

Building the Hamiltonian

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In[*]:= bsize = 20; ω0 = 1.0;
(*Two level system initial Hamiltonian*)
H0TSS = SparseArray[Band[{1, 1}] → { $-\frac{\omega_0}{2}, \frac{\omega_0}{2}$ }];
(*QHO Hamiltonian*)
H0H0 = SparseArray[Band[{1, 1}] → Table[n +  $\frac{1}{2}$ , {n, 0, bsize - 1}]];
σp = {{0, 0}, {1, 0}};
σm = {{0, 1}, {0, 0}};

(*Annihilation operator definition*)
a = SparseArray[Band[{1, 2}] → Table[Sqrt[n], {n, 1, bsize - 1}], {bsize, bsize}];

(*We have to choose a convention, i.e.,
the TSS is on the left in tensor products, while the H0 is on the right*)
H0 = KroneckerProduct[IdentityMatrix[2], H0H0] +
    KroneckerProduct[H0TSS, IdentityMatrix[bsize]];
(* Scaling via tensor product *)

(*The coupling terms*)
Hcoup = 0.1 (KroneckerProduct[σp, a] + KroneckerProduct[σm, a†]);
(*Hamiltonian for JC model with RWA made*)
γ = 0.005;
Decay = - I * γ * a† . a;
Hdecay = KroneckerProduct[IdentityMatrix[2], Decay];
Htot = H0 + Hcoup + Hdecay;

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Initial state

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In[*]:= ψ0[w_, x0_] =  $\frac{1}{\text{Sqrt}[\text{Sqrt}[\pi] w]} \text{Exp}\left[-\frac{(x - x_0)^2}{2 w^2}\right]$ ; (*Define initial Gaussian state*)
EigState[n_, x_] =  $\frac{\pi^{-1/4}}{\text{Sqrt}[2^n n!]} \text{Exp}\left[-\frac{x^2}{2}\right] \text{HermiteH}[n, x]$ ;
coeff[n_, w_, x0_] := NIntegrate[EigState[n, x] * ψ0[w, x],
    {x, -∞, ∞}, PrecisionGoal → 6, AccuracyGoal → 5]
ψ0H0 = Table[coeff[n, 1, 2], {n, 0, bsize - 1}];

(*excited state in TSS and Gaussian in the QHO*)
ψ0Vec = KroneckerProduct[{0, 1}, ψ0H0] // Flatten;

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Build observable matrices

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In[*]:= xM = KroneckerProduct[IdentityMatrix[2],  $\frac{1}{\text{Sqrt}[2]} (a^\dagger + a)$ ];
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(*Position of the oscillator*)

Test the observable matrix

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In[*]:= (*Expected x value for initial state*)
ConjugateTranspose[psi0Vec].xM.psi0Vec
xMSquared = xM . xM;
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Out[*]=
2.
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Propagate Initial State (position basis)

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In[ ]:= (* Define the time-evolved state vector *)
timeEvolutionOperator[t_] := MatrixExp[-I * Htot * t];
stateVector[t_] := timeEvolutionOperator[t] .  $\psi_0$ Vec;

(* Compute expectation values *)
expectationValueX[t_] := ConjugateTranspose[stateVector[t]] . xM . stateVector[t];
expectationValueXSquared[t_] :=
  ConjugateTranspose[stateVector[t]] . xMSquared . stateVector[t];

(*Tensor product with the QHO identity to get appropriately scaled operators*)
iqho = IdentityMatrix[bsize];
P1 = {{0, 0}, {0, 1}}; (*Excited state projection operator*)
P1full = KroneckerProduct[P1, iqho];
populationExcited[t_] :=
  ConjugateTranspose[stateVector[t]] . P1full . stateVector[t];

