

# Backtracking

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## Notes



## Output based questions

1.

```
int magicfun (int N){  
    if (N==0){return 0}  
    else{  
        return magicfun(N/2)*10+(N%2);  
    }  
}
```

mf ( 10 ) {

ret

$10 \% 2 + \text{mf}(5) * 10$  {

ret

$5 \% 2 + \text{mf}(2) * 10$  {

ret

$2 \% 2 + \text{mf}(1) * 10$  {

ret

$1 \% 2 + \text{mf}(0) * 10$

3

3

1

mf 1

mf 2

mf 5

mf 10

Stack

1010



```
void fun ( int N ) {  
    if ( N == 0 ) return  
    print ( N )  
    fun ( N - 1 )  
    print ( N )  
}
```

output

2

1

1

2

```
fun ( 2 ) {  
    print ( 2 )  
    fun ( 1 ) {  
        print ( 1 )  
        fun ( 0 )  
        print ( 1 )  
    }  
    print ( 2 )  
}
```



## Q1> Print valid Parenthesis

Given an int  $A$ .

write a function to generate all combinations of well formed parenthesis of length  $2A$   $()$

Input

$A = 1$

Output

$[ "()" ]$

$A = 2$

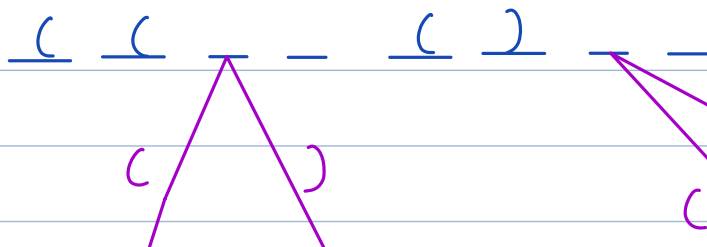
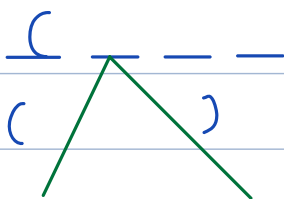
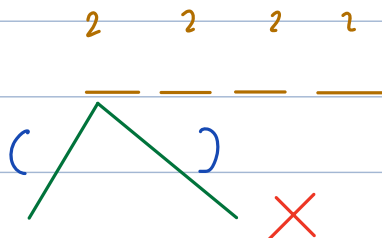
$[ "()", "()" , "()" ]$

$A = 3$

$[ "()", "()", "()",$   
 $"((()))",$   
 $"()(( ))",$   
 $"(( ))()",$   
 $"(( ))()" ]$

$A = 2$

$\approx 2^N$





main (A) {

this.A = A

this.ans = new ArrayList<>()

generateVP("", 0, 0)

