

# Template v2.0

poore

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# 1 Math

## 1.1 CRT

```
1 // 中国剩余定理
2 // x ≡ a[i] (mod m[i])
3 // m[i] is coprime
4 LL CRT(LL *a, LL *m, int n)
5 {
6     LL M = 1, Mi, x0, y0, d, ret = 0;
7     for(int i = 0; i < n; i++)
8         M *= m[i];
9     for(int i = 0; i < n; i++)
10    {
11        Mi = M/m[i];
12        EXT_GCD(Mi, m[i], d, x0, y0);
13        LL tmp = slow_mul(Mi, x0, M);
14        tmp = slow_mul(tmp, a[i], M);
15        ret = (ret + tmp) % M;
16        //ret = (ret+Mi*x0*a[i]) % M;
17    }
18    if(ret < 0)
19        ret += M;
20    return ret;
21 }
```

## 1.2 Gauss

```
1 /*
2  * a 保存系数矩阵和每个方程的值
3  * v 储存方程组的解
4  */
5 void gauss(int n, double a[SZ][SZ], double v[SZ]) {
6     int k=1;
7     for (int i=1;i<=n;i++) {
8         int p=0;
9         for (int j=k;j<=n;j++) if (fabs(a[j][i])>eps) {
10             p=j;
11             break;
12         }
13         if (!p) continue;
14         for (int l=1;l<=n+1;l++) swap(a[p][l],a[k][l]);
15         for (int j=k+1;j<=n;j++) {
16             double rate=a[j][i]/a[k][i];
17             for (int l=1;l<=n+1;l++)
18                 a[j][l]-=a[k][l]*rate;
19         }
20         k++;
21     }
22     for (int i=n;i;i--) {
23         v[i]=a[i][n+1];
24         for (int j=i+1;j<=n;j++)
25             v[i]-=v[j]*a[i][j];
26         v[i]/=a[i][i];
27     }
28 }
```

## 1.3 Mo's

```
1 /*
2  * offlien Algorithm
3  */
4 int rtn = sqrt(n);
5 bool operator < (const Query &a, const Query &b) {
6     if (a.lp == b.lp) return a.r < b.r;
7     else return a.lp < b.lp;
8 }
9
10 void update(int &l, int &r, int L, int R) {
11     while(r < R) {
12         r++;
13         bita.add(a[r], 1);
14         bitb.add(b[r], 1);
15     }
16     while(r > R) {
17         bita.add(a[r], -1);
18         bitb.add(b[r], -1);
19         r--;
20     }
21     while(l < L) {
22         bita.add(a[l], -1);
23         bitb.add(b[l], -1);
```

```
        l++;
    }
    while(l > L) {
        l--;
        bita.add(a[l], 1);
        bitb.add(b[l], 1);
    }
}
```

## 1.4 ext\_gcd1

```
1 // 扩展欧几里得
2 // a , b 任意
3 void EXT_GCD(LL a, LL b, LL &d, LL &x, LL &y)
4 {
5     if(!b) {d = a, x = 1, y = 0;}
6     else {EXT_GCD(b, a % b, d, y, x), y -= x * (a / b);}
7 }
```

## 1.5 ext\_gcd2

```
1 // 扩展欧几里得
2 // a >= 0, b > 0
3 LL ext_gcd(LL a, LL b, LL& x, LL& y)
4 {
5     LL x1=0LL, y1=1LL, x0=1LL, y0=0LL;
6     LL r = (a%b + b) % b;
7     LL q = (a-r) / b;
8     x = 0LL,y = 1LL;
9     while(r)
10    {
11        x=x0-q*x1;y=y0-q*y1;
12        x0=x1;y0=y1;
13        x1=x;y1=y;
14        a=b;b=r;
15        r=a%b;
16        q=(a-r)/b;
17    }
18    return b;
19 }
```

## 1.6 gcd

```
1 // 非递归
2 LL gcd(LL a,LL b)
3 {
4     if (a < b) swap(a, b);
5     LL Rem;
6     while(b > 0)
7     {
8         Rem = a % b;
9         a = b;
10        b = Rem;
11    }
12    return a;
13 }
```

## 1.7 gcd\_re

```
1 // 递归求gcd
2 LL GCD(LL a, LL b)
3 {
4     if(a < b) swap(a, b);
5     LL r = a % b;
6     if(r == 0) return b;
7     return GCD(b, r);
8 }
```

## 1.8 josephes

```
1 #include <iostream>
2 using namespace std;
3 //編號從0開始，也就是說如果編號從1開始結果要加1
4 int josephus(int n, int k) { //非遞回版本
5     int s = 0;
6     for (int i = 2; i <= n; i++)
7         s = (s + k) % i;
8     return s;
9 }
10 int josephus_recursion(int n, int k) { //遞回版本
11     return n > 1 ? (josephus_recursion(n - 1, k) + k) % n :
12     0;
```

```
12 }
13 int main() {
14     for (int i = 1; i <= 100; i++)
15         cout << i << ' ' << josephus(i, 5) << endl;
16     return 0;
17 }
```

