xLR(k): deterministic bottom-up parsing ISCL-BA-06

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Recap: bottom-up parsing

- . Start from the input symbols, try to reduce the input to the sta Unlike top-down parsing where productions drive the parsing, in bottom-up parsing reduction is the main operation
- Reduction matches RHS of a grammar rule, and replaces it with its LHS
- A typical bottom-up parser has two basic operations
 reduce replace one more more symbols in the sentential form with their LHS
 non-terminal
- shift move the next unprocessed symbol from the input to the sentential form

Bottom-up (shift-reduce) parsing: an example

Bottom-up (shift-reduce) parsing: an example

SENT. FORM	INPUT	Action
	dnvan	shift

Bottom-up (shift-reduce) parsing: an example

 $S \rightarrow NP \ VP \quad NP \rightarrow d \ AN \quad NP \rightarrow AN \ VP \rightarrow v \ NP \quad AN \rightarrow a \ AN \rightarrow n$

Sent. Form	Input	Action
dn	van	r. AN → n
dn	van	shift

shift/reduce conflict

Bottom-up (shift-reduce) parsing: an example

Sent. Form	Input	Action
dn	van	r. AN → n
dnva	n	shift

Bottom-up (shift-reduce) parsing: an example

 $S \rightarrow NP \ VP \quad NP \rightarrow d \ AN \quad NP \rightarrow AN \ VP \rightarrow v \ NP \quad AN \rightarrow a \ AN \quad AN \rightarrow n$

Sent. Form	INPUT	Action
dn	van	r. AN → n
dnva AN		r: AN → a AN
dnva AN		r: NP -> AN

Bottom-up (shift-reduce) parsing: an example

 $S \rightarrow NP \, VP \quad NP \rightarrow d \, AN \quad NP \rightarrow AN$ $VP \rightarrow v NP$ $AN \rightarrow a AN$ $AN \rightarrow n$

Sent. Form	INPUT	Action
dn	van	r. AN → n
dnv AN		r: AN a AN

d

Input	Action	
nvan	shift	
		Sorti Action rivan shift

Bottom-up (shift-reduce) parsing: an example

d

ENT. FORM	INPUT	Action
n	van	r: AN → n
nv	an	shift

Bottom-up (shift-reduce) parsing: an example

SENT. FORM	d Input	Action	
dn		van	r: AN -> n
dnvan			r: AN → n

dnvan	r: AN → n

INPUT ACTION

Bottom-up (shift-reduce) parsing: an example

SENT. FORM

S

dnva NP		reject
dnva AN		r: AN → a AN
dn	van	r: AN -> n

Bottom-up (shift-reduce) parsing: an example

ENT. FORM	Input	Action
ln .	van	r: AN -> n

Bottom-up (shift-reduce) parsing: an example Bottom-up (shift-reduce) parsing: an example $S \rightarrow NP \ VP \quad NP \rightarrow d \ AN \quad NP \rightarrow AN \ VP \rightarrow v \ NP \quad AN \rightarrow a \ AN \quad AN \rightarrow n$ SENT. FO Bottom-up (shift-reduce) parsing: an example Bottom-up (shift-reduce) parsing: an example \rightarrow NP VP NP \rightarrow d AN NP \rightarrow AN P \rightarrow v NP AN \rightarrow a AN AN \rightarrow n \rightarrow NP VP NP \rightarrow d AN NP \rightarrow AN P \rightarrow VNP AN \rightarrow a AN AN \rightarrow n $VP \rightarrow v NP$ $VP \rightarrow v NP$ INDIT ACTION INPUT ACTION SENT FORM SENT FORM Bottom-up (shift-reduce) parsing: an example Bottom-up (shift-reduce) parsing: an example $S \rightarrow NP \ VP \quad NP \rightarrow d \ AN \quad NP \rightarrow AN \ VP \rightarrow v \ NP \quad AN \rightarrow a \ AN \quad AN \rightarrow n$ \rightarrow NP VP NP \rightarrow d AN NP \rightarrow AN P \rightarrow v NP AN \rightarrow a AN AN \rightarrow n $VP \rightarrow v NP$ INPUT ACTION INPUT ACTION reduce/reduce conflic Bottom-up (shift-reduce) parsing: an example Bottom-up (shift-reduce) parsing: an example $S \rightarrow NP \ VP \quad NP \rightarrow d \ AN \quad NP \rightarrow AN \ VP \rightarrow v \ NP \quad AN \rightarrow a \ AN \quad AN \rightarrow n$ Bottom-up (shift-reduce) parsing: an example Bottom-up (shift-reduce) parsing: an example $S \rightarrow NP VP \quad NP \rightarrow d AN \quad NP \rightarrow AN \\ VP \rightarrow v NP \quad AN \rightarrow a AN \quad AN \rightarrow n$ ENT. FORM