return ans

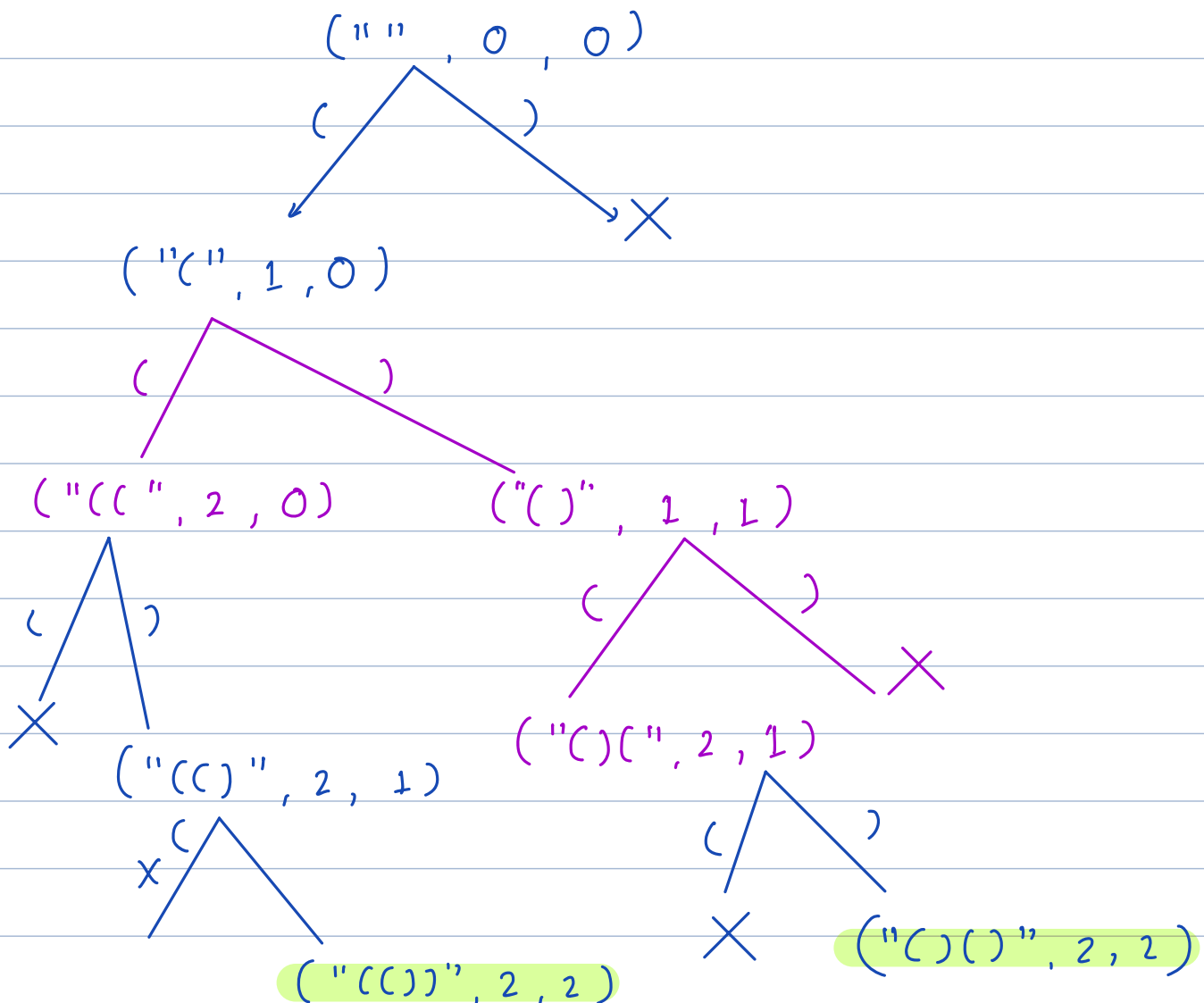
}

TC:  $O(n * 2^n)$

SC:  $O(n)$

Dry Run

A = 2



NO. of fn call \* TC per call  
 $2^n$   $O(N)$

TC:  $O(n * 2^n)$



## Definition of Subset and Subsequence

[ 2 8 12 5 3 16 ]