## 1.9 linear\_mod\_equation

```
1 // 线性方程求解
2 // ax = b (mod n)
3 vector<LL> linear_mod_equation(LL a, LL b, LL n)
4 {
5     LL x, y, d;
6     vector<LL> sol;
7     sol.clear();
8     EXT_GCD(a, n, d, x, y);
9     if( b%d ) d = 0;
10    else
11    {
12        sol.push_back(x * (b/d) % n);
13        for (int i = 1; i < d; i++)
14            sol.push_back((sol[i-1] + n/d + n) % n);
15    }
16    return sol;
17 }
```

## 1.10 matrix

```
1 //poj 3233
2 //cal (A + A^2 + A^3 + ... + A^K) % Mod
3 #define maxn 30
4 typedef long long LL;
5 struct Matrix{
6     LL m[maxn][maxn];
7     Matrix(){memset(m, 0, sizeof(m));}
8 };
9 typedef Matrix matrix;
10 LL Mod;
11 int n;
12 matrix operator* (matrix A, matrix B) {
13     matrix C;
14     for(int i = 0; i < n; i++)
15         for(int j = 0; j < n; j++) {
16             C.m[i][j] = 0LL;
17             for(int k = 0; k < n; k++)
18                 C.m[i][j] += A.m[i][k]*B.m[k][j];
19             C.m[i][j] %= Mod;
20         }
21     return C;
22 }
23 matrix operator+ (matrix A, matrix B) {
24     for(int i = 0; i < n; i++)
25         for(int j = 0; j < n; j++)
26             A.m[i][j] = (A.m[i][j] + B.m[i][j]) % Mod;
27     return A;
28 }
29 matrix operator% (matrix A, LL m) {
30     for(int i = 0; i < n; i++)
31         for(int j = 0; j < n; j++)
32             A.m[i][j] %= m;
33     return A;
34 }
35 matrix matrix_pow(int k, matrix M) {
36     if(k == 1) return M;
37     matrix ans;
38     memset(ans.m, 0, sizeof(ans.m));
39     for(int i = 0; i < n; i++)
40         ans.m[i][i] = 1LL;
41     while(k) {
42         if(k&1) {
43             ans = ans * M;
44             k--;
45         }
46         else {
47             k /= 2;
48             M = M * M;
49         }
50     }
51     return ans;
52 }
53 matrix sum(matrix ma, int k) {
```

```
matrix ret;
if(k == 1) return ma;
if(k&1) {
    matrix tmp = sum(ma, k/2) % Mod, tmp1 = matrix_pow(k
/2+1, ma) % Mod;
    ret = (tmp + tmp1 + tmp * tmp1) % Mod;
}
else {
    matrix tmp = sum(ma, k/2) % Mod, tmp1 = matrix_pow(k
/2, ma) % Mod;
    ret = (tmp + tmp * tmp1) % Mod;
}
return ret;
}
int main() {
    int k;
    matrix A;
    scanf("%d%d%lld", &n, &k, &Mod);
    for(int i = 0; i < n; i++)
        for(int j = 0; j < n; j++)
            scanf("%lld", &A.m[i][j]);
    A = sum(A, k);
    for(int i = 0; i < n; i++)
        for(int j = 0; j < n; j++)
        {
            printf("%lld%c", A.m[i][j], (j == n-1)? '\n': ' ');
        }
    return 0;
}
}
```

## 1.11 matrix\_pow

```
1 struct matrix {
2     ll m[SZ][SZ];
3     matrix() {
4         memset(m, 0, sizeof(m));
5     }
6     matrix(int x) {
7         memset(m, 0, sizeof(m));
8         for (int i = 0; i < SZ; i++) m[i][i] = x;
9     }
10    void clear() {
11        memset(m, 0, sizeof(m));
12    }
13    friend matrix operator *(matrix a, matrix b) {
14        matrix c;
15        for (int k = 0; k < SZ; k++)
16            for (int i = 0; i < SZ; i++) if (a.m[i][k])
17                for (int j = 0; j < SZ; j++)
18                    (c.m[i][j]+=a.m[i][k]*b.m[k][j]%oo)%=oo;
19        return c;
20    }
21    friend matrix operator ^(matrix e, ll k) {
22        matrix tmp = matrix(1);
23        while(k) {
24            if (k&1) tmp = tmp*e;
25            k>>=1;
26            e=e*e;
27        }
28        return tmp;
29    }
30    void show() {
31        printf("=====\n");
32        for (int i = 0; i < SZ; i++)
33            for (int j = 0; j < SZ; j++)
34                printf("%I64d%c", m[i][j], j == SZ-1? '\n': ' ');
35        printf("=====\n");
36    }
37 };
```

