A background image showing a coastal region with a color-coded map overlay indicating ground movement speeds. The colors range from dark blue (0 m/yr) to light orange (100 m/yr). A vertical color bar on the right side of the slide also shows this gradient.

Speed m/yr

0

100

EARTHSCOPE ISCE+ INSAR TRAINING

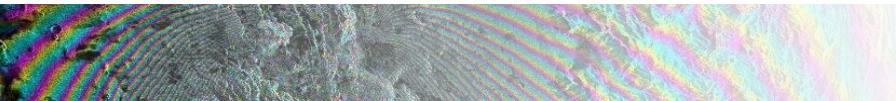
Lecturer:

Franz J Meyer, Geophysical Institute, University of Alaska Fairbanks, Fairbanks; fjmeyer@alaska.edu

Motion Mapping using Template Matching and Feature Tracking



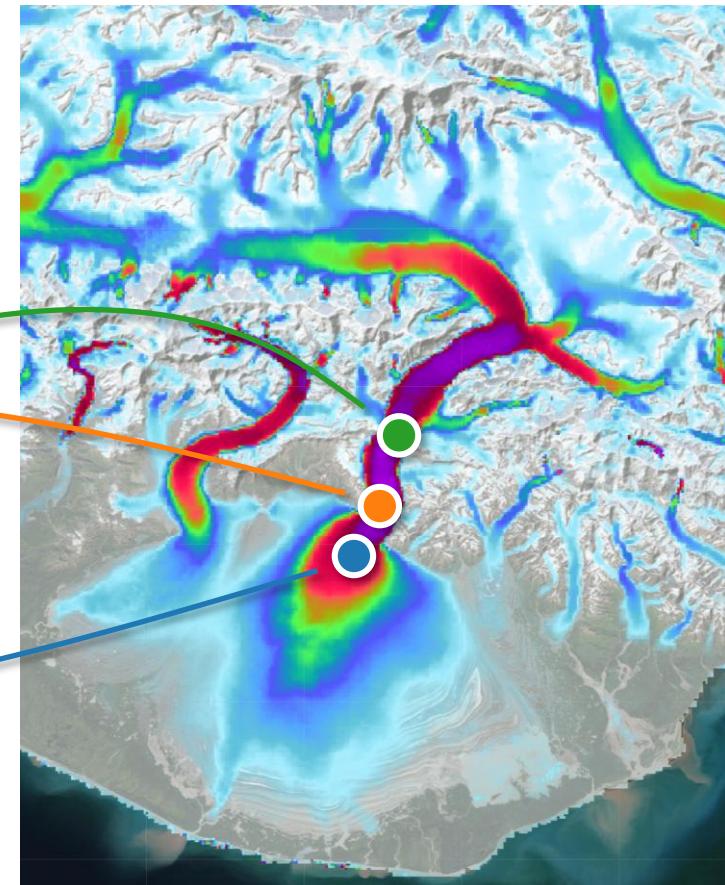
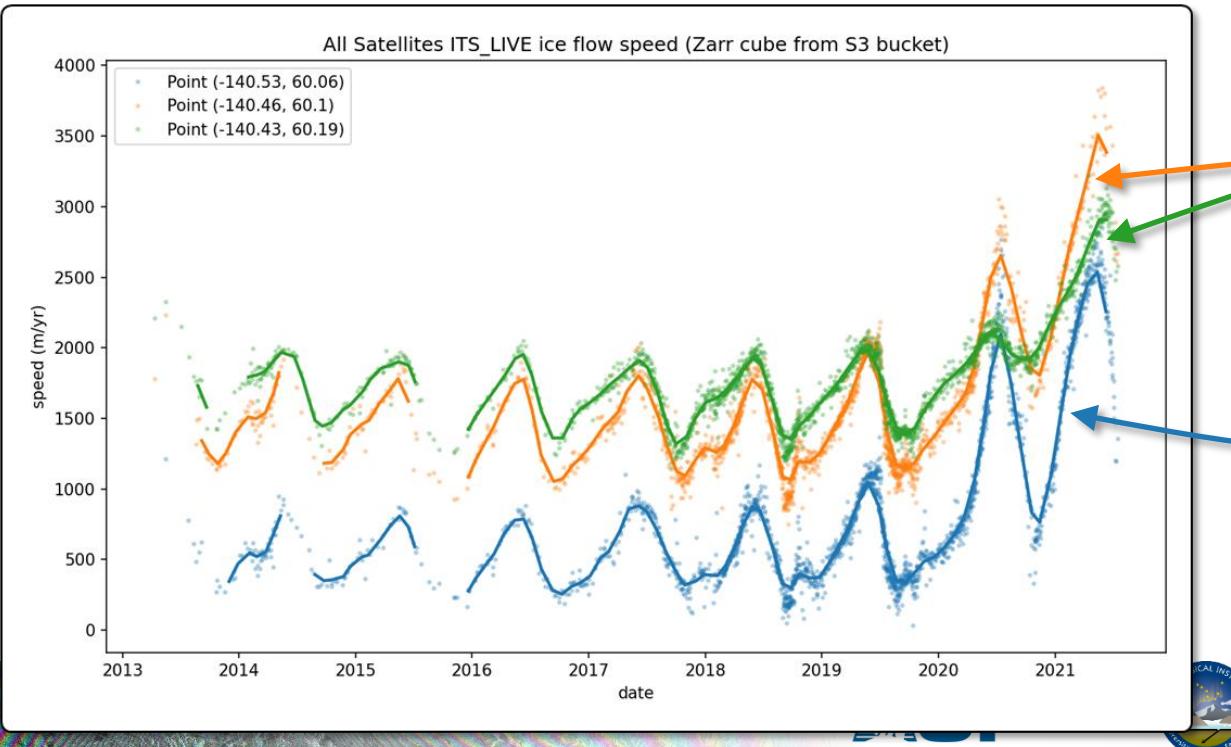
WHY A SECOND CONCEPT TO MOTION MAPPING?



Why Do We Need A Second Concept for Measuring Motion?

Limitation of InSAR

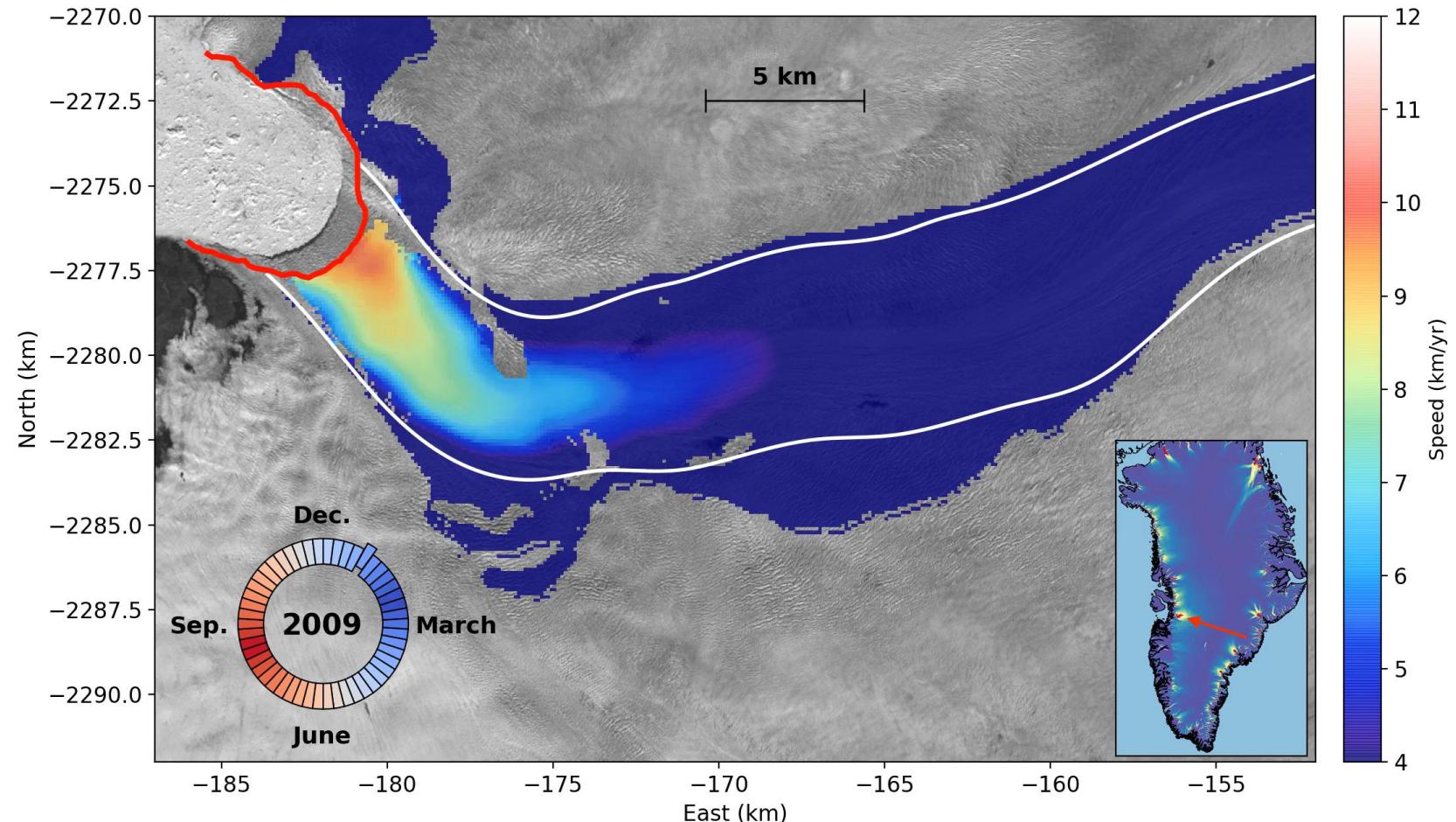
- InSAR-based motion tracking requires that the two images of an InSAR pair are aligned at a sub-pixel level ($\approx 1/100$ of a pixel)
- Assume pixel size of 80m (Sentinel-1 image after 20×4 multi-looking)
 - Maximum allowed movement between images: $\Delta x_{max} = 80/100 [m] = 0.8 [m]$
 - For images 12 days apart \rightarrow maximum measurable velocity: $v_{max} = 24 [m/yr]$
- Example: Glacier velocity Malaspina Glacier