subset  $\longrightarrow$  Any selection of elements of an array  
in any order

[ ]  $\checkmark$

[ 8 2 ]  $\checkmark$  == [ 2 8 ]  $\checkmark$

[ 12 3 16 ]  $\checkmark$

subsequence  $\longrightarrow$  It's a subset with order

[ 3 5 ]  $\times$

[ 2 12 5 ]  $\checkmark$

[ 12 5 8 ]  $\times$





2. Generate all subsets of the given arr[ ] {distinct}

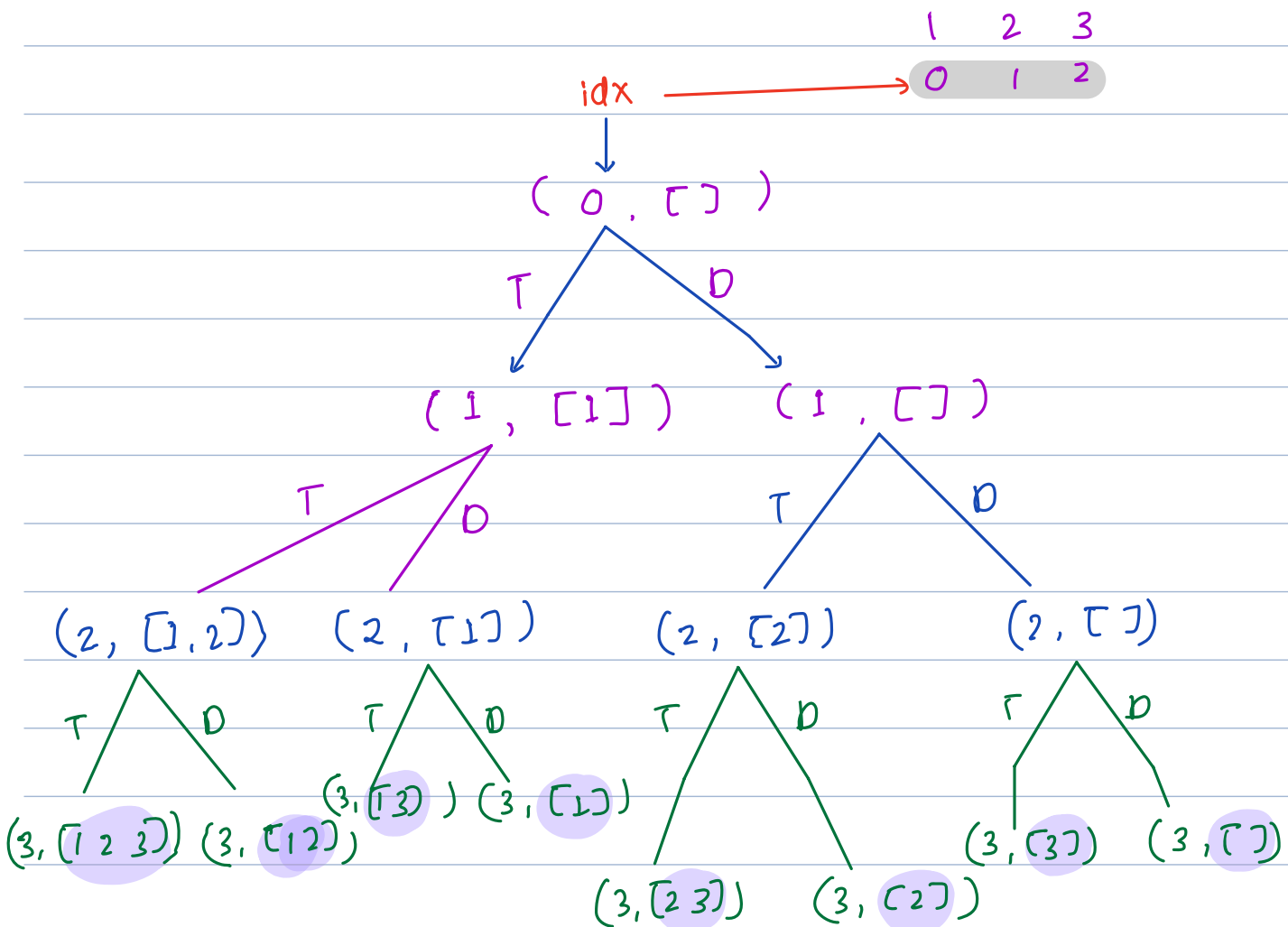
output

$A[] = [5 \ 8]$        $[]$     $[5]$     $[8]$     $[5, 8]$

$A[] = [1 \ 2 \ 3]$

$[]$        $[1 \ 3]$   
 $[1]$        $[2 \ 3]$   
 $[2]$        $[1 \ 2]$   
 $[3]$        $[1 \ 2 \ 3]$