## 1.12 matrix\_rotate

```
1 struct Matrix {
2     double m[3][3];
3     Matrix(){
4         for (int i = 0; i < 3; i++)
5             for (int j = 0; j < 3; j++)
6                 m[i][j]=0.0;
7     }
8     Matrix(double a) {
9         for (int i = 0; i < 3; i++)
10             for (int j = 0; j < 3; j++)
```

```
11     m[i][j]=0.0;
12     for (int i = 0; i < 3; i++)
13         m[i][i] = a;
14 }
15 Matrix operator * (Matrix M) {
16     Matrix ret;
17     for (int i = 0; i < 3; i++)
18         for (int j = 0; j < 3; j++)
19             for (int k = 0; k < 3; k++)
20                 ret.m[i][j] += m[i][k]*M.m[k][j];
21     return ret;
22 }
23 void init(double x, double y, double r) {
24     for (int i = 0; i < 3; i++)
25         for (int j = 0; j < 3; j++)
26             m[i][j]=0.0;
27     m[0][0]=cos(r);
28     m[0][1]=sin(r);
29     m[1][0]=-sin(r);
30     m[1][1]=cos(r);
31     m[2][0]=x*(1-cos(r))+y*sin(r);
32     m[2][1]=y*(1-cos(r))-x*sin(r);
33     m[2][2]=1.0;
34 }
35 }t;
36 int main() {
37     int T;
38     scanf("%d", &T);
39     while (T--) {
40         scanf("%d", &n);
41         Matrix ans = Matrix(1);
42         double x, y, r;
43         for (int i = 1; i <= n; i++) {
44             scanf("%lf%lf%lf", &x,&y,&r);
45             t.init(x,y,r);
46             ans = ans*t;
47         }
48         double theta = atan2(ans.m[0][1], ans.m[0][0]);
49         if (dcmp(theta) < 0) theta += pi*2.0;
50         double a = 1-ans.m[0][0];
51         double b = ans.m[0][1];
52         double A = ans.m[2][0];
53         double B = ans.m[2][1];
54         y = (b*A+a*B) / (a*a+b*b);
55         x = (a*A-b*B) / (a*a+b*b);
56         printf("%.8f %.8f %.8f\n", x, y, theta);
57     }
58     return 0;
59 }
```

### 1.13 mega\_mod

```
1 // 解 n 个一元线性同于方程组
2 // x ≡ r (mod a)
3 // 求x
4 LL mega_mod(int n)
5 {
6     LL a1, a2, r1, r2, d, c, x, y, x0,s;
7     bool flag = true;
8     scanf("%lld%lld", &a1, &r1);
9     for(int i = 1; i < n; i++)
10     {
11         scanf("%lld%lld", &a2, &r2);
12         if(!flag) continue;
13         c = r2 - r1;
14         EXT_GCD(a1, a2, d, x, y);
15         if(c%d!=0)
16         {
17             flag = false;
18             continue;
19         }
20         x0 = x*c/d;
21         s = a2/d;
22         x0 = (x0%s+s)%s;
23         r1=r1+x0*a1;
24         a1=a1*a2/d;
25     }
26     if(flag) return r1;
27     else return -1LL;
28 }
```

### 1.14 mersenneprime

```
// 判断Mp = 2^p-1 是否为梅森素数
bool lucas_lehmer(int p)
{
    if(p == 2) return true;
    LL m = (1LL<<p)-1LL, tmp = 4LL;
    for(int i = 0; i < p-2; i++)
    {
        tmp = (slow_mul(tmp, tmp, m) - 2 + m) % m;
    }
    if(tmp == 0LL) return true;
    return false;
}
```

### 1.15 miller\_rabin

```
LL witness(LL a,LL b,LL c)
{
    if(b==0)return 1;
    LL x,y,t=0;
    while((b&1)==0)
        b>>=1,t++;
    y=x=pow_mod(a,b,c);
    // 二次探测
    while(t--)
    {
        y=slow_mul(x,x,c);
        if(y==1 && x!=1 && x!=c-1)
            return false;
        x=y;
    }
    return y==1;
}
bool miller_rabin(LL n)
// ..质数为true, 非质数为false..
{
    if(n==2)return true;
    if(n<2 || (n&1)==0)return false;
    for(int i=0;i<3;i++)
        if(witness(rand()%(n-2)+2,n-1,n)!=1)
            return false;
    return true;
}
```

### 1.16 phi

```
// 欧拉函数预处理
int phi[maxn];
void getpphi(int n)
{
    memset(phi, 0, sizeof(phi));
    phi[1] = 1;
    for(int i = 2; i <= n; i++)if(!phi[i])
    {
        for(int j = i; j <= n; j+=i)
        {
            if(!phi[j])
                phi[j] = j;
            phi[j] = phi[j]/i*(i-1);
        }
    }
}
```

### 1.17 pollard\_rho

```
// ..随机返回一个 n 的约数..
LL ans = INF;
LL pollard_rho(LL n,LL c)
{
    if(n%2==0)return 2;
    LL i=1,k=2,x=rand()%n,y=x,d;
    while(1){
        i++;
        x=(slow_mul(x,x,n)+c)%n;
        d=gcd(y-x,n);
        if(d==n)return n;
        if(d!=n && d>1)return d;
        if(i==k) y=x,k<<=1;
    }
}
void calc(LL n,LL c=240)
// 寻找最小的约数..
```

```

18 {
19     if(n==1)return;
20     if(miller_rabin(n)){
21         ans=min(ans,n);
22         return;
23     }
24     LL k=n;
25     while(k==n)k=pollard_rho(n,c—);
26     calc(k,c),calc(n/k,c);
27 }