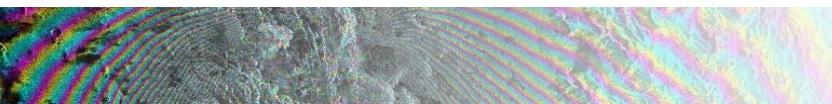
Topic 3: Surface Displacement from Images

Fast(er) Motion Monitoring [m/y to km/y] Using Feature Tracking and Optical Flow

- Lot's of surface motions can be too fast for InSAR to work (see lectures later on):
 - Glacier motion (and variations thereof)
 - Sea Ice motion
 - Large earthquake motion
- We will use feature tracking and optical flow techniques to estimate motion velocities and directions



Bryan Riel. 2020. [Animation of time-dependent velocity magnitudes for Sermeq Kujalleq \(Jakobshavn Isbræ\) from 2009 - 2019](#). Arctic Data Center. doi:[10.18739/A2W66990B](https://doi.org/10.18739/A2W66990B).





TEMPLATE AND FEATURE MATCHING PRINCIPLES

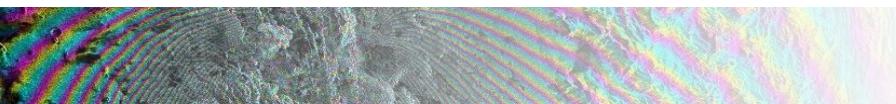


Image Matching Use Cases

Matching entities

- **Images from different viewpoints**
(e.g. stereo parallax matching; tie points)
- **Images from different times**
(e.g. change detection; terrain displacements)
- **Images from different sensors/sensor channels**
(multi-modal; e.g. co-registration; co-registration of channels or sub-systems; fusion)
- **Images of different ground, illumination and atmospheric conditions**
- **Images and templates / models (reference pattern, image chips)**
(e.g. fiducial marks, ground control point data base, objects)
- **DEM^s or other spatial datasets**

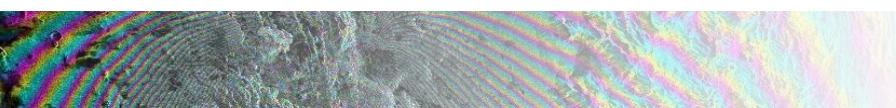
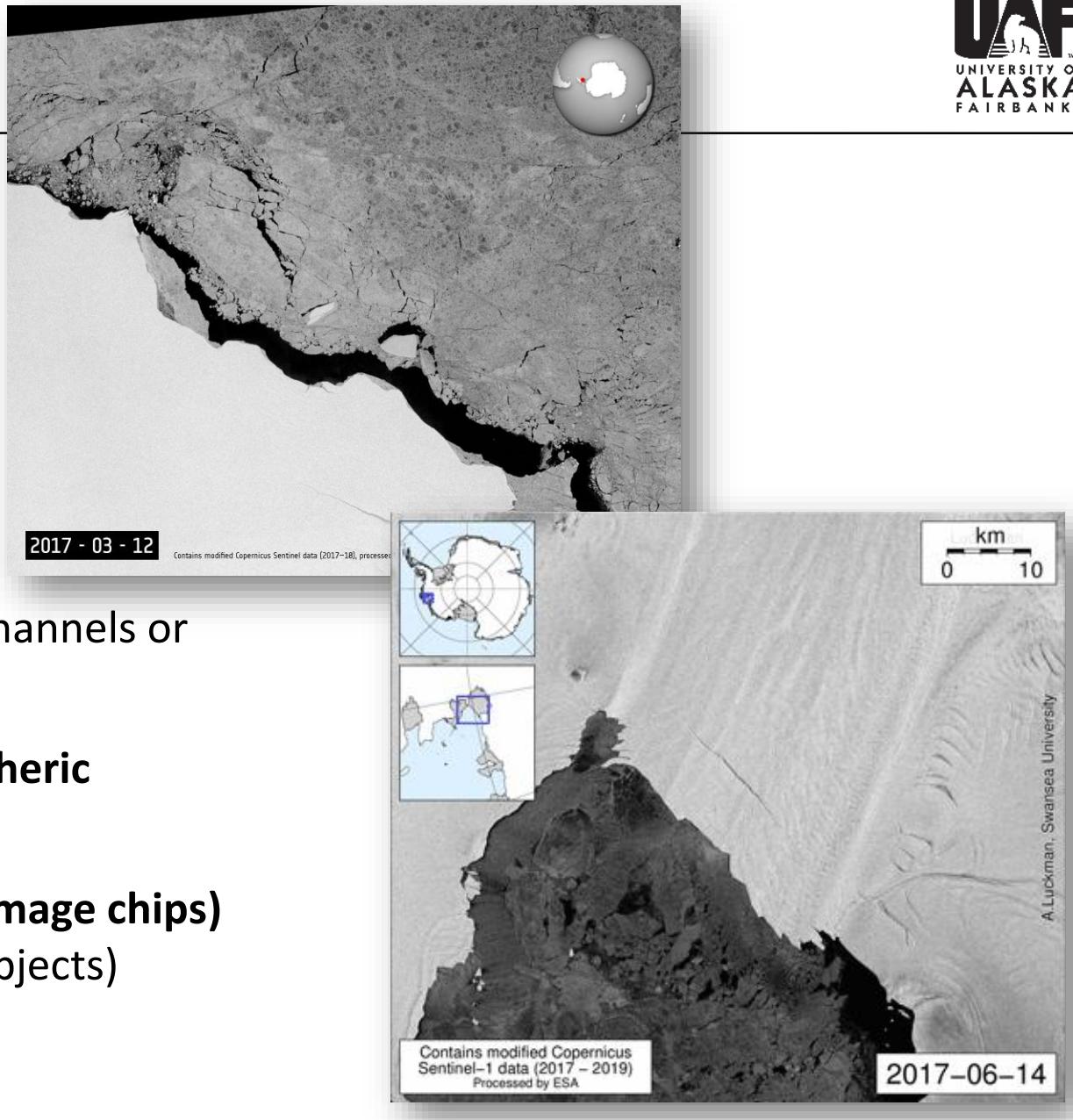


