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## **Edexcel A Level Maths: Pure**



## 2.4 Inequalities

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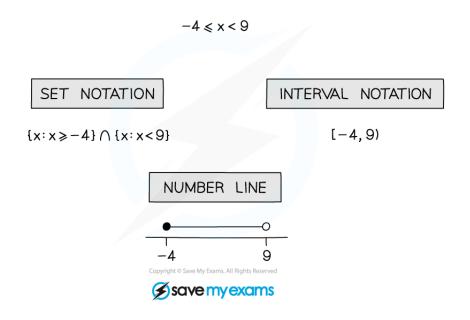
### 2.4.1 Linear Inequalities

## Your notes

## **Linear Inequalities**

### What are linear inequalities?

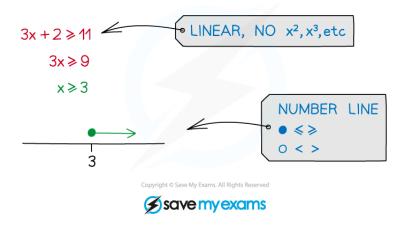
- Linear inequalities are similar to equations but answers take a range of values
- Linear means there will be no terms other than degree 1
  - no squared terms or higher powers, no fractional or negative powers
- Inequalities use the symbols following symbols
  - > Greater than e.g. 5 > 3
  - $\sim$  Less than e.g. -8 < 7
  - ≥ Greater than or equal to
  - ≤ Less than or equal to
- Inequalities can be represented in many ways using number lines, set notation and interval notation



#### Number line diagrams

- Number line diagrams are made up from circles and lines set above a number line
  - A filled-in circle or empty circle above a number denotes whether the number is included or not
    - filled in for the greater/less than or equal to symbols  $\leq \geq$
    - empty for the greater/less than symbols < >
  - Arrows show the range of values that are allowed

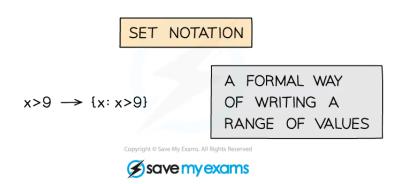






#### Set notation

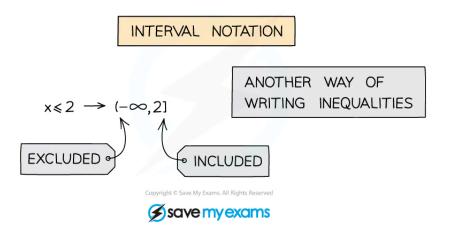
- Set notation is a formal way of writing a range of values
- Use of curly brackets {}
- Intersection ∩ and union u may be used
- Not to be confused with interval notation



#### Interval notation

- Interval notation uses different brackets to indicate whether a number is included or not
- Use of square [] and round () brackets
- [or] mean included
- (or) mean excluded
  - (4,8] means 4 < x < 8
- Note ∞ always uses (or)
- Not to be confused with set notation





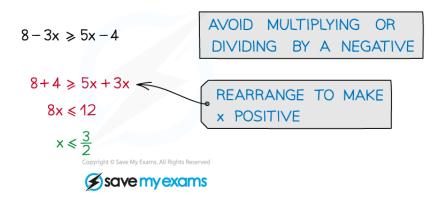


### Skills for solving linear inequalities

- representing and interpreting inequalities displayed on a number line
- writing and interpreting set notation
  - eg  $\{x: x > 1\} \cap \{x: x \le 7\}$  is the same as  $1 < x \le 7$
- writing and interpreting interval notation
  - eg [-4, 6) is the same as -4 ≤ x < 6</p>

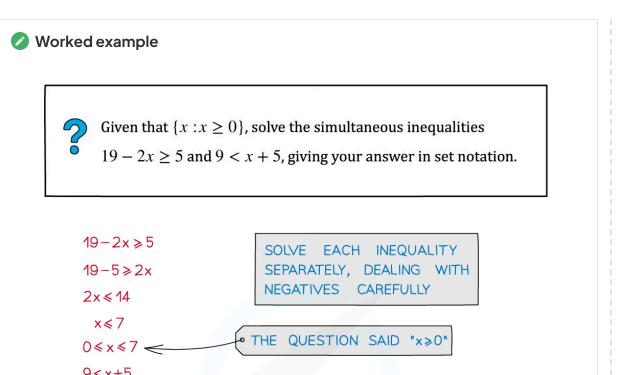
### How do I solve linear inequalities?