```

### 1.18 prime\_seive

```

1 // 筛法求质数
2 // prime[] 储存质数。1-based index;
3 const int maxn = 100020;
4 bool isprime[maxn];
5 LL prime[maxn];
6 int doprime(LL N)
7 {
8     int nprime = 0;
9     memset(isprime, true, sizeof(isprime));
10    isprime[1] = false;
11    for(LL i = 2; i <= N; i++)
12    {
13        if(isprime[i])
14        {
15            prime[++nprime] = i;
16            for(LL j = i*i; j <= N; j+=i)
17                isprime[j] = false;
18        }
19    }
20    return nprime;
21 }

```

### 1.19 quick\_pow

```

1 // 快速幂
2 // (a^b) % p
3 LL pow_mod(LL a, LL b, LL p)
4 {
5     LL ret = 1;
6     while(b) {
7         if(b & 1) ret = (ret*a)%p;
8         a = (a*a)%p;
9         b >>= 1;
10    }
11    return ret%p;
12 }

```

## 1.20 reverse\_extgcd

```

1 // 用扩展欧几里得求逆元
2 // 要求 a, c 互质
3 // 如果没有逆元返回 -1
4 LL inv(LL a, LL c)
5 {
6     LL d, x, y;
7     EXT_GCD(a, c, d, x, y);
8     return d == 1 ? (x + c) % c : -1;
9 }

```

**1.21** reverse rer

```

1 // 递归求逆元
2 //  $p, x$  互质
3 LL inv(LL x, LL m)
4 {
5     if (x == 1) return x;
6     return inv(m % x, m)*(m - m / x) % m;
7 }

```

1.22 slow mul

```

1 // 慢速乘
2 // a * b % p;
3 LL slow_mul(LL a, LL b, LL p)
4 {
5     if (b < 0 && a >= 0) swap(a, b);
6     else if (a < 0 && b < 0) {a = -a; b = -b;}
7     LL ret = 0;

```

```
while(b) {
    if(b & 1) ret = (ret + a) % p;
    a = (a + a) % p;
    b >>= 1;
}
return ret % p;
}
```

### 1.23 split\_int

```
// 把整数 n 拆分成几个数相加的形式，问有多少种拆分方法
int dp[maxn];
void splitint()
{
    memset(dp, 0, sizeof(dp));
    dp[0]=1;
    for(int i = 1; i <= maxn; i++)
    {
        for(int j = 1, r = 1; i - (3*j*j-j)/2 >= 0; j++, r
            *=-1)
        {
            dp[i] += dp[i-(3*j*j-j)/2]*r;
            dp[i] %= MOD;
            dp[i] = (dp[i]+MOD)%MOD;
            if(i-(3*j*j+j)/2 >= 0)
            {
                dp[i] += dp[i-(3*j*j+j)/2] *r;
                dp[i] %= MOD;
                dp[i] = (dp[i] + MOD)%MOD;
            }
        }
    }
}
```

## 1.24 stirling

```
// Stirling N的阶乘的长度
const double PI=3.1415926;
int main()
{
    int t,n,a;
    while(scanf("%d",&n)!=EOF)
    {
        a=(int)((0.5*log(2*PI*n)+n*log(n)-n)/log(10));
        printf("%d\n",a+1);
    }
    return 0;
}
```

1.25 zzz

```

/*
Something Tasteless

1. 素数个数估算
    设 $\pi(x)$  为小于  $x$  的素数的个数
    当  $x$  足够大时,  $\pi(x) = x/\ln x$ ;
2.  $n!$  的素因子分解中的素数  $p$  的次数 为
     $[n/p] + [n/(p^2)] + [n/(p^3)] + \dots +$ 

*/

```

## 2 strings

## 2.1 Acauto

```

struct ACAuto {
    deque<int>q;
    struct Trie{
        int fail, next[26], cnt;
    }trie[maxn];
    int tot;
    void insert(char *s) {
        int cur = 1;
        for(int i = 0; s[i]; i++) {
            if(!trie[cur].next[s[i]-'a'])
                trie[cur].next[s[i]-'a'] = ++tot;
            cur = trie[cur].next[s[i]-'a'];
        }
        trie[cur].cnt++;
    }
}

```

```

16 void build_acauto() {
17     q.clear();
18     q.push_back(1);
19     trie[1].fail = 1;
20     while(!q.empty()) {
21         int cur = q.front();
22         q.pop_front();
23         for(int i = 0; i < 26; i++) if(trie[cur].next[i]) {
24             int next = trie[cur].next[i];
25             if(cur == 1) {
26                 trie[next].fail = 1;
27             }
28             else {
29                 int tmp = trie[cur].fail;
30                 while(tmp != 1 && trie[tmp].next[i] == 0) tmp =
31                     trie[tmp].fail;
32                 if(trie[tmp].next[i]) {
33                     trie[next].fail = trie[tmp].next[i];
34                 }
35                 else {
36                     trie[next].fail = 1;
37                 }
38             }
39             q.push_back(next);
40         }
41     }
42     int query(char *s) {
43         int ans = 0, cur = 1, tmp;
44         for(int i = 0; s[i]; i++) {
45             if(trie[cur].next[s[i] - 'a']) cur = trie[cur].next[s[
46                 i] - 'a'];
47             else {
48                 while(cur != 1 && trie[cur].next[s[i] - 'a'] == 0)
49                     cur = trie[cur].fail;
50                 if(trie[cur].next[s[i] - 'a']) cur = trie[cur].next[
51                     s[i] - 'a'];
52             }
53             tmp = cur;
54             while(tmp != 1 && trie[tmp].cnt != -1) {
55                 ans += trie[tmp].cnt;
56                 trie[tmp].cnt = -1;
57                 tmp = trie[tmp].fail;
58             }
59             return ans;
60         }
61         void clear() {
62             memset(trie, 0, sizeof(trie));
63             tot = 1;
64         }
65     }
66     int main() {
67         // printf("%d\n", sizeof(trie) / 1024);
68         acat.insert(str);
69         acat.build_acauto();
70         acat.query();
71     }