Image Matching Approaches

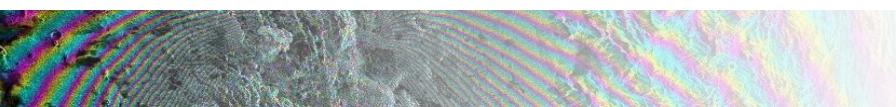
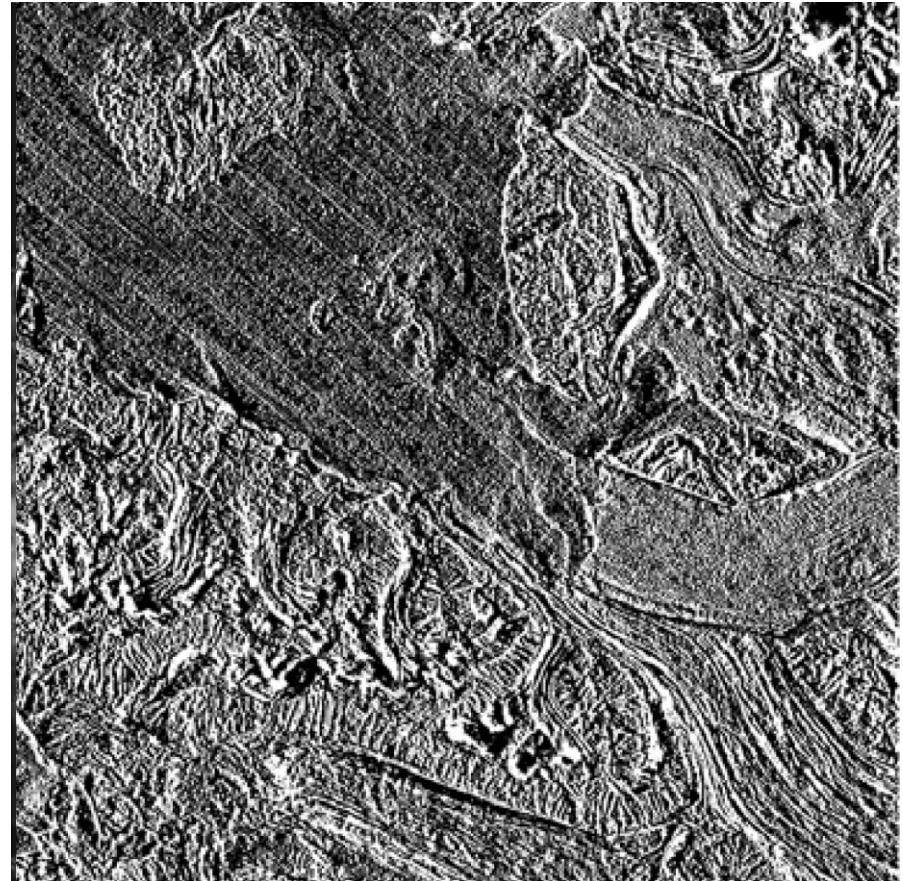
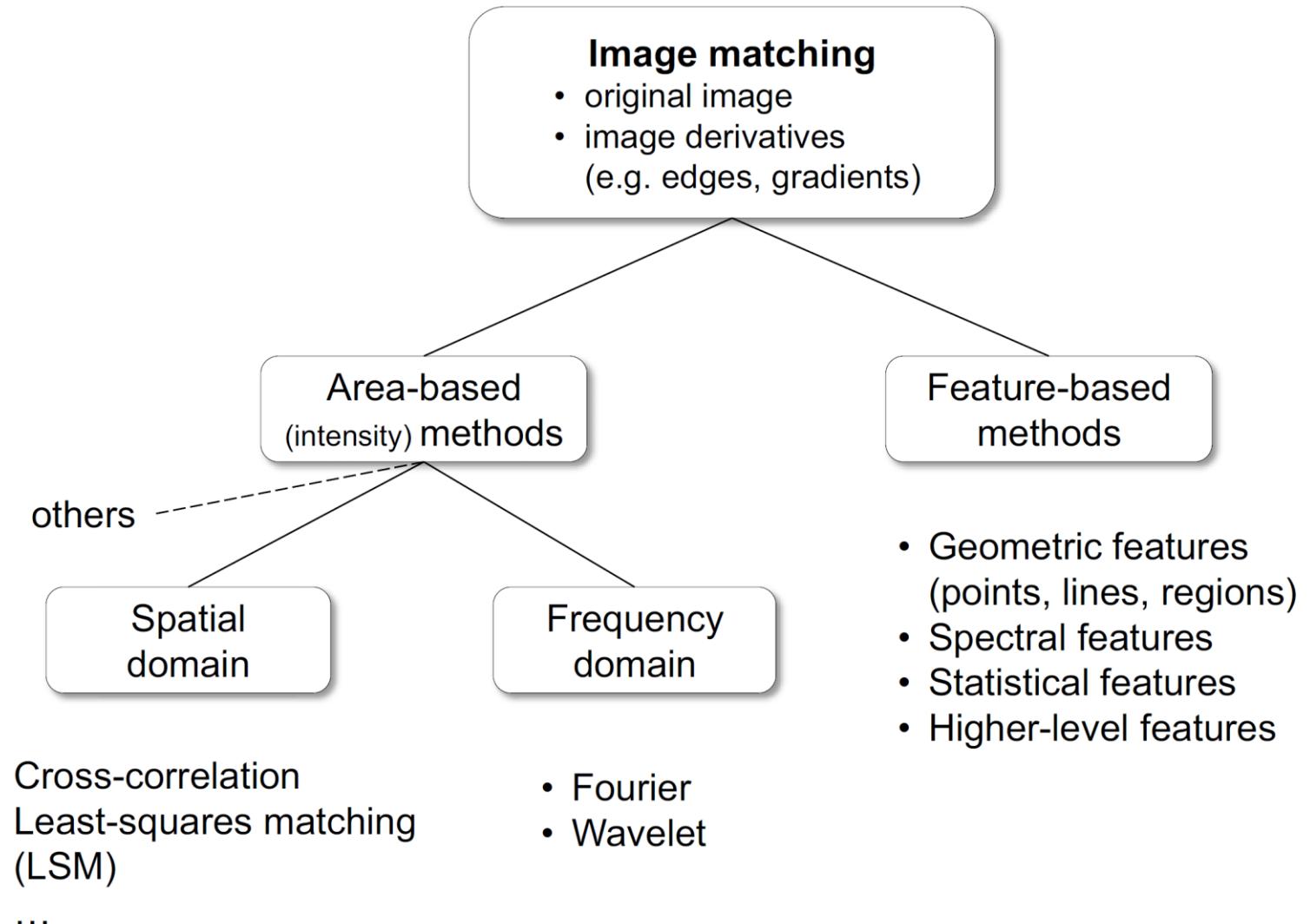
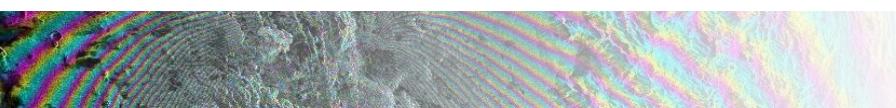
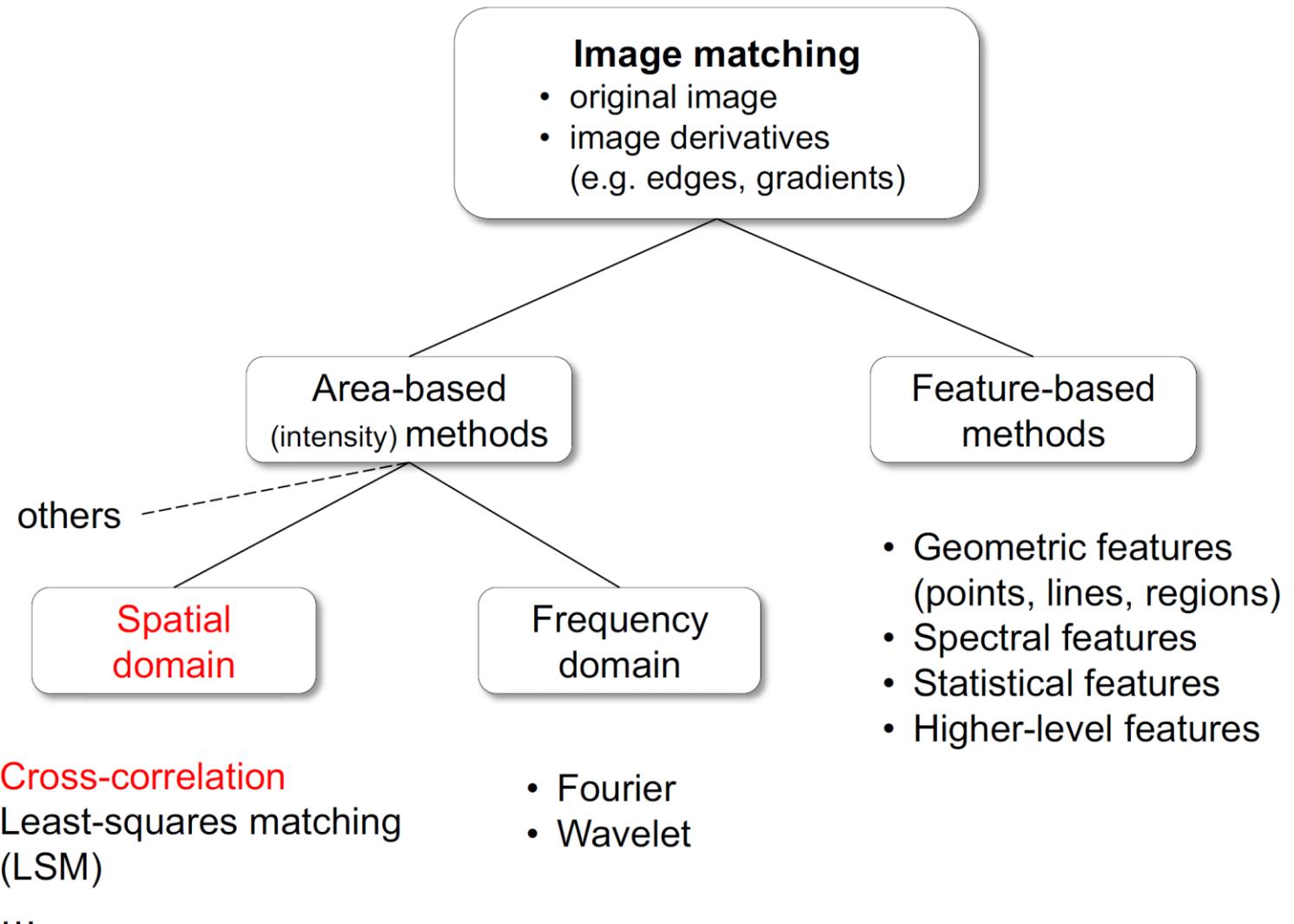


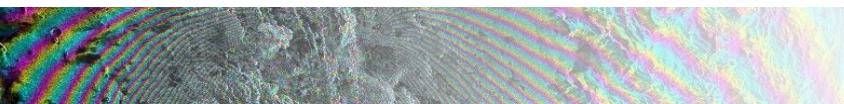
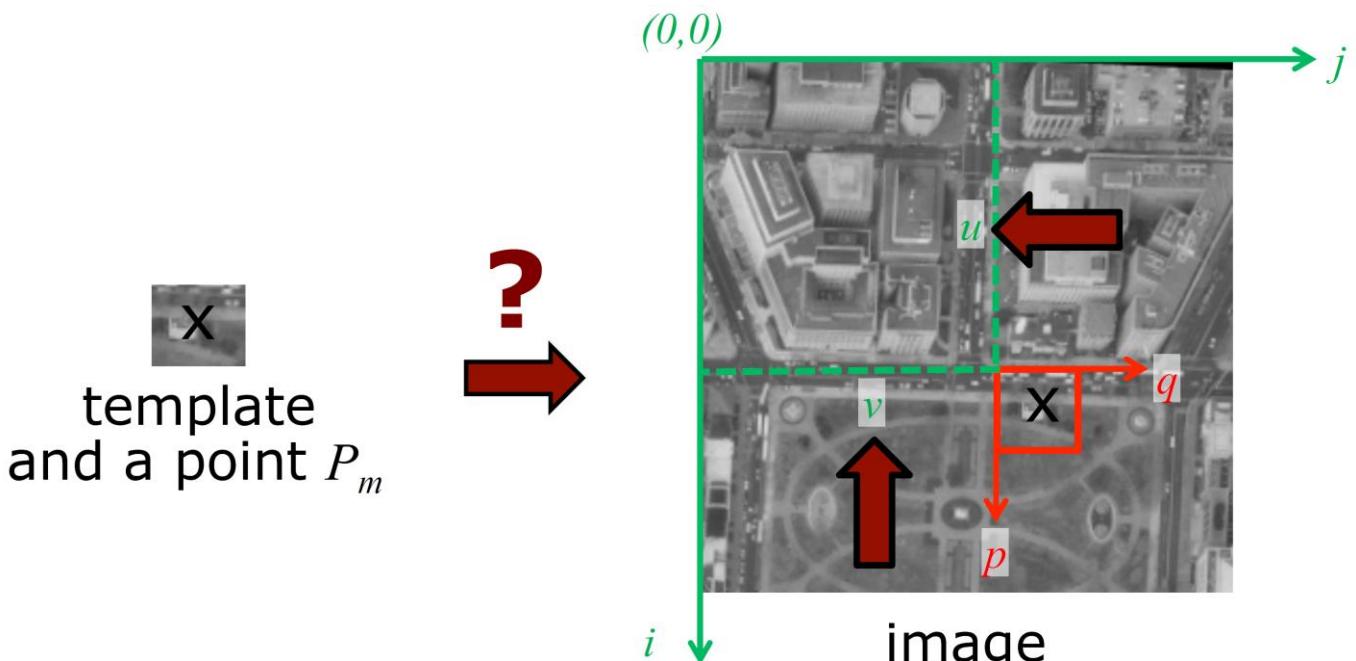
Image Matching Approaches



