between sites, the radiocarbon dates were initially binned using the *binPrep()* function from *rcarbon*, where dates were aggregated on a site by site basis if they fell within 200 uncalibrated ^{14}C years of each other. When calibrated, these are summed and divided by the number of dates in the bin before being included in the final RSPD. Furthermore, the ^{14}C -dates were not normalised. This follows from a peculiarity in the calibration procedure which can lead the probability mass of a date to sum to more than one (Weninger et al., 2015). As a consequence of this, normalising the dates before summing has been shown to create spurious spikes in the RSPD (e.g. Crema and Bevan, 2021). All calibration was done using the IntCal20 calibration curve (Reimer et al., 2020).

The RSPD was first subjected to the standard null-hypothesis testing approach through Monte Carlo simulation, as introduced above (see Shennan et al., 2013; Timpson et al., 2013), by fitting an exponential, logistic and uniform model to the observed RSPD. Following Timpson et al. (2021), the model parameters were identified by MLE search, using the differential evolution optimization algorithm *DEoptimR*. The Monte Carlo simulations were then performed using the *modelTest()* function from *rcarbon*. For each model, a series of individual calendar years are drawn from the model distribution, with replacement, the number of which equals the number of bins in the observed RSPD. These are then ‘uncalibrated’ to a single value on the ^{14}C scale and a random error from among the observed errors is added to the date. These are then calibrated back to the calendar scale and finally summed. Here, this procedure was repeated 10000 times for each null model. The 2.5th and 97.5th quantile of the resulting summed probability for each year across all simulations are then retrieved to create the 95% critical envelope with which to compare the observed RSPD. The degree to which the observed RSPD deviates from the critical envelope is then used to calculate a global p-value,

