

Machine Learning for Robotics

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Class 04-

- Linear Regression

Regression

Regression is a type of supervised learning where the goal is to **predict a continuous numerical value**.

Regression

Regression is a type of supervised learning where the goal is to **predict a continuous numerical value**.

What does “continuous value” mean?

A value that can take **any number within a range**, such as:

- 25.5
- 3.2
- 102.75

Regression

Example

House Price Prediction

- **Input (X):** house size, number of rooms
- **Output (y):** house price (for example: 250000)

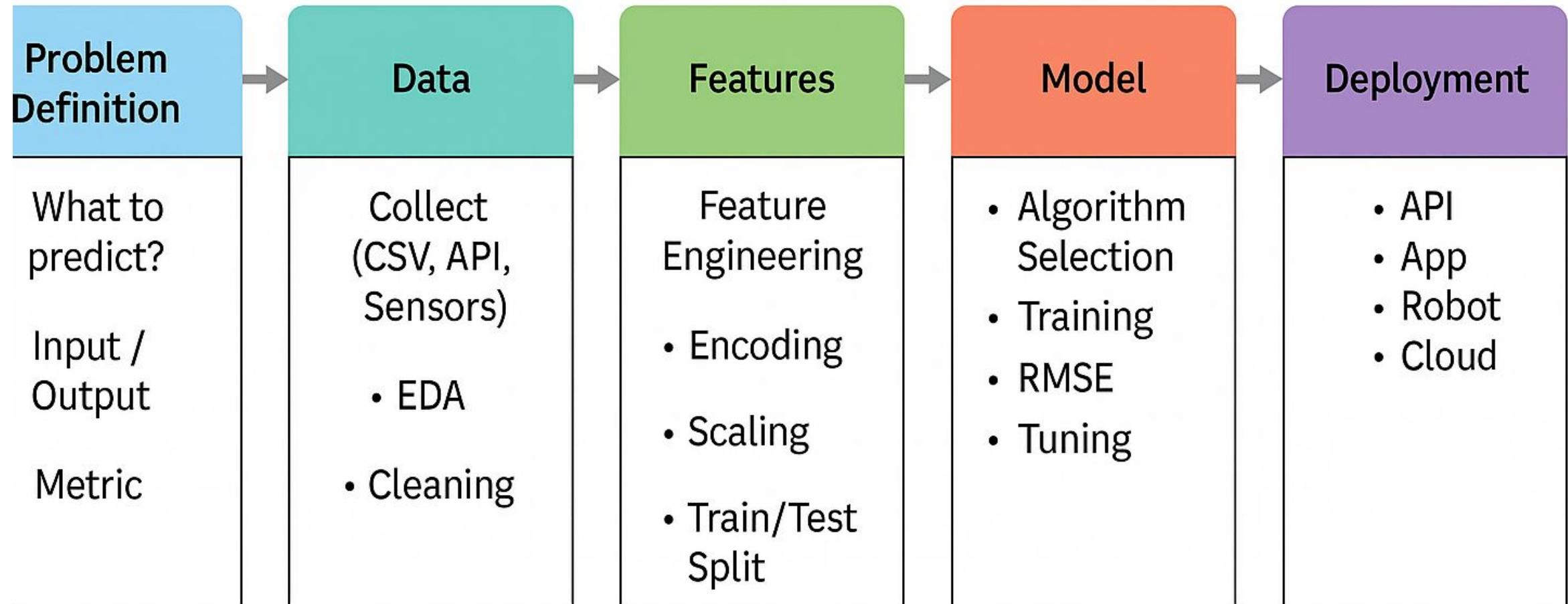
Because the output is a **number**, this is a **regression problem**.

Regression

Common regression types

- **Linear Regression**
- **Multiple Linear Regression**
- **Polynomial Regression**

