

# Monopsony with Dynamic Wage Contracts

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## Abstract

Monopsony power is often measured by interpreting firm wage and labor responses to shocks through static models. But when workers face frictions to changing jobs, employment adjusts gradually and workers respond to changes in the total value of a job—not just the current wage. We develop a general equilibrium dynamic monopsony model where firms contract with risk-averse workers over idiosyncratic shocks. We show that the shock-identified labor supply elasticity depends on the persistence of the shock, worker risk aversion, and the horizon over which it is estimated. These forces induce a wedge between the inverse shock-identified labor supply elasticity and the wage markdown. We estimate the model using U.S. Census employer-employee matched data. The small and persistent wage response to temporary shocks is consistent with firms insuring risk-averse workers. Search frictions explain why employment continues to rise even after wages have started to fall. We find the average worker’s wage is marked down 8.3%. By contrast, the static model approach of inverting the shock-identified labor supply elasticity implies a markdown estimate as wide as 26%. Lastly, we show that firm employment dynamics are not efficient: insurance distorts the job ladder, preventing productivity-improving job transitions from occurring.

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# 1 Introduction

Labor market power affects wage levels and wage inequality, and understanding firm wage setting behavior is key to evaluating how labor market policies will affect wages and employment. What determines how firms adjust to idiosyncratic shocks and what does this response tell us about the extent of labor market power? Static monopsony models suggest that wage markdowns can be estimated by inverting the labor supply elasticity, which has led a large literature to do exactly this.<sup>0</sup> This approach leads to implausibly large wage markdowns—if firms exert such a large degree of wage-setting power then why are they not more profitable?<sup>1</sup> In this paper, we show that, when considering realistic dynamics, inverting the shock-identified labor supply elasticity does not recover the markdown. When workers face frictions to switching jobs, employment adjusts gradually and workers respond to changes in the total value of a job—not just the current wage. The same initial wage increase may imply very different total earnings gains depending on whether the firm’s shock was temporary or persistent. Additionally, risk-averse workers will prefer smoother wage changes, which may influence how firms respond to shocks (Knight, 1921). In the presence of search frictions, risk-aversion, and temporary shocks, the shock-identified labor supply elasticity is a complex, dynamic object which does not neatly map onto the wage markdown.

In this paper, we build a general equilibrium random search model of monopsony where firms can provide risk-averse workers insurance against idiosyncratic shocks via state-contingent wage contracts. Firms face an insurance-incentive tradeoff when setting wage contracts; workers prefer stable pay, but allowing wages to move with productivity boosts employment when it is most profitable to the firm. We develop the notion of the *cross-sectional* labor supply elasticity—how much larger is the employment of firms which offer permanently higher wages?—and show that this is key to estimating wage markdowns. This steady-state analysis of dynamic monopsony models (as popularized by Manning (2003)) is common, but it does not allow us to interpret empirical objects that are identified from shocks. Indeed, when researchers use an idiosyncratic shock to the firm as an instrument for labor demand to estimate a labor supply elasticity this does not measure the cross-sectional labor supply elasticity, but instead what we call the *shock-identified* labor supply elasticity. Our model allows us to show how the level and dynamics of the shock-identified labor supply elasticity can identify the cross-sectional labor elasticity.

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<sup>0</sup>For example, the following papers use experimental/quasi-experimental variation in wages to identify a labor supply elasticity which they invert to estimate wage markdowns: Kroft et al. (2025); Amodio and De Roux (2024); Caldwell and Oehlsen (2023); Azar et al. (2022); Kline et al. (2019)

<sup>1</sup>In a review piece, Manning (2021) notes “The amount of monopsony power estimated in many studies is so high as to raise questions about how it can be reconciled with observed levels of profits.”

Additionally, it allows us to speak to how both insurance and market power influence the firm response to shocks and to ask whether firm employment dynamics are efficient.

To motivate the need to model dynamics of frictional labor adjustment, we use U.S. Census matched employer-employee data and estimate the response of wages and employment to firm-level shocks to value added per worker. Labor adjusts slowly, continuing to rise even as the wage response fades. This means that the shock-identified labor supply elasticity is more elastic when estimated over longer horizons. We also find a relatively small and persistent wage response to a temporary shock to firm performance—consistent with insurance motives smoothing the firm’s wage-setting behavior. To provide more direct evidence of insurance, we exploit variation in firms’ ability to smooth wages due to financial constraints (Ellul et al., 2018). We show that firms facing tighter financial constraints exhibit a larger wage response to idiosyncratic shocks, consistent with these firms providing less insurance to workers. This pattern holds across a broad range of measures of financial constraints.

To study how labor market power and insurance jointly shape wage setting, we develop a monopsony model with dynamic wage contracts. Firms post vacancies with state-contingent wage contracts, which allow them to offer insurance over idiosyncratic shocks. Risk-averse workers face search frictions: they infrequently receive a random job offer. Workers choose whether or not to accept based on the expected utility of the posted contract. Firms commit to the contracts, while workers cannot commit to staying at the firm. As firms experience idiosyncratic productivity shocks, their value to keeping (and recruiting) a worker changes which leads them to offer wage contracts which vary with their performance. But risk aversion limits how much firms pass through these shocks to wages: workers value a single-period wage increase less than the same total compensation spread over time. Firms thus face a tradeoff between adjusting labor in response to a shock (which requires adjusting wages) and insuring workers. Labor accumulates slowly and responds to changes in the total value of the contract. We show that, when a shock is not fully permanent, there is no horizon over which the inverse shock-identified elasticity equals the markdown.

Risk-averse workers value temporary wage changes less than permanent ones of the same discounted present dollar value. This makes it difficult to disentangle market power from risk aversion. Additionally, workers respond to changes in the value of the contract, but we empirically observe only a limited set of wage changes. To address these two challenges, we leverage the fact that the firm provision of insurance has a unique dynamic pattern: risk aversion makes it costly for firms to lower the promised utility after the shock has dissipated. So when workers are risk neutral, the firm will raise wages sharply after a productivity shock and then lower them quickly as the shock dissipates. But when workers are risk averse, the wage response is relatively more persistent as risk aversion induces wage smoothing.

We use simulated method of moments to estimate our model to match the dynamic response of wages and labor to idiosyncratic shocks that we present in Section 2, as well as several aggregate moments. The average worker’s wage is marked down 8.3%—a relatively modest markdown compared with the literature, which typically finds markdowns between 15% and 50% (Azar and Marinescu, 2024). If we adopted the static model approach of inverting the shock-identified labor supply elasticity, we would have estimated a markdown as wide as 26%. We also estimate a coefficient of relative risk aversion of 5.97, suggesting that workers are considerably risk-averse: the average worker would give up roughly 3% of pay to avoid a 10% symmetric gamble in wages. Indeed, risk aversion is necessary to explain the small, relatively flat wage response to idiosyncratic shocks. When we re-estimate our model assuming workers are risk neutral, we dramatically overshoot the level of the wage response in the first years following the shock and find that it fades away too quickly in the later years.

The response of wages to idiosyncratic productivity shocks is also commonly used to estimate wage markdowns, independently of how labor responds (Kline, 2025; Lamadon et al., 2022; Card et al., 2018). Using our estimated model, we show that the extent of worker risk aversion strongly influences the level and persistence of the wage pass-through. If workers were risk neutral, we would expect an average 0.086% wage increase in the six year window following the 1% shock—almost three times larger than the 0.03% average increase we observe. This shows that the choice to model the firm provision of wage insurance highly influences our understanding of what drives the firm’s wage response to shocks. The empirical fact that firms adjust wages in response to idiosyncratic productivity shocks is evidence of the *existence* of monopsony power—there is not one market wage—but using the wage pass-through to infer the *extent* of market power is very sensitive to modeling decisions.

Finally, we document that insurance has direct consequences for the economy. Since firms face a tradeoff between insuring workers and adjusting labor following a shock, wage insurance prevents some productivity-improving job-to-job transitions from occurring. Relative to a social planner who can perform redistribution but is constrained by search frictions, labor responds too slowly to shocks—especially when workers are risk-averse. This suggests that the firm provision of insurance distorts the job ladder and may reduce labor market dynamism.

**Literature.** We contribute to a large and growing literature that models and quantifies labor market power.<sup>2</sup> Manning (2021) highlights that the extent of monopsony power typically estimated is so large as to be puzzling—if firms have such enormous market power, why are profits not higher? Recent work has proposed resolutions to this puzzle: Bloesch

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<sup>2</sup>See Kline (2025); Azar and Marinescu (2024); Manning (2021) for recent surveys

et al. (2024) show that adjusting the wage markdown to account for recruiting costs can reconcile measured labor supply elasticities with observed firm profits. This parallels Seegmiller (2021); Chan et al. (2020) which both show that labor adjustment costs can influence the wage markdown. Berger et al. (2022) and Agostinelli et al. (2025) both show that the labor supply elasticity which is typically estimated empirically is not a sufficient statistic for the wage markdown, highlighting the role of strategic interactions and human capital accumulation, respectively. Similarly, we show that in the presence of search frictions and risk aversion, the shock-identified labor supply elasticity does not map onto the cross-sectional elasticity relevant for wage markdowns.<sup>3</sup> Neglecting these dynamics can lead to a substantial overestimate of market power.

To model the dynamics of frictional labor adjustment, we build on the “dynamic monopsony” framework of Manning (2003), where search frictions and wage posting in the style of Burdett and Mortensen (1998) give firms monopsony power. The other common microfoundation for monopsony power is job-differentiation, where the absence of labor market frictions mean that labor responds instantaneously to a wage change (Berger et al., 2022; Lamadon et al., 2022; Chan et al., 2020). Dynamic monopsony models all feature worker-level dynamics, as workers receive random job offers and are exogenously separated into unemployment, but often have no idiosyncratic firm shocks or other firm dynamics (Bontemps et al., 2000; Jarosch et al., 2024; Gottfries and Jarosch, 2023). Gouin-Bonenfant (2022) and Bloesch et al. (2024) feature idiosyncratic shocks, but we directly focus on how these firm dynamics shape the measurement and interpretation of monopsony power. Additionally, a distinctive feature of our model is that we incorporate worker risk aversion and allow firms to offer state-contingent wage contracts. This allows us to show how risk aversion shapes workers’ responses to temporary wage changes and how the firm provision of insurance affects wage-setting behavior.

By modeling how monopsonistic firms provide wage insurance and using this to match the empirical wage pass-through that we estimate, we also contribute to the literature measuring and interpreting the wage pass-through. The wage pass-through refers to the elasticity of wages with respect to value added per worker (or other measures of firm performance). This empirical object is often interpreted through a market power framework and labeled as “rent sharing” (Van Reenen, 1996; Card et al., 2016, 2018; Kline et al., 2019; Lamadon et al., 2022; Garin and Silvério, 2023) or through an insurance framework and labeled as “risk sharing” (Guiso et al., 2005; Friedrich et al., 2019; Balke and Lamadon, 2022). We show that both

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<sup>3</sup>This point that a short-run labor supply elasticity might not be enough to determine wage markdowns dates back to Boal and Ransom (1997), but by formalizing the relationship between shock-identified and cross-sectional labor supply elasticities we show how the researcher can infer the extent of monopsony power through how firms respond to shocks.

worker risk aversion and search frictions can reduce the wage pass-through, which suggests that using the level of pass-through to infer wage markdowns without modeling insurance, as in Card et al. (2018) and Lamadon et al. (2022), will bias the estimate of market power.

This paper builds on the literature studying wage contracts by writing a novel model with firms that contract with workers over *idiosyncratic* productivity shocks and where *random* search frictions influence the worker’s ability to commit. Early papers study the insurance-incentive tradeoff in wage contracts in a competitive setting where the worker’s ability to quit for an exogenous outside option limits the extent of insurance (e.g., Baily (1974); Azariadis (1975); Harris and Holmstrom (1982)).<sup>4</sup> Recent work has studied wage contracting in the context of directed (competitive) search which is tractable due to having a block recursive equilibrium (Menzio and Shi, 2010; Balke and Lamadon, 2022; Souchier, 2022). We overcome the tractability problems associated with an equilibrium that is not block recursive to allow us to study wage contracting over idiosyncratic shocks within the workhorse monopsony model of random search. Finally, relative to Moscarini and Postel-Vinay (2013, 2016); Fukui (2020) who adopt random search models with wage contracting over aggregate shocks to study business cycle dynamics, we model idiosyncratic shocks which are the most directly related to the empirical monopsony literature. We also show that idiosyncratic shocks lead to inefficient job-to-job transitions even with risk-neutral workers, which contrasts with Moscarini and Postel-Vinay (2013) where the decentralized equilibrium with aggregate shocks features efficient labor reallocation.

**Road Map.** Section 2 offers motivational empirical evidence on how wages and employment respond to shocks and how this varies by firm financial constraints. Section 3 develops our model. We characterize the optimal contract in 4. We quantify the model in Section 5. Finally, we turn to the planner’s problem and show how idiosyncratic shocks distort the job ladder in Section 6.

## 2 Empirical Patterns

In this section, we present several empirical facts. First, we study the dynamics of how idiosyncratic shocks pass through to wages and employment. We show that the wage pass-through is small and relatively persistent over time, while the labor response accumulates in the years following the shock. This motivates a model with search frictions (to explain labor dynamics) and insurance (to explain the small, persistent wage pass-through). Finally, we show that wages and employment respond more to shocks at financially constrained firms

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<sup>4</sup>Similarly, Rudanko (2009, 2011); Kudlyak (2014) study wage contracting in a search-and-matching model without on-the-job search

which may be less able to offer insurance.

## 2.1 Data

We use several US Census Bureau data products: the Revenue-Enhanced Longitudinal Business Database (LBD), the Longitudinal Employer-Household Dynamics (LEHD), and the Quarterly Financial Report. We complement these with Compustat data for publicly traded firms.

**Longitudinal Employer-Household Dynamics (LEHD)** The LEHD is a Census Bureau employer-employee matched dataset containing restricted-use microdata with quarterly earnings for jobs in the United States. The LEHD data is created by combining data shared by states on state Unemployment Insurance earnings records and the Quarterly Census of Employment and Wages with other censuses and surveys. We have access to data from 28 states and from 1997 to 2022. We annualize earnings by adjusting for the number of quarters a worker worked at a firm, following Sorkin (2018) and Abowd et al. (2003). Details of the data construction are in Appendix A1. Our primary variable that we construct using the LEHD is a residualized measure of average annual earnings at the firm, where individual earnings are annualized, and then adjusted by removing person-state fixed effects. This allows us to control for composition changes when studying the response of wages to shocks.

**Longitudinal Business Database (LBD)** The U.S. Census Bureau Longitudinal Business Database (LBD) is a restricted-use establishment-level panel that links the Census Business Register across years to track all U.S. employer businesses with paid employees. The LBD is built from the Business Register and integrates administrative tax records with Census surveys. It provides annual coverage at both the establishment and firm levels, spanning all industries and states. We have access to the LBD from 1997 to 2022. The revenue-enhanced LBD also contains firm-level revenue. We use the LBD primarily for employment, payroll, revenue, and NAICS. Note that our payroll and employment measures are for the first quarter of the year and revenue is an annual measure.

**Quarterly Financial Report (QFR)** The Quarterly Financial Report (QFR) is a survey of firms conducted by the US Census Bureau, providing income statements and balance sheets. The survey targets manufacturing companies with total assets of \$250,000 or more, and companies in other industries (mining, wholesale trade, retail trade, information, or professional and technical services) with total assets of \$50 million or more. Relative to Compustat, the QFR provides data for smaller and private firms, which are likely to be

more financially constrained than Compustat firms. We use the QFR to provide new descriptive evidence of the correlation between the wage pass-through and measures of financial constraints. We have access to the QFR in Census years—every 5 years from 1997 to 2022. When constructing firm-level measures of financial constraints used in our analysis in Section 2.3 we take the average across all available years to generate a time-invariant measure.

**Compustat** We link our firm-level Census Bureau datasets to Compustat, which allows us to construct firm-level measures of value added per worker. Compustat provides standardized annual and quarterly financial statement information for publicly traded U.S. corporations. This allows us to define value-added as the sum of operating income before depreciation, changes in inventories, and labor expenses, as in Donangelo et al. (2019). We calculate labor expenses as the product of Compustat employment and LEHD earnings.<sup>5</sup> This also allows us to define the input cost share. Specifically, we calculate non-labor input costs as being the difference between revenue and total value-added and define the ratio of non-labor input costs to total revenue as the non-labor input cost share.

## 2.2 Dynamic responses of wages and employment to shocks (+ cut by financial constraints)

Relative to existing models of monopsony, a key contribution of ours is to match the dynamics of wages and employment in response to idiosyncratic shocks.

To understand how firms respond to shocks, we estimate the following relationship between changes to value added per worker and cumulative firm outcomes over time.

$$\log(Y_{j,t+\tau}) - \log(Y_{j,t}) = \alpha + \beta_\tau(\log(\text{VA pw})_{j,t+1} - \log(\text{VA pw}_{j,t})) + \mathbf{X}_{jt} + \varepsilon_{jt} \quad (1)$$

$Y$  is (residualized) firm level wages or firm employment. We estimate equation 1 for  $\tau \in [1, 6]$  to capture dynamics in the response. Control variables  $\mathbf{X}_{jt}$  include two digit NAICS by year fixed effects and controls for 2 lags of the growth of  $Y$  and 2 lags of the growth of value added per worker.<sup>6</sup> Standard errors are clustered by  $gvkey$  (the firm identifier) and year.