Bottom-up (shift-reduce) parsing: an example

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Bottom-up (shift-reduce) parsing: an example

ENT. FORM

Bottom-up (shift-reduce) parsing: an example Bottom-up (shift-reduce) parsing: an example $S \rightarrow NP VP \quad NP \rightarrow d AN \quad NP \rightarrow AN \\ VP \rightarrow v NP \quad AN \rightarrow a AN \quad AN \rightarrow n$ Bottom-up (shift-reduce) parsing: an example Bottom-up (shift-reduce) parsing: an example $S \rightarrow NP \ VP \quad NP \rightarrow d \ AN \quad NP \rightarrow AN \ VP \rightarrow v \ NP \quad AN \rightarrow a \ AN \quad AN \rightarrow n$ T Acre Bottom-up (shift-reduce) parsing: an example Bottom-up (shift-reduce) parsing: an example \rightarrow NP VP NP \rightarrow d AN NP \rightarrow AN $\rightarrow NP \ VP \quad NP \rightarrow d \ AN \quad NP \rightarrow AN$ $VP \rightarrow v NP$ $AN \to a \; AN \quad AN \to n$ $VP \rightarrow v NP$ $AN \rightarrow a \ AN \quad AN \rightarrow n$ INDIT ACTION INDUT ACTION SENT FORM SENT FORM NP va AN Bottom-up (shift-reduce) parsing: an example Bottom-up (shift-reduce) parsing: an example $\rightarrow NP \; VP \quad NP \rightarrow d \; AN \quad NP \rightarrow AN$ $\rightarrow NP \, VP \quad NP \rightarrow d \, AN \quad NP \rightarrow AN$ $VP \rightarrow v NP$ $AN \to a \; AN \quad AN \to n$ $VP \rightarrow v NP$ $AN \rightarrow a \ AN \quad AN \rightarrow n$ Імент Астю INDUT ACTION Bottom-up (shift-reduce) parsing: an example Bottom-up (shift-reduce) parsing: an example $\rightarrow NP \; VP \quad NP \rightarrow d \; AN \quad NP \rightarrow AN$ \rightarrow NP VP NP \rightarrow d AN NP \rightarrow AN P \rightarrow v NP AN \rightarrow a AN AN \rightarrow n $VP \rightarrow v NP$ $VP \rightarrow v NP$ $AN \rightarrow a AN \quad AN \rightarrow n$ Two issues with a backtracking shift-reduce parser Table driven bottom-up parsing * The extra work done by a backtracking shift-reduce parser can be elimi for a large class of grammars The general idea is the same with LL(k) grammars: preprocess the grammar to construct a table + Obvious one: reduce/reduce and shift/reduce conflicts m The class of LR(k) (scanning from Left-to-right, producing a Rrightn · Not-so-obvious one: recognizing 'handles': derivation) grammars can be parsed deterministically using k lookahead - The rule that we locate at the right edge of the active sentential form is called a symbols handle

— For variable RHS, we need to search the grammar to determine which rule $\ast \stackrel{'}{k}=1$ is most common, LR(0) parser are also useful in some cases, larger kapplies (if any) allows expressive grammars

* LL(k) grammars are a subset of LR(k) grammars . In a efficient parser we want to avoid both Most practical programming language compilers are LR(1) parsers
 LR(k) parsers are difficult to build manually, but tools that take a CF nar and construct and LR(1) parser are in con non user (e.g., yacc)