ML Pipeline

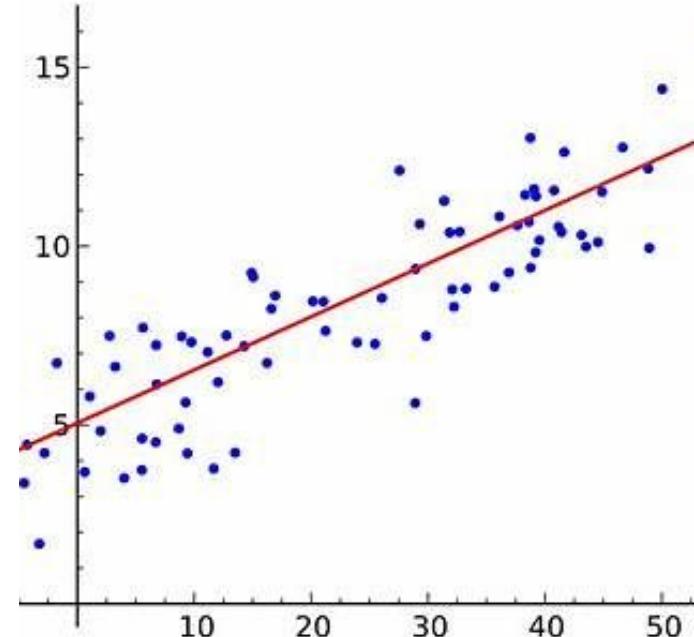


Linear Regression

Simple Linear Regression is a **supervised learning regression** method where:

- there is **one input feature (x)**
- and **one output target (y)**
- the relationship is modeled using a **straight line**

study_hours	math_marks
1.0	35
1.2	37
1.5	40
1.7	38
2.0	42



Linear Regression

Mathematical model

The equation of simple linear regression is:

$$y=mx+b$$

Where:

- $x \rightarrow$ input feature
- $y \rightarrow$ predicted output
- $m \rightarrow$ slope (how fast y changes when x increases)
- $b \rightarrow$ intercept (value of y when $x = 0$)

Linear Regression

- Step 01: Define Goal

Linear Regression

- Step 02: Data Analysis

Load Dataset

- Read csv file: **pandas**

Visualize the Dataset

- Draw Scatter Plot to find whether data is in linear: **matplotlib**

Data Preprocessing

- Check Missing Values : **pandas**

Linear Regression

- Step 03: Feature Engineering

Feature Engineering

- Scaling (Standardization): sklearn

Train / Test Split

- Separate features (X) and labels (y): pandas
- Split data to train, test: sklearn

Linear Regression

- Step 04: Model Training

- Model selection
 - Linear Regression

- Model training

Linear Regression

- **Step 05: Model Evaluation**

- Prediction on test data
- Error: MAE, MSE, RMSE
- Performance: R², Adjusted R²
- New Prediction

Error

① MAE — Mean Absolute Error

Formula

$$MAE = \frac{1}{n} \sum |y - \hat{y}|$$

Meaning

- Average of **absolute differences**
- Treats **all errors equally**

Pros	Cons
<ul style="list-style-type: none">• Easy to understand• Robust to outliers (less sensitive)• Error is in same unit as target	<ul style="list-style-type: none">• Does not penalize large errors strongly• Less useful when large mistakes are critical

Error

② MSE — Mean Squared Error

Formula

$$MSE = \frac{1}{n} \sum (y - \hat{y})^2$$

Meaning

- Squares the error before averaging
- Large errors get much higher penalty

Pros	Cons
<ul style="list-style-type: none">• Strongly penalizes large errors• Smooth and mathematically convenient• Used in model training	<ul style="list-style-type: none">• Very sensitive to outliers• Unit becomes squared, hard to interpret

Error

③ RMSE — Root Mean Squared Error

Formula

$$RMSE = \sqrt{MSE}$$

Meaning

- Square root of MSE
- Balances MAE and MSE behavior

Pros	Cons
<ul style="list-style-type: none">• Penalizes large errors• Error is in same unit as target• Easy to compare with MAE	<ul style="list-style-type: none">• Still sensitive to outliers• More complex than MAE

Error

Metric	Penalizes large error	Outlier sensitivity	Unit
MAE	Low	Low	Same as target
MSE	Very high	Very high	Squared
RMSE	High	High	Same as target

Performance Metrics

① R Square (R^2)

Formula

$$R^2 = 1 - \frac{SS_{res}}{SS_{tot}}$$

Where:

- **SS res** → prediction error
- **SS tot** → total variation in data

Meaning

- R Squared tells us how much of the variance in the target is explained by the model.
- How good the model fits the data.

Pros	Cons
<ul style="list-style-type: none">• Easy to understand• Good for comparing models with same features• Popular and widely used	<ul style="list-style-type: none">• Always increases when you add more features• Cannot detect overfitting• Misleading for multiple features

Performance Metrics

② Adjusted R Square (Adjusted R²)

Formula

Where:

$$\text{Adjusted } R^2 = 1 - (1 - R^2) \frac{n - 1}{n - p - 1}$$

- $n \rightarrow$ number of samples
- $p \rightarrow$ number of features

Meaning

- Adjusted R Square fixes the main problem of R².
- It penalizes unnecessary features.
- Only increases if the new feature actually improves the model.