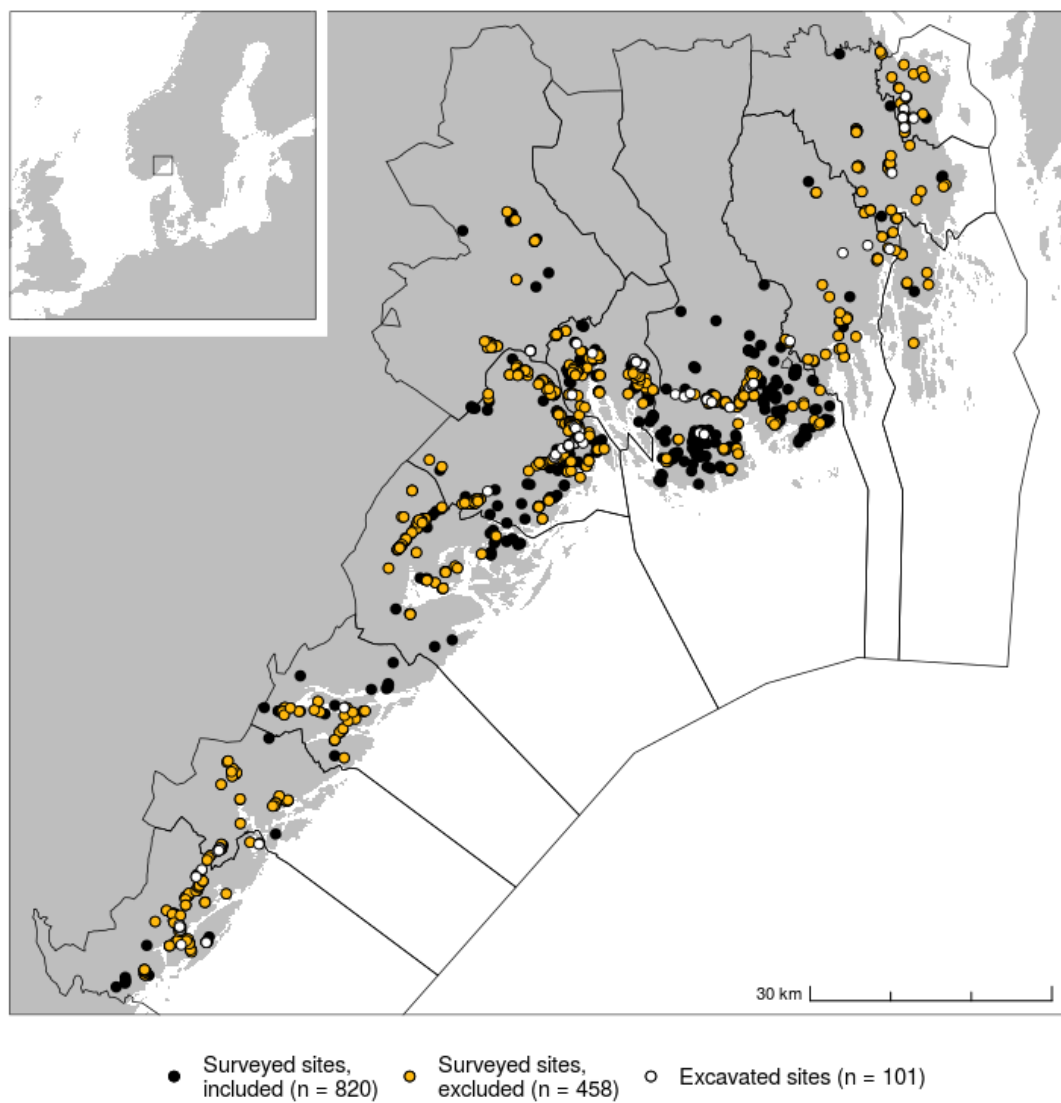


Figure 1: Map of the study area and shoreline dated sites. Black lines indicate the borders between municipalities. The surveyed sites included in the analysis are the ones given a quality score of 3 or higher using the framework in Table 1.

indicating whether or not the null can be rejected.

3.2 Summed probability of shoreline dated sites

Summing the probability of the shoreline dated sites and the model-fitting procedures followed the same structure as that for radiocarbon dates and was partly based on re-purposed programming code from *rcarbon*. However, idiosyncrasies in the dating method did necessitate some adjustments. To illustrate this, the procedure for shoreline dating a single site, as suggested in Roalkvam (2023a), is provided in Figure 2 and outlined below.

Four geological reconstructions of shoreline displacement in the region lays the foundation for the method as implemented here (Figure 2B). These shoreline displacement curves are from Horten (Romundset, 2021), Porsgrunn (Sørensen et al., in press, 2014a, 2014b), Tvedestrand (Romundset et al., 2018; Romundset, 2018) and Arendal (Romundset, 2018), each associated with a shoreline isobase along which the trajectory for relative sea-level change has been the same (see Svendsen and Mangerud, 1987). The first step in the dating procedure is to interpolate the shoreline displacement to the location to be dated. This is done by inverse distance weighting (e.g. Conolly, 2020), interpolating the relative sea-level change to the location of a site to be dated, based on it's distance from the isobases of the displacement curves.

With an estimated trajectory of shoreline displacement at the site to be dated, the elevation of the site can be drawn on to find a likely date for when it was in use, under the assumption that it was in use when located on or close to the shoreline. Figure 2C indicates where the elevation of the example site intersects the interpolated displacement curve. As it can be reasonably be assumed that a site was not in use when located under water, this effectively represents a *terminus post quem* (TPQ) date. However, a fairly common approach to shoreline dating has been find where the elevation of the site intersects the mean of the upper and lower limit of the displacement curve, and then adding a somewhat arbitrary error of ± 100 years to this point-estimate. However, finding TPQ dates that do not account for the likely distance between site and sea when the site was in use, limits, as with TPQ dates in general, the further inferential steps that can be taken. Furthermore, the more common practice of adding a constant error to a point-estimate does not take into account that the rate of shoreline displacement varies both spatially and temporally, and therefore introduces bias to the result on both the spatial and temporal scale, while also overestimating the precision of the method in most cases. This last point can be illustrated by finding the range between the upper and the lower limit of the four geological displacement curves for every meter from the marine limit and down to elevations that do not give an earliest date younger than 2500 BCE. This gives a mean TPQ range of 276 years with a standard deviation of 156 years across all four displacement curves, with this range varying significantly over time and between curves.