Dotted rules, or 'items', (again) and augmented grammars

- An LR parser keeps a set of states (actually a finite-state automore represent the current parser state during parsing
- An LR parser's states are sets of 'dotted rules' similar to Early or chart par we discussed earlier
- $-A \rightarrow \bullet \alpha$ $-A \rightarrow \alpha \bullet \beta$ $-A \rightarrow \alpha \bullet$
- + We also introduce a new start symbol, with a single production $S^{'} \, \rightarrow \, S$
- This rule helps parser to determine when to stop: the parser accepts the input
- only when reducing S to S'

Shift-reduce parsing with LR(0) automaton

- The simplest version of the LR parsers uses LR(0) automaton to guide the parsing decisions
 Use a stack to keep track of active states

 - Use a stack to keep tract or active same
 Sate with state or Sate with state or
 If there is an outgoing edge labeled with the current input, shift push the target
 state to the state.
 Otherwise reduce based on consistent of the current state. For example, if the
 current state representation of the current state. For example, if the
 other state is a symbols (in NP and VP) from the state.

 push the state reachable through 5 from the state on the top of the stack.

LR(0) automator

 $\begin{array}{l} shift \\ reduce \: S' \: \to \: S \\ reduce \: NP \: \to \: AN \\ shift \end{array}$ 0 shift 1 reduce 4 4 reduce S → NP VF 5 e 5 chife 6 5 8 shift 9 reduce AN → n 10 reduce VP → v NP 11 reduce NP → d AN

a d n v

e

5 8 9 e 5 e 9 e

GOTO S NE

a d n v S NP VP AN

9

5 8 9 e 5 e 9 e

27 → 1×20 25 → +2 4 25 → +2 4 45 → +2 4 45 → +2

AN -- ea AN AN -- ea

vo. B

AN -- sa AN AN -- sa

Example

ACTION a d n v $\begin{array}{c} \mathbf{reduce} \ S' \ \to \ S \\ \mathbf{reduce} \ NP \ \to \ AN \\ \mathbf{shift} \end{array}$ reduce S → NP VP shift 9 t ace AN → a AN 5 8 9 e 5 e 9 e uce AN \rightarrow n uce VP \rightarrow v NP uce NP \rightarrow d AN

Example

Parsing: state ACTION

a d n v S NP shift shift reduce $S' \rightarrow S$ reduce $NP \rightarrow AN$ shift reduce $S \rightarrow NP VP$ shift reduce $AN \rightarrow a AN$ shift 5 e 9 5 8 9 e 5 e 9 e 7 shift 8 shift 9 reduce AN → n 10 reduce VP → v NP 11 reduce NP → d AN

Example

state ACTION

shift reduce S′ → S reduce NP → AN shift soift reduce S → NP VP shift shift reduce AN → a AN shift shift reduce AN 6 o start 9 reduce AN → n 10 reduce VP → v NP 11 reduce NP → d AN

Example state ACTION

shift reduce $S' \rightarrow S$ reduce $NP \rightarrow AN$ shift reduce $S \rightarrow NP VP$ shift

reduce AN → a AN shift shift 9 reduce AN → n 10 reduce VP → v NP 11 reduce NP → d AN

Example Parsing with LR(

reduce S' → S reduce NP → AN shift iceS → NP VP ice AN → a AN

Example

Parsing with LR(0 shift

 $\begin{array}{c} \text{reduce S}' \rightarrow \text{S} \\ \text{reduce NP} \rightarrow \text{AN} \\ \text{shift} \\ \text{reduce S} \rightarrow \text{NP VP} \end{array}$ reduce S → NP VP shift reduce AN → a AN shift shift reduce AN → n reduce VP → v NP reduce NP → d AN

sh LR(0)

reduce S' → S reduce NP → AN shift reduce S → NP VP shift reduce AN → a AN shift shift 5 e

reduce AN → n reduce VP → v NP reduce NP → d AN

Example

state ACTION

shift reduce $S' \rightarrow S$ reduce $NP \rightarrow AN$ shift reduce $S \rightarrow NP VP$ shift reduce AN → a AN shift shift reduce AN \rightarrow n reduce VP \rightarrow v NP reduce NP \rightarrow d AN



state	ACTION					GO	Ю		
		a	đ	n	v	S	NP	VP	AN
- 0	shift	5	8	9	e	1	3	e	2
1	reduce S → S								
2	$reduce NP \rightarrow AN$								
3	shift	e	e		7			- 4	
4	$reduce S \rightarrow NP VP$	_							
5	shift reduce AN → a AN	5	e	9	e				6
2	shift	-					10		2
	shift	- 2	8	2	-		10		ń
9	reduce AN → n	-	•	-					
10	reduce VP → v NP								
11	$reduceNP\rightarrowdAN$								
STACK	SINT. FORM					IN	UT J	ACTION	
0372	NP v AN						\$.	AN →	a AN
n. 10 / December of Table							_		Titrary N