To isolate exogenous, idiosyncratic shocks, we instrument for the change in value added per worker  $\log(\text{VA pw})_{j,t+1} - \log(\text{VA pw})_{j,t}$  using (non-labor) input cost share shocks. We

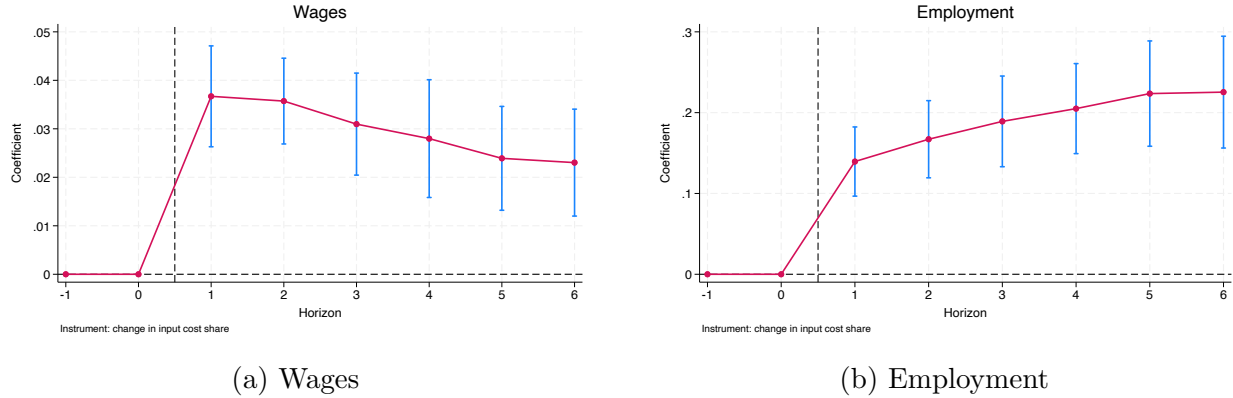
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<sup>5</sup>This is because wage information is not readily available for most firms in Compustat. LEHD earnings are annualized as described in Appendix A1

<sup>6</sup>This specification is a Jordà (2005) local projection: separate linear regressions by horizon, so  $\beta_\tau$  is the  $\tau$ -step impulse response.

use the change in the cost share—the ratio of non-labor input costs to revenue—between  $t - 1$  and  $t$  as our instrument for changes in value-added per worker. We use the input cost share, rather than input costs in levels, because this isolates changes in profitability without mechanically picking up changes in quantity.<sup>7</sup> This allows us to isolate changes in wages and employment driven by shocks to labor demand, rather than to labor supply. By including NAICS by year fixed effects we also isolate idiosyncratic cost shocks, which is desirable because sectoral labor supply elasticities are unlikely to be the same as firm-level elasticities (Souchier, 2022; Garin and Silvério, 2023). As an example, our instrument would pick up if a manufacturer’s gas contract was renegotiated—but *not* oil price shocks (fixed effects will expunge industry shocks). Similarly, our instrument would pick up if a restaurant’s food wholesaler goes bankrupt—but *not* a business cycle shock (due to our time fixed effects).

Figure 1: Impulse responses to value-added per worker shocks



*Notes:* These figures show the impulse response of wages and employment to value-added per worker changes (where the input cost share is the instrument). Our wage measure is the firm’s LEHD annualized earnings with person-state fixed effects residualized. Employment is Compustat employment. Horizons are years. All specifications include NAICS2×year fixed effects and two lags of wage changes and value-added per worker changes. Standard errors are two-way clustered by firm and year. This exhibit is from FSRDC Project Number 3060 (CBDRB-FY25-P3060-R12493).

Figure 1 plots the coefficients  $\beta_\tau$ . There are several empirical patterns here that motivate our model. First, the response of wages to this value-added shock is small. The one year wage pass-through is 0.0367. Card et al. (2018) discuss that the elasticity of wages with respect to value added per worker typically falls between 0.05 and 0.15. They also note that studies which estimate the pass-through of firm shocks to individual wages find smaller

<sup>7</sup>For example, a labor supply shock could induce a change in quantity produced which would imply higher input expenditure without any change in profitability

values, sometimes below 0.05, suggesting that the fact we control for worker-state fixed effects in constructing our wage measure may explain our small wage pass-through. Our shock is also fairly transitory; when we estimate the annual persistence of the shock,<sup>8</sup> we find  $\hat{\rho} = 0.561$  (0.042). Our model will explicitly treat this shock as temporary and match the measured persistence.

Next, note that the wage response is fairly stable. Despite the value-added shock being non-permanent, by year six the wage pass-through is 0.023—not too dissimilar from the one year wage pass-through of 0.037. In our model, insurance will be key to matching both the small wage pass-through as well as the relatively flat wage response.

Finally, we can see that labor accumulates gradually in response to the shock. This means that the labor supply elasticities implied by the analysis also increase when estimated over a longer horizon. The one year labor supply elasticity is 3.8 which is standard for the literature—Azar and Marinescu (2024) note that values between 2 and 6 are standard. By year six, the wage response has fallen somewhat while labor has continued to increase—resulting in a labor supply elasticity of 9.78. The empirical fact that the labor supply elasticities may be larger when estimated over a wider horizon is known<sup>9</sup>, and our paper interprets these dynamics through our model. Intuitively, when workers infrequently receive job offers it takes time for employment to adjust following a wage change. Additionally, even when the firm has begun to reduce the wage back to its baseline levels, it takes time for workers to receive better offers. These two forces both can lead to a larger labor supply elasticity when estimated over a wider horizon.

To get more directly at how insurance influences the wage and labor response to shocks, we estimate the following equation:

$$\begin{aligned} \log(Y_{j,t+\tau}) - \log(Y_{j,t}) = & \alpha + \beta_{\tau} \Delta \log(\text{VA pw})_{j,t+1} + X_{jt} \\ & + \gamma_{\tau} [\Delta \log(\text{VA pw})_{j,t+1} \times L_{j,t}] + \varepsilon_{jt}. \end{aligned} \quad (2)$$

This is the same as the previous equation 1 but it now contains an interaction for firm leverage,  $L_{j,t}$ . Levered firms may face financial constraints which make offering insurance to workers against shocks more costly. For example, in response to a negative shock they may have to cut wages and employment despite this being costly—and they may have to ex-ante pay higher wages due to this risk. Indeed, the corporate finance literature has noted that

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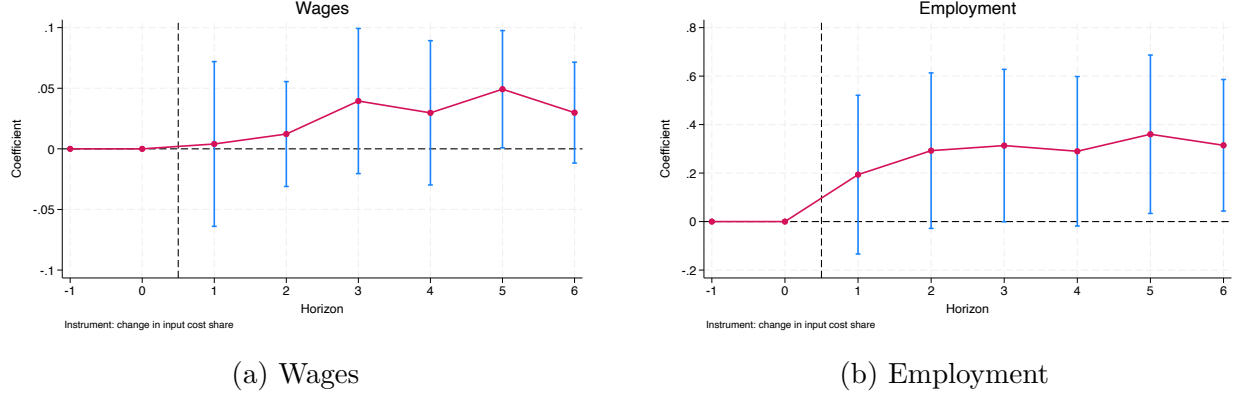
<sup>8</sup>Specifically, we estimate  $\log(\text{VA pw}_{j,t+2}) - \log(\text{VA pw}_{j,t}) = \alpha + \rho (\log(\text{VA pw}_{j,t+1}) - \log(\text{VA pw}_{j,t})) + \mathbf{X}_{jt} + \varepsilon_{jt}$ . Our estimate  $\hat{\rho}$  captures the extent that a shock to value added per worker in  $t = 1$  persists in  $t = 2$

<sup>9</sup>Seegmiller (2021) establishes this fact using stock returns as an instrument and finds a similar pattern in the dynamics of the labor supply elasticity

leverage may result in a firm’s workers being exposed to more risk.<sup>10</sup>

In Figure 2 we plot the continuous interaction  $\gamma_\tau$ . Indeed, more levered firms have more volatile wages and labor. Going from a firm with a leverage ratio of 0.25 to 0.75 would predict an average 0.0137pp (46%) larger wage pass-through in the six year post period and an average 0.147pp (77%) larger employment response.

Figure 2: Heterogeneous response by firm leverage



*Notes:* These figures plot the estimated interaction coefficients  $\gamma_\tau$  from Eq. 2, which capture how the response of wage and employment growth to value-added-per-worker changes varies with firm leverage  $L_{j,t}$ . Our wage measure is the firm’s LEHD annualized earnings with person-state fixed effects residualized. Employment is Compustat employment. Horizons are years. All specifications include NAICS2×year fixed effects and two lags of wage changes and value-added-per-worker changes. Standard errors are two-way clustered by `gvkey` and year. This exhibit is from FSRDC Project Number 3060 (CBDRB-FY25-P3060-R12493).

## 2.3 The wage pass-through and financial constraints

In this section, we explore heterogeneity by financial constraints and find, broadly, that less financially constrained firms have a lower pass-through of revenue per worker into wages, suggesting insurance may also be relevant to explaining patterns in the relationship between wages and firm performance. This motivates our goal of understanding how insurance affects firms’ wage-setting behavior.

How does the pass-through of revenue per worker into wages vary by measures of financial constraints? This exercise uses several measures of financial constraints that we measure in

<sup>10</sup>For example, Giroud and Mueller (2017) show that levered firms cut employment more during the Great Recession and Sharpe (1994) finds that levered firms have more cyclical employment

Table 1: Pass-through of  $\Delta \log \text{rev pw}$  into  $\Delta \log w$  by financial constraints ( $\hat{\beta}_2$ )

	(1) $\Delta \log w$	(2) $\Delta \log w$	(3) $\Delta \log w$	(4) $\Delta \log w$	(5) $\Delta \log w$
$\Delta \log \text{rev pw} \times F$	−0.00727 (0.000344)	0.0160 (0.00205)	−0.00985 (0.00240)	0.0125 (0.00483)	−0.00233 (0.000258)
$F =$	log total assets	$\frac{\text{ST debt}}{\text{Total debt}}$	$\frac{\text{Total debt}}{\text{Total assets}}$	$\frac{\text{ST debt}}{\text{Total assets}}$	Cash per worker
1 SD effect in $F$ (as % of baseline $\hat{\beta}_2$ )	−147.4	33.9	−20.8	12.6	−41.6
$N$	3,080,000	3,080,000	3,080,000	3,080,000	3,080,000

Outcome is  $\Delta \log w_{it}$  (LBD payroll per worker). Establishment–year data weighted by establishment share of firm employment. SEs clustered at the firm level. Models include NAICS 4-digit  $\times$  year fixed effects and main effects for  $\Delta \log \text{rev pw}$  and  $F$ . “1 SD effect in  $F$ , as % of baseline  $\hat{\beta}_2$ ” =  $100 \times \frac{(1 \text{ SD effect of } F \text{ on } \hat{\beta}_2)}{0.009907}$ . This exhibit is from FSRDC Project Number 3060 (CBDRB-FY25-P3060-R12493).

the Quarterly Financial Report microdata (QFR). The QFR allows us to observe the financial constraints for smaller, private firms—including those with as little as \$250,000 in assets. This gives us much more heterogeneity in financial constraints than Compustat (Crouzet and Mehrotra, 2020).

We use several firm-level measures of financial constraints that are common in the corporate finance literature: (1) log total assets (Hadlock and Pierce, 2010) (2) the ratio of short-term liabilities to total liabilities (Kalemli-Özcan et al., 2022) (3) the ratio of total liabilities to total assets (Sharpe, 1994) (4) the ratio of short-term liabilities to total assets (Tian et al., 2015) and (5) cash per worker (Campello et al., 2010).

$$\Delta \log(w)_{it} = \beta_0 + \beta_1 \Delta \log(\text{revenue pw})_{f(i)t} + \beta_2 \Delta \log(\text{revenue pw})_{f(i)t} \times F_{f(i)} + \beta_3 F_{f(i)} + \gamma_{kt} + \varepsilon_{it} \quad (3)$$

where  $i$  indexes establishments,  $f(i)$  and denotes firms,  $F_{f(i)}$  is the measure of financial constraints,  $\log(w)_{it}$  is LBD payroll per worker. We cluster at the firm level, and  $\gamma_{kt}$  denotes fixed effects for NAICS 4  $k$  by year  $t$ .

In Table 1 we report the values of  $\hat{\beta}_2$  for our five different measures of financial constraints. To aid interpretation, we also report the effect of a one standard deviation change in each financial constraint measure as a percentage of the baseline pass-through coefficient. These results broadly reveal that less financially constrained firms have smaller wage pass-throughs. Firms with more total assets may be more able to spend down or borrow to smooth against shocks. Indeed, they have a lower wage pass-through. Similarly, firms with cash per worker

may be more liquid and able to smooth their payroll—this is consistent with these firms also having a smaller wage pass-through. Firms with a higher share of short-term liabilities (either relative to total liabilities or relative to total assets) may be more vulnerable to rollover risk which could translate to more volatile pay. We do see that both having a higher share of short-term liabilities to total liabilities and short-term liabilities to total assets are correlated with having a larger wage pass-through. Lastly, we would expect that firms which are more levered—that is, have a higher share of total liabilities to total assets—would be less able to borrow in response to shocks and would pass more risk onto their workers. We find the opposite of this, but this might be explained by the fact that levered firms tend to be larger and larger firms generally have lower productivity-wage pass-throughs (Rajan and Zingales, 1995). Notably, in our Compustat sample which is large, public firms, we have shown in Figure 2 that levered firms have a larger wage pass-through.

We have shown that financially constrained firms have larger wage pass-throughs, that the wage response to shocks is small and relatively flat, and that the labor response accumulates over time. Now, we write a model which will allow us to use the wage and labor dynamics to disentangle market power and insurance.

### 3 Model

We write a random search model with on the job search (Burdett and Mortensen, 1998), idiosyncratic shocks, risk-averse workers, and dynamic wage contracts. This model parsimoniously allows us to model how insurance and monopsony both shape the wage and labor response to shocks—and, in turn, understand which empirical moments are required to estimate the level of market power.

By adding idiosyncratic shocks, we are able to match the empirical within-firm labor supply elasticity and the within-firm wage pass-through which are estimated using shocks. We will refer to these objects as the *shock-identified* labor supply elasticity and *shock-identified* wage pass-through. We allow firms to contract over these shocks when hiring risk-averse workers—this means the firm’s role as an insurer can shape the wage and labor dynamics. These dynamics are not just shaped by worker risk aversion but also by firm market power which influences the firm’s ability to recruit and retain more workers as it adjusts the compensation.

### 3.1 Market Power in Search Models

We begin by offering an intuition for what generates monopsony power in this class of models. In random search monopsony models, firms have market power because workers face search frictions. The use of Burdett and Mortensen (1998) as a model of “dynamic monopsony” was popularized by Manning (2003).<sup>11</sup> Any active firm will recruit all the unemployed workers it contacts, but it will only successfully poach employed workers who are compensated less. Since these employed workers only receive a job offer with odds  $\lambda_e$ , this means that a firm will not immediately lose all of its workers to a competitor if it pays a lower wage—as would be true in the competitive case. The extent of these search frictions affects the competitive pressure firms face and, in the edge case where there are infinite search frictions and employed workers never receive competing offers, firms will mark down the wage fully to the worker’s outside option.

Search frictions are not the only force that influences firm monopsony power in this setting. Firms vary in their permanent productivity which means that a firm’s relative position on the job ladder can influence the amount of local competition it is exposed to. Gouin-Bonenfant (2022) formalizes and quantifies how increased dispersion in the productivity distribution can lead to a smaller labor share.

Search frictions and dispersion in the productivity distribution are two key parameters that influence monopsony power because they affect how firms are able to accumulate workers in the long run. If a firm permanently offers a more desirable contract, how many workers will it accumulate? Proposition 1 formalizes this concept as the *cross-sectional* labor supply elasticity.

### 3.2 Environment

Time is discrete and all agents discount future utility at a rate  $\beta$ . There is a unit mass of workers who can be either employed or unemployed. There is a unit mass of firms which can either be active or inactive (employing zero workers). Workers are hand-to-mouth and have a utility function  $u(\cdot)$ . This assumption can be justified by the fact that many workers, even in wealthy countries, have little or no liquid wealth (Kaplan et al., 2014).<sup>12</sup> Firms face idiosyncratic shocks. Firms post state-contingent wage contracts, and risk-averse workers accept a job they match with if the expected value of taking the job exceeds the value of not taking the job. Both employed and unemployed workers search. Search frictions govern the probability that they receive job offers.