- Treat the inequality as an equation and solve
  - avoid multiplying or dividing by a negative
  - if unavoidable, "flip" the inequality sign so  $< \rightarrow >$ ,  $\ge \rightarrow \le$ , etc
  - try to rearrange to make the x term positive

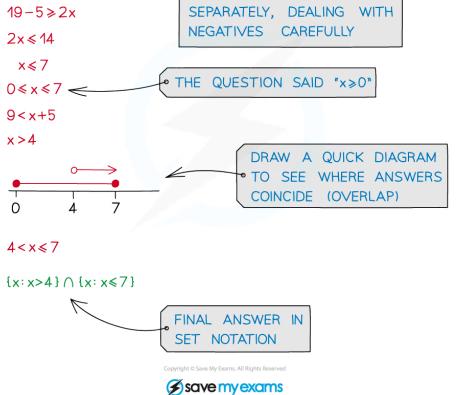


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## 2.4.2 Quadratic Inequalities

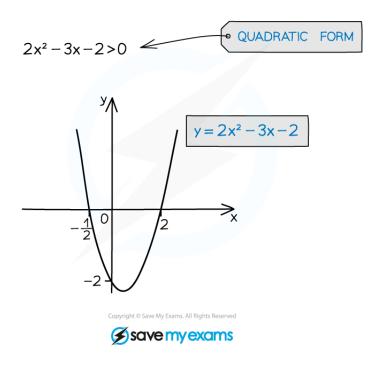
# Your notes

## **Quadratic Inequalities**

### Quadratic inequalities

- Similar to quadratic equations quadratic inequalities just mean there is a range of values that satisfy the solution
- Sketching a quadratic graph is essential

Can involve the discriminant or applications in mechanics and statistic

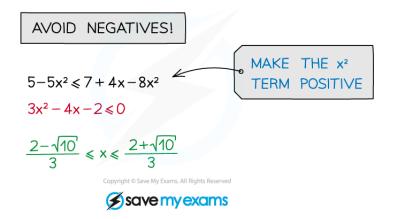


### How do I solve quadratic inequalities?

- STEP 1: Rearrange the inequality into quadratic form with a positive squared term
  - $ax^2 + bx + c > 0 (>, <, \le or \ge)$
- STEP 2: Find the roots of the quadratic equation
  - Solve  $ax^2 + bx + c = 0$  to get  $x_1$  and  $x_2$  where  $x_1 < x_2$
- STEP 3: Sketch a graph of the quadratic and label the roots
  - As the squared term is positive it will be "U" shaped
- STEP 4: Identify the region that satisfies the inequality



- For  $ax^2 + bx + c > 0$  you want the region above the x-axis
  - The solution is  $x < x_1$  or  $x > x_2$
- For  $ax^2 + bx + c < 0$  you want the region below the x-axis
  - The solution is  $x > x_1$  and  $x < x_2$
  - This is more commonly written as  $x_1 < x < x_2$
- avoid multiplying or dividing by a negative number
  if unavoidable, "flip" the inequality sign so < → >, ≥ → ≤, etc
  - avoid multiplying or dividing by a variable (x) that could be negative
     (multiplying or dividing by x² guarantees positivity (unless x could be 0) but this can create extra,
     invalid solutions)
  - **do** rearrange to make the x<sup>2</sup> term positiveBe careful:



#### Solving quadratic inequalities on a calculator

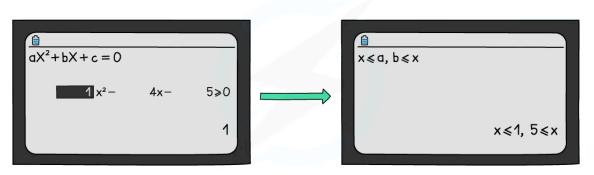
Be aware of unconventional ways calculators can display an answer
 eq 8 > x > 2 rather than 2 < x < 8</li>





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## Examiner Tip

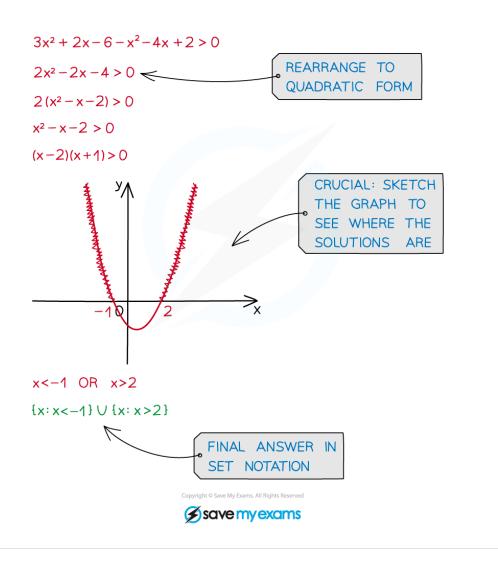
- A calculator can be super-efficient but some marks are for method.
- Use your judgement:
  - is it a "show that" or "prove" question?
  - how many marks?
  - how long is the question?