The analysis in Roalkvam (2023a) found that site phases ^{14}C -dated to before 2500 BCE were found to have a likely elevation above sea-level that can be reasonably approximated by a gamma distribution with shape = 0.286 and scale = 20.833. This is incorporated in the procedure for shoreline dating used for this study (Figure 2D). When performing this dating procedure, the gamma distribution is sequentially stepped through and transferred to the calendar scale by uniformly distributing the probability across the years in the range between the lower and upper limit of the interpolated displacement curve. This procedure thus gives the the shoreline date of a site when accounting for the likely elevation of the site above sea-level when it was in use (see Roalkvam, 2023a for details). Given that the shoreline displacement curves have no inversions and should therefore be commutative (cf. Weninger et al., 2015, p. 545), each shoreline date is normalised to sum to unity. To reduce the computational cost of the simulation procedures to follow below, the gamma distribution is here stepped through at increments of 0.1 m and the calendar scale is kept at a resolution of 5 years.

The implications of different approaches to shoreline dating and summing the results is further illustrated in Figure 3. In Figure 3A the sites to be shoreline dated are plotted according to their elevation. Due to the variable rates of shoreline displacement within the study region, the same elevation does not necessarily equate to the same date, and so this does not directly tell us much about their temporal distribution. For example, as the trajectory for sea-level regression is starker towards the north-east, the same elevation at a location to the south-west implies a younger date than one towards the north-east.