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<sup>11</sup>“Dynamic” refers to modeling labor flows, not modeling productivity dynamics

<sup>12</sup>For an exploration of savings in a model of wage contracting see Souchier (2025)

### 3.2.1 Timing

Each period, the timing of actions is as follows:

1. Production and wage payments take place in time  $t$ ; unemployed workers receive flow utility  $b$
2. Exogenous separations occur with odds  $\delta$
3. Firms post vacancies with state-contingent wage contracts
4. Idiosyncratic productivity shocks are drawn  $s_{t+1}$
5. Unemployed and employed workers match with vacancies with odds  $\lambda_u, \lambda_e$  and decide whether to accept or reject the job offer
6. Endogenous separations occur

### 3.2.2 Contracts

Firms post and commit to state-contingent wage contracts. The future history of productivity shocks is observable to both workers and firms and so can be contracted on. Firms can commit to the contract, but workers cannot commit to not leave for a better employer if they receive a competing offer. The firm is subject to a fairness constraint—it must pay all workers the same wage. This fairness constraint rules out tenure-based contracts, as in Burdett and Coles (2003), and counter-offers as in Cahuc et al. (2006). This also means that firms cannot offer insurance to workers over the risk of exogenous separations. Our strict fairness constraint is common within the wage contracting literature (the Burdett and Mortensen (1998) wage posting tradition features only a single posted wage) because it aids tractability and because internal equity is a real managerial concern (Bewley, 1999; Breza et al., 2018).

### 3.2.3 Unemployed Workers

Unemployed workers earn a flow utility  $b$  and receive an offer from a random employer with probability  $\lambda_u$ . They can choose to accept or reject the offer.

$$V_U = b + \beta(1 - \lambda_u)V_U + \beta\lambda_u \int_V^{\bar{V}} \max\{V_U, V_0\} dF(V_0) \quad (4)$$

The first term  $b$ , is the flow utility of unemployment. In the second term, the worker does not receive a job offer and stays unemployed. In the third term, the worker receives a job offer

with probability  $\lambda_u$  and accepts if the value from the job exceeds the value of unemployment.  $F(\cdot)$  denotes the distribution of posted utilities.

### 3.2.4 Employed Workers

Employed workers are risk-averse and receive utility  $u(w_t)$  from the wage  $w_t$  paid out by their current job's wage contract at the state realized in  $t$ . Search is random. They receive job offers with odds  $\lambda_e$  and can choose to accept or reject the offer, but cannot use the offer to renegotiate pay at their current employer. Notably, they cannot commit to stay at their current employer if the offer they receive exceeds the value of staying. They exogenously separate into unemployment with probability  $\delta$  and may endogenously separate into unemployment if the value of their contract falls below the value of being unemployed. The value of employed workers is thus given by  $V_t$ .

$$V_t = u(w_t) + \beta(1 - \lambda_e)(1 - \delta)\mathbb{E}_{s_{t+1}} [\max(V_{t+1}, V_U)] \\ + \beta\lambda_e(1 - \delta)\mathbb{E}_{s_{t+1}} \left[ \int \max(V_0, V_{t+1}, V_U) dF(V_0) \right] + \beta\delta V_U \quad (5)$$

In Equation 5, the first term is the utility from wages received today. The second term describes the worker who does not receive a job offer and does not separate exogenously. The worker will stay at their current firm unless the value of staying is worse than quitting into unemployment. The third term describes the worker receiving a job offer and accepting it if the value exceeds the value of staying at the current job and the value of unemployment. The fourth term describes the worker exogenously separating into unemployment.

### 3.2.5 Firms

Firms vary in their permanent productivity  $z_j$  and also face idiosyncratic, temporary productivity shocks  $s_{jt}$ , making their total productivity in  $t$   $(1 + s_{jt})z_j$ . The productivity shocks are drawn from the following mean-reverting process:

$$s_{jt} = \rho s_{j,t-1} + \varepsilon_{jt}$$

The firm's productivity level and its labor,  $L_t$ , determine its output which is produced using a linear production technology,  $(1 + s_{jt})z_j L_{jt}$ . The firm's labor evolves as its incumbent workers separate into unemployment or leave for another job and it recruits new workers through its posted wage contract. As discussed previously, the wage contracts are state-

contingent and firms can commit. Instead of optimizing over the optimal wage to offer in every possible state (which is an infinite dimensional problem), we can follow Spear and Srivastava (1987) and write the firm's problem recursively. The firm takes its incumbent workers' promised utility as a state variable and chooses which utility to post in each state next period—subject to the promise-keeping constraint that its incumbents must receive the utility (current wage and future promised utilities) they were promised.

The firm solves:

$$\Pi(V_t, L_t, s_t, z) = \max_{w_t, V_{t+1}(s_{t+1})} ((1 + s_t)z - w_t)L_t + \beta \mathbb{E}_{s_{t+1}} [\Pi(V_{t+1}, L_{t+1}, s_{t+1}, z)] \quad (6)$$

subject to a promise-keeping constraint:

$$\begin{aligned} V_t = & u(w_t) + \beta(1 - \lambda_e)(1 - \delta) \mathbb{E}_{s_{t+1}} [V_{t+1}] \\ & + \beta \lambda_e(1 - \delta) \mathbb{E}_{s_{t+1}} \left[ \int \max(V_0, V_{t+1}) dF(V_0) \right] + \beta \delta V_U \end{aligned} \quad (7)$$

Firms post promised utilities  $V$  for each state  $s$  for  $t + 1$ , which affects the number of workers  $L_{t+1}(V_{t+1}, L_t)$  in each state. The promise-keeping constraint implies a wage  $w_t$  that the firm must pay out to incumbent workers to satisfy the utility they were promised  $V_t$ . For example, to reduce the number of workers it has (say, in response to a bad shock), the firm must cut the posted  $V$  from one period to the next. When cutting  $V$ , the firm will have to pay a high enough wage to incumbent workers to satisfy this constraint. The impact of the promise-keeping constraint grows as the firm has more incumbent workers. If workers are risk neutral, the promise-keeping constraint does not influence the firm's problem since utility is transferrable; the firm will choose the future utilities to post to maximize profits and then will pay the incumbents the wage required to satisfy the promise. Paying the worker a large sum at once becomes costly when the worker is risk-averse.

Labor evolves as follows:

$$\begin{aligned} L_{t+1}(V_{t+1}, L_t) = & L_t(1 - \delta)(1 - \lambda_e(1 - F(V_{t+1})) \times \mathbb{I}[V_{t+1} > V_U]) + \lambda_u u \times \mathbb{I}[V_{t+1} > V_U] \\ & + \lambda_e(1 - u)(1 - \delta)G(V_{t+1}) \end{aligned} \quad (8)$$

The first term reflects that the firm will keep incumbents who do not exogenously separate, leave for a better job, nor endogenously separate. The second term reflects hiring from unemployment. The third term reflects poaching of employed workers from other firms.  $G(\cdot)$  denotes the distribution of employed workers' current promised utilities.

### 3.3 Equilibrium Definition

Let  $\mu(V, L, s, z)$  refer to the joint distribution of firms across incumbent promised utility, labor, productivity shocks, and productivity levels. A *recursive equilibrium* is a set of value functions, policies, and distributions  $\{V_U, V^{POL}(V, L, s, z), \Pi(V, L, s, z), \mu(V, L, s, z)\}$  such that (i) firms' policies maximize profits subject to the promise-keeping constraint and fairness constraint (ii) workers decide whether to accept job offers to maximize utility (iii) the distribution  $\mu(V, L, s, z)$  is consistent with firms' posting strategies and workers' acceptance rules (iv) labor market clearing holds:  $\int L(V, L, s, z) d\mu(V, L, s, z) + u = 1$ .

The equilibrium is a fixed point in the distribution  $\mu(V, L, s, z)$ . Note that the cross-sectional distributions of posted contracts and employment across promised utilities,  $F(V)$  and  $G(V)$ , are implied from  $\mu(V, L, s, z)$ .

## 4 Characterizing the optimal contract

Here we characterize the equilibrium by considering the firm's first order conditions associated with the optimization problem (6). The firm chooses the incumbent workers' wage payments for this period  $w_t$  and the posted state-contingent promised utilities  $V_{t+1}(s_{t+1})$ .

$$\mu_t u'(w_t) = L_t \tag{9}$$

$$\mu_{t+1} = \mu_t [(1 - \lambda_e)(1 - \delta) + \lambda_e(1 - \delta)F(V_{t+1})] + \Pi_L L'(V_{t+1}) \tag{10}$$

where  $\mu$  is the Lagrange multiplier on the promise-keeping constraint. Recall that the promise-keeping constraint pins down the wage, given the incumbent's previous promised utility. To cut the expected promised utility in  $t + 1$ , firms must pay workers a sufficiently high wage to keep previous promises. Equation 9 is the FOC with respect to  $w_t$ . Here, we see that the firm trades off the cost of a higher wage,  $L_t$  (since they must pay all incumbents the higher wage), against the benefit of a higher wage, that they relax the promise-keeping constraint by  $u'(w_t)$ , scaled by the benefit to the firm of a looser promise-keeping constraint  $\mu_t$ . Note that cost of a higher wage increases with the number of incumbents. The curvature of the utility function also matters: since  $u'(\cdot)$  falls with  $w$ , delivering a given increase in promised utility through the wage is more expensive as the wage increases. Equation 10 is the FOC with respect to  $V_{t+1}$ . The left hand side reflects tomorrow's promise-keeping constraint—the cost of increasing  $V_{t+1}$  is a tighter promise-keeping constraint tomorrow. The benefit of increasing  $V_{t+1}$  is made up of two terms. The first term is the benefit of loosening today's promise-keeping constraint  $\mu_t$  (scaled by share of workers who stay—which will

increase in response to an increase in  $V_{t+1}$ ). The second term is the direct effect on profits  $\Pi$  of having more workers, scaled by the increase in workers associated with the increase in  $V_{t+1}$ .

## 4.1 Solution method

Burdett and Mortensen (1998) and a broad class of related models are tractable because the equilibrium is ranking preserving—the ranking of firms by posted wages is the same as the ranking of firms by productivity<sup>13</sup>. By allowing firms to contract over idiosyncratic risk, our economy no longer has a ranking preserving equilibrium. A firm with a higher permanent productivity experiencing a negative temporary shock may post a promised utility above or below a firm with low permanent productivity experiencing a positive shock.

The equilibrium is characterized by a fixed point in the distribution of firms over promised utilities, employment, and productivity states. Solving for a fixed point in four continuous state variables is computationally challenging. To make progress, we develop a first-order approximation to the full risk equilibrium, which permits estimation and analytical characterization of firms' responses to shocks.

Specifically, we consider a first order perturbation of the zero-risk steady state equilibrium. The economy is in the zero-risk ( $s = 0$ ) steady state equilibrium at time 0 and then learn that at time  $t = 1$  there will be a small amount of idiosyncratic risk— $s_1 \in \{-\epsilon, +\epsilon\}$  with equal odds for all firms. This small shock has a persistence  $\rho$  so that  $s_{j+1} = \rho^j s_1$ . Note that, to first order, this introduction of a small amount of idiosyncratic risk does not change  $F(V)$  or other equilibrium objects.

To see this, let  $F(\bar{V}; \epsilon)$  denote the cumulative distribution function with  $\epsilon$ -sized symmetric shocks,  $V(z, s)$  denote the value posted by a firm with permanent productivity  $z$  who has experienced a shock  $s \in \{-\epsilon, +\epsilon\}$ , and  $J(z)$  be the distribution of permanent productivity levels.

$$F(\bar{V}; \epsilon)|_{\epsilon=0} = \int Pr(\mathbb{I}\{V(z, s) \leq \bar{V}\}) dJ(z)$$

Linearizing around our small shock  $s = \{-\epsilon, \epsilon\}$ ,

$$F(\bar{V}; \epsilon)|_{\epsilon=0} = \int Pr(\mathbb{I}\{V(z, 0) + V_s(z, 0)s \leq \bar{V}\}) dJ(z)$$

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<sup>13</sup>For example, this is also true in Gouin-Bonenfant (2022) where wages are exclusively a function of productivity or in Moscarini and Postel-Vinay (2013) where there are aggregate shocks but no idiosyncratic shocks

$$= \frac{1}{2} \int \mathbb{I}\{V(z, 0) + V_s(z, 0)\epsilon \leq \bar{V}\} dJ(z) + \frac{1}{2} \int \mathbb{I}\{V(z, 0) - V_s(z, 0)\epsilon \leq \bar{V}\} dJ(z)$$

Let  $z^*$  solve  $V(z^*, 0) = \bar{V}$  so this is the productivity cutoff where  $J(z^*) = F(\bar{V}; 0)$ . So following the positive shock we have  $V(z_+(\epsilon), 0) + V_s(z_+(\epsilon), 0)\epsilon = \bar{V}$ . Linearizing around  $z^*$ , we have  $V(z_+(\epsilon), 0) = V(z^*, 0) + V_z(z^*, 0)(z_+(\epsilon) - z^*)$ . We can rearrange to show that, to first order:

$$z_+(\epsilon) = z^* - \frac{V_s(z^*, 0)}{V_z(z^*, 0)}\epsilon$$

Similarly for the negative shock, we can show:

$$z_-(\epsilon) = z^* + \frac{V_s(z^*, 0)}{V_z(z^*, 0)}\epsilon$$

We know that  $F(\bar{V}; \epsilon)|_{\epsilon=0} = \frac{1}{2}J(z_+(\epsilon)) + \frac{1}{2}J(z_-(\epsilon))$ . So we can see that this does not change to first order with  $\epsilon$ :

$$\frac{dF(\bar{V}; \epsilon)}{d\epsilon} = -\frac{1}{2}J'(z_+(\epsilon))\frac{V_s(z^*, 0)}{V_z(z^*, 0)} + \frac{1}{2}J'(z_-(\epsilon))\frac{V_s(z^*, 0)}{V_z(z^*, 0)} = 0$$

Intuitively, a small amount of idiosyncratic risk will not change the rank-preserving equilibrium properties of the zero-risk equilibrium. This is desirable because it means that we can solve for the productivity-wage pass-through while holding fixed the equilibrium objects from the zero-risk steady state—which can be solved for in closed form.

## 4.2 The wage markdown

What is the relevant labor supply elasticity for estimating wage markdowns? What can the flow labor response to shocks tell us about the markdown? And how does the markdown depend on worker risk aversion? In this section, we will leverage our first order approximation to show that the wage markdown depends on the cross-sectional labor supply elasticity. How employment adjusts to shocks can also be used to infer the markdown—but this relationship is not direct. Risk aversion reduces the worker's reservation wage which widens the average wage markdown, but this is the only channel through which risk aversion affects firm's wage-setting power.

**Proposition 1** (Wage markdown). *To first order in the extent of idiosyncratic risk  $s$ , the*

firm with permanent productivity  $z$  has a wage markdown,  $m(z) \equiv \frac{z-w(z)}{w(z)}$ , equal to:

$$m(z) = \frac{1 - q(z)}{u'(w(z)) \frac{w(z)L_V}{L(z)}} (1 - \beta q(z)) \quad (11)$$

$$= \frac{1}{\varepsilon_{Lw}^{CROSS}} \quad (12)$$

where  $L_V$  is the flow labor response to a change in promised utility,  $q(z) \equiv (1 - \delta)[1 - \lambda_e(1 - F(V(z)))]$  is the share of workers who quit each period, and  $\varepsilon_{Lw}^{CROSS}$  is the elasticity of steady-state employment with respect to an increase in the wage.

See Appendix A2 for proof

Proposition 1 highlights that the elasticity of steady-state employment with respect to a permanent increase in the wage can be inverted to estimate the wage markdown in a search model. We refer to this object as the *cross-sectional* labor supply elasticity because it is analogous to comparing the employment at firms with permanently different productivity levels (which offer permanently different wages).

What does the firm response to shocks tell us about the wage markdown? Consider a firm which increases its promised utility and, in the following period, its workforce expands. What does this flow labor response,  $L_V$ , tell us about the markdown? The expression 11 relates how labor adjusts to a shock to the markdown. Notably, this expression does not contain the frequently empirically estimated shock-identified labor supply elasticity—what percent does employment respond to a percent increase in wages induced by a productivity shock—which we will discuss in more detail in Section 4.3. Here, we focus on how firm wage and employment dynamics can be used to estimate wage markdowns<sup>14</sup>. We ask, what does  $L_V$  tell us about the long-run labor response to a permanent wage increase?

The flow labor response,  $L_V$ , differs in two important ways from the cross-sectional labor response. First, labor adjusts slowly over time. This means that if the firm maintained the same promised utility over future years, it would accumulate more workers. Some simple arithmetic allows us to relate the short-run labor response to a steady-state labor response. When we write  $\frac{dL_t}{dV_1} = (1 - q)\frac{dL_{t-1}}{dV_1} + L_V$  we can solve for the steady state and get  $\frac{dL_{CROSS}}{dV} = \frac{L_V}{q}$ . This means that we need to adjust the flow labor response by the fraction of workers which quit each period. Second,  $L_V$  is how labor responds to a change in value, not a change in the wage. The firm can increase the worker's promised utility with many different types of wage contracts that may vary in their cost to the firm, but in steady-state this is

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<sup>14</sup>Empirical estimates of the cross-sectional labor supply may be confounded by amenities and other permanent differences across firms. Therefore, it may be easier to find credible empirical estimates of how firms respond to shocks

achieved through a constant, permanent wage increase. To determine the costs increasing the value of the contract through a permanent wage increase, we can differentiate the promise-keeping constraint with respect to a permanent promised utility increase to find that the corresponding wage change is  $\frac{1-\beta(1-\delta)[1-\lambda_e(1-F(V(z)))]}{u'(w(z))}$  (details in Appendix A2).

**Proposition 2** (Risk aversion and the wage markdown). *To first order in the extent of idiosyncratic risk  $s$ , increasing worker risk aversion lowers the reservation wage and results in wider wage markdowns  $m(z) = \frac{z-w(z)}{w(z)}$  when the search efficiency of unemployed workers is greater than that of employed workers,  $\lambda_u > \lambda_e$ .*

*There is no effect of worker risk aversion on the wage markdown when the reservation wage is held constant.*

*See Appendix A2 for proof*

Do equilibrium wage markdowns depend on worker risk aversion? There are two channels through which risk aversion can affect markdowns: (1) through the reservation wage and (2) through the extent of between-firm competition. While the arrival rate of job offers to employed workers and the productivity distribution itself both can affect the extent of local competition, worker risk aversion has no such direct effect. Intuitively, this can be thought of as capturing the notion that firms cannot insure workers against permanent shocks.