Pros	Cons
<ul style="list-style-type: none">• Detects overfitting• Best for multiple linear regression• More reliable than R²	<ul style="list-style-type: none">• Slightly harder to interpret• Can decrease when weak features are added

Performance Metrics

Metric	Penalizes extra features	Best use case
R Square	No	Simple models
Adjusted R Square	Yes	Multiple features

Performance Analysis for LR

Metric	Penalizes large error	Outlier sensitivity	Unit
MAE	Low	Low	Same as target
MSE	Very high	Very high	Squared
RMSE	High	High	Same as target

Metric	Penalizes extra features	Best use case
R Square	No	Simple models
Adjusted R Square	Yes	Multiple features

Multiple Linear Regression

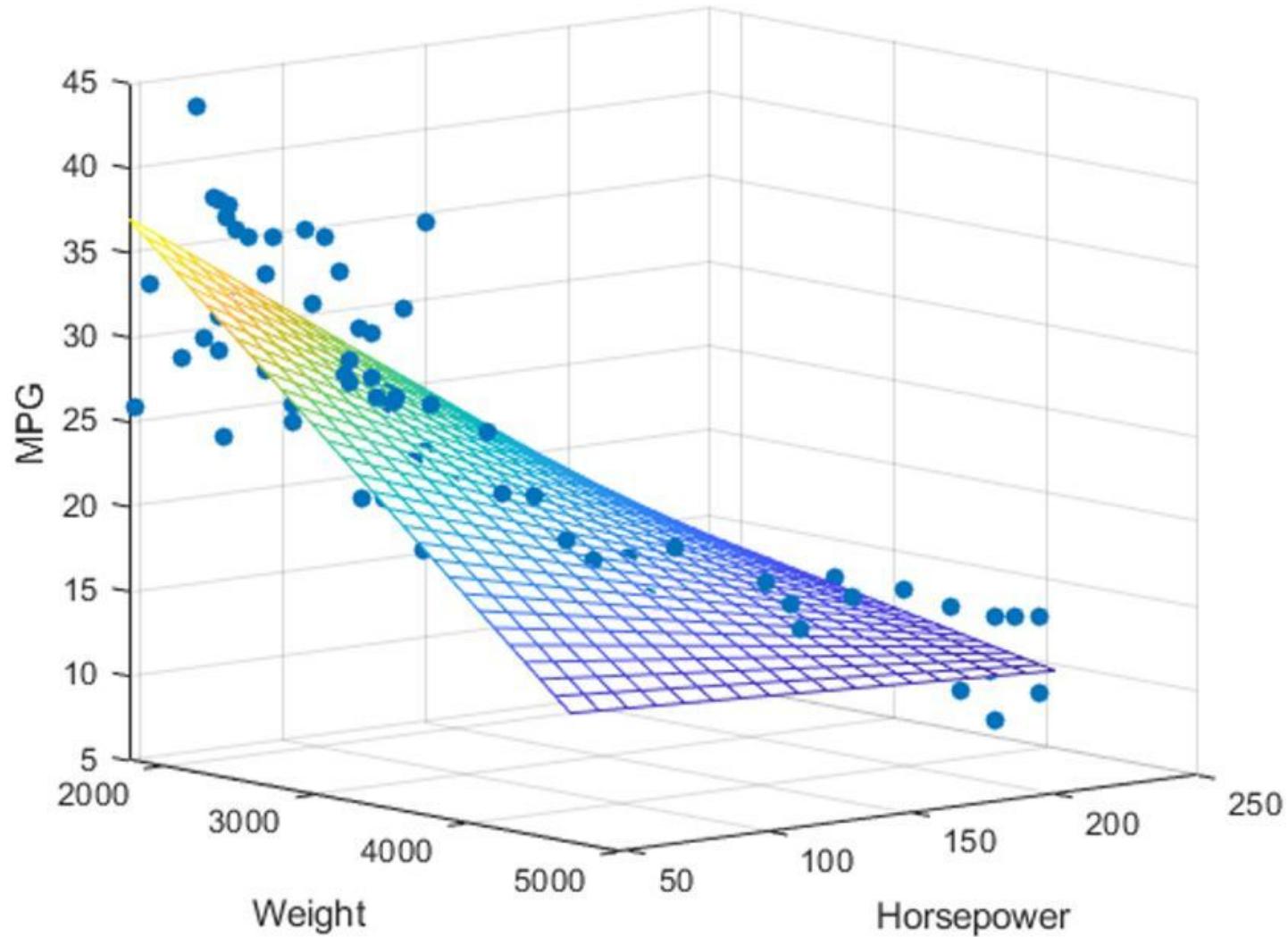
Multiple Linear Regression is a supervised learning regression technique used to predict one continuous target value using **two or more input features**.