Cross Correlation-Based Image Matching

Cross Correlation:

- **Cross correlation is a powerful tool to:**
 - Find certain image content in an image
 - Determine its location in the image
- **Key assumption: Images differ only by**
 - Translation
 - Brightness
 - Contrast
- **Cross correlation is a template matching approach**
 - Find the location of a small template image within a (larger) image
 - Usually: size of template \ll size of image



Cross Correlation Principle

Cross Correlation:

- Given image $g_1(i, j)$ and template $g_2(p, q)$, find offset $[\hat{u}, \hat{v}]$ between g_1 and g_2

Assumptions:

- Geometric Transformation

$$T_G: \begin{bmatrix} p \\ q \end{bmatrix} = \begin{bmatrix} i \\ j \end{bmatrix} - \begin{bmatrix} u \\ v \end{bmatrix}$$

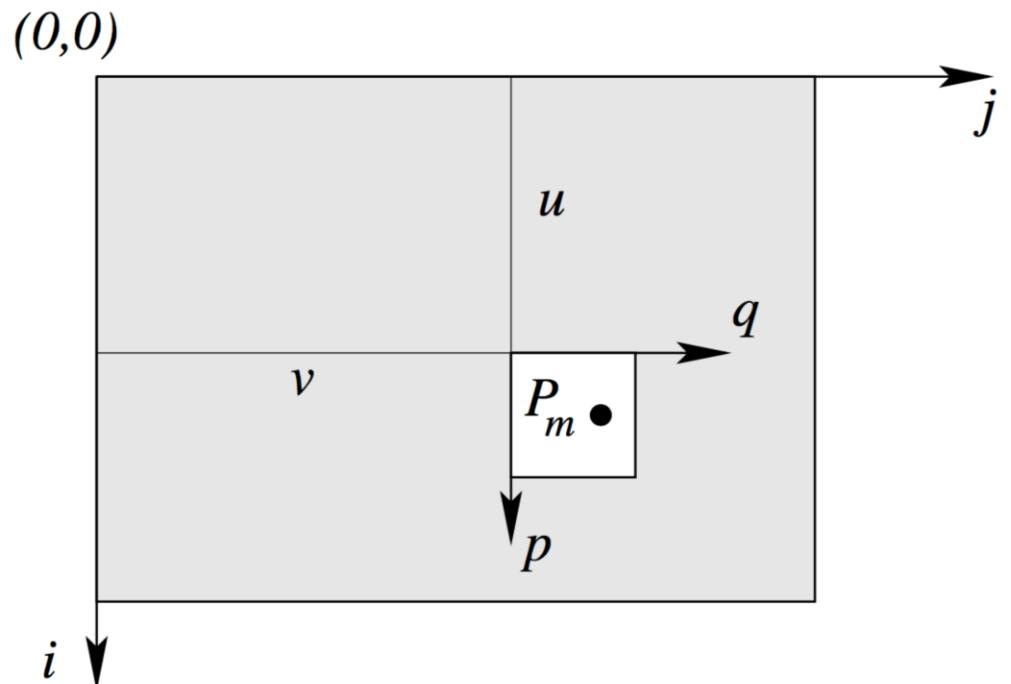
- Two unknown parameters: $p_g = [u, v]^T$

- Radiometric transformation

$$T_I: g_2(p, q) = a + b g_1(i, j)$$

- Intensities of each pixel in g_2 are linearly dependent on those of g_1
- Two additional unknown parameters: $p_R = [a, b]^T$

Task: Find the offset $[\hat{u}, \hat{v}]$ that maximizes the similarities of the corresponding intensity value

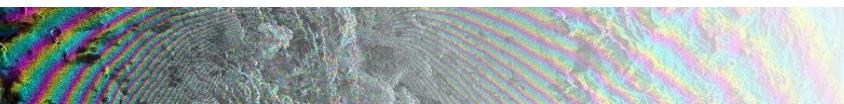


Cross Correlation quantifies image template similarity



Examples of Template-Based Similarity Measures

f	Standard	Normalised
Absolute	$\sum A - B $	$\frac{\sum A - B }{\sqrt{(\sum A)(\sum B)}}$
Square	$\sum (A - B)^2$	$\frac{\sum (A - B)^2}{\sqrt{(\sum A^2)(\sum B^2)}}$
Power	$\sum A - B ^p$	$\frac{\sum A - B ^p}{\sqrt{(\sum A ^p)(\sum B ^p)}}$
Correlation	$\sum AB - \frac{(\sum A)(\sum B)}{N}$	$\frac{\sum AB - \frac{(\sum A)(\sum B)}{N}}{\sqrt{\left(\sum A^2 - \frac{(\sum A)^2}{N} \right) \left(\sum B^2 - \frac{(\sum B)^2}{N} \right)}}$



Cross Correlation: Search Strategy

How to Find the Offset that Maximizes Similarity?

Exhaustive Search

- For all offsets $[u, v]$ compute Cross Correlation $\rho(u, v)$
- Select offset $[u, v]$ for which $\rho(u, v)$ is maximized

More Efficient Approach: Use Image Pyramid

- Iteratively use resized images from small to large
- Start on top of the pyramid → match gives initialization for next level

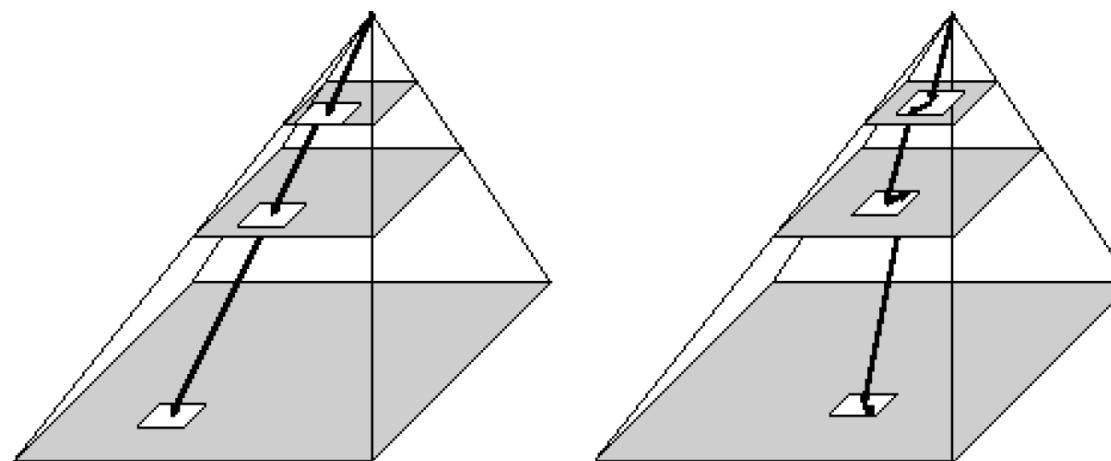
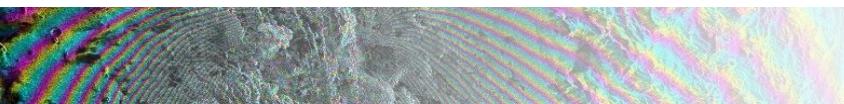
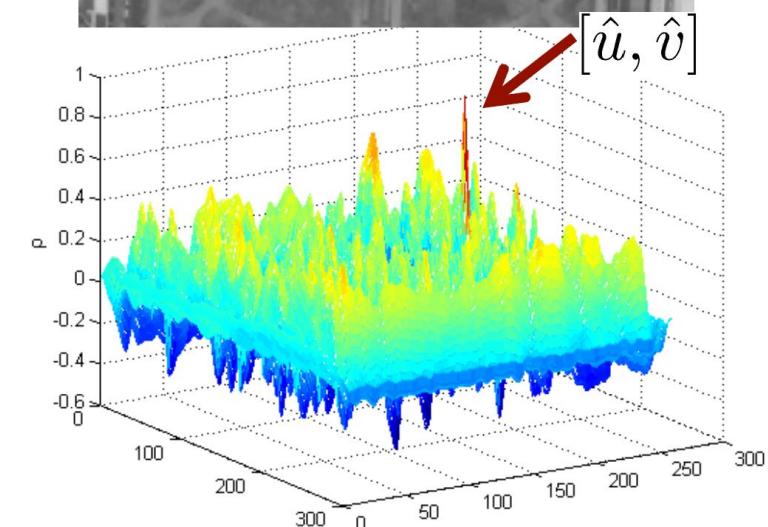
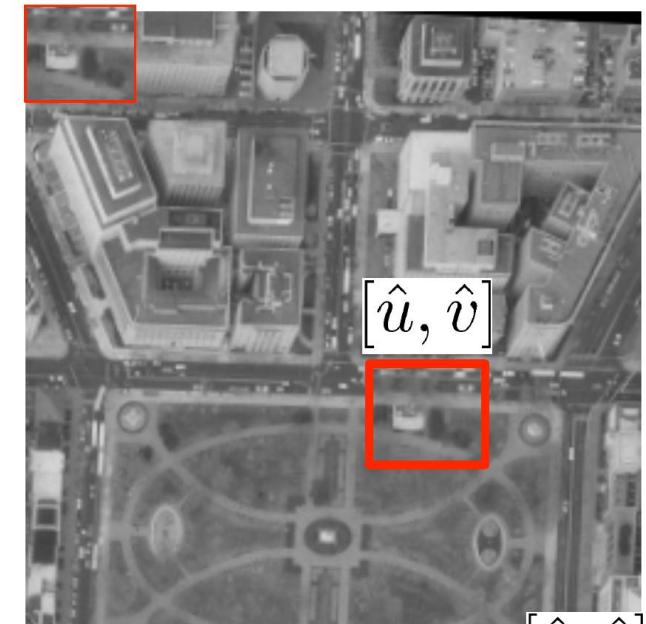