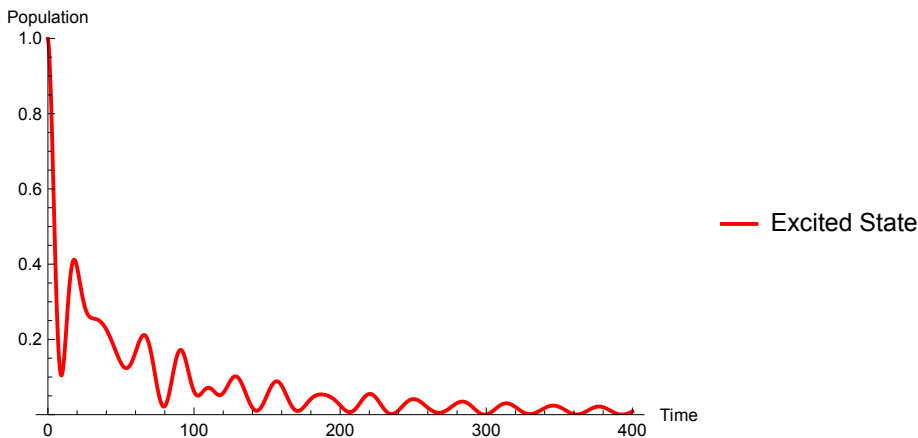
tMax = 400;

avgPositionPlotQHO = Plot[Re[expectationValueX[t]],
  {t, 0, tMax}, PlotLabel → "Average Position <x>",
  AxesLabel → {"Time", "<x>"}, PlotRange → Full];
avgStatePlotTSS =
  Plot[{Re[populationExcited[t]]}, {t, 0, tMax}, PlotLegends → {"Excited State"},
  AxesLabel → {"Time", "Population"}, PlotRange → {0, 1}, PlotStyle → Red]

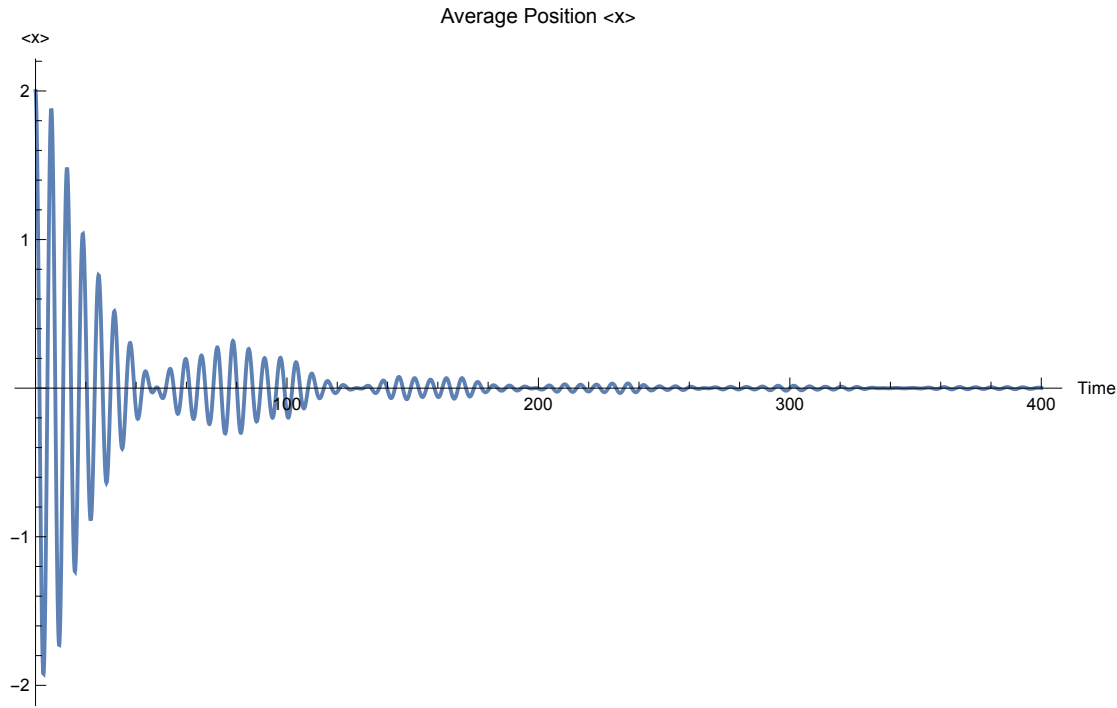
Show[avgPositionPlotQHO, PlotRange → All, ImageSize → Large]

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Out[]:=



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