```

## 2.2 Hash

```

1  /*
2  * getH(s, l, H)
3  * 求从位置s开始长度为l的字符串的hash值
4  * O(n) 预处理, O(1) 查询
5  */
6  const ull xxx = 131;
7  ull H[maxn], xl[maxn];
8  void prepre() {
9      xl[0] = 1;
10     for (int i = 1; i < maxn; i++)
11         xl[i] = xxx * xl[i-1];
12 }
13 void pre(char *str, ull *H) {
14     memset(H, 0, sizeof(H));
15     int len = strlen(str);
16     H[len] = 0;
17     for (int i = len-1; i >= 0; i--) {
18         H[i] = H[i+1]*xxx + str[i];
19     }
20 }
21 ull getH(int s, int l, ull *H) {
22     return H[s] - H[s+l] * xl[l];

```

```

}
23
24
25 /*
26 * BKDR Hash Function
27 * 也可以将返回类型设为ull, 免去取模运算(&)
28 */
29 unsigned int BKDRHash(char *str) {
30     unsigned int seed = 131; // 31 131 1313 13131 131313 etc
31     ..
32     unsigned int hash = 0;
33     while (*str) {
34         hash = hash * seed + (*str++);
35     }
36     return (hash & 0x7FFFFFFF);
37 }

```

## 2.3 KMP

```

1  const int maxn = 1000020;
2  char src[maxn], substring[maxn];
3  int nxt[maxn];
4  void get_nxt(char* substring) {
5      int substring_len = strlen(substring);
6      memset(nxt, 0, sizeof(nxt));
7      nxt[0] = -1;
8      int j = -1;
9      for(int i = 1; i < substring_len; i++)
10     {
11         while(j > -1 && substring[i] != substring[j + 1])
12             j = nxt[j];
13         if(substring[j+1] == substring[i])
14             j = j + 1;
15         nxt[i] = j;
16     }
17 }
18 //process src & substring to get the position
19 int kmp(char* src, char* substring) {
20     int j = -1; int ans = 0;
21     int substring_len = strlen(substring);
22     int src_len = strlen(src);
23     for(int i = 0; i < src_len; i++) {
24         while(j > -1 && src[i] != substring[j + 1])
25             j = nxt[j];
26         if(src[i] == substring[j + 1])
27             j++;
28         if(j == substring_len - 1) {
29             ans ++;
30             printf("From position %d to position %d\n", i +
31                 2 - substring_len, i+1);
32             j = nxt[j];
33         }
34     }
35     return ans;
36 }

```

## 2.4 SuffixArray

```

1  /*
2  * 后缀数组
3  * dc3 的时间是 da的 3/4
4  * da/dc3(int *r, int *sa, int n, int m);
5  * n 为字符串的长度+1, m 为 r中值的范围
6  *
7  * calheight(int *r, int *sa, int n)
8  * n 为字符串的长度
9  *
10 * r 数组为处理的串的int值
11 * sa[i] 表示排名第i的后缀的起始下标
12 * heigh[i] 表示排名第i的后缀于排名第 i-1 的后缀的最长公共
13 前缀
14 * Rank[i] 表示以i开始的后缀的排名
15 *
16 */
17 const int maxn = 1000020;
18 const int oo = 0x3f3f3f3f;
19 int tta[maxn], ttb[maxn], ww[maxn], tts[maxn];
20 int Rank[maxn], height[maxn];
21 int cmp(int *r, int a, int b, int l)
22 {
23     return r[a]==r[b]&&r[a+l]==r[b+l];
24 }
25 void da(int *r, int *sa, int n, int m)

