## Typing Rule of Baremetalisp

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Table 1: Notation
                                       variable
                                 T type variable
                                 D type name of user defined data
                                 L label of user defined data
                                        type
                                 C constraint
                                 Γ
                                        context
  L_{type}:L
ightarrow\mathcal{T} \ L_{nth}:L
ightarrow\operatorname{Int}
ightarrow\mathcal{T}
                                         function from label to type
                                         function to n-th type of label L
         The first part of the type of rate \mathcal{P}_{let} pattern of let expression \mathcal{T}_1 \equiv_{\alpha} \mathcal{T}_2 pattern of let expression \mathcal{S} substitution \mathcal{S} substitution \mathcal{S} to a \{T\} set of T

Fig. 7. \mathcal{T} \to \{T\} function from a \mathcal{T} to its free first part of \mathcal{T}.
                                        apply a substitution S to a type T
                                        function from a \mathcal{T} to its free variables
          FV_{\Gamma}:\Gamma\to\{T\}
                                        function from a \Gamma to its free variables
    \Gamma := x : \mathcal{T}, \Gamma context
    \mathcal{C} \quad := \quad \mathcal{T} = \mathcal{T}, \mathcal{C}
                                        constraint
    \mathcal{T} := Int
          .— Int

| Bool
| '(\mathcal{T}) list type
| [\mathcal{T}+] tuple type
| D user defined
| (D \mathcal{T}+) user defined
                                        user defined type
                                        user defined type with type arguments
                                         type variable
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Figure 1: Syntax

$$\begin{split} \Gamma \vdash \mathsf{true} : \mathsf{Bool} \mid_{\varnothing} \big\{ \big\} &\quad (\mathsf{T}\text{-}\mathsf{True}) \qquad \Gamma \vdash \mathsf{false} : \mathsf{Bool} \mid_{\varnothing} \big\{ \big\} &\quad (\mathsf{T}\text{-}\mathsf{False}) \\ &\quad \frac{x : T \in \Gamma}{\Gamma \vdash x : T \mid_{\{\}} \big\{ \big\}} &\quad (\mathsf{T}\text{-}\mathsf{Var}) \\ \\ &\quad \Gamma \vdash \mathcal{P}_{let} : T_0 \mid_{\mathcal{X}_0} C_0 \qquad \Gamma \vdash e_1 : T_1 \mid_{\mathcal{X}_1} C_1 \qquad \Gamma \vdash e_2 : T_2 \mid_{\mathcal{X}_2} C_2 \\ &\quad \frac{\mathcal{X}_0 \cap \mathcal{X}_1 \cap \mathcal{X}_2 = \varnothing \qquad C' = C_0 \cup C_1 \cup C_2 \cup \{T_0 = T_1\}}{\Gamma \vdash (\mathsf{let1} \ \mathcal{P}_{let} \ e_1 \ e_2) : T_2 \mid_{\mathcal{X}_1 \cup \mathcal{X}_2 \cup \{T_0\}} C'} \end{split} \tag{T-Let1}$$

Figure 2: Typing rule

$$\frac{x:T\in\Gamma}{\Gamma\vdash x:T\mid_{\{\}}\{\}} \quad \text{(PL-Var)}$$

$$\Gamma\vdash \mathcal{P}_{let_1}:T_1\mid_{\mathcal{X}_1}C_1\wedge\cdots\wedge\Gamma\vdash\mathcal{P}_{let_n}:T_n\mid_{\mathcal{X}_n}C_n$$

$$L_{type}(L)[\mathcal{S}]\equiv_{\alpha}T_0 \quad FV(T_0)\cap\mathcal{X}_1\cap\cdots\cap\mathcal{X}_n=\varnothing$$

$$FV_{\mathcal{T}}(T_0)\cap FV_{\Gamma}(\Gamma)=\varnothing \quad \mathcal{X}=FV(T_0)\cup\mathcal{X}_1\cup\cdots\cup\mathcal{X}_n$$

$$C=\{L_{nth}(L,1)[\mathcal{S}]=T_1,\cdots,L_{nth}(L,n)[\mathcal{S}]=T_n\}\cup C_1\cup\cdots\cup C_n$$

$$\Gamma\vdash (L\ \mathcal{P}_{let_1}\ \cdots\ \mathcal{P}_{let_n}):T_0\mid_{\mathcal{X}}C$$

$$\Gamma\vdash \mathcal{P}_{let_1}:T_1\mid_{\mathcal{X}_1}C_1\wedge\cdots\wedge\Gamma\vdash\mathcal{P}_{let_n}:T_n\mid_{\mathcal{X}_n}C_n$$

$$\frac{\mathcal{X}_1\cap\cdots\cap\mathcal{X}_n=\varnothing \quad \mathcal{X}=\mathcal{X}_1\cup\cdots\cup\mathcal{X}_n \quad C=C_1\cup\cdots\cup C_n}{\Gamma\vdash [\mathcal{P}_{let_1}\ \cdots\ \mathcal{P}_{let_n}]:[T_1\cdots T_n]\mid_{\mathcal{X}}C}$$
(PL-Tuple)

Figure 3: Typing rule of let expression's pattern