But risk aversion does affect the reservation wage. Unemployed workers are exposed to risk in the job search process—they trade off waiting longer in unemployment and potentially receiving a better job offer with having to spend more time receiving only unemployment benefits for income. Taking a job quickly means workers give up the higher search efficiency of being in unemployment, but risk averse workers value a potentially high income job relatively less.

This means that if the reservation wage is held fixed, worker risk aversion has no effect on wage markdowns. In contrast, even when the reservation wage is constant, worker risk aversion may influence the contract value change that we infer from the empirical wage changes. This means that worker risk aversion influences how we use the firm response to shocks to estimate market power.

### 4.3 The pass-through of idiosyncratic shocks

How do shocks influence the firm’s wage decision? How does the shock-identified labor supply elasticity differ from the cross-sectional labor supply elasticity? What does the firm response to shocks tell us about the extent of market power? To get at these questions, we will study how the firm’s choice of the promised utility to offer its workers responds to the

shock. From these promised utility changes we will use the labor flow equation to back out the labor response and the promise-keeping constraint to solve for the wage response.

We can differentiate the policy function for the promised utility to offer at time  $t + 1$ ,  $V^{POL}(s_{t+1}, L_t, V_t)$ , with respect to the shock that hit at time 1,  $s_1$ .<sup>15</sup>

$$\frac{dV^{POL}(s_{t+1}, L_t, V_t)}{ds_1} = V_s^{POL} \frac{ds_{t+1}}{ds_1} + V_L^{POL} \frac{dL_t}{ds_1} + V_V^{POL} \frac{dV_t^{POL}}{ds_1} \quad (13)$$

There are three channels through which the shock affects the promised utility. The direct channel,  $V_s^{POL}$ , captures how the shock boosts profitability. This incentivizes the firm to have a larger workforce, so they increase the promised utility. The strength of this channel over time depends on the persistence of the shock,  $\frac{ds_{t+1}}{ds_t}$ .

Next, as the firm accumulates (or sheds) workers following the shock, its incentive to offer a higher promised utility changes. When the firm has more workers, offering a higher promised utility will scale up the retention of a larger number of workers. So immediately after the shock,  $\frac{dL_0}{ds_1}$  will be zero, but in the following periods the promised utility will respond to changes in the workforce through the  $V_L^{POL}$  channel.

Lastly, the promised utility of the firm's incumbent workers impacts its choice of a promised utility the following period when the workers are risk-averse. When the workers are risk neutral, the promise-keeping constraint does not distort the firm's choice of the next period promised utility—utility is transferable so the firm will “pay out” its incumbents whatever is required to allow for the posting decision next period to recruit/retain the profit-maximizing number of workers. But when the workers are risk-averse, it becomes costly to shift the next period promised utility far from today's promised utility. Cutting the promised utility requires boosting the wage and, with risk-averse workers, a sufficiently large decrease might be *impossible* to achieve with a wage payment that satisfies the promise-keeping constraint. Similarly to the  $V_L^{POL}$  channel, the  $V_V^{POL}$  kicks in over time as the increase to the promised utility in period  $t$ ,  $\frac{dV_t}{ds_1}$ , makes it cheaper to keep the promised utility high in  $V_{t+1}$  (and vice versa for the negative shock).

This final channel is critical for understanding how insurance impacts the dynamics of wages and labor following a shock. Risk aversion smooths the promised utility response to the shock—making it more costly to adjust the promised utility initially, but then causing the affect to be more persistent as it is costly to sharply return the promised utility to its steady state value even as the shock has dissipated.

The promised utility response determines the wage response and the labor response through the promise-keeping constraint 46 and the labor flow equation 8 respectively. First,

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<sup>15</sup>note that because we are evaluating at the zero risk steady state, we know that the partial derivatives are constant over time to first order

we can differentiate the labor flow equation at period  $t + 1$  with respect to the shock which hit at period 1:

$$\frac{dL_{t+1}}{ds_1} = [(1 - \lambda_e)(1 - \delta) + \lambda_e(1 - \delta)F(V_{t+1})] \frac{dL_t}{ds_1} + L_V \frac{dV_{t+1}^{POL}}{ds_1} \quad (14)$$

The increase in promised utility in period  $t + 1$  directly affects the labor that period as it causes the firm to retain more incumbents and recruit more new hires. This change is captured in the partial derivative of the flow labor equation 8 with respect to  $V_{t+1}$  and is scaled up by the magnitude of  $\frac{dV_{t+1}}{ds_1}$ . Additionally, labor accumulates over time as some fraction of the firm's incumbent workers will either not receive an offer  $((1 - \lambda_e))$  or receive an offer from a worse firm  $(\lambda_e F(V_{t+1}))$  and will not be exogenously separation  $(1 - \delta)$ . This means that the entire history of promised utility responses to the shock feeds into the labor response at period  $t + 1$  through this  $\frac{dL_t}{ds_1}$  term which represents the change in incumbent workers.

Similarly, to understand what the path of promised utility response implies about how wages adjust to this productivity shock, we differentiate the promise-keeping constraint 46.

$$\frac{dV_t^{POL}}{ds_1} = u'(w) \frac{dw_t}{ds_1} + \beta [(1 - \lambda_e)(1 - \delta) + \lambda_e(1 - \delta)F(V_{t+1})] \frac{dV_{t+1}^{POL}}{ds_1} \quad (15)$$

Rearranging this expression we have the wage response,  $\frac{dw_t}{ds_1}$  as a function of the current and future promised utility changes following the shock:

$$\Rightarrow \frac{dw_t}{ds_1} = \frac{\frac{dV_t^{POL}}{ds_1} - \beta [(1 - \lambda_e)(1 - \delta) + \lambda_e(1 - \delta)F(V_{t+1})] \frac{dV_{t+1}^{POL}}{ds_1}}{u'(w)} \quad (16)$$

Intuitively, if the current promised utility is higher then, all else equal, this increases the wage the firm will pay out—and the extent of this change depends on the worker's marginal utility  $u'(w)$ . But, if the firm also increases the promised utility *next* period then this reduces its need to increase wages to fulfill the promise-keeping constraint.

**Proposition 3** (Shock-identified labor supply elasticity). *In the first period following an idiosyncratic productivity shock, the shock-identified labor supply elasticity is as follows:*

$$\varepsilon_{shock,Lw} = \frac{L_V u'(w) \frac{w}{L}}{1 - \beta q(z) \frac{\frac{dV_2}{ds_1}}{\frac{dV_1}{ds_1}}}$$

*Inverting this shock-identified labor supply elasticity fails to recover the wage markdown.*

*See Appendix A2 for proof*

Inverting this shock identified labor supply elasticity does not produce the wage markdown—how do these two values compare? Recall from Proposition 1 the flow labor formulation of the wage markdown is  $m(z) = \frac{1-q(z)}{u'(w(z)) \frac{w(z)L_V}{L(z)}} (1 - \beta q(z))$ . The inverse shock-identified labor supply elasticity does not account for labor accumulating over time (the fraction of workers who quit each period which is on the numerator of  $m(z)$ ). This biases us to estimate a wider markdown by inverting the shock-identified—that is, we would overestimate the extent of market power.

Additionally, firms may choose wage payments over time implement the same  $V$  change differently when responding to a temporary shock. While the permanently more productive firm pays a constantly higher wage, a firm who is temporarily more productive may front-load its wage payments during the periods that it is most productive. If the wage is decreasing over time, this would make  $\frac{\frac{dV_2}{ds_1}}{\frac{dV_1}{ds_1}}$  less than 1. This would also lead us to overestimate the extent of market power. Intuitively, the same wage change would produce a larger labor response if it is permanent and so estimating a labor supply elasticity using a more temporary shock can make labor appear more inelastic.

It is not guaranteed that inverting this labor supply elasticity (which is estimated immediately following the shock) will imply too much market power. As we have discussed, as the firm increases its promised utility and accumulates more workers the dynamic channels— $V_L^{POL}$  and  $V_V^{POL}$ —will kick in and this can cause  $\frac{dV_2}{ds_1} > \frac{dV_1}{ds_1}$ . Especially if the shock is very persistent (so the direct channel  $V_s^{POL}$  remains strong) and the workers are risk averse (so the  $V_V^{POL}$  is very relevant), it is possible for the wage to *increase* in the years following the shock. If the wage increases strongly in the years following the shock, then it is possible that using the first period wage change would result in a shock-identified labor supply elasticity which is more elastic than the cross-sectional elasticity.

What if we calculate the labor supply elasticity several periods after the shock or take an average over a longer window? Empirically, we know that the labor supply elasticity  $t$  periods after the shock,  $\frac{\frac{dL_{t+1}w}{ds_1}}{\frac{dw_{t+1}L}{ds_1}}$ , is more elastic over time (i.e., as  $t$  is larger). As more time goes on, the labor response accumulates and, as the shock fades, the firm lowers the wage. These both can reduce the measured labor supply elasticity. At an extreme, if the firm maintained a high wage for three periods and then cut the wage back to baseline, if we estimated a labor supply elasticity at period four we would deem the firm's labor supply elasticity was infinitely elastic.

The shock-identified labor supply elasticity is a complex, dynamic object and it does not directly map onto the wage markdown. But we can leverage the dynamic wage and labor response to shocks to estimate wage markdowns. By modeling the firm's choice of

the optimal contract we can understand how wages vary beyond the years we observe and by modeling the worker’s behavior we can use their risk aversion, the arrival rate of jobs, and other relevant parameters to map these wages changes onto an implied promised utility change. This allows us to infer the wage markdown.

## 4.4 Identification intuition

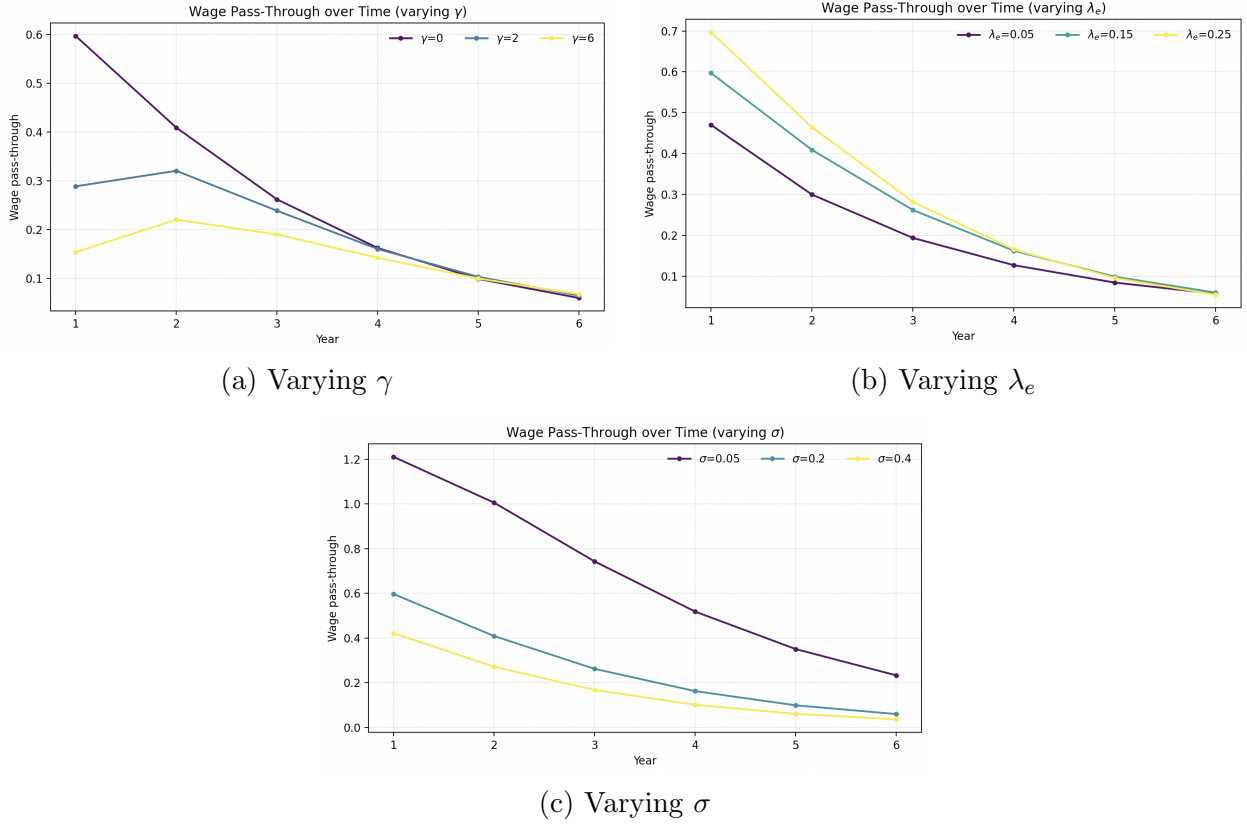
We have characterized how firms contract over idiosyncratic shocks. Now, we will discuss how our model can leverage the firm’s wage and labor response to shocks to estimate the extent of monopsony power and the degree of wage insurance. First, we need to take the empirical wage changes, infer future unobserved wage changes, and convert this to a change in promised utility at each point in time. We accomplish this by solving the firm’s contracting problem.

To deepen the intuition for what determines how firms respond to shocks, we simulate the model. Here, we parameterize the worker’s utility function as constant relative risk aversion with coefficient  $\gamma$ , the firm permanent productivity distribution as being log-normal with mean  $\mu$  and standard deviation  $\sigma$ , and we hold the reservation wage constant so changing the extent of risk aversion has no effect on market power.

Search frictions and dispersion in the productivity dispersion both influence firm’s market power and in Figure 3, we show that these parameters also affect the wage pass-through. Increasing search frictions, increasing productivity dispersion—and reducing worker risk aversion—all broadly result in a larger wage pass-through. But notably, increasing worker risk aversion results in a more persistent, flatter wage response. This is because when there are costs to adjusting incumbent worker’s promised utility, this induces larger promised utility increases in the future, as it is costly to reduce pay back down as the shock is dissipating. This means that the early wage increases are muted and the overall wage effect is flatter over time when worker risk aversion is higher. In other words, insurance induces a more persistent wage response.

Modeling the firm’s problem allows us to understand how the value of the contract is changing in the years following the shock. Then, we can look at the labor response that these promised utility changes induce over time. The rate at which workers receive job offers and the productivity distribution both influence how employment adjusts to changes in the value of the contract. We search for the set of parameters where the solution to the firm’s problem matches the observed wage changes and where the solution to the worker’s problem matches the observed labor changes.

Figure 3: Wage pass-through over years under different parameters



*Notes* We take the average across all active firms and plot the response from years 1 to years 6 following the shock. Each panel varies one of the parameters of interest and other parameters will take the following values:  $\delta = 0.016$ ,  $\beta = 0.996$ ,  $\rho = 0.95$ ,  $\mu = 2$ ,  $z_{min} = 1$ ,  $w_R = 1.8$ ,  $\lambda_u = 0.4$ ,  $\lambda_e = 0.15$ ,  $\sigma = 0.2$ ,  $\gamma = 0$ .

## 5 Estimating the Model

We have established that worker risk aversion induces a smaller, more persistent wage response. This allows us to use the observed wage changes and infer the contract’s value change. Then, the dynamics of how labor responds to these promised utility changes allows us to estimate the wage markdown. We now turn to the data to quantify our model and estimate the prevalence of insurance and market power in the U.S. labor market.

Each period corresponds to one month and we set  $\beta = 0.996$  to match an annual interest rate of 4%. We also externally calibrate  $\delta = 0.016$ . The productivity distribution is log-normal with mean  $\mu$  and standard deviation  $\sigma$ . It is truncated so that the minimum productivity value is  $z_{min}$ . This parameter will influence the share of firms which are below the reservation wage (and therefore inactive) and allow us to better match the unemployment rate. The utility function is CRRA with coefficient  $\gamma$ . Lastly, we have to estimate the arrival rate of job offers to the unemployed,  $\lambda_u$ , and to the employed,  $\lambda_e$ .

We will match these six parameters by using simulated method of moments. In addition to the dynamic response of wages and labor to the productivity shock, we will match the standard deviation of revenue, wages, and employment as well that employment-to-employment transition rate (EE rate) and the unemployment rate. Together, we are estimating these six parameters by matching seventeen moments.

In our model, large firms and small firms behave very differently. Large firms are further up the productivity distribution where the odds of a worker getting an offer better than their current job are smaller—leading them to face a more inelastic labor supply and mark down wages more. Our wage and labor pass-through estimates come from Compustat firms which are substantially larger and more productive than the median American firm. To take this concern seriously, we generate our model wage and labor pass-through measures on the top of the productivity distribution employing 30% of the workforce. This roughly matches the share of workers at publicly traded firms in the United States. Our standard deviation moments were made on the LBD-LEHD sample which is fairly representative of the economy and does not have this concern. Similarly, the unemployment rate and the EE rate are economy-wide moments.

We use simulated method of moments and minimize the loss function

$$L = \sum_i \left| \frac{m_i^{\text{model}} - m_i^{\text{data}}}{m_i^{\text{data}}} \right|, \quad (17)$$

where  $m_i^{\text{model}}$  and  $m_i^{\text{data}}$  denote the model-implied and empirical values of moment  $i$ , respectively.

## 5.1 Baseline Estimation

Figure 4 plots our simulated wage and labor pass-throughs over time against the empirical analogs. Table 2 reports the fit for cross-sectional moments. Our model fit is broadly good. We match the small wage pass-through, the relatively flat wage response, the accumulation of labor over time, and the cross-sectional dispersion. Notably, our model fails to match the first period wage response. This is because our model features perfect firm commitment; because there is such a large, persistent wage increase in the subsequent years, the firm does not initially raise wages but is successfully able to recruit/retain additional workers. Relaxing the assumption of perfect commitment would likely facilitate our ability to match this moment.