Image courtesy: Förstner

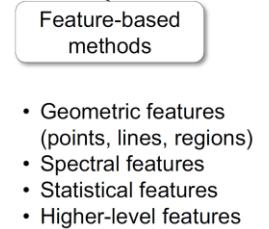
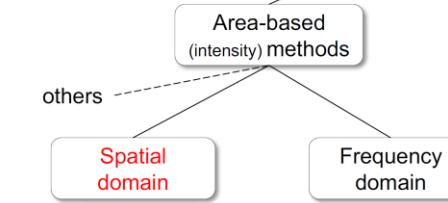
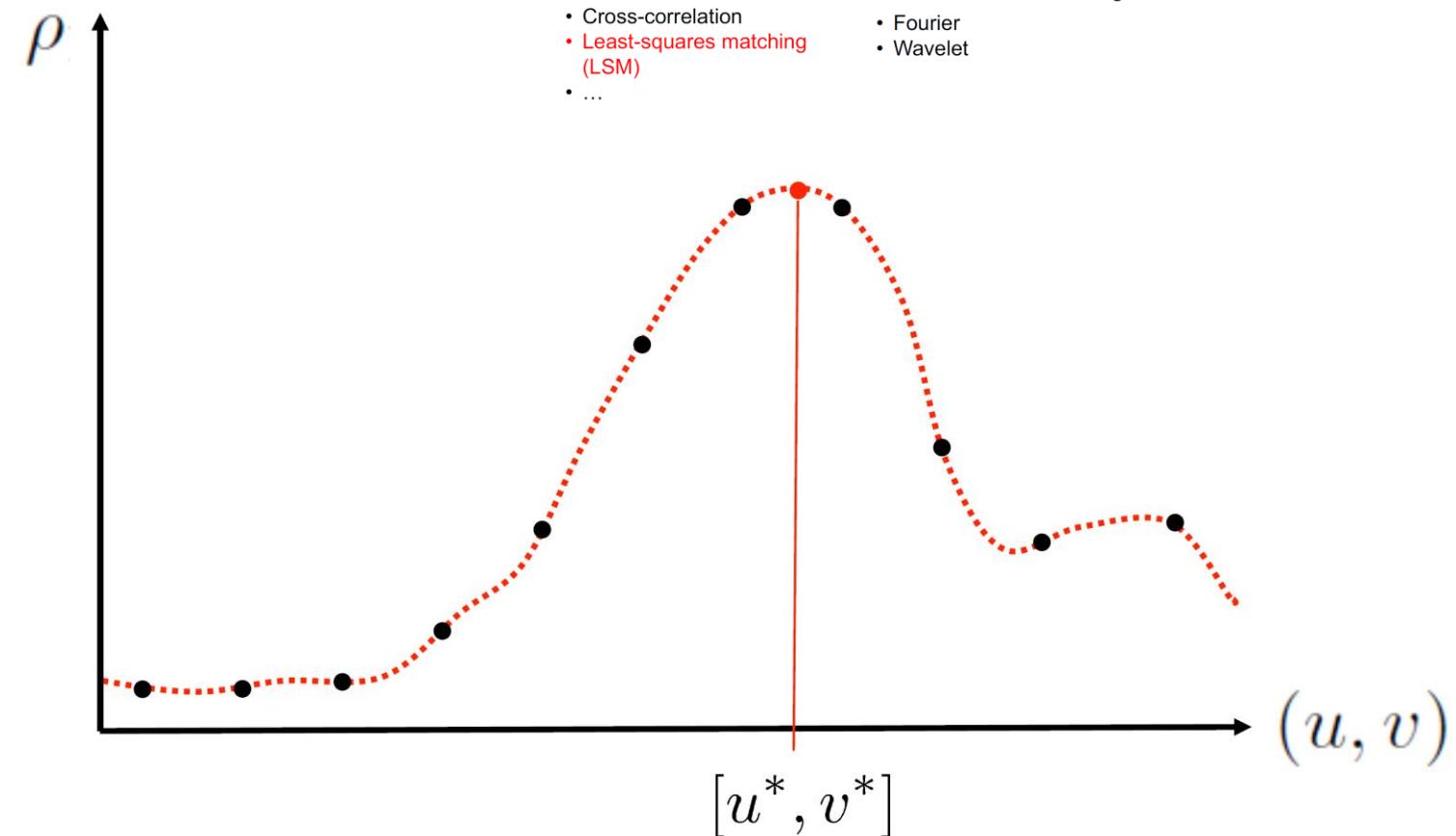


Cross Correlation: Sub-Pixel Estimation of Offsets

- Result of template matching by cross correlation provides initially only integer-valued offsets
- More precise estimate can be obtained through subpixel estimation

Procedure:

- Fit a locally smooth surface through $\rho(u, v)$ around the initial position $[\hat{u}, \hat{v}]$
- Estimate it's local maximum using **least-squares matching** to arrive at subpixel estimate of offsets $[u^*, v^*]$



- Cross-correlation
- Least-squares matching (LSM)
- ...
- Fourier
- Wavelet

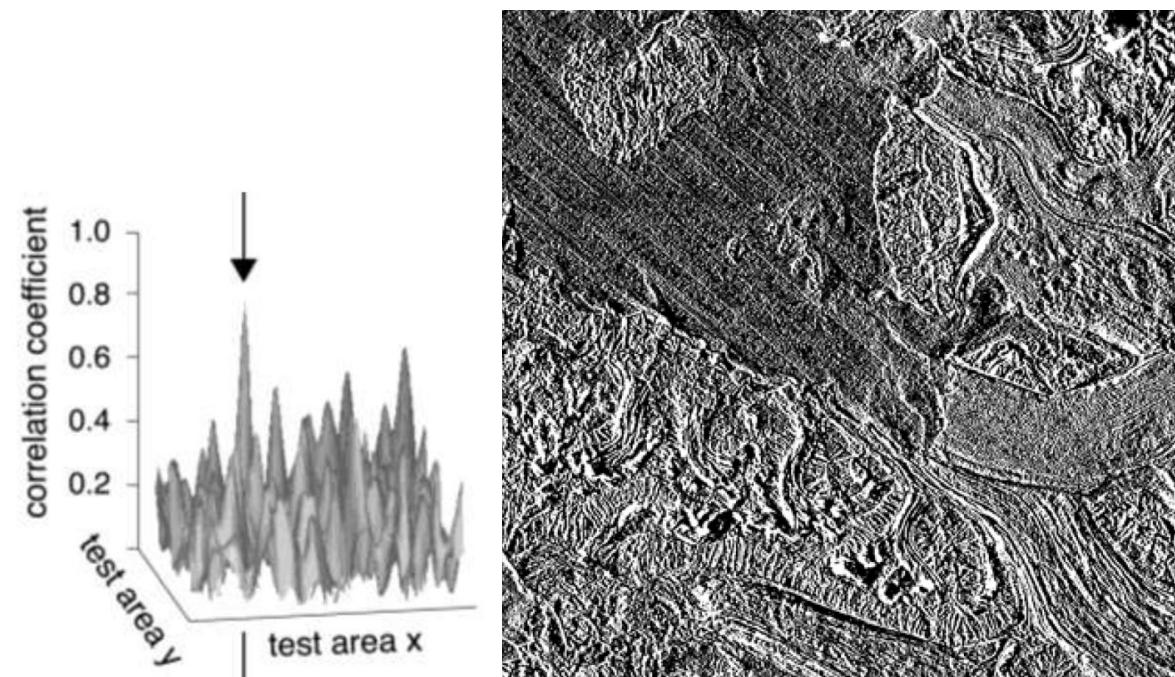
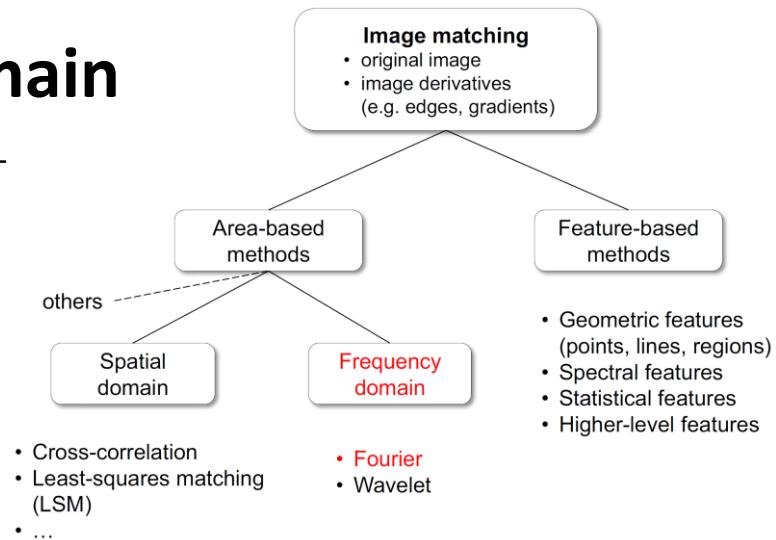