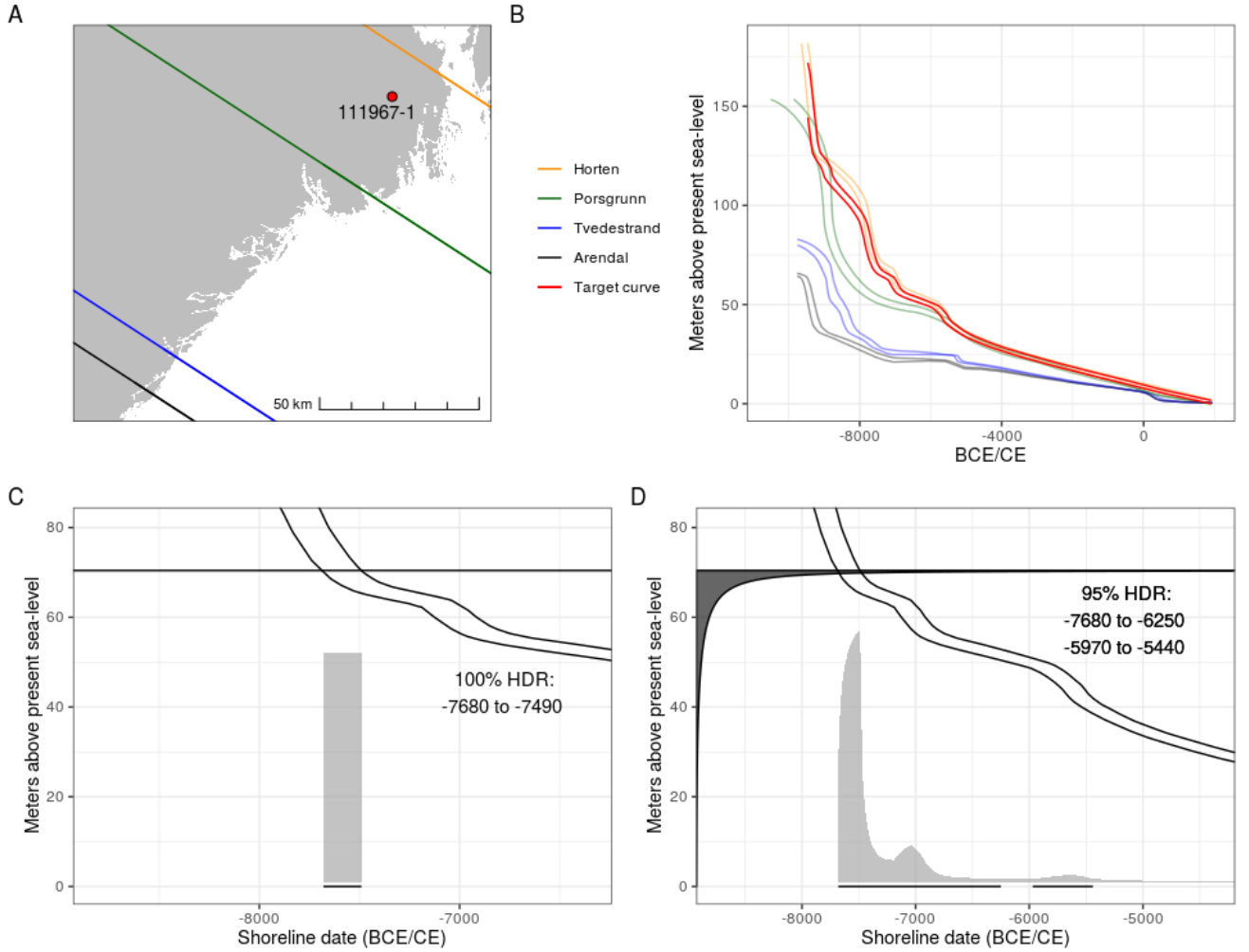


Figure 2: A) An example site (Askeladden ID 111967-1) relative to the isobases of the displacement curves. B) The geological displacement curves in the region and the curve interpolated to the example site. C) The black line on the y-axis represents the elevation of the site. This crosses the interpolated displacement curve at 7680 and 7490 BCE, which thus in practice gives an estimate of when the location of the site emerged from the sea, giving a *terminus post quem* date. D) The shoreline dating approach used for this study, where the gamma distribution on the y-axis describes the likely vertical relationship between the shoreline and the site when it was in use.

When the frequency distribution of shoreline dates have been investigated in the past, this has typically involved finding point-estimates of dates by either using the mean of displacement curves, or by taking mean of the TPQ dates for each site (as illustrated in Figure 2C). These point-estimates are then aggregated in bins of 200 or 500 years (e.g. Breivik, 2014; Fossum, 2020; Mjærø, 2022; Solheim and Persson, 2018; Tallavaara and Pesonen, 2020). This approach is illustrated in Figure 3B. The SSPD resulting from instead using the probabilistic method of shoreline dating, given in Figure 3C, clearly demonstrates that accounting for the site-sea relationship gives a substantially different result compared to the more traditional approach, which is clearly indicated by the shifts in the positions of peaks and troughs in the distribution after c. 8000 BCE.

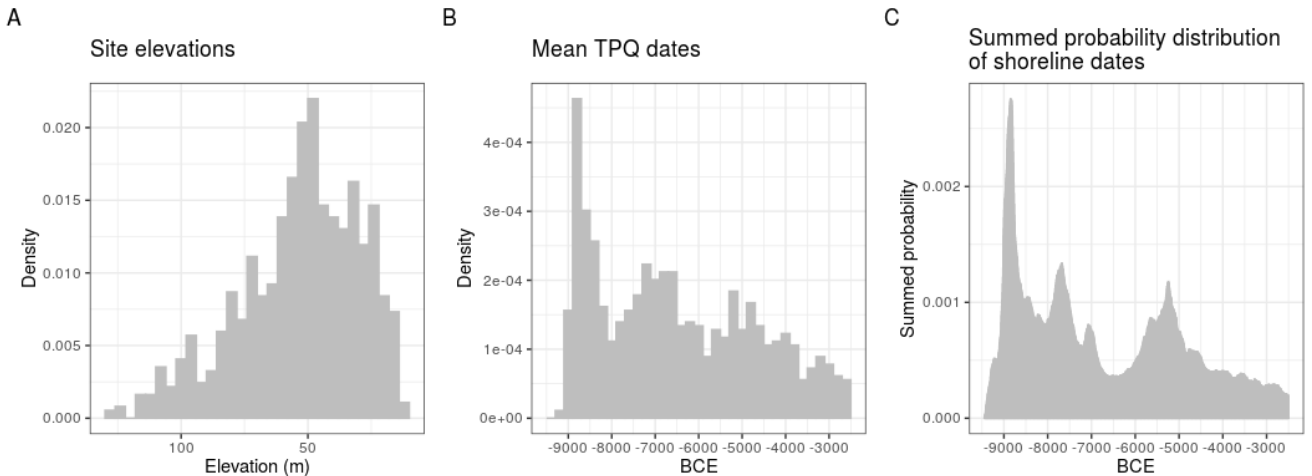


Figure 3: A) The distribution of the shoreline dated sites ($n = 921$) by elevation. The binwidth is 4 m. B) The mean of *terminus post quem* dates for the sites, plotted with a binsize of 200 years, reflecting the common approach to summing shoreline dates. C) The result of instead summing the probability of the shoreline dates achieved with the method employed here, which accounts for the likely distance between sites and shoreline. The binwidth is 5 years, following the resolution used with the dating procedure.