Our estimate of  $\gamma$  is on the large side, but the literature estimating the coefficient of relative risk aversion produces a wide range of values—Gandelman and Hernández-Murillo (2015) note that these estimates range from 0.2 to over 10. This suggests workers strongly value stable pay: a worker would accept approximately 3% lower pay to avoid a 10% symmetric wage gamble<sup>16</sup>. We find a relatively high level of  $\lambda_e$  and a relatively small  $\sigma$ . This suggests that firms face considerable competition—both due to their workers frequently receiving outside offers and because they are relatively close, in terms of productivity, to their competitor firms.

What do our parameter estimates imply about the level of labor market power? Our estimates of  $\sigma$  and  $\lambda_e$  imply that firms exert a relatively small degree of monopsony power. Indeed, we estimate that the average worker’s wage is marked down by 8.3%. This is a modest markdown relatively to the literature which typically finds markdowns between 15% and 50% (Azar and Marinescu, 2024).

Table 2: Aggregate Moments and Model Fit

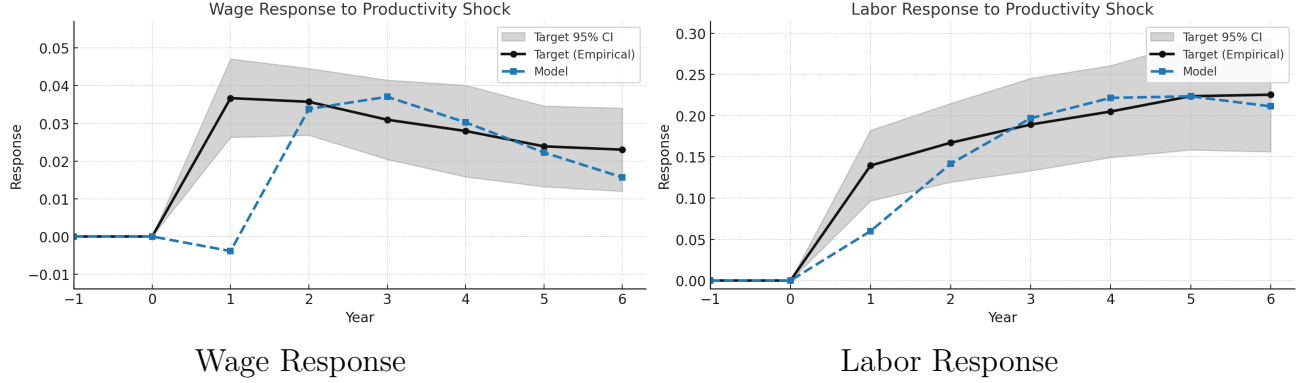
Moment	Target	Model
$ee$	0.022000	0.024856
$sd[\log L]$	1.309000	1.226063
$sd[\log \text{Rev}]$	1.513000	1.289961
$sd[\log w]$	0.442000	0.432393
$u$	0.043000	0.042354

*Notes:* “Target” are data moments; “Model” are simulated moments at baseline parameters; dispersion moments from LBD–LEHD, EE and  $u$  are economy-wide. Target moments are from FSRDC Project Number 3060 (CBDRB-FY25-P3060-R12493)

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<sup>16</sup>The Arrow-Pratt risk premium approximation is  $\pi \approx \frac{1}{2}\gamma\text{Var}(w) = \frac{1}{2} \cdot 5.97 \cdot 0.01 = 2.99$  for a 10% gamble

Figure 4: Baseline impulse responses of wages and labor



*Notes:* Empirical impulse response to value-added per worker shocks from Eq. (1) and model-simulated paths; horizons are years; Compustat-LEHD-LBD sample; 95% confidence intervals if shown. Target moments are from FSRDC Project Number 3060 (CBDRB-FY25-P3060-R12493).

Table 3: Estimated structural parameters

Parameter	Estimate	Description
$\gamma$	5.973	Worker risk aversion
$\lambda_e$	0.145	Employed worker job arrival rate
$\lambda_u$	0.362	Unemployed worker job arrival rate
$\mu$	0.683	Mean of productivity distribution
$\sigma$	0.057	Standard deviation of the productivity distribution
$z_{\min}$	0.682	Truncation point of productivity distribution

*Notes:* SMM point estimates;  $\beta = 0.996$ ,  $\rho = 0.953$ , and  $\delta = 0.016$  fixed (monthly); CRRA utility; productivity is log-normal truncated at  $z_{\min}$ .

## 5.2 Alternate Specifications

Our model features sluggish labor adjustment due to search frictions and the firm provision of wage insurance. How would our estimate of the wage markdown differ if we adopted an approach which did not account for these dynamics? We can compare our estimate of an 8.3% markdown to what we would get if we inverted our shock-identified labor supply elasticities. If we inverted the year 1 labor supply elasticity we would estimate a 26% markdown, while if we inverted the year 6 labor supply elasticity we would estimate a 10% markdown. Alternatively, if we pooled the average response across the six years, we would estimate a 16% wage markdown. These markdown values are standard for the literature and suggest that modeling dynamics can hugely affect how we interpret shock-identified labor supply elasticities as evidence of market power.

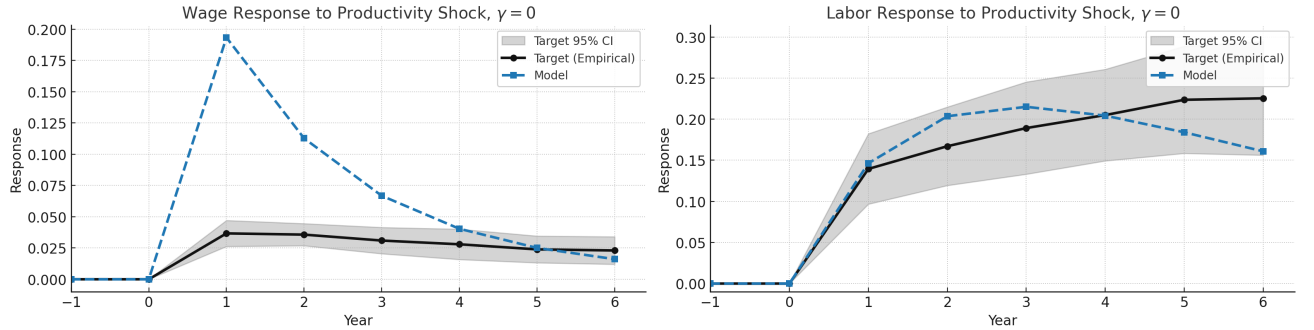
How important is the provision of insurance for matching wage and employment dynamics? To answer this, we shut down the insurance channel in our baseline model by fixing  $\gamma = 0$  and estimate this risk-neutral, wage contracting monopsony model.

Table 4: Aggregate Moments and Model Fit

Moment	Target	Model
$ee$	0.022000	0.033129
$sd[\log L]$	1.309000	1.388853
$sd[\log \text{Rev}]$	1.513000	1.547781
$sd[\log w]$	0.442000	0.373331
$u$	0.043000	0.042553

*Notes:* “Target” are data moments; “Model” are simulated moments at baseline parameters; dispersion moments from LBD–LEHD, EE and  $u$  are economy-wide. Target moments are from FSRDC Project Number 3060 (CBDRB-FY25-P3060-R12493).

Figure 5: Wage and labor fit with wage contracts and risk neutral workers



*Notes:* Empirical impulse response to value-added per worker shocks from Eq. (1) and risk-neutral model-simulated paths; horizons are years; Compustat-LEHD-LBD sample; 95% CIs if shown. Target moments are from FSRDC Project Number 3060 (CBDRB-FY25-P3060-R12493).

Figure 5 shows the wage and labor response to the estimated risk-neutral wage contract model. Without insurance, the model is unable to match the small wage pass-through. Additionally, the wage response is far too steep—initially, the model produces a wage increase that is 600% larger than the one year pass-through but by year six the wage response is below the empirical moment. This highlights how insurance is key to generating a small, flat wage response to shocks.

Notably, the model almost exclusively struggles to fit the wage response. It roughly matches the aggregate moments, except for the employment-to-employment transition rate which it overshoots, and it matches the labor response.

Table 5: Estimated structural parameters ( $\gamma = 0$ )

Parameter	Estimate	Description
$\gamma$	Fixed: 0	Worker risk aversion
$\lambda_e$	0.280	Employed worker job arrival rate
$\lambda_u$	0.360	Unemployed worker job arrival rate
$\mu$	2.298	Mean of productivity distribution
$\sigma$	0.166	Standard deviation of productivity distribution
$z_{\min}$	2.608	Truncation point of productivity distribution

*Notes:* SMM point estimates for model with risk-neutral workers and dynamic wage contracts;  $\beta = 0.996$ ,  $\rho = 0.953$ , and  $\delta = 0.016$  fixed (monthly); CRRA utility; productivity is lognormal truncated at  $z_{\min}$ .

We can also compare the value of the loss function between the estimation when we model insurance and this version where we set  $\gamma = 0$ . The error is 0.744 in our baseline, insurance wage contract model and the error is 5.654 in the risk-neutral wage contract model—over 7 times worse.

Clearly, the risk-neutral wage contract model is unable to match the observed wage and labor dynamics. To understand the implications of worker risk aversion for our estimate of labor market power, we will re-estimate the model to match a more limited set of moments. Specifically, we will target the same aggregate moments and, rather than targeting the full path of wages and labor to an idiosyncratic shock, we will match the average labor supply elasticity over the six year horizon. We define the average labor supply elasticity as the average labor response divided by the average wage response. Empirically, the value of the average labor supply elasticity is 6.44.

We display the estimated parameters in Table 6 and the model fit in Table 7. The parameters imply an average wage markdown of 11%—between the insurance contract model wage markdown (8.3%) and the static model wage markdown estimate that inverts this targeted average labor supply elasticity (16%). Risk aversion causes workers to value temporary wage changes by less than permanent wage changes with the same present dollar value. This is because risk aversion induces an intertemporal smoothing motive where workers would prefer the same dollar change spread out over more years. Assuming that workers are risk neutral would result in overestimating the utility value change associated with a temporary wage change, leading the researcher to infer that the labor response is more inelastic than it truly is. This is reflected in the fact that we estimate wider wage markdowns when we model workers as risk-neutral than when we estimate our full insurance wage contracting model.

Table 6: Estimated structural parameters

Parameter	Estimate	Description
$\gamma$	<b>Fixed:</b> 0	Worker risk aversion
$\mu$	12.379	Mean of log productivity
$\sigma$	0.060	Std. dev. of log productivity
$\lambda_e$	0.222	Employed worker job arrival rate
$\lambda_u$	0.302	Unemployed worker job arrival rate
$z_{\min}$	19.980	Truncation point of productivity distribution

Table 7: Aggregate moments and model fit

Moment	Target	Model
Average $\varepsilon_{Lw}$	6.448320	6.392164
$ee$	0.022000	0.030103
sd[log $L$ ]	1.309000	1.316793
sd[log Rev]	1.513000	1.374384
sd[log $w$ ]	0.442000	0.382863
$u$	0.043000	0.050342

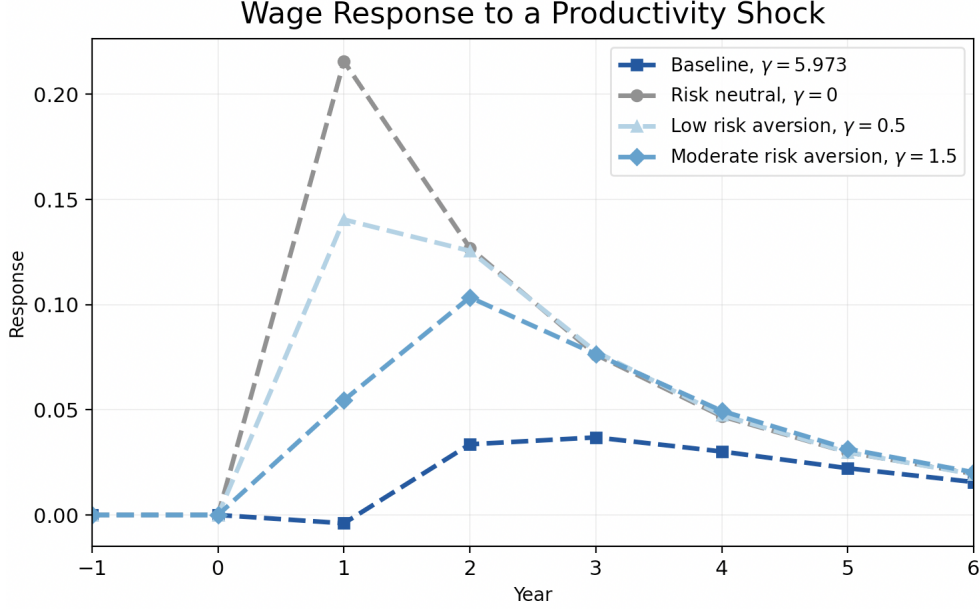
*Notes:* “Target” are data moments; “Model” are simulated moments at the estimated parameters. Target moments are from FSRDC Project Number 3060 (CBDRB-FY25-P3060-R12493).

### 5.3 Insurance and the Wage Pass-Through

We have shown that the wage patterns we observe are consistent with the firm provision of insurance. Our baseline estimation finds that workers are considerably risk-averse, and when we re-estimate the model under the assumption that workers are risk-neutral we dramatically overshoot the wage pass-through. Now, we ask a related question: how does the firm provision of insurance affect the observed wage pass-through? That is, if workers were less risk averse but we retain the same other structural parameters, how would the simulated wage response to an idiosyncratic shock change?

Figure 6 shows that the firm provision of insurance results in a strikingly smaller and more persistent wage pass-through. If workers were risk neutral, firms would respond to the 1% temporary, idiosyncratic shock by increasing wages 0.21% in the first year and quickly reducing pay closer to baseline in the subsequent years. Across the six year following the shock, the average wage increase would be 0.086% without insurance—much larger than the 0.03% average increase we observe empirically. The wage responses when workers are only

Figure 6



*Notes:* Wage response to a temporary ( $\rho = 0.953$ ) 1% idiosyncratic shock among the most productive firms employing 30% of workers (as in baseline estimation); the extent of worker risk aversion is varied and all other parameter values are those reported in Table 3.

somewhat risk averse ( $\gamma = 0.5$ ) or are moderately risk averse ( $\gamma = 1.5$ ) display a similar pattern—worker risk aversion causes firms to offer wage insurance which has a profound effect on the wage pass-through.

How firms adjust wages following shocks is very dependent on the extent of worker risk aversion. This parallels Kline (2025), which notes that the wage pass-through is sensitive to the functional form of the labor supply curve firms.<sup>17</sup> Empirical estimates of how wages respond to firm performance are important evidence of monopsony power—if labor markets were perfectly competitive, there would be one market wage. But can these wage pass-through measures be used to infer the level of wage-setting power? We have demonstrated that this requires carefully modeling the firm provision of insurance, as well as the persistence of shocks and the dynamics of firm adjustment.

## 6 The Constrained Efficient Allocation

We have shown that the firm’s role as an insurer for the worker results in a small and flatter wage response to productivity shocks. This causes firms to hoard labor, adjusting the

<sup>17</sup>Notably, the wage pass-through can either rise or fall with the labor supply elasticity depending on the firm labor supply curve assumed

size of their workforce by less following shocks. We estimate that workers are considerably risk-averse and that firms' behavior reflects this fact. Now, we turn to ask the efficiency implications of this firm provision of insurance. We will show that the provision of wage insurance distorts the job ladder, leading to fewer job-to-job transitions than would be socially optimal. This means that understanding the extent of wage insurance is not just important for our measurement of market power but also has direct policy implications—policies which reduce the need for firms to insure workers will improve labor market dynamism.

Consider a social planner who is constrained by search frictions but can perform transfers. This planner cannot influence how many job offers a worker receives—they can only decide whether the worker should make a transition. Notably, since the planner can perform transfers this problem is not influenced by worker risk aversion. The planner's solution may differ from the decentralized equilibrium in two ways—in which job offers unemployed workers accept and in which job-to-job moves employed workers make.

First, we will briefly describe the unemployed worker's decision. When the search efficiency of employed and unemployed workers is not equal, unemployed workers who are deciding whether to accept or reject a job offer will trade off staying in unemployment for longer with the opportunity to potentially receive a better job offer more quickly. Wages are marked down relative to productivity, so the worker's choice may not align with the planner's solution (as the planner will maximize total value). When workers are risk-averse, they will be quicker to accept job offers. This suggests that the extent of worker risk aversion is important for the optimal unemployment insurance as the level of  $b$  influences the worker's decision over which jobs to accept. This point parallels Acemoglu and Shimer (2000), which shows how unemployment insurance can increase productivity by allowing workers to direct their search to riskier (but more productive) jobs.

Now, we characterize the optimal job-to-job transitions. This will allow us to ask whether firms respond optimally to shocks. We will show that in response to idiosyncratic shocks, firms initially engage in too much labor hoarding and that this is exacerbated by the presence of insurance. Using our parameter estimates from Section 5.1 we will quantify the planner's response to shocks and compare it to the decentralized equilibrium with risk-averse workers *and* the decentralized equilibrium with risk neutral workers.