Multiple Linear Regression

Multiple Linear Regression is a supervised learning regression technique used to predict one continuous target value using **two or more input features**.

lin_acc_x	lin_acc_y	ang_vel_z	robot_linear_velocity
0.10	0.01	0.01	0.43
0.13	0.06	0.02	0.44
0.13	0.03	0.03	0.37
0.14	NaN	0.02	0.48
0.17	0.04	0.01	0.49

Multiple Linear Regression



Multiple Linear Regression

Mathematical model

The equation of Multiple linear regression is:

$$y = b_0 + b_1 X_1 + b_2 X_2 + \dots + b_n X_n$$

Where:

- y → predicted output (target)
- b_0 → intercept (bias term)
- X_1, X_2, \dots, X_n → input features
- b_1, b_2, \dots, b_n → coefficients (weights of each feature)

Multiple Linear Regression

Mathematical model : Example

Predict house price

- $x_1 \rightarrow$ house size
- $x_2 \rightarrow$ number of rooms
- $x_3 \rightarrow$ distance from city
- $y \rightarrow$ price

$$\text{price} = b_0 + b_1(\text{size}) + b_2(\text{rooms}) + b_3(\text{distance})$$

Data Distribution

Data distribution describes how values in a dataset are spread or arranged.

It tells us:

- which values occur **most frequently**
- how **spread out** the data is
- whether the data is **symmetric or asymmetric**

Data Distribution

Normal Distribution

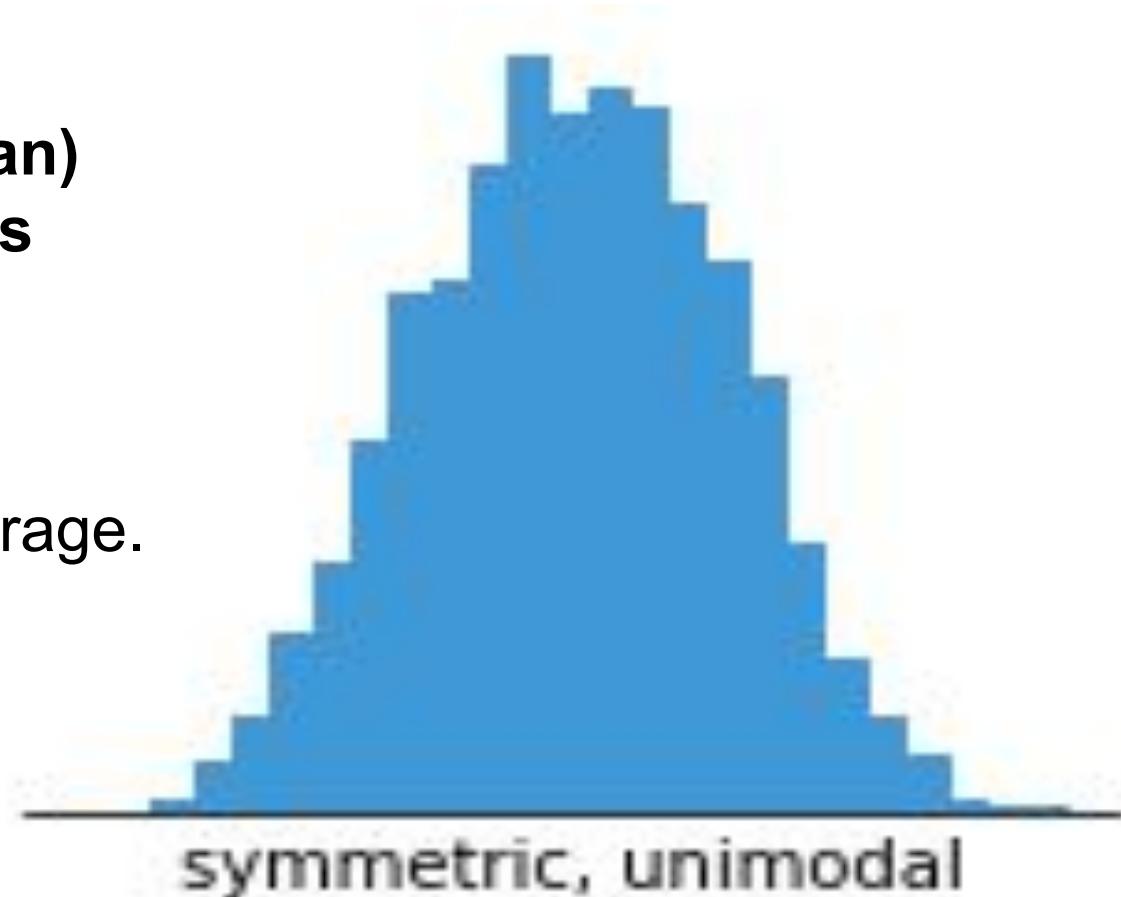
A **normal distribution** is a **symmetric, bell-shaped** distribution.