However, in the same way as with RSPDs, the SSPD cannot be directly interpreted as reflecting the intensity of sites over time, due to the summation issues introduced above. Furthermore, similar to how characteristics of the calibration curve can introduce bias to the RSPD, the same is true for the SSPD, where the local trajectory of relative sea-level change effectively functions as the calibration curve for each site. As the shoreline displacement curves are interpolated to the sites based on their location along a south-west–north-east gradient, each site is effectively associated with a unique shoreline displacement curve, provided they are not located on exactly the same isobase. With analogy to the radiocarbon methodology, this would be equivalent to each date being associated with a unique calibration curve. As it would be computationally prohibitive to interpolate the shoreline displacement trajectory for each date to be simulated in the Monte Carlo procedure, one shoreline displacement curve was initially interpolated to the centre of each of a series of 2 km wide line segments running perpendicular to the shoreline gradient between the extremes of the distribution of sites. These intervals were then assigned a weight based on how the density of observed sites is distributed among them (Figure 4).

Following from the commutative nature of the shoreline dates dealt with here, the Monte Carlo simulation with the SSPD is here based on drawing a sample of calendar dates from the observed date range in the SSPD, equalling the number of shoreline dated sites, where the probability of drawing any individual year is determined by the null model of choice. This is equivalent to the sampling method *calsample* from *rcarbon* (Crema and Bevan, 2021). Each sampled date is then assigned one of the pre-interpolated displacement curves, the probability of which is weighted by the density of observed sites within each 2 km interval. The calendar date is then ‘uncalibrated’ – to follow the RSPD terminology – to an elevation range from which a single elevation value is then drawn with uniform probability between the lower and upper limit of the displacement curve at that calendar year, using intervals of 5 cm. As shoreline dating is here done with a gamma distribution