The planner will move the worker if the social value of the new job,  $W(z_1, s_1)$ , exceeds the social value of their current job,  $W(z_0, s_0)$  where these value functions are defined as follows:

$$\begin{aligned}
W(z, s) = & (1 + s)z + \beta(1 - \lambda_e)(1 - \delta) \mathbb{E}[W(z, s')] \\
& + \beta\lambda_e(1 - \delta) \mathbb{E} \left[ \int \max(W(z, s'), W_0) dF(W_0) \right] + \delta\beta W_U
\end{aligned} \tag{18}$$

We want to know how idiosyncratic risk affects the job ladder. To do this, we will leverage the same first order approximation approach used to characterize the decentralized equilibrium. This will allow us to solve for the efficient firm-level labor response to an idiosyncratic shock and compare that to the decentralized equilibrium.

Since the aggregate distributions are unaffected by the small amount of risk, we know that  $F(W(z, 0)) = J(z)$ . This is because, without risk, firms with a higher permanent productivity  $z$  will always have a higher social value  $W(z, 0)$ . Differentiating 18 with respect to the shock  $s$  and evaluating at  $s = 0$  we can rearrange to show:

$$W_s = \frac{z}{1 - \beta(1 - \delta)\rho[1 - \lambda_e + \lambda_e J(z)]} = z\Phi_0 \tag{19}$$

where  $\rho$  is the persistence of the shock. Intuitively, the value of having a worker at a firm with productivity  $z$  increases in response to the shock and the extent of this benefit depends on a present-value multiplier style term which reflects the persistence of shock and the odds of the worker leaving.

Labor evolves according to:

$$L^*(z, s_t) = L^*(z, s_{t-1})(1 - \delta)(1 - \lambda_e(1 - F(W(z, s_t))) + \lambda_u u + \lambda_e(1 - u)(1 - \delta)G(W(z, s_t)) \tag{20}$$

Differentiating this labor flow expression with respect to the shock  $s_1$ , we can show that the planner's choice of labor at firm with productivity  $z$  will respond by  $\frac{dL^*(z, s_t)}{ds_1}$  in period  $t$  after the shock in period 1:

$$\begin{aligned}
\frac{dL^*(z, s_t)}{ds_1} = & \frac{dL^*(z, s_{t-1})}{ds_1} (1 - \delta)(1 - \lambda_e(1 - J(z))) \\
& + L^*(1 - \delta)\lambda_e F'(W)W_s + \lambda_e(1 - u)(1 - \delta)G'(W)W_s
\end{aligned} \tag{21}$$

**Proposition 4** (Planner response to permanent shock). *Following a permanent shock, at each point in time the planner's labor response is larger than the decentralized labor response, but the two converge to the same value over time.*

$$\frac{dL^*(z, s_t)}{ds_1} > \frac{dL(z, s_t)}{ds_1}$$

$$\lim_{t \rightarrow \infty} \frac{dL^*(z, s_t)}{ds_1} = \frac{dL(z, s_t)}{ds_1} = \frac{2(1 - \delta)\lambda_e J'(z)zL}{1 - (1 - \delta)[1 - \lambda_e(1 - J(z))]}$$

Proposition 4 reveals that the planner responds more aggressively to permanent shocks than the decentralized equilibrium. The planner ranks firms by the permanent productivity differences (since there is only a small amount of idiosyncratic risk) so if the firm receives a positive shock it will be immediately moved to the new position on the job ladder—where it will stay indefinitely as it continues to accumulate more workers and converges to its new, larger employment level. But in the decentralized equilibrium, firms move slowly up the job ladder following a positive permanent shock. As they accumulate workers this boosts the retention motive, so they increase the promised utility and this is reinforced by the fact the incumbents’ promised utility is a state variable—so when today’s promised utility is higher it is even more desirable to offer a higher promised utility tomorrow. In the long-run they converge to the same place on the job ladder as the planner’s solution, but along the transition path they are slower to accumulate workers.

This highlights an important implication of idiosyncratic shocks for the efficiency properties of models in the style of Burdett and Mortensen (1998). While job-to-job transitions when there are no firm-level shocks *and* the job-to-job transitions with wage contracting over aggregate shocks (see Moscarini and Postel-Vinay (2013)) are constrained efficient, the job ladder is no longer efficient in the presence of idiosyncratic risk.

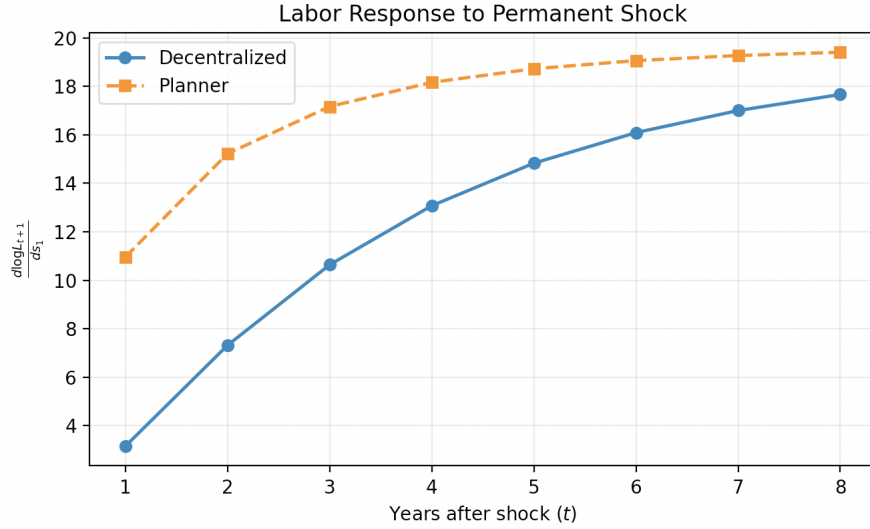
With this equation 21 in hand, we can simulate the planner labor response and compare it to the decentralized labor response. This allows us to quantify the importance of Proposition 4 given the parameters that we estimated in Section 5. In Figure 7, we plot the decentralized equilibrium and planner response to a permanent productivity shock. As expected, we see that the planner responds far more aggressively to the shock and firms are too slow to accumulate workers. This effect is quantitatively large—in the first year the planner has a three times larger labor response than the decentralized equilibrium. Even eight years following the shock there is still a meaningful gap between the planner and decentralized responses.

How does the decentralized response to a *temporary* shock compare to the constrained efficient benchmark? While Proposition 4 is specific to permanent shocks, many of the same forces are present in how firms adjust to the temporary shocks. In Figure 8, we plot the decentralized response to a temporary productivity shock that we estimated in Section 5.1.<sup>18</sup>

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<sup>18</sup>Note that the labor response plotted is different than what we plot in Figure 5.1. This is because we previously matching the response of firms in the top of the productivity distribution (representing 30% of employment) to the empirical response of Compustat firms. For this exercise, we are plotting the response of all firms.

Figure 7



*Notes:* Employment response to a permanent ( $\rho = 1$ ) 1% idiosyncratic shock; decentralized equilibrium vs constrained-efficient planner; parameter values are those reported in Table 3 horizons are years.

Then, we take these same underlying parameters and plot the planner solution.

In the first years following the shock, the planner response is strikingly larger. In response to a 1% productivity shock<sup>19</sup>, the planner moves more workers to the firm, causing it to grow by 5% one year after impact. In contrast, the decentralized equilibrium features a far more modest labor response, with employment increasing by less than 1%. This suggests that the economy features too much labor hoarding in response to temporary shocks relative to the planner's solution.

Notably, by year 7 this pattern reverses with firms holding onto more workers than the planner would choose. The firm provision of insurance results in a stable wage response which causes labor to stay higher for longer. The shock has largely faded away, so the planner would prefer the workers be moved to a more productive firm, but insurance prevents this.

How important is the provision of insurance in distorting the job ladder? Now, we replicate the earlier exercises but change  $\gamma = 0$  when solving the decentralized equilibrium. In Figure 10 we plot this risk-neutral decentralized labor response. Directionally, the patterns look similar—firms adjust slower than the planner wants. But the magnitude of this gap is very different—one year after the shock, the response to the temporary shock and the permanent shock when workers are risk neutral is more than *double* than when workers are as risk-averse as we estimate. By year 4, the risk neutral decentralized response is qualitatively

<sup>19</sup>with persistence  $\rho = 0.953$

Figure 8

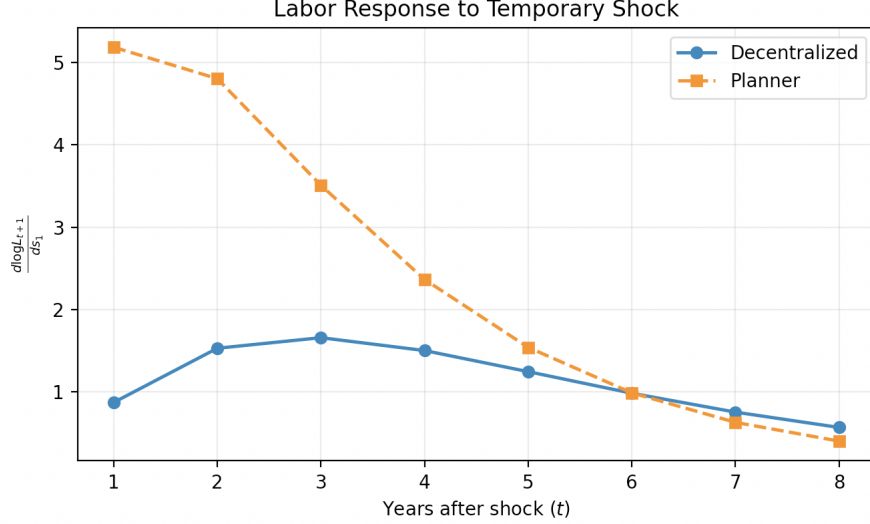


Figure 9

*Notes:* Employment response to a temporary ( $\rho = 0.953$ ) 1% idiosyncratic shock; decentralized equilibrium vs constrained-efficient planner; parameter values are those reported in Table 3 horizons are years.

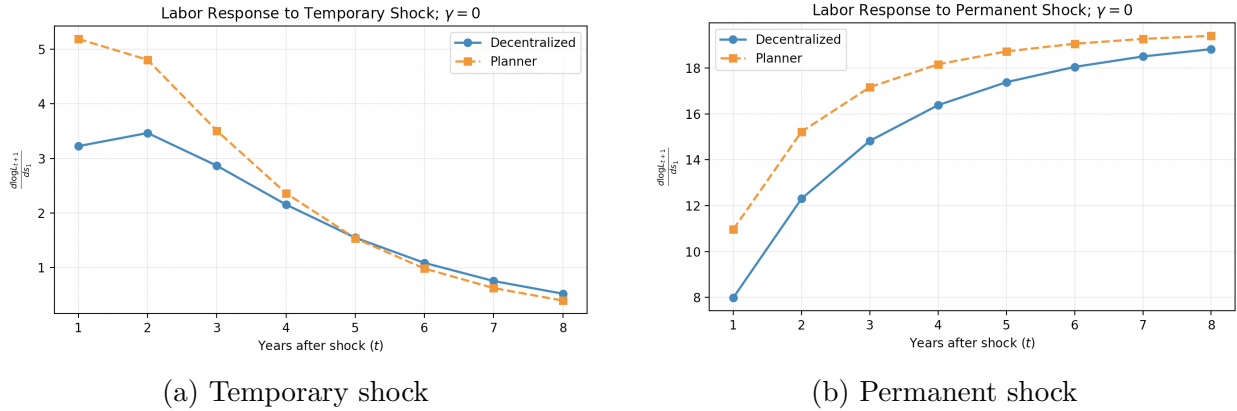
similar to the planner and, similarly, the response to the permanent shock converges much quicker to the planner when workers are risk neutral.

Notably, we have shown that a more aggressive labor response is efficient when the planner can perform transfers. In practice such transfers may be unrealistic. Firms offer wage insurance because workers demand it—but it comes at the cost of reducing job-to-job transitions following shocks. This suggests that policies which reduce the workers’ demand for wage insurance—expanding workers’ access to credit, social insurance, encouraging household savings—would cause firms to adjust labor more aggressively in response to shocks. And by allowing workers to transition to more productive jobs, this would boost output.

## 7 Conclusion

How do we interpret empirical estimates of labor market power that are identified off shocks? We write a random search model where firms offer wage contracts over idiosyncratic shocks to risk-averse workers. We estimate that the average worker’s wage is marked down 8.3% which is a narrower markdown than the literature and smaller than what we find when estimate markdowns by inverting the shock-identified labor supply elasticity. The firm provision of

Figure 10: Risk neutrality brings the decentralized equilibrium close to the planner solution



*Notes:* Employment response to a temporary ( $\rho = 0.953$ ) and permanent ( $\rho = 1$ ) 1% idiosyncratic shock with risk-neutral workers  $\gamma = 0$ ; decentralized equilibrium vs constrained-efficient planner; other parameter values are those reported in Table 3 horizons are years.

insurance is critically important to explaining how firms respond to shocks. Insurance leads firms to hoard labor beyond what is socially efficient and reducing worker risk aversion can bring the firm response to shocks closer to the planner's solution.

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# Appendix

## A1 Data

We construct our earnings data to adjust for the duration of time a worker was employed at a firm and ultimately create an annual measure of earnings. This follows the approach in Abowd et al. (2003) and Sorkin (2018). Specifically, we define a worker to be full-quarter employed if in the preceding and subsequent quarters they also received earnings from the firm. Additionally, we define the worker as continuously employed if they received earnings in *either* the preceding or subsequent quarters. We can now aggregate the quarterly earnings data into an annual measure as follows:

1. If the worker has any full-quarter employment, we take the average over those full quarters and multiply by 4
2. If the worker has no full-quarter employment but does have at least one continuous quarter of employment, we take the average over the continuous employment quarters and multiply this number by 8

## A2 Proofs

### A2.1 Proofs for Section 4

#### A2.1.1 Proposition 1

We know that the first order conditions for the firm's problem satisfy:

$$\begin{aligned} \mu_{t+1}(V_{t+1}, L_{t+1}(L_t, V_{t+1}), V_{t+2}(L_{t+1}, V_{t+1}, s_{t+2})) &= \mu_t(V_t, L_t, V_{t+1}) [(1 - \lambda_e)(1 - \delta) + \lambda_e(1 - \delta)F(V_{t+1})] \\ &\quad + \Pi_L(V_{t+1}, L_{t+1}(L_t, V_{t+1}), s_{t+1})L_V(V_{t+1}, L_t) \end{aligned} \quad (22)$$

$$\mu_t(V_t, L_t, V_{t+1}) = \frac{L_t}{u'(w_t(V_t, V_{t+1}))} \quad (23)$$

To first order in  $s$ , we have shown that the equilibrium is the same as the zero-risk equilibrium. So that means we have a steady state. Rearranging and dropping time subscripts:

$$\frac{L}{u'(w)} = \frac{L}{u'(w)}(1 - \delta)[1 - \lambda_e(1 - F(V))] + \Pi_L L_V \quad (24)$$

We can differentiate  $\Pi$  with respect to  $L$  to show:

$$\Pi_L = \frac{z - w}{1 - \beta(1 - \delta)[1 - \lambda_e(1 - F(V))]} \quad (25)$$

Now, plugging in 25 to 24 and rearranging:

$$\frac{z - w}{w} = \frac{1 - (1 - \delta)[1 - \lambda_e(1 - F(V))]}{u'(w) \frac{w L_V}{L}} (1 - \beta(1 - \delta)[1 - \lambda_e(1 - F(V))]) \quad (26)$$

Note that this is the flow labor response to a change in  $V$ . If we wanted to convert this to a permanent response, we can use that  $L_{stock,V} = \frac{L_V}{1 - (1 - \delta)[1 - \lambda_e(1 - F(V))]}$ . So we have:

$$\frac{z - w}{w} = \frac{1 - \beta(1 - \delta)[1 - \lambda_e(1 - F(V))]}{u'(w) \frac{w L_{stock,V}}{L}} \quad (27)$$

Lastly, we might want to have this expression in terms of an elasticity of stock labor with respect to wages, since the utility of a contract is not observable. There are many ways one could adjust the wage to achieve the same increase in promised utility, but since we are consider the stock (long-run) elasticity we can focus on what permanent wage increase achieve a given increase in promised utility. To achieve this, we can write the promise-keep constraint as follows (constant  $V$ ):

$$V = u(w) + \lambda_e(1 - \delta)\beta \int \max(V, V_0) dF(V_0) + (1 - \lambda_e)(1 - \delta)\beta V + \delta\beta V_U \quad (28)$$

implicitly differentiating with respect to  $V$  shows that:

$$w_V = \frac{1 - (1 - \delta)\beta[1 - \lambda_e + \lambda_e F(V)]}{u'(w)} \quad (29)$$

So, we can write  $L_{stock,V} = \frac{dL_{stock}}{dw} w_V = \frac{dL_{stock}}{dw} \frac{1 - (1 - \delta)\beta[1 - \lambda_e + \lambda_e F(V)]}{u'(w)}$ . Plugging this in and letting  $\varepsilon_{stock,Lw}$  be the elasticity of stock labor with respect to a permanent increase in the wage:

$$\frac{z - w}{w} = \frac{1}{\varepsilon_{stock,Lw}} \quad (30)$$

Now, turning to solving for the wages and labor. To first order in  $s$ , we have shown that the equilibrium is the same as the zero-risk equilibrium. This is similar to Bontemps et al. (2000) in that it is a Burdett and Mortensen (1998) model with heterogeneous productivity drawn from a continuous distribution, but also features risk-averse workers.