Key characteristics

- Most values are near the **center (mean)**
- Left and right sides are **mirror images**
- Mean \approx Median \approx Mode

Intuition

👉 Data is evenly spread around the average.

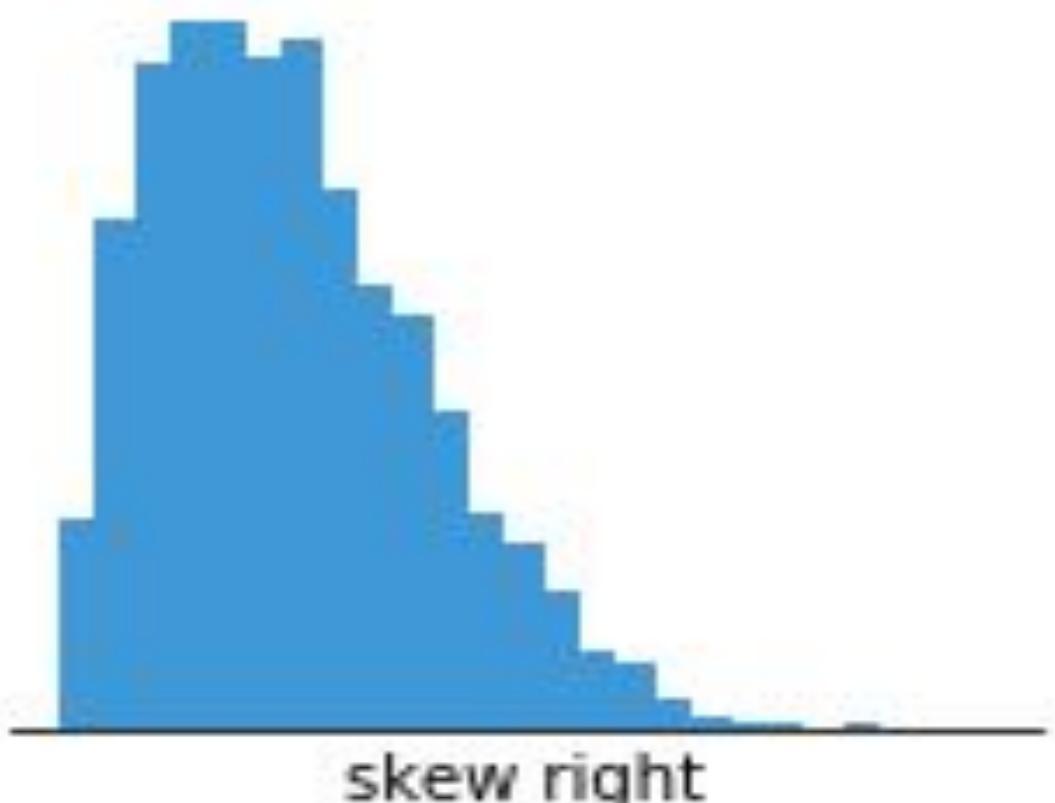
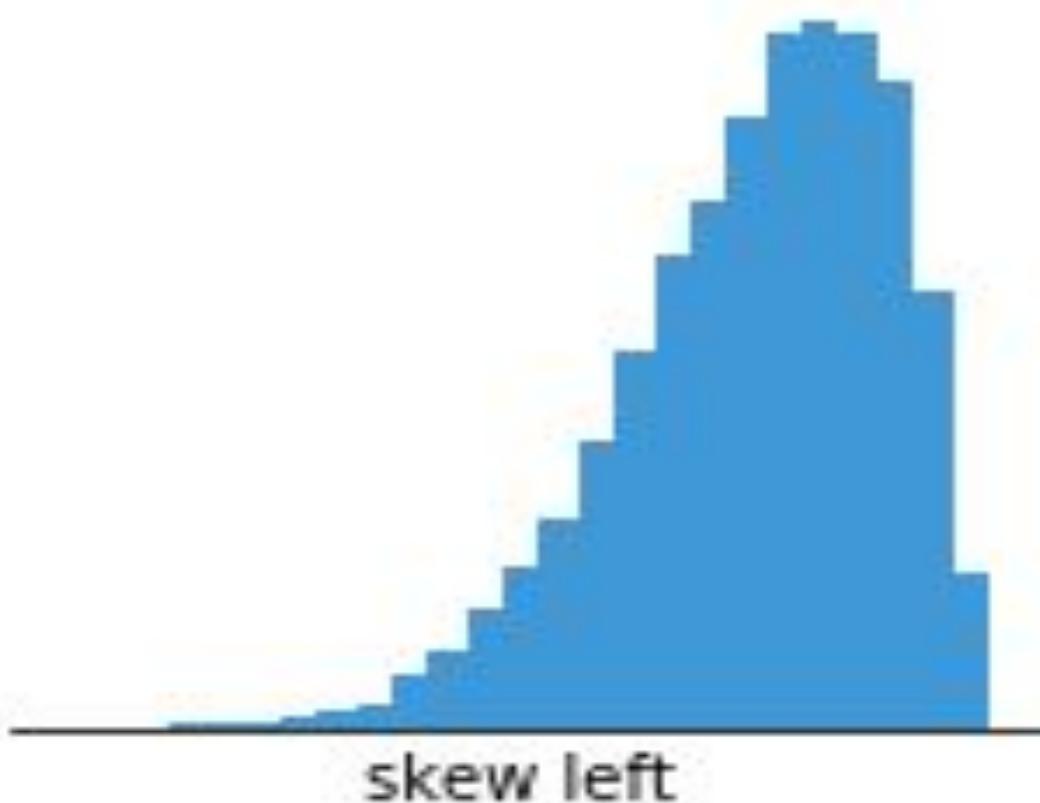