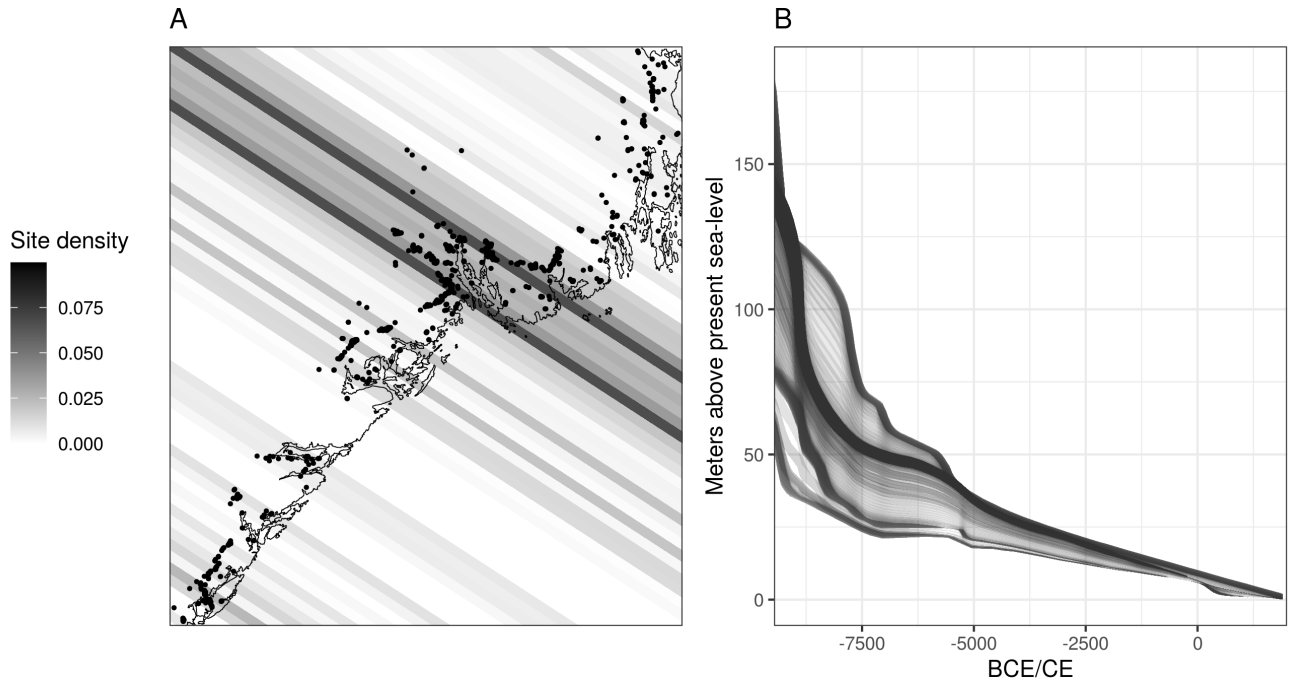


Figure 4: A) Density of included surveyed sites and excavated sites dated by means of shoreline dating ($n = 921$) as distributed across 2 km wide line segments that run perpendicular to the shoreline gradient. B) The displacement curves interpolated to the centre of each segment for use in the Monte Carlo simulations below.

with the same parameters across all sites, there is no equivalent of the error term for ^{14}C -dates that determine the shape of the Gaussian distribution associated with the ^{14}C age. Consequently, the elevation value retrieved by ‘uncalibrating’ the shoreline date was then shoreline dated using the displacement curve for the relevant 2 km interval with the same gamma distribution for all samples. Having dated the number of samples equalling the number of shoreline dated sites, these were then summed, and the entire process repeated a total of 10000 times. The 97.5% highest and 2.5% lowest summed probability at each interval of 5 years across all simulations was then retrieved to create the 95% critical envelope, and the global p-value found in the same manner as for the RSPDs. This was done using re-purposed code from *rcarbon*.

3.3 Continuous piece-wise linear models

The procedures outlined above represent standard approaches when modelling population dynamics in archaeology. These can be helpful for determining whether the population behaviour has followed the trajectories of common theoretical population models, and is an especially useful exercise here as few assumptions concerning the behaviour and overall development of number of shorebound sites over time could be made. However, standard models frequently used to evaluate RSPDs are consistently being rejected in the literature, and deviations from these rejected null-models do not in themselves allow for any interpretations of the deviations, nor a subsequent direct analysis of the SPDs – although this has frequently been the case. As a result, Timpson et al. (2021) have recently suggested an alternative framework for modelling past population dynamics. This involves fitting continuous piece-wise linear (CPL) models in addition to the standard models to the data, subjecting these to a procedure for model comparison, and finally testing the best model using the approach outlined above. The benefit of the CPL models is that these define discrete periods between hinge points that marks points in time in which the trajectory of relative population size changes direction, thus identifying key events and characteristics of the population dynamics between these. Following the evaluation of standard models outlined above, the data was therefore subsequently subjected to the approach outlined by Timpson et al. (2021).

3.4 Comparing model performance

For each dating method, the relative performance of the exponential, logistic, uniform and CPL models was compared. This was done by finding the overall relative log-likelihoods of the models using the *loglik* function from *ADMUR*. For any given model, this involves finding the likelihood for each shoreline date against the null-model, and in the case of the ^{14}C -dates, each site-phase. The overall model likelihood is the product of each of these individual likelihoods and is not, critically (Timpson et al., 2021), found by estimating the likelihood using the final SPD. From these likelihoods, the Bayesian (or Schwarz) information criterion (BIC) for each model was then found. This penalises the models for the number of parameters in use to avoid over-fitting.

4 Results

Comparing the the directions and deviations from the three standard models, Figure appears to indicate some process of overall general increase or uniform distribution in the frequency of radiocarbon dates over time, contrasted to a general decrease in shoreline dated sites over time. However, with global p-values all below X, all three models can be rejected as explaining the data they have been fit to, both for the SSPD and RSPD. Based on common demographic developments and previous suggestions, there is possibly some theoretical justification for expecting an exponential or logistic model to explain the shape of the RSPD, thus giving some further credence to interpreting deviations from this overall development as potentially meaningful signals of demographic developments. However, as introduced above, several authors have warned against over-interpreting such deviation. Furthermore, there are even less foundations on which to hypothesise what processes have dictated the development of site frequency over time, thus offering even further challenges to the interpretation of the SSPD and it’s relationship with the null-models.