Side Note: Image Matching In the Frequency Domain

- Correlation is a time demanding process when done in the spatial domain, but in the frequency domain this process can be done much more efficiently with a single multiplication (convolution theorem):

$$CC(i,j) = \text{IFFT}(F(u,v)G^*(u,v))$$

- Image normalization cannot be done easily in frequency domain
- Approaches of normalization:
 - Phase correlation
 - Orientation images



Feature-Based Image Matching

- Feature-based approaches use easily identifiable image features such as corners, edges, street corners ...
- Identification and matching of features was addressed in Lecture 5 and include techniques such as **SIFT** = Scale Invariant Feature Transform

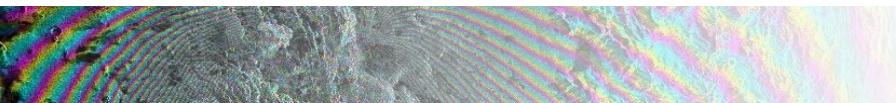
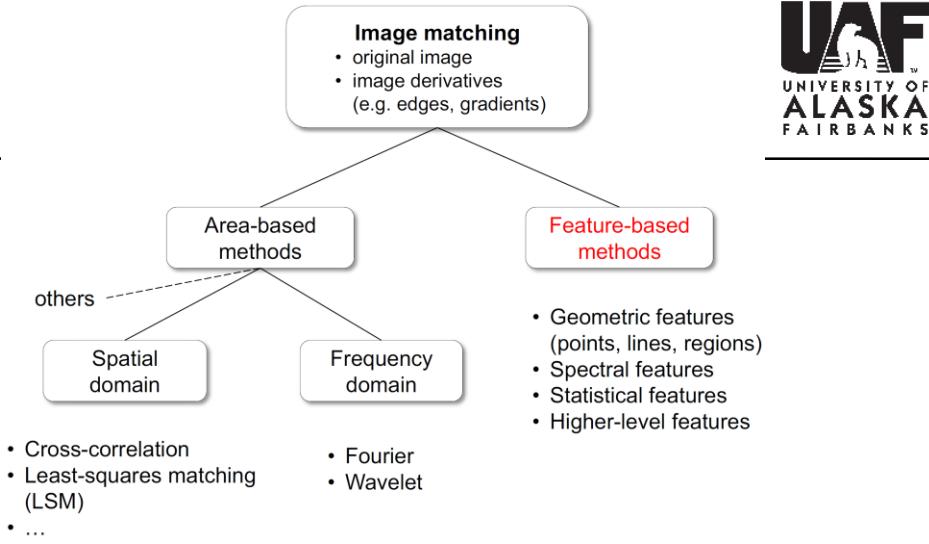
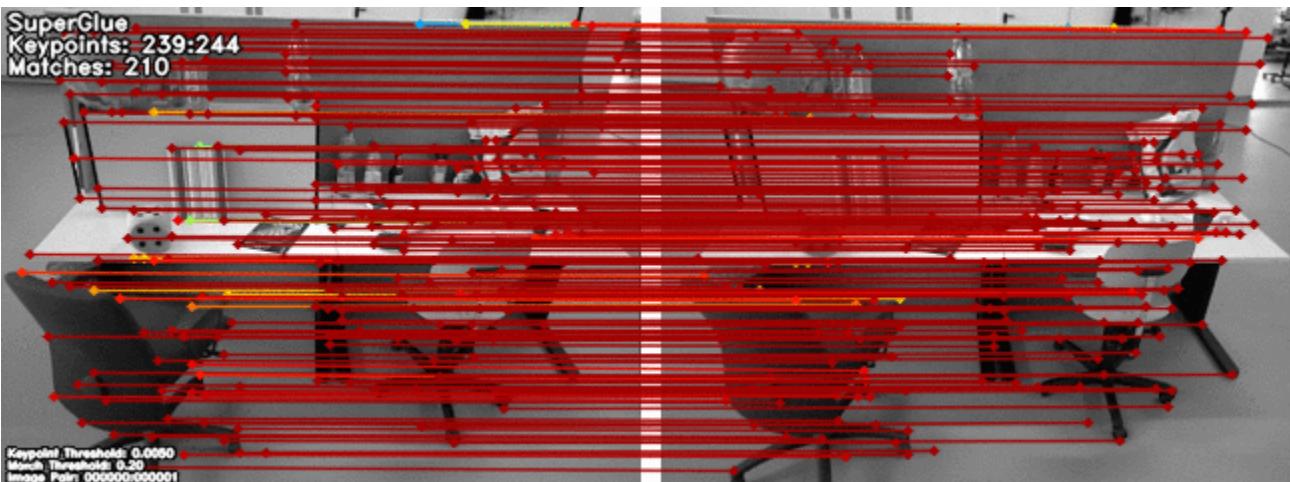




IMAGE PRE- AND POST-PROCESSING ERROR SOURCES

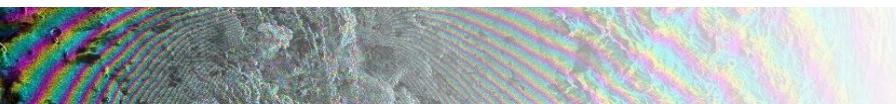
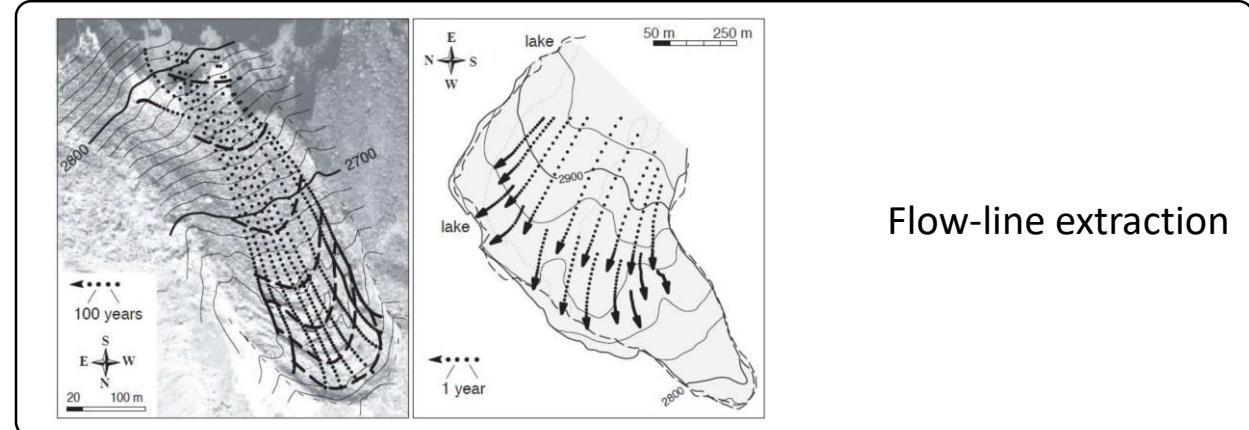


Image Pre-Processing and Product Post-Processing

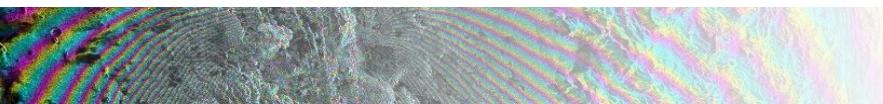
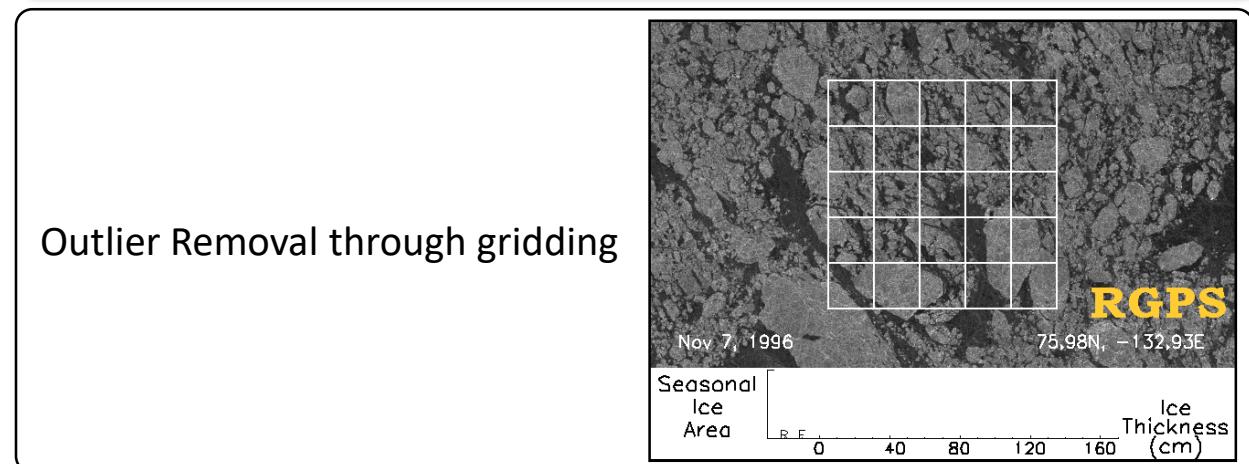
Pre-Processing:

- Image enhancements / transforms such as gradient calculation and noise filtering
- Image pyramid calculation to speed up processing
- Image alignment
- Interest point extraction for feature-based methods



Post-Processing:

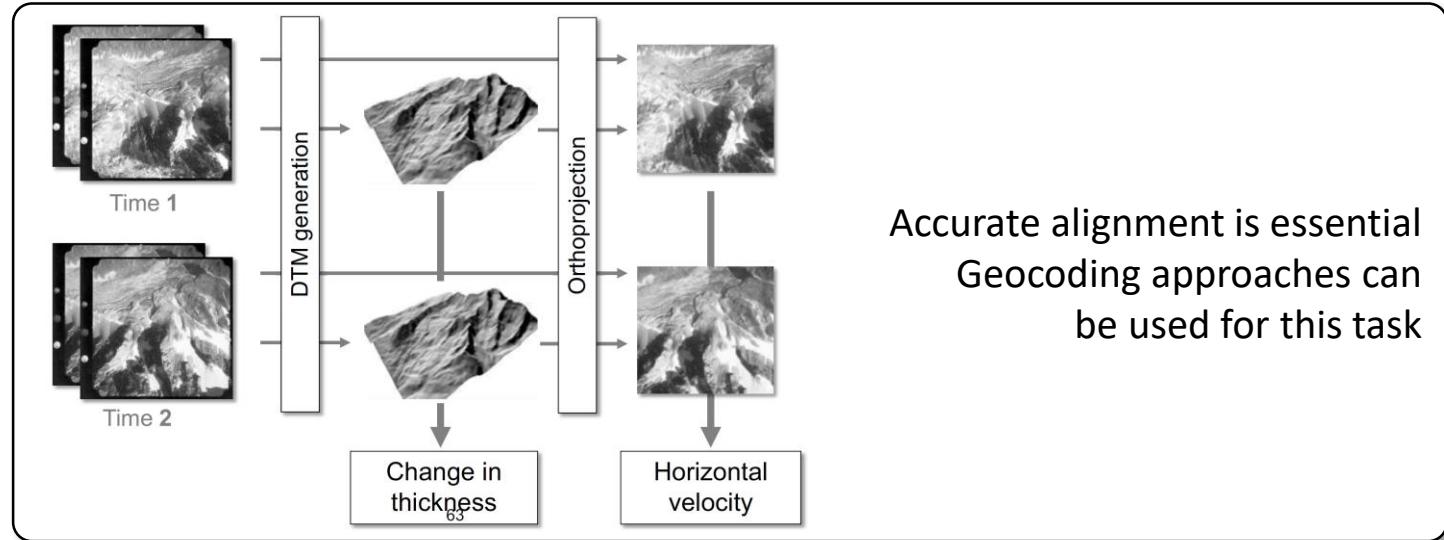
- Outlier-detection and removal (e.g., using geometric constraints; neighborhoods; quality metrics)
- Filtering
- Derivatives
- Extraction of streamlines and trajectories



Error Sources and Problematic Areas for Image Matching

Error Sources

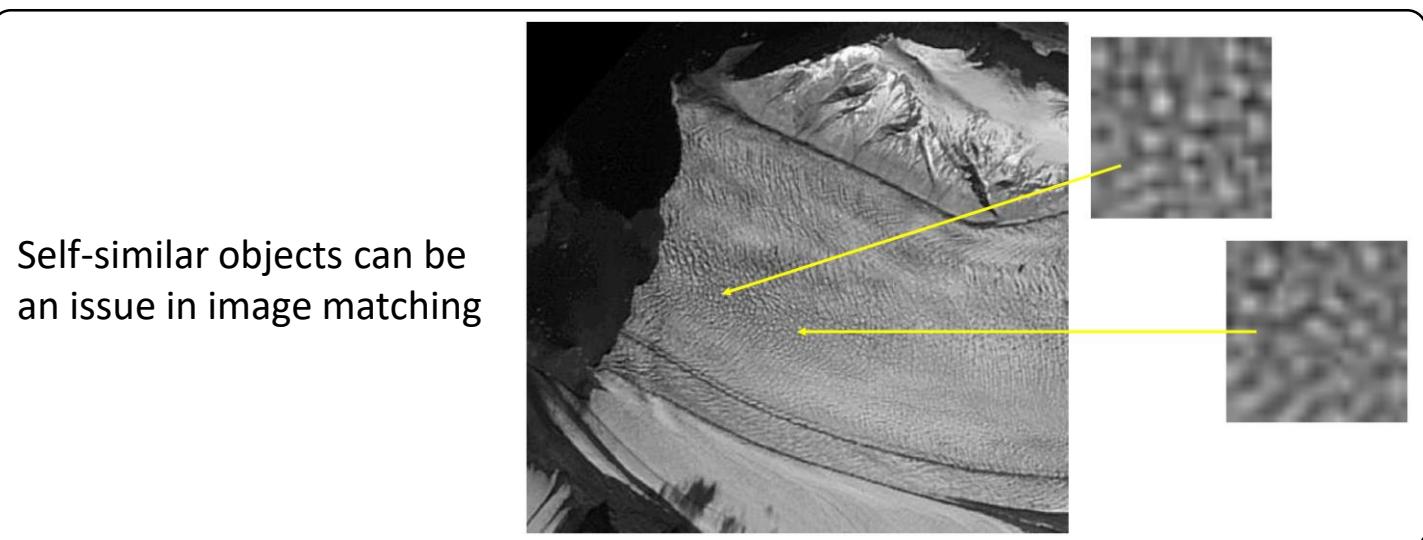
- Image alignment
- Matching error (mismatch; e.g. similar features, lack of contrast)
- Matching accuracy
- Self similar objects



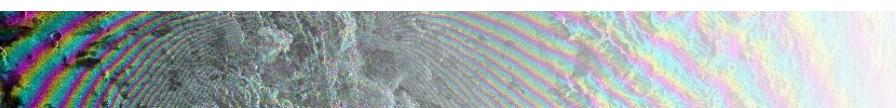
Accurate alignment is essential
Geocoding approaches can
be used for this task

Problem Areas:

- Areas with low contrast (accumulation areas)
- Areas with much surface transformation
- Cloudy areas



Self-similar objects can be
an issue in image matching



Accuracy of Cross-Correlation Estimates in SAR Images

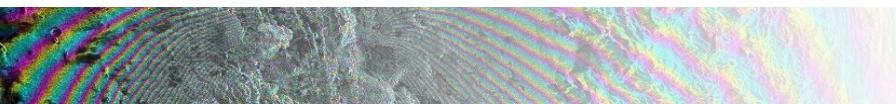
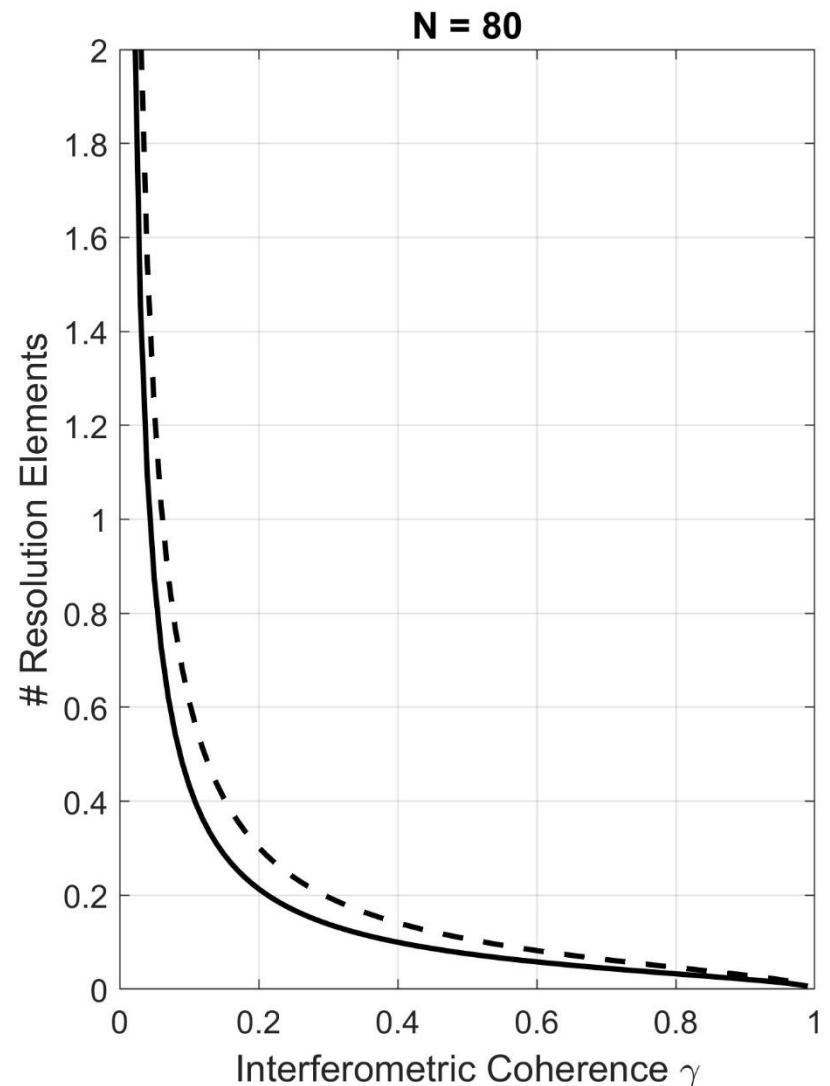
Speckle Tracking

- SAR images lend themselves well for template-based offset tracking because**
 - SAR images have speckle noise → images are very noisy
 - Noise can be tracked with high accuracy if noise remains coherent
- Speckle tracking can be implemented either through**
 - Complex Cross-Correlation, OR
 - Amplitude-only Cross-Correlation (see previous discussion)
- Speckle tracking accuracy can be calculated for coherent (σ_{CR}) & amplitude (σ_C) CC as function of interferometric coherence γ & the window size N used in CC calculation**