Data Distribution

Skewed Distribution

A **skewed distribution** is not symmetric.

One side has a **longer tail** than the other.

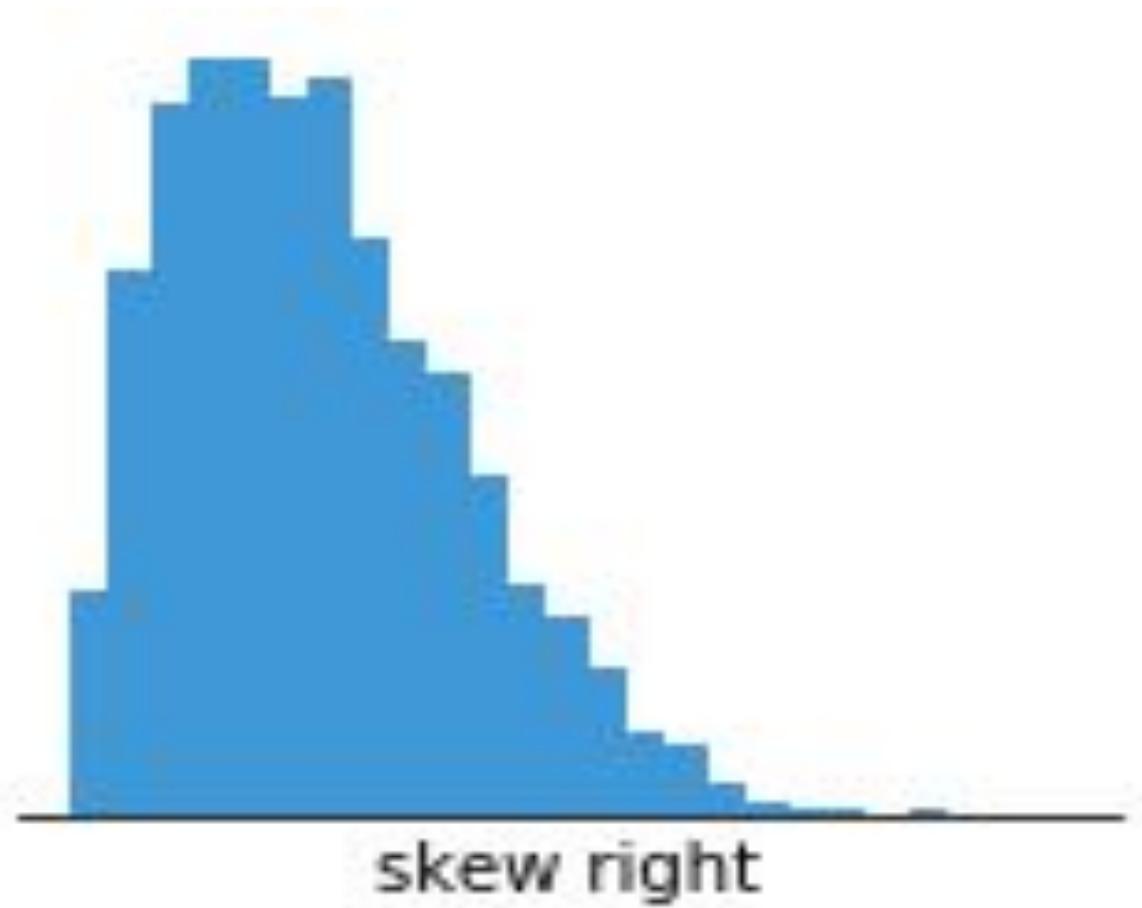


Data Distribution

Skewed Distribution

1. Right-skewed (Positive skew)

- Tail is **long on the right side**