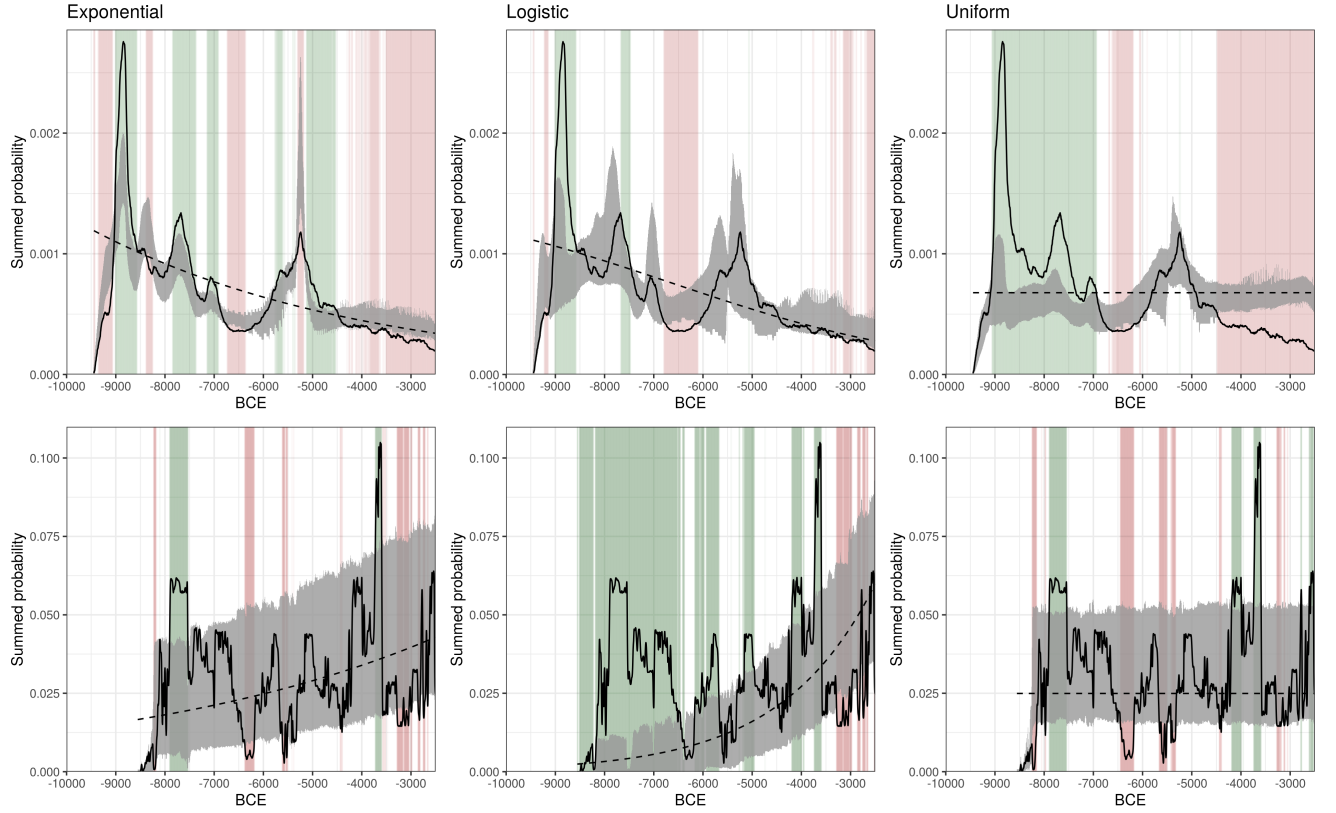


Figure 5: Monte Carlo simulation for shoreline and radiocarbon dates. A) Summed probability of shoreline dated sites ($n = 934$) compared to a uniform null model. B) Same as A, but with a exponential model. C) Summed probability of calibrated radiocarbon dates ($n = 678$) compared to a uniform null model. D) Same as C, but with a exponential null model.

For the RSPD the rejected logistic model offers the best approximation of the data of the compared models. If taken as an indication of demographic developments this would indicate a first migration of people that is more substantial than what would be expected under the logistic null. Further deviations are then evident with the negative deviation and the positive deviation *c.* These are, however, brief and can be left as little more than suggestions for possible meaningful demographic events.