```

```
25 {
26     int i,j,p,*x=tta,*y=ttb,*t;
27     for(i=0;i<m;i++) tts[i]=0;
28     for(i=0;i<n;i++) tts[x[i]=r[i]]++;
29     for(i=1;i<m;i++) tts[i]+=tts[i-1];
30     for(i=n-1;i>=0;i--) sa[—tts[x[i]]]=i;
31     for(j=1,p=1;p<n;j*=2,m=p)
32     {
33         for(p=0,i=n-j;i<n;i++) y[p++]=i;
34         for(i=0;i<n;i++) if(sa[i]>=j) y[p++]=sa[i]-j;
35         for(i=0;i<n;i++) wv[i]=x[y[i]];
36         for(i=0;i<m;i++) tts[i]=0;
37         for(i=0;i<n;i++) tts[wv[i]]++;
38         for(i=1;i<m;i++) tts[i]+=tts[i-1];
39         for(i=n-1;i>=0;i--) sa[—tts[wv[i]]]=y[i];
40         for(t=x,x=y,y=t,p=1,x[sa[0]]=0,i=1;i<n;i++)
41             x[sa[i]]=cmp(y,sa[i-1],sa[i],j)?p-1:p++;
42     }
43     return;
44 }
45
46 // dc3 算法
47 #define N 1000005
48 #define MOD 1000000007
49 #define F(x) ((x)/3+((x)%3==1?0:tb))
50 #define G(x) ((x)<tb?(x)*3+1:((x)-tb)*3+2)
51 int wsf[N],wa[N],wb[N],wv[N],sa[N],rank[N],height[N],f[N];
52 int s[N],a[N];
53 char str[N],str1[N],str2[N];
54 //sa:字典序中排第i位的起始位置在str中第sa[i]
55 //rank:就是str第i个位置的后缀是在字典序排第几
56 //height:字典序排i和i-1的后缀的最长公共前缀
57 int c0(int *r,int a,int b)
58 {
59     return r[a]==r[b]&&r[a+1]==r[b+1]&&r[a+2]==r[b+2];
60 }
61 int c12(int k,int *r,int a,int b)
62 {
63     if(k==2) return r[a]<r[b]||r[a]==r[b]&&c12(1,r,a+1,b+1);
64     else return r[a]<r[b]||r[a]==r[b]&&wv[a+1]<wv[b+1];
65 }
66 void sort(int *r,int *a,int *b,int n,int m)
67 {
68     int i;
69     for(i=0;i<n;i++) wv[i]=r[a[i]];
70     for(i=0;i<m;i++) wsf[i]=0;
71     for(i=0;i<n;i++) wsf[wv[i]]++;
72     for(i=1;i<m;i++) wsf[i]+=wsf[i-1];
73     for(i=n-1;i>=0;i--) b[—wsf[wv[i]]]=a[i];
74     return;
75 }
76 void dc3(int *r,int *sa,int n,int m)
77 {
78     int i,j,*rn=r+n,*san=sa+n,ta=0,tb=(n+1)/3,tbc=0,p;
79     r[n]=r[n+1]=0;
80     for(i=0;i<n;i++) if(i%3!=0) wa[tbc++]=i;
81     sort(r+2,wa,wb,tbc,m);
82     sort(r+1,wb,wa,tbc,m);
83     sort(r,wa,wb,tbc,m);
84     for(p=1,rn[F(wb[0])]=0,i=1;i<tbc;i++)
85         rn[F(wb[i])]=c0(r,wb[i-1],wb[i])?p-1:p++;
86     if(p<tbc) dc3(rn,san,tbc,p);
87     else for(i=0;i<tbc;i++) san[rn[i]]=i;
88     for(i=0;i<tbc;i++) if(san[i]<tb) wb[ta++]=san[i]*3;
89     if(n%3==1) wb[ta++]=n-1;
90     sort(r,wb,wa,ta,m);
91     for(i=0;i<tbc;i++) wv[wb[i]]=G(san[i])=i;
92     for(i=0,j=0,p=0;i<ta&&j<tbc;p++)
93         sa[p]=c12(wb[j]%3,r,wa[i],wb[j])?wa[i++]:wb[j++];
94     for(;i<ta;p++) sa[p]=wa[i++];
95     for(;j<tbc;p++) sa[p]=wb[j++];
96     return;
97 }
98
99 void calheight(int *r,int *sa,int n)
100 {
101     int i,j,k=0;
102     for(i=1;i<=n;i++) Rank[sa[i]]=i;
103     for(i=0;i<n;height[Rank[i+1]]=k)
104         for(k?k—:0,j=sa[Rank[i]-1];r[i+k]==r[j+k];k++);
105     return;
106 }
107 }
```

```
// 查询[s, e](排名)区间中最小的height值
// 即s-1 与 e 的最长公共前缀的长度
int query(int s, int e)
{
    int k = log2(e - s + 1);
    return min(low[s][k], low[e - (1 << k) + 1][k]);
}

// 查询s1, s2开始的后缀的最长公共前缀的长度
// 注意s1 != s2
int callen(int s1, int s2)
{
    int l = Rank[s1], r = Rank[s2];
    if (l > r) swap(l, r);
    return query(l+1, r);
}

void rmqinit()
{
    int mxbit = 20;
    for (int i = 0; i <= n; i++)
        low[i][0] = height[i];
    for (int j = 1; j <= mxbit; j++)
        for (int i = 1; i <= n; i++) if (i + (1<<j) - 1 <= n)
            low[i][j] = min(low[i][j-1], low[i+(1<<(j-1))][j-1]);
}

int main()
{
    s[len] = 0;
    da(s, sa, len+1, 256);
    calheight(s, sa, len);
    return 0;
}
```