- Most values are **small**
- Mean > Median

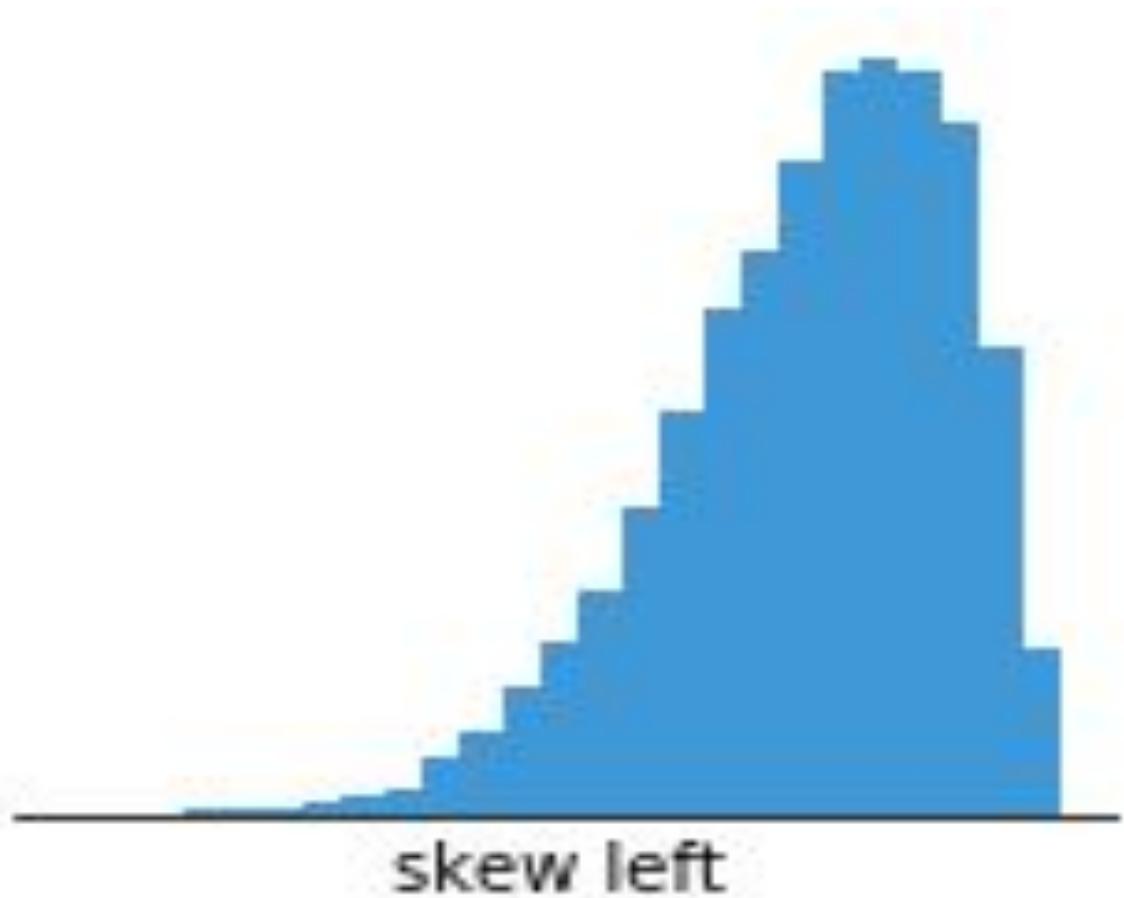


Data Distribution

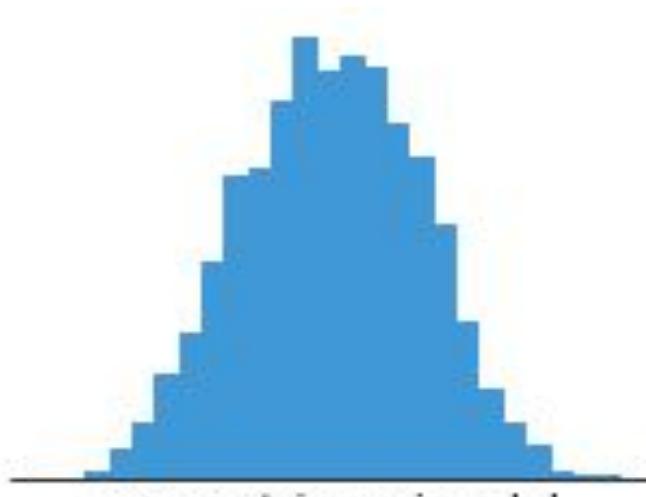
Skewed Distribution

2. Left-skewed (Negative skew)

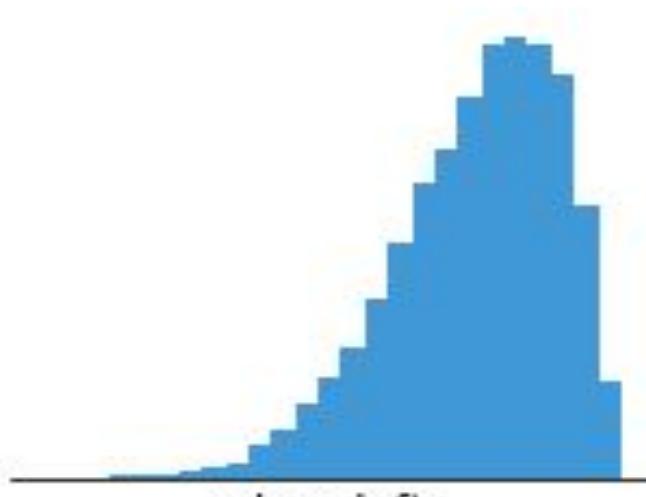
- Tail is **long on the left side**
- Most values are **large**
- Mean < Median



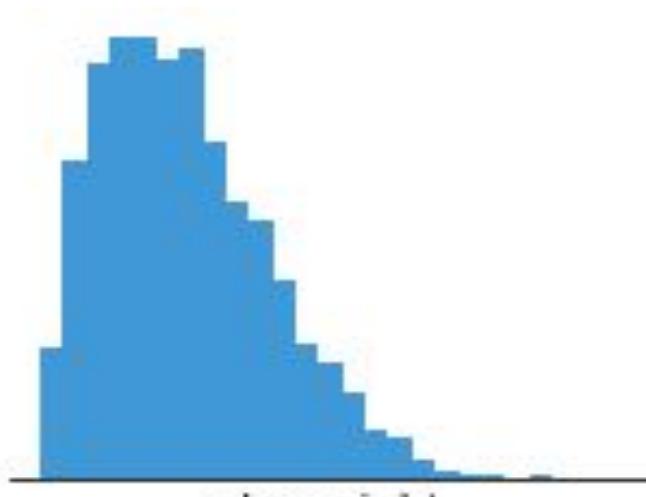
Data Distribution



symmetric, unimodal



skew left



skew right



uniform



bimodal



multimodal



ANY QUESTIONS ?

THANK YOU

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