# subsets for  $A.length == n = 2^n$





## Pseudocode

A[] global

ans global

```

void generateSub (int idx , ArrayList cur ) {
    // Base cond"
    if ( idx == A.length ) {
        ans.add (cur) // shallow copy
        return
    }
    // take idx in subset
    cur.add ( A[idx] ) // do
    generateSub ( idx+1 , cur )
    cur.remove ( cur.size() -1 ) // undo

    // Dont take
    generateSub ( idx+1 , cur )
}

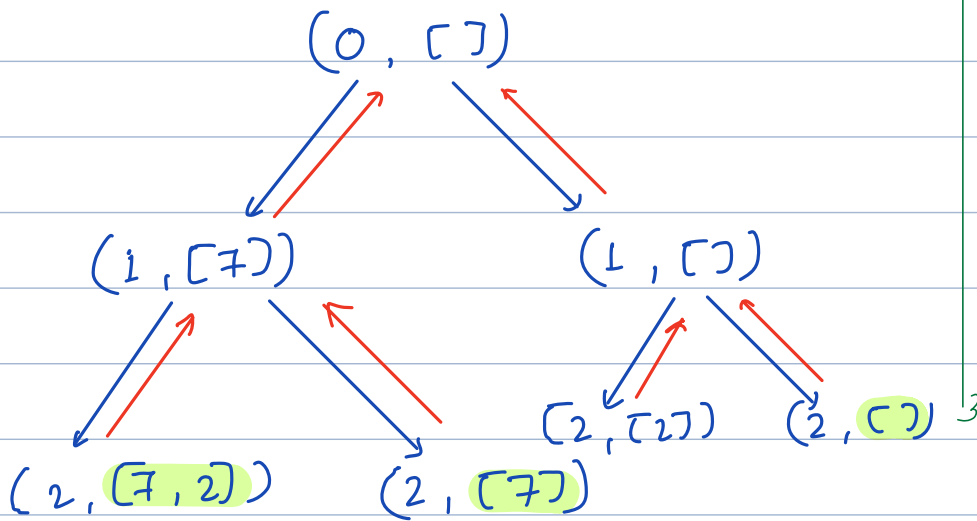
```

There are 2 issues in the above code ?

TC:  $O(n * 2^n)$ SC:  $O(N)$ 

Break : 10:46

$A = [7, 2]$   
 0 1



ans [7, 2] [7]

```
void generateSub (int idx, A<int> cur) {
    // Base cond"
    if (idx == A.length) {
        ans.add (cur)
        return
    }

    // take idx in subset
    cur.add (A[idx])
    generateSub (idx+1, cur)
    cur.remove (cur.size()-1) // undo

    // Don't take
    generateSub (idx+1, cur)
}
```

## Template Backtracking

generate all possibilities via recursion

DO

recurse

UNDO

## Fitness Meets Variety

A popular Fitness app FitBit, is looking to make workouts more exciting for its users. The app has noticed that people get bored when the same exercises are shown in the same order every time they work out. To mix things up, FitBit wants to show all the different ways the exercises can be arranged so that each workout feels new.

Your challenge is to write a program for FitBit that takes a string A as input, where each character in the string represents a different exercise. Your program should then find and display all possible arrangements of these exercises.

Example:

A = Push-ups

B = Squats

C = Burpees

D = Planks

A B C D

A B D C

A C B D

⋮

permutations

## Permutations

Given a string with distinct elements.

Print all permutations of it **without modifying input**

Eg

Input

output

"abc"

abc

acb

bac

bca

cab

cba

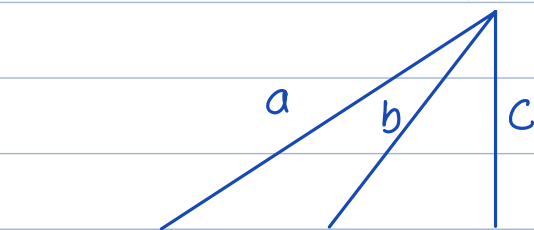
$$3! = 6$$

We let to maintain characters used.

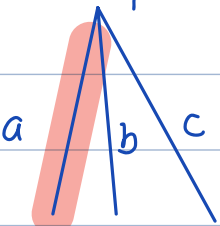
Idea →

( "", { } )

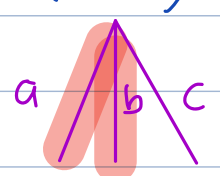
s = abc.



('a', {a})   'b', {b}   'c', {c}



('ab', {a,b})   ('ac', {a,c})



"abc"

{a,b,c}

"acb"

{a,b,c}

s is global

""

{}

```
void generatePerm (String cur, HashSet set) {
```

```
    // Base cond"
```

```
    if (cur.length() == s.length()) {
```

```
        print(cur)
```

```
        ret
```

```
    for i → 0 to s.length - 1 {
```

```
        ch = s.charAt(i)
```

```
        if (!set.contains(ch)) {
```

```
            // DO
```

```
            set.add(ch)
```

```
            generatePerm (cur + ch, set)
```

```
            // undo
```

```
            set.remove(ch)
```

TC:  $O(n * n!)$

equivalent

→  $O(n!)$

SC:  $O(n)$

Doubt session

$$A[i] = \begin{matrix} \downarrow \\ 7, 8 \\ 0, 1 \end{matrix}$$

DT  
~  
T  
x

