Dicke Hamiltonian, Reduced Basis

Jz, J+, J- Construction

```
In[1]:= Jz[K_Integer] := Module[{J, dim, Jz},
       J = K / 2;
       dim = 2J + 1;
       Jz = SparseArray[DiagonalMatrix[Reverse[Range[-J, J]]]];
       Return[Jz];
      ]
    Jp[K_Integer] := Module[{J, dim, Jplus, mValues, i, j},
       J = K / 2;
       dim = 2J + 1;
       Jplus = SparseArray[{}, {dim, dim}];
       mValues = Reverse[Range[-J, J]];
       For[i = 1, i < dim, i++,
        Jplus[i, i+1] = Sqrt[J * (J+1) - mValues[i+1] * (mValues[i+1] + 1)];
       Return[SparseArray[Jplus]];
      ]
     Jm[K_Integer] := Module[{J, dim, Jplus, mValues, i, j},
       J = K / 2;
       dim = 2J + 1;
       Jplus = SparseArray[{}, {dim, dim}];
       mValues = Reverse[Range[-J, J]];
       For [i = 2, i \le dim, i++,
        Jplus[i, i - 1] = Sqrt[J * (J + 1) - mValues[i] * (mValues[i] + 1)];
       ];
       Return[Jplus];
```

Complete Construction

Initial States, Observables Construction

Initial States

Observable Matrices

Oscillator Position

```
In[18]:= xM = KroneckerProduct[IdentityMatrix[K + 1], \frac{1}{Sqrt[2]} (a<sup>†</sup> + a)];
        ConjugateTranspose[\psi0vec].xM.\psi0vec
Out[19]=
        Ο.
```

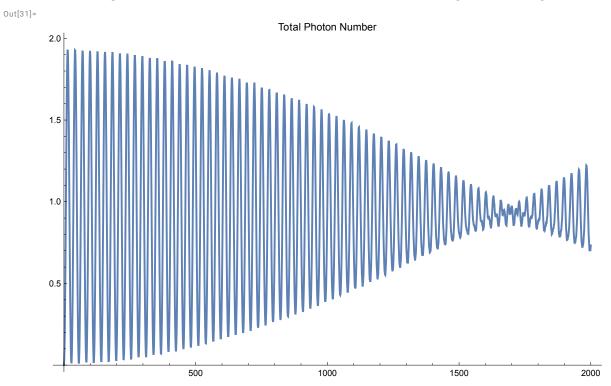
Propagation

Calculating States

```
In[34]:= stateVector[t_] := MatrixExp[-I * Htot * t, \psi 0vec];
     tMax = 2000;
     tRange = Range[0, tMax, 1];
     \psi = ParallelTable[stateVector[t], {t, tRange}];
```

Photon Number Expectation in Cavity

```
In[28]:= aDaggerA = KroneckerProduct[IdentityMatrix[K+1], a<sup>†</sup>.a];
    aDaggerAsr = aDaggerA.aDaggerA;
    photons = Table[Conjugate[\susuesus[n]].aDaggerA.\susuesus[n]], {n, Length@tRange}];
    ListLinePlot[{tRange, photons // Re} // Transpose,
        PlotRange → All, PlotLabel → "Total Photon Number", ImageSize → Large]
```



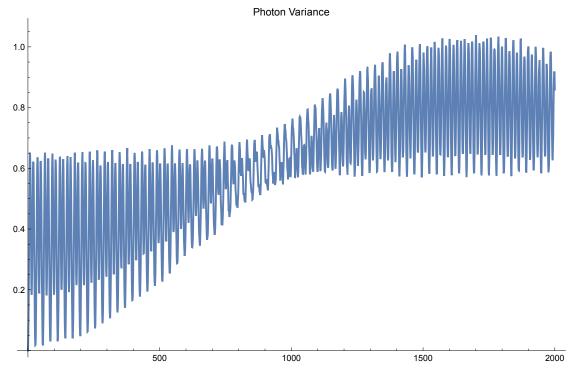
Photon Statistics, Variance

In[32]:= newPhotons =

 $Table[Conjugate[\psis[n]].aDaggerAsr.\psis[n]], \{n, Length@tRange\}] - photons^2;$ ListLinePlot[{tRange, newPhotons // Re} // Transpose,

 ${\tt PlotRange} \rightarrow {\tt All}, \, {\tt PlotLabel} \rightarrow {\tt "Photon Variance"}, \, \, {\tt ImageSize} \rightarrow {\tt Large}]$

Out[33]=



Excitation Spectrum

In[@]:= eigv = Eigenvalues[N[Htot]]; ListLinePlot[{Sort[eigv]}, PlotRange → All, ImageSize → Large]

••• Eigenvalues: Because finding 240 out of the 240 eigenvalues and /or eigenvectors is likely to be faster with dense matrix methods, the sparse input matrix will be converted. If fewer eigenvalues and /or eigenvectors would be sufficient, consider restricting this number using the second argument to Eigenvalues.