In the following, some of these deviations will nonetheless be narratively linked to some major developments that have previously been proposed to characterise the Stone Age of south-eastern Norway, with the goal of suggesting some potential. It is, however, important to underscore that the *ad-hoc* coupling of the results achieved here with these developments should only be considered suggestions that can offer some potential avenues for further inquiry, for example using the approach outlined by Timpson et al. (2021).

5 Discussion

It is firmly established that Stone Age sites in the region date to the period from before the earliest ^{14}C -dates, and at least from as far back as around 9300 BCE. While the SSPD starts from *c.* , thus suggesting that the first date of human occupation in south-eastern Norway can be pushed back, this will require further corroboration from excavations and more meticulous evaluations of the evidence at hand. Furthermore, what has caused the lack of ^{14}C -dates from this earliest period has been given many possible explanations, ranging from taphonomic loss, to diverse cultural factors, such as the potential use of rapidly deteriorating seal blubber for burning, which could also be related to a possible lack of reliable access to firewood. While taphonomic and ecological factors cannot be written off, we view it as likely that the initial jump in ^{14}C -dates at the start of RSPD combined with the magnitude of the SSPD in the period preceding this, suggest that cultural factors is a central driver behind this pattern.

While all the considered models can be rejected as explaining the analysed data, they do nonetheless indicate that some process of decrease in site frequency occurs throughout the period, contrasted by a general increase in the frequency of ^{14}C -dated material. The most immediate explanation of this mismatch would be that the SSPD largely reflects variations in land-use and mobility patterns, while the RSPD mainly reflects population numbers. The modelled process of logistic decay markedly under-predicts the number of sites in the period X–X, and a deviation is also apparent in the period X–X, where the number of observed sites is significantly lower than what would be expected under the logistic model. While we are wary of over-interpreting these signals, they strike us as warranting more consideration than the other deviations that are barely outside the critical envelope, or are of a short duration. The deviations from after 4000 BCE should also be treated with further care, following both from questions concerning the reliability of shoreline dating after 4000 BCE (cf. Roalkvam, 2023a), and the noise in the critical envelope following from the practical implementation of the simulation procedures.

The initial peak in the SSPD would be congruent with a process of rapid colonisation of the Norwegian coast, coupled with a high degree of mobility, leading to the overall high site-count in the earliest period. As evidenced by both genetic data and technological analyses of lithic inventories, this initial phase of human occupation appears to be followed by an influx of people from the . If this narrative is coupled to the data observed here, this process would appear to result in a relatively sudden drop in site-count as indicated in the SSPD, while the end of this drop corresponds to the first ^{14}C -dates in the RSPD – giving further credence to the suggestion that the appearance of material to be ^{14}C -dated is related to cultural processes. In the period X–X following this, there is also a marked positive deviation from the RSPD under the exponential model, indicting a population boom, which, although barely breaking the critical envelope of the logistic model, is also evident in the SSPD.

Berg-Hansen et al. (2022) have argued that there is an increase in sites in the first half of the MM in the northern part of the study area of this paper. However, their analysis is seemingly also based on the aggregation of point-based estimates of shoreline dates, which are aggregated within periods of variable length. Apart from the limitations with using point-based estimates, the use of disjoint time-intervals of variable duration could cause issues for comparing the relative counts across these units (Bevan and Crema, 2021).

This analysis instead indicates a drop in the number of sites through this time-interval

While population numbers would likely impact the SSPD as well, the overall mismatch between the two proxies used here means that the magnitude of demographic influence on the SSPD is difficult to speculate about. However, the positive deviation in the SSPD from the logistic model at c. does correspond to a similar deviation of the RSPD from the exponential model. Matching negative deviations, on the other hand, can be observed around the middle of the 7th century BCE and in the period after 3500 BCE. While we are, as mentioned, cautious in giving these much weight in the SSPD alone, the correspondence of these deviations across the two proxies gives some reason to suggest that these might reflect meaningful demographic signals. This would also i

The finding that the frequency of radiocarbon dates and frequency of shoreline dated sites, in general, follow inverse trajectories is a valuable insight. Although a more precise understanding of this relationship

Furthermore, seeing as the method implemented here was recently developed and has been subjected to limited evaluation and testing, there are still considerable uncertainties associated with the method (see Roalkvam, 2023a). While we still believe the approach represents a considerable improvement over previous approaches, the results should

6 References

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