First, we will solve for the steady state labor at a promised utility  $V$ . The labor flow equation in steady state must satisfy:

$$L(V) = L(V)(1 - \delta)(1 - \lambda_e F(V)) + \lambda_u u + \lambda_e(1 - u)(1 - \delta)G(V) \quad (31)$$

We can rearrange to show that:

$$L(V) = \frac{\lambda_u u + \lambda_e(1 - u)(1 - \delta)G(V)}{1 - (1 - \delta)(1 - \lambda_e)F(V)} \quad (32)$$

Now we need to solve for  $u$ ,  $G(V)$ , and  $F(V)$ . We know that we have a rank-preserving equilibrium, so  $F(V) = J(z)$ . The unemployment flow equation in steady state satisfies:

$$u = \delta(1 - u) + (1 - \lambda_u \int_{V_R} dF(V))u \quad (33)$$

where  $V_R$  is the reservation promised utility (which can also be formulated as a reservation wage since wages are constant in the first order approximation).

$$\implies u = \frac{\delta}{\delta + \int_{V_R} dF(V)} \quad (34)$$

The reservation promised utility is equal to  $V_U$ :

$$V_U = u(b) + \lambda_u \beta \int_{V_U} V_0 dF(V_0) + (1 - \lambda_u[1 - F(V_U)])\beta V_U \quad (35)$$

When the wage is constant, we can solve also for a reservation wage which will satisfy:

$$V_U = u(w_R) + \lambda_e(1 - \delta)\beta \int \max(V_U, V_0) dF(V_0) + \beta(1 - \lambda_e)(1 - \delta)V_U + \beta\delta V_U \quad (36)$$

Now we must solve for  $G(V)$ . For this, we can consider the flows into and out of employment below the promised utility  $V$ . Let  $\hat{G}(V)$  be the mass of workers with a promised utility below  $V$ :

$$\hat{G}(V) = \lambda_u F(V)u + [(1 - \lambda_e)(1 - \delta) + (1 - \delta)\lambda_e F(V)]\hat{G}(V) \quad (37)$$

Rearranging and using that  $\frac{\hat{G}(V)}{1 - u} = G(V)$  and  $F(V) = J(z)$ :

$$G(V) = \frac{u}{1 - u} \frac{\lambda_u F(V)}{1 - (1 - \delta)[1 - \lambda_e + \lambda_e F(V)]} \quad (38)$$

Now we have all the requisite components to solve for  $L(V)$  in closed form.

Now, we can take the wage solution,  $w(z) = z - \int_{w_R}^z \frac{[\delta + (1 - \delta)\lambda_e(1 - J(x))]}{[\delta + (1 - \delta)\lambda_e(1 - J(x))]} dx$ , and calculate

$$m(z) = \frac{z-w}{w}:$$

$$m(z) = \frac{\int_{w^R}^z \frac{[\delta+(1-\delta)\lambda_e(1-J(z))]^2}{[\delta+(1-\delta)\lambda_e(1-J(x))]^2} dx}{z - \int_{w^R}^z \frac{[\delta+(1-\delta)\lambda_e(1-J(z))]^2}{[\delta+(1-\delta)\lambda_e(1-J(x))]^2} dx} \quad (39)$$

### A2.1.2 Proposition 2

We know that  $w(z) = z - \int_{w^R}^z \frac{[\delta+(1-\delta)\lambda_e(1-J(z))]^2}{[\delta+(1-\delta)\lambda_e(1-J(x))]^2} dx$ .

And also:

$$m(z) = \frac{\int_{w^R}^z \frac{[\delta+(1-\delta)\lambda_e(1-J(z))]^2}{[\delta+(1-\delta)\lambda_e(1-J(x))]^2} dx}{z - \int_{w^R}^z \frac{[\delta+(1-\delta)\lambda_e(1-J(z))]^2}{[\delta+(1-\delta)\lambda_e(1-J(x))]^2} dx} \quad (40)$$

Clearly, this expression only depends on the wage through  $w^R$ . We know that the reservation wage satisfies the following equation:

$$V_U = u(w_R) + \lambda_e(1-\delta)\beta \int \max(V_U, V_0) dF(V_0) + \beta(1-\lambda_e)(1-\delta)V_U + \beta\delta V_U \quad (41)$$

where  $V_U$  is determined by:

$$V_U = u(b) + \lambda_u\beta \int_{V_U} \max(V_U, V_0) dF(V_0) + (1-\lambda_u)\beta V_U \quad (42)$$

We can rearrange these two expression to write the reservation wage as follow:

$$u(w_R) = u(b) + \beta[\lambda_e(1-\delta) - \lambda_u] \left( \int_{V_U} \max(V_U, V_0) dF(V_0) + V_U \right) \quad (43)$$

To see that this implies that  $w_R$  is decreasing in  $\gamma$ , consider the difference between the utility reservation wage and a hypothetical wage at a new job,  $u(w) - u(w_R) = \frac{w^{1-\gamma} - w_R^{1-\gamma}}{1-\gamma}$ . Differentiating with respect to  $\gamma$  gives us:

$$= \frac{(1-\gamma) [-\ln(w)w^{1-\gamma} + \ln(w_R)w_R^{1-\gamma}] + (w^{1-\gamma} - w_R^{1-\gamma})}{(1-\gamma)^2} \quad (44)$$

This is negative when  $w > w_R$ . So the gap in utility decreases between the reservation wage and a future higher wage. This means that the right-hand side of 43 is smaller (because

$\lambda_e(1 - \delta) - \lambda_u > 0$  in the proposition), so the reservation wage must fall as  $\gamma$  rises.

### A2.1.3 Derivation of the wage and labor response to idiosyncratic shocks:

#### Set Up Reminder

Firm solves:

$$\Pi(V_t, L_t, s_t, \bar{z}) = \max_{w_t, V_{t+1}(s_{t+1})} ((1 + s_t)\bar{z} - w_t)L_t + \beta \mathbb{E}_{s_{t+1}} [\Pi(V_{t+1}, L_{t+1}, s_{t+1}, \bar{z})] \quad (45)$$

subject to a promise-keeping constraint:

$$V_t = u(w_t) + \beta(1 - \lambda_e)(1 - \delta)\mathbb{E}_{s_{t+1}} [V_{t+1}] + \beta\lambda_e(1 - \delta)\mathbb{E}_{s_{t+1}} \left[ \int \max(V_0, V_{t+1})dF(V_0) \right] + \beta\delta V_U \quad (46)$$

47 and 48 are the promised utility and wage FOCs respectively with every relevant dependency written out explicitly to facilitate differentiation.

$$\begin{aligned} \mu_{t+1}(V_{t+1}, L_{t+1}(L_t, V_{t+1}), V_{t+2}(L_{t+1}, V_{t+1}, s_{t+2})) &= \mu_t(V_t, L_t, V_{t+1}) [(1 - \lambda_e)(1 - \delta) + \lambda_e(1 - \delta)F(V_{t+1})] \\ &\quad + \Pi_L(V_{t+1}, L_{t+1}(L_t, V_{t+1}), s_{t+1})L_V(V_{t+1}, L_t) \end{aligned} \quad (47)$$

$$\mu_t(V_t, L_t, V_{t+1}) = \frac{L_t}{u'(w_t(V_t, V_{t+1}))} \quad (48)$$

#### First Order Approximation for Wage/Labor Pass-Throughs

We start in the zero-risk steady state in period 0. The firm learns that in period 1 there will be a shock that is either a small positive or small negative  $s_1$ . Now we will solve for the entire path of promised utility, wages, and labor in response to this shock. Consider the first order conditions for wages and promised utility for the firm at time  $t$  which is choosing which promised utility to offer in  $t + 1$ —these are 47 and 48 shown above. We can implicitly differentiate these equations with respect to the initial shock  $s_1$  to ask how promised utility, wages, and labor adjust on impact ( $t = 1$ ) and over time in response to this idiosyncratic shock.

First, note that the response of promised utility in period  $t + 1$  depends on how the firm state variables—incumbent labor, incumbent promised utility, and the shock itself—have adjusted due to the shock. 49 decomposes the total derivative into these three partial

derivatives. Note that the small idiosyncratic risk has no effect on any equilibrium objects to first order, so we have omitted the time subscripts when writing these partial derivatives. Once we solve for the partial derivatives, we will be able to evaluate them at the closed form zero-risk steady state equilibrium values (for labor, wages, etc.).

$$\frac{dV_{t+1}}{ds_1} = V_s \frac{ds_{t+1}}{ds_1} + V_L \frac{dL_t}{ds_1} + V_V \frac{dV_t}{ds_1} \quad (49)$$

In period  $t = 1$ , right when the shock hits, we will have  $\frac{dL_0}{ds_1} = 0$  and  $\frac{dV_0}{ds_1} = 0$ . For  $t > 0$ ,  $\frac{dL_t}{ds_1}$  and  $\frac{dV_t}{ds_1}$  vary as the firm's labor responds and their existing promised utility reflects their previous decisions.

The shock has persistence  $\rho$ —which implies 50.

$$\frac{ds_{t+1}}{ds_1} = \rho^t \quad (50)$$

We can differentiate the flow labor equation 51 with respect to  $L_t$  and with respect to  $V_{t+1}$  to recursively define the  $\frac{dL_t}{ds_1}$  based on the current and prior promised utility responses. This is shown in 52.

$$\begin{aligned} L_{t+1,flow}(V_{t+1}, L_t) &= L_t(1 - \delta)(1 - \lambda_e(1 - F(V_{t+1})) \times \mathbb{I}[V_{t+1} > V_U]) \\ &\quad + \lambda_u u \times \mathbb{I}[V_{t+1} > V_U] + \lambda_e(1 - u)(1 - \delta)G(V_{t+1}) \end{aligned} \quad (51)$$

$$\frac{dL_t}{ds_1} = [(1 - \lambda_e)(1 - \delta) + \lambda_e(1 - \delta)F(V_t)] \frac{dL_{t-1}}{ds_1} + L_V \frac{dV_t}{ds_1} \quad (52)$$

Stacking these equations, the first-order responses satisfy the linear system

$$x_{t+1} = Ax_t, \quad x_t \equiv \begin{pmatrix} \frac{dL_t}{ds_1} \\ \frac{dV_t}{ds_1} \\ \frac{ds_t}{ds_1} \end{pmatrix} \quad (53)$$

where:

$$A \equiv \begin{pmatrix} C + L_V V_L & L_V V_V & \rho L_V V_s \\ V_L & V_V & \rho V_s \\ 0 & 0 & \rho \end{pmatrix} \quad (54)$$

Note that  $A$  is upper block-triangular, so its eigenvalues are the AR(1) root  $\rho$  and the two eigenvalues of the  $2 \times 2$  endogenous block. The latter solve:

$$\lambda^2 - (C + L_V V_L + V_V)\lambda + C V_V = 0 \quad (55)$$

Given one predetermined state ( $L_t$ ) and one forward-looking variable ( $V_t$ ), the Blanchard–Kahn condition implies that this quadratic has one root inside and one root outside the unit circle. We will solve for the different endogenous terms of  $A$  and then numerically compute these eigenvalues and select the stable root (the one with  $|\lambda| < 1$ ). This pins down the response over time of promised utility and labor to the shock.

Let us use the FOC 47 to define  $\mathcal{H}(V_{t+1}, L_t, V_t, s_t)$ :

$$\begin{aligned} \mathcal{H}(V_{t+1}, L_t, V_t, s_t) \equiv & \mu_{t+1}(V_{t+1}, L_{t+1}(L_t, V_{t+1}), V_{t+2}(L_{t+1}, V_{t+1}, s_{t+2})) \\ & - \mu_t(V_t, L_t, V_{t+1}) [(1 - \lambda_e)(1 - \delta) + \lambda_e(1 - \delta)F(V_{t+1})] \\ & - \Pi_L(V_{t+1}, L_{t+1}(L_t, V_{t+1}), s_{t+1})L_V(V_{t+1}, L_t) \end{aligned} \quad (56)$$

Note that we have the following three identities by the implicit function theorem:

$$V_L = -\frac{\mathcal{H}_L}{\mathcal{H}_{V_{t+1}}} \quad (57)$$

$$V_s = -\frac{\mathcal{H}_s}{\mathcal{H}_{V_{t+1}}} \quad (58)$$

$$V_{V_t} = -\frac{\mathcal{H}_{V_t}}{\mathcal{H}_{V_{t+1}}} \quad (59)$$

Starting with solving for  $\mathcal{H}_{V_{t+1}}$ , we will let  $C(V) \equiv [(1 - \lambda_e)(1 - \delta) + \lambda_e(1 - \delta)F(V)]$  and differentiate with respect to  $V_{t+1}$  to show:<sup>20</sup>

$$\mathcal{H}_{V_{t+1}} = \mu_V + \mu_L L_V + \mu_{V'}(V_V + V_L L_V) - \mu C_V - \mu_{V'} C - \Pi_{LV} L_V - \Pi_{LL} L_V^2 - \Pi_L L_{VV} \quad (60)$$

$$\mathcal{H}_L = \mu_L L_L + \mu_{V'} V_L L_L - \mu_L C - \Pi_{LL} L_L L_V - \Pi_L L_{VL} \quad (61)$$

$$\mathcal{H}_s = \mu_{V'} V_s \frac{ds_{t+2}}{ds_{t+1}} - \Pi_{Ls} L_V \quad (62)$$

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<sup>20</sup>sometimes we omit time subscripts for notational simplicity because we are evaluating at steady state. additional let  $\frac{\partial \mu(V_t, L_t, V_{t+1})}{\partial V_{t+1}} \equiv \mu_{V'}$

$$\mathcal{H}_{V_t} = -\mu_V C \quad (63)$$

Now we begin deriving the term in these equations to be solely in terms of zero risk equilibrium objects. First, we will solve for  $\Pi_L$  and its subsequent derivatives.

$$\begin{aligned} \Pi_L(V_{t+1}, L_{t+1}(L_t, V_{t+1}), s_{t+1}) &= (1 + s_{t+1})z - w_{t+1}(V_{t+1}, V_{t+2}(L_{t+1}, s_{t+2})) \\ &\quad + \beta(1 - \delta) \left[ (1 - \lambda) + \lambda F(V_{t+2}(L_{t+1}, s_{t+2})) \right] \\ &\quad \times \Pi_L(V_{t+2}(L_{t+1}, s_{t+2}), L_{t+2}(L_{t+1}, V_{t+2}(L_{t+1}, s_{t+2})), s_{t+2}) \end{aligned} \quad (64)$$

Note that  $\Pi_V = -\mu(V_{t+1}, L_{t+1}, V_{t+2}(L_{t+1}, V_{t+1}, s_{t+2}))$ , so we have that:

$$\Pi_{LV} = \Pi_{VL} = -\mu_L - \mu_{V'} V_L \quad (65)$$

Next, solving for  $\Pi_{LL}$

$$\Pi_{LL} = -\frac{dw_{t+1}}{dV_{t+2}} V_L + \beta C_V V_L \Pi_L + \beta C \Pi_{LL} \left( \frac{dL_{t+2}}{dL_{t+1}} \right) + \beta C \Pi_{LV} V_L \quad (66)$$

We can solve for  $w_V$  from the promise-keeping constraint (67):

$$V_t = u(w_t) + \beta(1 - \lambda_e)(1 - \delta)V_{t+1} + \beta\lambda_e(1 - \delta) \int \max(V_0, V_{t+1}) dF(V_0) + \beta\delta V_U \quad (67)$$

Differentiating with respect to  $V_{t+1}$ :

$$\frac{dw_t}{dV_{t+1}} = \frac{1}{u'(w)} [-\beta(1 - \lambda_e)(1 - \delta) - \beta\lambda_e(1 - \delta)F(V)] = \frac{-\beta C}{u'(w)} \quad (68)$$

Now simplifying 67 using 68 and 65 and rearranging:

$$\Pi_{LL} = \frac{\beta C_V V_L \Pi_L + \frac{L\gamma}{u'(w)^2 w} (\beta C)^2 V_L^2}{1 - \beta C \left( \frac{dL_{t+2}}{dL_{t+1}} \right)} \quad (69)$$

Now turning to  $\Pi_{Ls}$ :

$$\Pi_{Ls} = z - \frac{dw_{t+1}}{dV_{t+2}} \frac{ds_{t+2}}{ds_{t+1}} V_s + \beta C_V \frac{ds_{t+2}}{ds_{t+1}} V_s \Pi_L + \beta C \frac{ds_{t+2}}{ds_{t+1}} \Pi_{Ls} + \beta C \Pi_{LV} \frac{ds_{t+2}}{ds_{t+1}} V_s + \beta C \Pi_{LL} \frac{ds_{t+2}}{ds_{t+1}} L_V V_s \quad (70)$$

Using 50, 65, and 68 and letting  $\Phi_0 \equiv \frac{1}{1-\beta\rho C}$ , we can simplify:

$$\Pi_{Ls} = \Phi_0 z + \beta\Phi_0\rho C_V V_s \Pi_L + \beta\Phi_0\rho C \Pi_{LL} L_V V_s + (\beta C)^2 \rho \Phi_0 \frac{L\gamma}{u'(w)^2 w} V_L V_s \quad (71)$$

Next, we solve for labor related objects.

$$L_L(V_{t+1}, L_t) = [(1 - \lambda_e)(1 - \delta) + \lambda_e(1 - \delta)F(V)] = C \quad (72)$$

$$L_V(V_{t+1}, L_t) = (1 - \delta)\lambda_e F'(V)L + \lambda_e(1 - u)(1 - \delta)G'(V) \quad (73)$$

Combining 73 and 72 we have:

$$\frac{dL_{t+1}}{dL_t} = L_L + L_V V_L = C + (1 - \delta)\lambda_e F'(V)V_L L + \lambda_e(1 - u)(1 - \delta)G'(V)V_L \quad (74)$$

Additionally, we have:

$$L_{VV} = (1 - \delta)\lambda_e F''(V)L + \lambda_e(1 - u)(1 - \delta)G''(V) \quad (75)$$

also:

$$L_{LV} = \lambda_e(1 - \delta)F'(V) = C_V \quad (76)$$

Finally, we need to solve for the derivatives of the Lagrange multiplier:

$$\mu_V = -\frac{L \frac{\partial w_{t+1}}{\partial V_{t+1}} u''(w)}{u'(w)^2} = \frac{\gamma L}{u'(w)w} \frac{\partial w_{t+1}}{\partial V_{t+1}} \quad (77)$$

$$\mu_L = \frac{1}{u'(w)} \quad (78)$$

$$\mu_{V'} = \frac{\gamma L}{u'(w)w} \frac{\partial w_{t+1}}{\partial V_{t+2}} \quad (79)$$