Find the set of values for which  $3x^2 + 2x - 6 > x^2 + 4x - 2$  giving your answer in set notation.



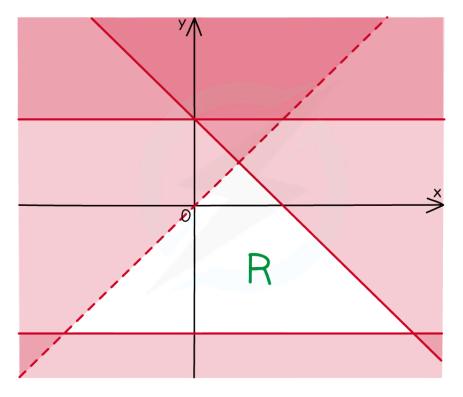
## 2.4.3 Inequalities on Graphs

## Your notes

## Inequalities on Graphs

### Inequalities on graphs

• Inequalities can be represented on graphs by shaded regions and dotted or solid lines







- These inequalities have two variables, **x** and **y**
- Several inequalities are used at once
- The solution is an **area** on a graph (often called a **region**)
- The inequalities can be linear or quadratic

### How do I draw inequalities on a graph?

- Sketch each graph
  - If the inequality is strict (< or >) then use a dotted line
  - If the inequality is **weak** (≤ or ≥) then use a **solid line**
- Decide which side of the line satisfies the inequality



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- Choose a coordinate on each side and **test** it in the inequality
  - The origin is an easy point to use
- If it satisfies the inequality then that whole side of the line satisfies the inequality
  - For example: (0,0) satisfies the inequality  $y < x^2 + 1$  so you want the side of the curve that contains the origin



STEP 1: FIND THE KEY POINTS FOR EACH GRAPH e.g. x+y=4 CROSSES THE AXES

AT (0,4) AND (4,0)

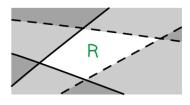
STEP 2: DRAW LINE FOR EACH INEQUALITY

--- DOTTED FOR < OR >
———— SOLID FOR ≤ OR ≥

STEP 3: SHADE THE UNWANTED AREA



STEP 4: LABEL THE UNSHADED AREA



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## Examiner Tip

- **Recognise** this type of inequality by the use of **two** variables
- You may have to **deduce** the inequalities from a **given** graph
- Pay careful attention to which **region** you are **asked to shade**
- Sometimes the exam could ask you to shade the region that **satisfies the inequalities this means** you should **shade** the region that is **wanted**.
  - If you're unsure, you could ...
  - ... draw the (dotted and/or solid) lines in on the answer diagram and use a rough sketch to find the region required ...
    - ... and/or ...
  - ... write clearly you have "shaded the unwanted area"
- As long as your final answer is clear you should get the marks!





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Worked example	



Your notes



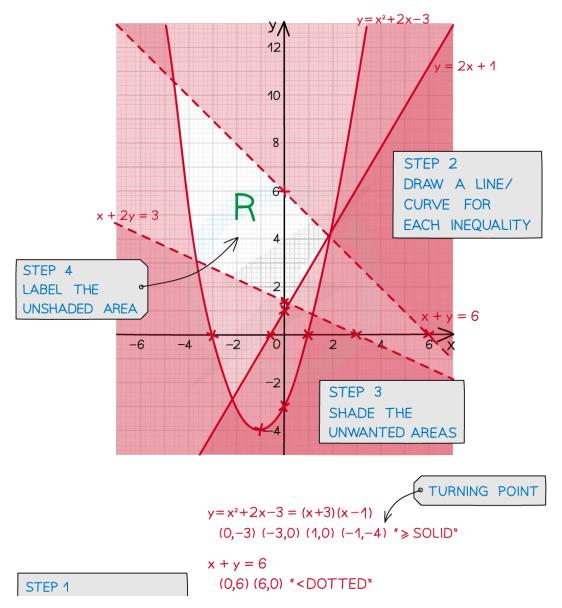
On the graph below show the region bounded by the following inequalities:

$$y \ge x^2 + 2x - 3 \qquad \qquad x + y < 6$$

$$x + y < 6$$

$$y \ge 2x + 1$$

$$y \ge 2x + 1 \qquad \qquad x + 2y > 3$$



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FIND THE KEY POINTS FOR EACH GRAPH

$$y = 2x + 1$$
  
 $(0,1) \left(\frac{-1}{2},0\right) \text{ "} \geqslant \text{SOLID"}$   
 $x + 2y = 3$   
 $(0,\frac{3}{2}) (3,0) \text{ "} > \text{DOTTED"}$   
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