## 2.5 extKMP

```
/*
 * getExtNext(char *s, char *t, int *ex)
 * ex 保存s[i...n] 和 t[0...m] 的最长公共前缀的长度
 * next[i] = 保存 t[0...m] 和 t[i...m] 的最长公共前缀的长
 * 度
 */
#define next Nnext
int next[maxn], ex[maxn];
void getExtNext(const char *t, int *next)
{
    int lt = strlen(t);
    next[0] = lt;
    for (int i = 1, j = -1, a, p; i < lt; i++, j—)
        if (j < 0 || i + next[i-a] >= p)
        {
            if (j < 0) j = 0, p = i;
            while(p < lt && t[j] == t[p]) j++, p++;
            next[i] = j, a = i;
        }
        else next[i] = next[i-a];
}

void getExtend(const char *s, const char *t, int *extend)
{
    int ls = strlen(s), lt = strlen(t);
    getExtNext(t, next);
    // a : 最长匹配的下标
    // p : s中最长匹配的位置+1
    for (int i = 0, j = -1, a, p; i < ls; i++, j—)
        if (j < 0 || i + next[i-a] >= p)
        {
            if (j < 0) j = 0, p = i;
            while(p < ls && j < lt && s[p] == t[j]) j++, p++;
            extend[i] = j, a = i;
        }
        else
            extend[i] = next[i-a];
}
```

## 2.6 manacher

```
/*
 * 求最长回文字串
 * O(n);
 * Ma 为增加了分隔符之后的字符串
 * Mp[i] 表示以i为中心的回文串的半径(包括自身)
```

```
6  * mx, 最长长度, id下标
7  */
8  char Ma[maxn*2];
9  int Mp[maxn*2];
10 void manacher(char *s, int *Mp) {
11     int l = 0, len = strlen(s);
12     Ma[l++] = '$';
13     Ma[l++] = '#';
14     for(int i = 0; i < len; i++) {
15         Ma[l++] = s[i];
16         Ma[l++] = '#';
17     }
18     Ma[l] = 0;
19     int mx = 0, id = 0;
20     for(int i = 0; i < l; i++) {
21         Mp[i] = mx>i? min(Mp[2*i-id-i],mx-i):1;
22         while(Ma[i+Mp[i]] == Ma[i-Mp[i]]) Mp[i]++;
23         if(i+Mp[i]>mx) {
24             mx = i + Mp[i];
25             id = i;
26         }
27     }
28 }
```

## 2.7 minSTR

```
1  /*
2  * minstr/maxstr(char *s)
3  * 返回一个pair<int,int>
4  * first 表示最小/最大表示的起始下表
5  * second 表示出现的次数
6  */
7  typedef pair<int,int> pii;
8  pii minstr(char *s) {
9      int l = strlen(s);
10     for (int i = 0; i < l; i++) s[i+1] = s[i];
11     s[2*l] = 0;
12     int i = 0, j = 1;
13     while(i < l && j < l) {
14         int k = 0;
15         while(s[i+k] == s[j+k] && k < l) k++;
16         if (k == l)
17             return pii(min(i, j), 1/(abs(i-j)));
18         else if(s[i+k] > s[j+k]) i = max(i+k+1, j+1);
19         else j = max(j+k+1, i+1);
20     }
21     return pii(min(i, j), 1);
22 }
23 pii maxstr(char *s) {
24     int l = strlen(s);
25     for (int i = 0; i < l; i++) s[i+1] = s[i];
26     s[2*l] = 0;
27     int i = 0, j = 1;
28     while(i < l && j < l) {
29         int k = 0;
30         while(s[i+k] == s[j+k] && k < l) k++;
31         if (k == l)
32             return pii(min(i, j), 1/(abs(i-j)));
33         else if(s[i+k] < s[j+k]) i = max(i+k+1, j+1);
34         else j = max(j+k+1, i+1);
35     }
36     return pii(min(i, j), 1);
37 }
```

## 3 CG

### 3.1 4\_points\_1\_plane

```
1  struct Point3 {
2      double x, y, z;
3      Point3 operator - ( Point3 & p ) {
4          Point3 ans;
5          ans.x = this->x - p.x;
6          ans.y = this->y - p.y;
7          ans.z = this->z - p.z;
8          return ans;
9      }
10 };
11 Point3 operator * ( const Point3 & a, const Point3 & b ) {
12     Point3 ans;
13     ans.x = a.y * b.z - a.z * b.y;
```

```
    ans.y = a.z * b.x - a.x * b.z;
    ans.z = a.x * b.y - a.y * b.x;
    return ans;
}
double dot( const Point3 & a, const Point3 & b ) {
    return a.x * b.x + a.y * b.y + a.z * b.z;
}
int main() {
    Point3 p[4];
    int T;
    cin >> T;
    while(T--)
    {
        for( int i = 0; i < 4; ++i ) scanf( "%lf%lf%lf", &p[i].x, &p[i].y, &p[i].z );
        puts( dot( p[3] - p[0], (p[2] - p[0])*(p[1] - p[0]))
              == 0.0 ? "Yes" : "No" );
    }
    return 0;
}
```