We can solve for  $\frac{dw_{t+1}}{dV_{t+1}}$  from the promise-keeping constraint 67 (holding  $V_{t+2}$  constant)

$$\frac{\partial w_{t+1}}{\partial V_{t+1}} = \frac{1}{u'(w)} \quad (80)$$

Now for  $\frac{dw_{t+1}}{dV_{t+2}}$

$$\frac{dw_{t+1}}{dV_{t+2}} = \frac{-\beta C}{u'(w)} \quad (81)$$

To have completely defined the system of equations which pins down the response to promised utility (and therefore wages and labor) to the shock, we now need some objects from the zero-risk steady state solution. First, how does  $F$  and  $G$  change with  $V$ ? We have a rank-preserving equilibrium, which implies that:

$$F(V(z)) = J(z) \quad (82)$$

The following two equations follow:

$$F'(V(z))V'(\bar{z}) = J'(z) \quad (83)$$

$$F''(V) = \frac{J''(z) - F'(V)V''(z)}{V'(z)^2} \quad (84)$$

We can also solve for  $G'$  and  $G''$  in terms of  $F$ ,  $F'$ , and  $F''$ .

$$G'(V) = \frac{(\delta + (1 - \delta)\lambda_e)\delta F'(V)}{(\delta + (1 - \delta)\lambda_e(1 - F(V)))^2} \quad (85)$$

$$G''(V) = (\delta + (1 - \delta)\lambda_e)\delta \frac{F''(V)(\delta + (1 - \delta)\lambda_e(1 - F(V))) + 2F'(V)^2(1 - \delta)\lambda_e}{(\delta + (1 - \delta)\lambda_e(1 - F(V)))^3} \quad (86)$$

Also note that we have the following two steady state equations:

$$L(z) = \frac{\frac{\lambda_u \delta}{\lambda_u + \delta} [\delta + (1 - \delta)\lambda_e]}{[\delta + (1 - \delta)\lambda_e(1 - J(z))]^2} \quad (87)$$

$$u = \frac{\delta}{\lambda_u + \delta} \quad (88)$$

Next, we can plug 85 and 83 into 73 and 75: Plugging in 85 and 83 into ?? and then simplifying using 87 and 88 we have:

$$L_V = 2(1 - \delta)\lambda_e F'(V)L = 2(1 - \delta)\lambda_e \frac{J'(\bar{z})}{V'(\bar{z})}L \quad (89)$$

Now, we plug in 86 into 75 and simplify using the steady-state labor stock 87<sup>21</sup> and the unemployment rate 88 to get  $L''(V)$  in terms of  $F'$ ,  $F''$ :

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<sup>21</sup>in contrast to the previous expression 51 which is a flow equation for labor

$$L_{VV} = \lambda_e(1 - \delta)L \left[ 2F''(V) + \frac{2\lambda_e F'(V)^2(1 - \delta)}{\delta + (1 - \delta)\lambda_e(1 - F(V))} \right] \quad (90)$$

Using 84 and 83 we can continue to simplify 90:

$$L_{VV} = \frac{2\lambda_e(1 - \delta)L}{V'(\bar{z})^2} \left[ J''(\bar{z}) - \frac{J'(\bar{z})V''(\bar{z})}{V'(\bar{z})} + \frac{\lambda_e J'(\bar{z})^2(1 - \delta)}{\delta + (1 - \delta)\lambda_e(1 - J(\bar{z}))} \right] \quad (91)$$

Now we need to know  $V'(\bar{z})$ , and  $V''(\bar{z})$  to simplify  $L_{VV}$  and  $L_V$ . Since we are asking how the promised utility varies with productivity in the zero-risk steady state, we know the wage the firms offer is constant. So we can explicitly map  $w(z)$  onto  $V(z)$  and so forth. This also allows us to solve for  $\Pi_L$ .

$$V'(z) = \frac{u'(w)w'(z)}{1 - \beta(1 - \lambda_e)(1 - \delta) - \beta\lambda_e(1 - \delta)F(V)} \equiv \Phi_1 u'(w)w'(z) \quad (92)$$

Where  $\Phi_1$  is the present-value multiplier associated with permanent differences. It is the same as  $\Phi_0$  if  $\rho = 1$ , but is strictly larger if the shock we are considering is not entirely permanent. Similarly for  $V''(\bar{z})$ :

$$V''(z) = \left[ -\frac{\gamma w'(z)^2}{w(z)} + w''(z) + \beta\lambda_e(1 - \delta)J'(\bar{z})w'(z)\Phi_1 \right] \Phi_1 u'(w) \quad (93)$$

Additionally, note that we can solve for  $\Pi_L$ :

$$\Pi_L = (z - w)\Phi_1 \quad (94)$$

We can use the steady-state wage equations to continue to simplify:

$$w(\bar{z}) = \bar{z} - \int_{w^R}^{\bar{z}} \frac{[\delta + (1 - \delta)\lambda_e(1 - J(\bar{z}))]^2}{[\delta + (1 - \delta)\lambda_e(1 - J(x))]^2} dx \quad (95)$$

$$w'(\bar{z}) = (\bar{z} - w(\bar{z})) \frac{2(1 - \delta)\lambda_e J'(\bar{z})}{\delta + (1 - \delta)\lambda_e(1 - J(\bar{z}))} \quad (96)$$

$$w''(\bar{z}) = w'(\bar{z}) \left[ \frac{1 - w'(\bar{z})}{\bar{z} - w(\bar{z})} + \frac{J''(\bar{z})}{J'(\bar{z})} - \frac{(1 - \delta)\lambda_e J'(\bar{z})}{\delta + (1 - \delta)\lambda_e(1 - J(\bar{z}))} \right] \quad (97)$$

In order to simplify our expression for  $L_{VV}$  90, the following equation is useful:

$$\frac{V''(\bar{z})}{V'(\bar{z})} = \frac{V''(\bar{z})}{\Phi_1 u'(w)w'(z)} = \left[ -\frac{\gamma w'(\bar{z})}{w(z)} + \frac{w''(\bar{z})}{w'(\bar{z})} + \beta\lambda_e(1 - \delta)J'(\bar{z})\Phi_1 \right] \quad (98)$$

Using 98, 97, and 96: we can to continue to simplify 91 and remove all  $V'$  and  $V''$  terms:

$$L_{VV} = \frac{2\lambda_e(1-\delta)L}{V'(\bar{z})^2} \left[ \frac{\gamma w'(\bar{z}) J'(\bar{z})}{w(\bar{z})} - \frac{J'(\bar{z})(1-w'(\bar{z}))}{\bar{z}-w(\bar{z})} - \beta\lambda_e(1-\delta)J'(\bar{z})^2\Phi_1 \right] \quad (99)$$

Now we collect our terms and simplify our expressions for  $V_s$ ,  $V_L$ , and  $V_V$ :

$$\begin{aligned} \mathcal{H}_{V_{t+1}} = & \frac{2(1-\delta)\lambda_e F'(V)L}{u'(w)} - \frac{L(1-\beta CV_V)u''(w)}{u'(w)^3} - \frac{L\lambda_e(1-\delta)F'(V)}{u'(w)} + \frac{2(1-\delta)\lambda_e F'(V)L}{u'(w)} - \Pi_{LL}L_V^2 \\ & - \frac{2\lambda_e(1-\delta)L(z-w)\Phi_1}{V'(\bar{z})^2} \left[ \frac{\gamma w'(\bar{z}) J'(\bar{z})}{w(\bar{z})} - \frac{J'(\bar{z})(1-w'(\bar{z}))}{\bar{z}-w(\bar{z})} - \beta\lambda_e(1-\delta)J'(\bar{z})^2\Phi_1 \right] - \frac{2L_V V_L L \gamma}{u'(w)^2 w} \beta C + \frac{\gamma L \beta C^2}{u'(w)^2 w} \end{aligned} \quad (100)$$

Collecting like terms and simplifying:

$$\begin{aligned} \mathcal{H}_{V_{t+1}} = & \frac{(1-\delta)\lambda_e F'(V)L}{u'(w)} - \frac{L(1-\beta CV_V)u''(w)}{u'(w)^3} - \Pi_{LL}L_V^2 \\ & - \frac{2\lambda_e(1-\delta)L(z-w)\Phi_1 J'(z)}{V'(\bar{z})^2} \left[ \frac{\gamma w'(z)}{w(z)} - \frac{1}{z-w(z)} - \beta\lambda_e(1-\delta)J'(z)\Phi_1 \right] - \frac{2L_V V_L L \gamma}{u'(w)^2 w} \beta C + \frac{\gamma L \beta C^2}{u'(w)^2 w} \end{aligned} \quad (101)$$

Further simplifying:

$$\begin{aligned} \mathcal{H}_{V_{t+1}} = & \frac{L_V}{2u'(w)} + \frac{\gamma}{u'(w)w} \left( \frac{L(1-\beta CV_V)}{u'(w)} - (z-w)L_V + \frac{L\beta C^2}{u'(w)} \right) \\ & - \Pi_{LL}L_V^2 + \frac{L_V}{u'(w)w'(z)} + \frac{\beta\Phi_1 L_V(1-C)}{2u'(w)} - \frac{2L_V V_L L \gamma}{u'(w)^2 w} \beta C \end{aligned} \quad (102)$$

Similarly, simplifying  $\mathcal{H}_L$ :

$$\mathcal{H}_L = -\Pi_{LL}L_V C - \frac{1-C}{2u'(w)} - \frac{L\gamma}{u'(w)^2 w} \beta C^2 V_L \quad (103)$$

$$\mathcal{H}_s = -L_V[\Phi_0 z + \frac{\beta\Phi_0(1-C)\rho V_s}{2u'(w)} + \beta\Phi_0\rho C\Pi_{LL}L_V V_s + (\beta C)^2\rho\Phi_0\frac{L\gamma}{u'(w)^2 w}V_L V_s] - \frac{\gamma L\beta C\rho V_s}{u'(w)^2 w} \quad (104)$$

$$\mathcal{H}_{V_t} = -\frac{CL\gamma}{u'(w)^2 w} \quad (105)$$

This is all the expressions required to solve the system of equations to simulate how promised utility and labor respond to a shock. We do this numerically, picking the stable solution (eigenvalues inside the unit circle).

Now, how do we get the wage?

$$\frac{dV_t}{ds_1} = u'(w) \frac{dw_t}{ds_1} + \beta C \frac{dV_{t+1}}{ds_1} \quad (106)$$

$$\implies \frac{dw_t}{ds_1} = \frac{\frac{dV_t}{ds_1} - \beta C \frac{dV_{t+1}}{ds_1}}{u'(w)} \quad (107)$$

#### A2.1.4 Planner problem

Here, we focus on the planner's choice of whether to move an employed worker who has received a job offer. The planner will move the worker if the social value of the new job,  $W(z_1, s_1)$ , exceeds the social value of their current job,  $W(z_0, s_0)$  where these value functions are defined as follows:

$$W(z, s) = (1+s)z + \beta(1-\lambda_e)(1-\delta)\mathbb{E}[W(z, s')] + \beta\lambda_e(1-\delta)\mathbb{E}\left[\int \max(W(z, s'), W_0)dF(W_0)\right] + \delta\beta W_U \quad (108)$$

Now, considering the first order approximation. Since the aggregate distributions are unaffected by the small amount of risk, we know that  $F(W(z, 0)) = J(z)$ .

$$W_s = z + \beta(1-\lambda_e)(1-\delta)\rho W_s + \beta\lambda_e(1-\delta)J(z)\rho W_s \quad (109)$$

$$W_s = \frac{z}{1 - \beta(1-\delta)\rho[1 - \lambda_e + \lambda_e J(z)]} = z\Phi_0 \quad (110)$$

Labor evolves according to:

$$L(z, s_t) = L(z, s_{t-1})(1-\delta)(1-\lambda_e(1-F(W(z, s_t)))) + \lambda_u u + \lambda_e(1-u)(1-\delta)G(W(z, s_t)) \quad (111)$$

$$G(W(z, 0)) = \frac{\delta F(W(z, 0))}{\delta + (1-\delta)\lambda_e(1-F(W(z, 0)))} \quad (112)$$

Note that we have:

$$F'(W)W_z = J'(z) \quad (113)$$

And similarly:

$$G'(W) = \frac{(\delta + (1 - \delta)\lambda_e)\delta F'(W)}{(\delta + (1 - \delta)\lambda_e(1 - F(W)))^2} = \frac{(\delta + (1 - \delta)\lambda_e)\delta \frac{J'(z)}{W_z}}{(\delta + (1 - \delta)\lambda_e(1 - J(z)))^2} \quad (114)$$

Now, what is  $W_z$ ? We can return to 108 to solve for this (again, this is with  $s = 0$ ):

$$W_z = 1 + \beta(1 - \lambda_e)(1 - \delta)W_z + \beta\lambda_e(1 - \delta)J(z)W_z \quad (115)$$

Rearranging, we have:

$$W_z = \frac{1}{1 - \beta(1 - \delta)[1 - \lambda_e + \lambda_e J(z)]} = \Phi_1 \quad (116)$$

So we can solve for the socially optimal labor response:

$$\begin{aligned} \frac{dL(z, s_t)}{ds_1} &= \frac{dL(z, s_{t-1})}{ds_1} (1 - \delta)(1 - \lambda_e(1 - J(z))) \\ &\quad + \rho^{t-1}(1 - \delta)\lambda_e \frac{J'(z)z\Phi_0}{\Phi_1} L + \rho^{t-1}(1 - \delta)\lambda_e(1 - u) \frac{(\delta + (1 - \delta)\lambda_e) \delta \frac{J'(z)z\Phi_0}{\Phi_1}}{(\delta + (1 - \delta)\lambda_e(1 - J(z)))^2}. \end{aligned} \quad (117)$$

Simplifying using  $u = \frac{\delta}{\lambda_u + \delta}$  and steady state labor:

$$\frac{dL(z, s_t)}{ds_1} = 2\rho^{t-1}(1 - \delta)\lambda_e \frac{J'(z)z\Phi_0}{\Phi_1} L + \frac{dL(z, s_{t-1})}{ds_1} (1 - \delta)(1 - \lambda_e(1 - J(z))) \quad (118)$$

### A2.1.5 Proof of Proposition

From the previous section, we know that the planner response in period  $t$  following a shock in period 1 is:

$$\frac{dL(z, s_t)}{ds_1} = 2\rho^{t-1}(1 - \delta)\lambda_e \frac{J'(z)z\Phi_0}{\Phi_1} L + \frac{dL(z, s_{t-1})}{ds_1} (1 - \delta)(1 - \lambda_e(1 - J(z))) \quad (119)$$

So when the shock is permanent we have  $\Phi_0 = \Phi_1$  and  $\rho = 1$  and:

$$\frac{dL(z, s_t)}{ds_1} = 2(1 - \delta)\lambda_e J'(z)zL + \frac{dL(z, s_{t-1})}{ds_1} (1 - \delta)(1 - \lambda_e(1 - J(z))) \quad (120)$$

First, note that this is the cumulative labor change associated with increasing the promised utility by  $V'(z)z$  in the decentralized equilibrium. The instantaneous flow labor change associated with this increase is:

$$L_{V,t=1}V'(z)z = 2(1 - \delta)\lambda_e J'(z)zL \quad (121)$$

And the increase over time is:

$$L_{V,t}V'(z)z = 2(1 - \delta)\lambda_e J'(z)zL + L_{V,t-1}V'(z)z(1 - \delta)(1 - \lambda_e(1 - J(z))) \quad (122)$$

This is analogous to 120, so we know that the planner's labor response to a permanent shock is analogous to the shock induced by increasing the utility  $V'(z)z$  in the decentralized equilibrium. Intuitively, this is because the shock  $s$  increased the productivity by  $z$  so the firm should move up the job ladder based on that change,  $V'(z)z$ . Productivity is CRS and there are no other output-related scale effects so this change should happen immediately (in contrast, if there were direct adjustment costs then the planner might slowly adjust over time too).

Next, note that the decentralized response converges to  $V'(z)z$  over time. In the long run after the permanent shock, in the new steady state the firm's productivity has increased by  $z$  and so its promised utility will have increased by  $V'(z)z$ . But what happens along the transition path? It is always lower than this value. To see this recall that, the promised utility response is:

$$\frac{dV_{t+1}}{ds_1} = V_s \frac{ds_{t+1}}{ds_1} + V_L \frac{dL_t}{ds_1} + V_V \frac{dV_t}{ds_1} \quad (123)$$

In response to a permanent shock, the  $V_s$  channel is the same over time because  $\frac{ds_{t+1}}{ds_1} = 1$ . The  $V_L$  and  $V_V$  channels both change over time as  $\frac{dL_t}{ds_1}$  and  $\frac{dV_t}{ds_1}$  adjust following the permanent shock. Both  $V_L$  and  $V_V$  are positive. Accumulating workers boosts the retention margin and offering a higher promised utility makes it more costly to reduce the promised utility later (except when workers are risk neutral).

So  $\frac{dL_t}{ds_1}$  and  $\frac{dV_t}{ds_1}$  both are initially zero (when  $t = 0$ ) and then positive which increases the promised utility until it converges to  $zV'(z)$ . What is the labor increase associated with this? Solving for steady state in labor:

$$\frac{dL^*}{ds_1} = \frac{2(1 - \delta)\lambda_e J'(z)zL}{1 - (1 - \delta)[1 - \lambda_e(1 - J(z))]} \quad (124)$$