	Balloway paning may	Table above bottom up parsing
Example		

state	ACTION					Gσ	TO		
		a	d	n	v	S	NP	VP	AN
- 0	shift	5	8	9	e	1	3	e	2
1	reduce S → S								
2	reduce NP → AN								
3	shift	e	e	e	7	e		4	
4 5	reduce S → NP VP shift	5		9	e				6
6	reduce AN → a AN	3	e	7	e				
7	shift	5	8	9	e		10		2
8	shift	5	e		ě		-		11
9	reduce AN → n								
10									
11	reduce NP \rightarrow d AN								
EACK	SENT. FORM					Ьs	ut A	CTION	
3 7 10	NP v NP	\neg					\$ N	Ρ →	AN



ceS → NP VP

oe AN → a AN

5 e 9 €

5 8 9 e 5 e 9 e

art entries (items) with lookahe

Example



9 reduce AN → n 10 reduce VP → v NP 11 reduce NP → d AN					9 reduc 10 reduc 11 reduc									
	Stack	Sent Form	Input	Action		SEACK SENT. FORM INPUT					Action			
	0 1	S	\$	S → NP VP				01	S	\$	accept			
College, 10	/ University of Tillringers			Water Sensotes 20	9/20		C Cillelin, M	1/Debendy of Silvingen			Tile	sier Newsoler 20	00(21	
	Beth	may produce may Table des	on hollow up parting					-	majority my Shirak	on bullion up parsing				
Limita	tions of LR(0)						LR par	sers with look	cahead					

Example

- . This would lead to a LR(0) automaton entry
 - VP → V* VP → V*3P 3D → *4 AN 3D → *AN AN → *a AN AN → *a
- We have a shift/reduce conflict
- * A simple solution (SLR): shift if possible, otherwise reduce
- . In general LR(0) parsers/grammars are limited, for most purposes we need
- more powerful parsers

onal rule: VP -> v

+ LR(k): pa

Another option is the LALR(k) parsers which use a smaller automaton
* LALR(1) parsers and parser generators are commonly used in practice

. Lookahead allows LR(k) parser to parse a larger class of gramman · The disadvantage is much larger chart sizes

Why use xLR(k) parsers?

- * LR(k) parsers general, efficient (non-backtracking) shift-re LR(k) parsers can be constructed for (almost) any formal/programming
- language constructs
- In general LR(k) grammars are more expressive. LL(k) is a subset of LR(k)
 LR(k) parsers can detect syntax errors as soon as it is possible to detect then

LR grammars and ambiguity

- . LR(k) parsers cannot handle ambiguity . If a grammar is ambiguous we cannot construct an LR(k) parse table for it
- . In general, determining whether a grammar is ambiguous is intractable
- This is sometimes used for a test for ambiguity:
 If we can build a LR(k) parser for a grammar, then it is not ambiguous
 If we cannot, it is inconclusive

What about natural language parsing

- · Natural languages are inherently ambigue
- · As a result, we cannot use these parsers for parsing natural languages · Nevertheless, the techniques are useful
- We can use LR-like parsers to reduce the non-determinism: GLI known as Tomita parser)
 Instead of a table-driven parser, we can predict the action with a learning method: transition-based dependency parsers do that

Summary

- xLR(k) parsers are powerful bottom-up deterministic parsers . LR grammars are more general than LL grammars
- · These parsers are difficult to build manually, but automatic parser generators
- · Although they cannot handle ambiguity, the sin natural language parsers to reduce the non-determinism
- Understanding the concepts here is useful for building parser generators and understanding the related natural language parsers
- Reading suggestion: Grune and Jacobs (2007, ch.9), Aho et al. (2007, Section 45-47)