– **Coherent** CC accuracy: $\sigma_C = \sqrt{\frac{3}{2N}} \cdot \frac{\sqrt{1-\gamma^2}}{\pi\gamma}$

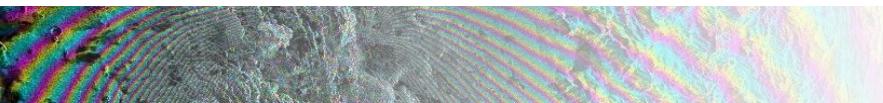
– **Amplitude** CC accuracy: $\sigma_A = \sqrt{\frac{3}{2N}} \cdot \frac{\sqrt{1-\gamma^2}}{\pi\gamma} \cdot \sqrt{2}$

Amplitude CC uses only half of the available information → factor of $\sqrt{2}$ less accurate



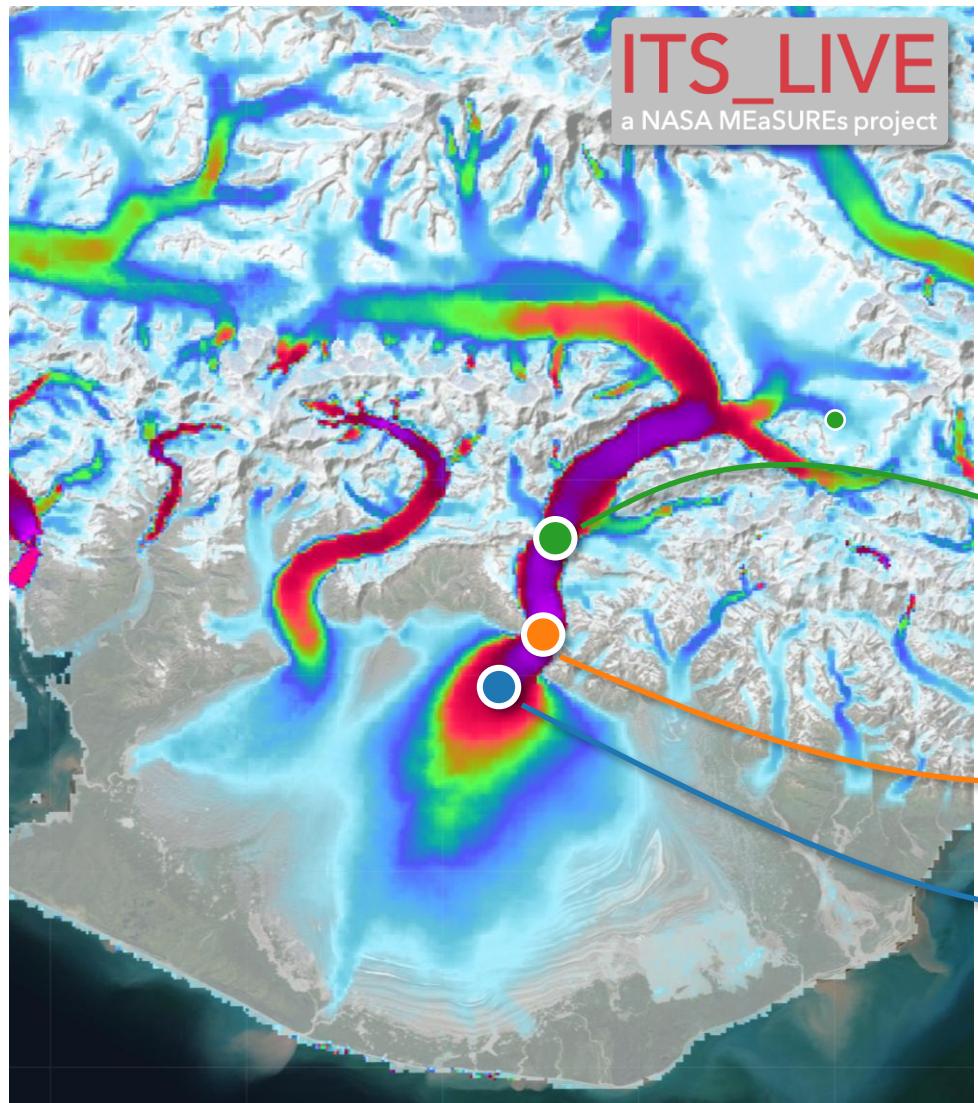


FEATURE MATCHING – AN EXAMPLE [PREPARATION FOR THE LAB]

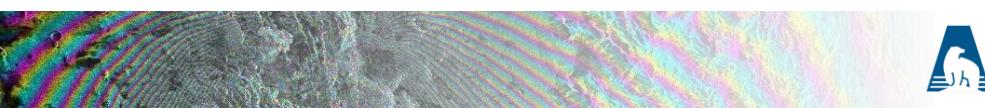
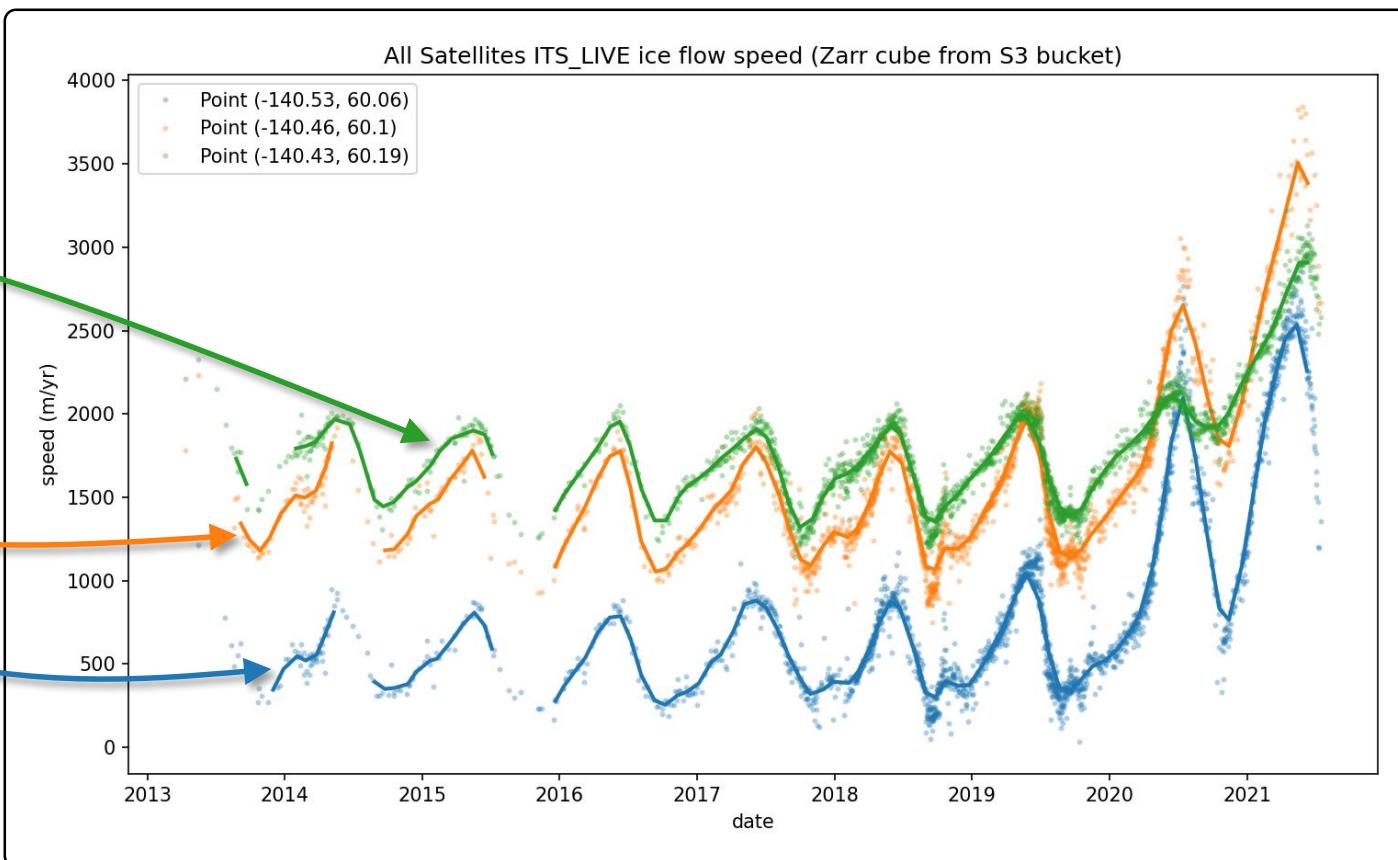


Why We Measure Displacements

Monitoring Surge of Malaspina Glacier, Alaska using Optical and SAR Data



ITS_LIVE is led by Alex Gardner, JPL and includes partners at UAF. The project uses Feature Tracking from Landsat, Sentinel-2, and Sentinel-1 data to monitor velocities at all glaciers in the world!



Think – Pair – Share:



- **Explore Glacier Velocity Information generated by ITS_LIVE**

- **Activity #1:** Explore ITS_LIVE archive

- Go to the project website at <https://its-live.jpl.nasa.gov/> and let's explore the data viewer on that page
 - Alternatively, you can access the data through the ITS_LIVE GitHub repository (https://github.com/nasa-jpl/its_live) and start the ITS_LIVE Binder Notebook (click on)
 - Follow the instructions to access the glacier velocity information
 - Pick your favorite glacier
 - Select points and plot velocity time series information
 - Look up some background on your glacier to understand what is happening at the site you picked

- **Activity #2:** Share your results

