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# E0:270 - Machine Learning - Adversarial Attacks on Latent Dirichlet Allocation

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## Abstract

The authors intend to replicate the work by (Mei & Zhu, 2015a). In this paper, an adversarial attack on LDA is carried out by manipulating the corpus so as to make a particular word appear in a certain topic (at a higher rank, say top 10). This is done making minimal modifications in the data. This results in solving a bilevel optimization problem where attacker's risk function is minimized as high-level objective and learner's optimization for LDA as the lower-level objective. So far, the algorithm has been understood by the authors and the dataset to be used has been preprocessed. Authors intend to develop Python code (with or without a library) for the purpose.

## 1. Introduction

In the recent years text mining has proved to be a useful tool in a lot of applications. Topic modelling is a subset of text mining where one tries to extract the topics which forms the basis of the given corpus. Topic modelling can be used to form summaries, draw inferences, filter spam and the likes. Hence it is very likely that external forces will try to alter the model generated by the topic modelling tool especially in situations where the inferences from the document are used to drive decision or when topic modelling is used to filter spam.

LDA is a go to tool used in topic modelling. Given that the attacking party know the tools we use in topic modelling, we would like to discuss ways in which an external force might change the results of the model generated by minimally modifying the input to our corpus.

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## 2. Motivation

Decisions are in general "data driven" nowadays. Data can be used to effect and affect changes. This is not just applicable to the corporate sector but to the politics as well. A recent example are the claims that user data from Facebook was used to sway the decisions of the voters in the US which might have contributed to the success of Trump's campaign. To be able to gain 'genuine' inferences is of importance now more than ever.

To be able to skew the inferences from data in ones own favor can be considered very powerful in the environment we live in. Small changes in the emails data can shift the particular email from spam to non-spam. By perturbing the online data one can shift something not so important into the political agenda. we need an in depth study on how much the data needs to be perturbed to make such changes in the output so that one can account for these and make adjustments accordingly.

## 3. Literature Review

LDA using variational inference techniques was invented by Blei et al (Blei et al., 2003). This paper describes the mathematical framework required for the model. Adversarial attacks on a variety of machine learning techniques have been studied extensively eg. (Nelson et al., 2008), (Mei & Zhu, 2015b) etc. However to the best of our knowledge, the work by (Mei & Zhu, 2015a), which we intend to reproduce, is the only existing work for attack on LDA. Further, to understand variational inference and KKT conditions, authors have referred to (Christopher, 2016) extensively

## 4. Model Description

### 4.1. LDA Variational inference

LDA is a generative model for K topics.  $k^{th}$  topic is multinomial  $\psi_k$  with  $\psi_k \sim \text{dirichlet}(\beta)$  or  $\text{Dir}(\beta)$ .

Each document d has a topic proportion multinomial  $\theta_d$  with distribution  $\text{Dir}(\alpha)$ . The posterior of interest is  $p(\psi, \theta, Z | W, \alpha, \beta)$ . We estimate this using variational methods.

Our objective function for the problem is a bilevel objective function given by -

$\min_{\mathbf{M} \in M, \mu(M)} (R_A(\psi(M), \psi^*)), \text{s.t. } \psi(M) \text{ are LDA topics learnt from } \mathbf{M}$ , where  $\mathbf{M}$  is the modified training corpus and can belong to a specific set  $M$  of modified corpus.

#### 4.2. The design choice of $R_A$ functions and $M$ sets

$R_A$  is a loss function between the learned topic distribution  $\psi(M)$  and the distribution that attacker wants the user to learn  $\psi^*$ . We have 2 options for this loss function -

- $l_2$  attacker risk function - Calculates the sum of the squares of the difference of the topics.
- $\epsilon$ -insensitive  $l_2$  attacker risk function defined as:  $R_{A, \epsilon-l_2}(\psi(\eta(M)), \psi^*) = (1/2) * \sum_k \sum_v (|\psi(\eta(M))_{kv} - \psi^*_{kv}| - \epsilon)_+^2$

We define a  $M$  set in which the  $l_1$  distance between the original matrix  $M_0$  and the manipulated  $\mathbf{M}$  is within a total change limit of  $L$  and the  $l_1$  distance of each row is within a per-document change limit  $L_d$ . The small attacks are

$$M = \{\mathbf{M} \in R^{D \times V} : \|\mathbf{M}_0 - \mathbf{M}\|_1 \leq L, \forall d : \|\mathbf{M}_{0,d,\cdot} - \mathbf{M}_{d,\cdot}\|_1 \leq L_d\} \quad (1)$$

#### 4.3. Descent Method

We use descent method to update  $\mathbf{M}$  as

$$\mathbf{M}^{(t)} = \text{Proj}_M[\mathbf{M}^{(t-1)} - \lambda_t \nabla_M R_{A, \epsilon-l_2}(\psi(\eta(M)), \psi^*)] \quad (2)$$

We can calculate  $\nabla_M R_{A, \epsilon-l_2}(\psi(\eta(M)), \psi^*)$  using chain rule.

### 5. Dataset description

As used in the paper (), we'll use the CONG dataset (Thomas et al., 2006). This contains floor-debate transcripts from the United States House of Representatives in 2005. We also intend to use the NIPS conference papers

Number of documents	6362
Average words per document	118
Size of the vocabulary	15547

Table 1. CONG dataset description

dataset consisting of abstracts, authors and texts of research papers presented in NIPS 2000 through 2012, downloaded from <http://www.cs.toronto.edu/~roweis/>.

### 6. Preliminary Results

After some preprocessing, LDA was run on the CONG dataset and one of the topic contained top 10 words as displayed in fig.1. For experiment we intend to insert words like 'solar' in the top 20 words of this topic. The code can be found at <https://bit.ly/2GuOo5C>

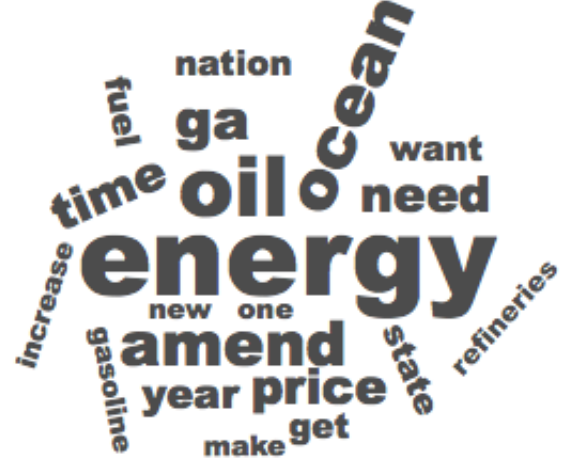


Figure 1. Top 20 words in the topic Energy

### 7. Future Work

To extend the current work, authors intend to explore deep-learning based topic modelling tools such as deep exponential families (Ranganath et al., 2014) and carry out a similar adversarial attack on them.

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