### 3.2 CG

```
1  const double PI = acos(-1.0);
2  const double MAXN = 1000000.0;
3  struct Point{
4      double x,y;
5      Point(double x=0,double y=0):x(x),y(y){}
6  };
7  typedef Point Vec;
8  //向量+向量 = 向量, 点+向量 = 点
9  Vec operator +(Vec A,Vec B){return Vec(A.x+B.x,A.y+B.y);}
10 //点-点 = 向量
11 Vec operator -(Point A,Point B){return Vec(A.x-B.x,A.y-B.y);}
12 //向量*数 = 向量
13 Vec operator *(Vec A,double p){return Vec(A.x*p,A.y*p);}
14 //向量/数 = 向量
15 Vec operator /(Vec A,double p){return Vec(A.x/p,A.y/p);}
16 bool operator <(const Point& a,const Point& b){
17     return a.x<b.x || (a.x == b.x && a.y<b.y);
18 }
19 const double EPS = 1e-10;
20 int dcmp(double x){
21     if(fabs(x)<EPS) return 0;else return x<0? -1: 1;
22 }
23 bool operator == (const Point& a,const Point &b){
24     return dcmp(a.x-b.x)==0 &&dcmp(a.y-b.y) == 0;
25 }
26 double ang(Vec v){return atan2(v.y,v.x);}
27 /*=====直线基本定义=====*/
28 struct Line{
29     Point P;
30     Vec v;
31     double ang;
32     Line(){
33         Line(Point P,Vec v):P(P),v(v){ang = atan2(v.y,v.x);}
34     bool operator < (const Line& L) const {
35         return ang < L.ang;
36     }
37     Point point(double a){
38         return P+v*a;
39     }
40 };
41 /*=====圆的基本定义=====*/
42 struct Circle{
43     Point c;
44     double r;
45     Circle(Point c,double r):c(c),r(r){}
46     Point point(double a){
47         return Point(c.x+cos(a)*r,c.y + sin(a)*r);
48     }
49 };
50 /*=====以上为基本定义=====*/
51
52 double Dot(Vec A,Vec B){return A.x*B.x+A.y*B.y;}
53 double Length(Vec A){ return sqrt(Dot(A,A));}
54 //只能就算较小的那个角!
55 double Angle(Vec A,Vec B){return acos(Dot(A,B)/Length(A)/Length(B));}
56 /*=====用点积算向量长度和两个向量夹角=====*/
57
58
```



```

59 double Cross(Vec A,Vec B){return A.x*B.y - A.y*B.x;}
60 //ABC的三角形有向面积的两倍
61 double Area2(Point A,Point B,Point C){return Cross(B-A,C-A
62 );}
63 //rad是弧度 逆时针旋转 //注意: 是绕原点旋转, 否则要加上坐
64 标
65 Vec Rotate(Vec A,double rad){
66     return Vec(A.x*cos(rad)-A.y*sin(rad),A.x*sin(rad)+A.y*
67     cos(rad));
68 }
69 //逆时针旋转90°的单位法向量
70 Vec Normal(Vec A){
71     double L = Length(A);
72     return Vec(-A.y/L,A.x/L);
73 }
74 /*=====以上为叉积的基本运算=====*/
75 //P+tv和Q+tw两条直线的交点, 确保有唯一交点
76 Point GetlineIntersection(Line a,Line b){
77     Point P = a.P,Q = b.P;
78     Vec v = a.v,w = b.v;
79     Vec u = P-Q;
80     double t = Cross(w,u)/Cross(v,w);
81     return a.point(t);
82 }
83 //点到直线的距离
84 double DistanceToLine(Point P,Line a){
85     Point A = a.P,B = a.P + a.v;
86     Vec v1 = B-A,v2 = P-A;
87     return fabs(Cross(v1,v2)/Length(v1)); //不取绝对值那么得
88     到的是有向距离
89 //点到线段的距离
90 double DistanceToSegment(Point P,Point A,Point B){
91     if(A == B)return Length(P-A);
92     Vec v1 = B - A, v2 = P - A, v3 = P - B;
93     if(dcmp(Dot(v1,v2))<0)return Length(v2);
94     else if(dcmp(Dot(v1,v3))>0) return Length(v3);
95     else return fabs(Cross(v1,v2))/Length(v1);
96 }
97 //点在直线上的投影
98 Point GetLineProjection(Point P,Line a){
99     Point A = a.P,B = a.P + a.v;
100     Vec v = B - A;
101     return A + v*(Dot(v,P-A) / Dot(v,v));
102 }
103 //判断两条线段是否相交 此处必须为规范相交
104 bool SegmentProperIntersection(Point a1,Point a2,Point b1,
105 Point b2){
106     double c1 = Cross(a2-a1,b1-a1),c2 = Cross(a2-a1,b2-a1);
107     double c3 = Cross(b2-b1,a1-b1),c4 = Cross(b2-b1,a2-b1);
108     return dcmp(c1)*dcmp(c2)<0 && dcmp(c3)*dcmp(c4)<0;
109 }
110 //如果允许端点相交, 则用以下代码, 判断一个点是否在一条线段
111 上
112 bool OnSegment(Point p,Point a1,Point a2){ //不对, 不允
113     许端点相交
114     if (p == a1 || p == a2) return 1;
115     return dcmp(Cross(a1-p,a2-p)) == 0 && dcmp(Dot(a1-p,a2-p
116 ))<0;
117 }
118 /*=====以上为点和直线, 直线和直线关系的内容=====*/
119 //判断点和多边形位置关系
120 int isPointInPolygon(Point p, const vector<Point>& poly){
121     int w = 0;
122     int n = poly.size();
123     for(int i=0;i<n;i++){
124         if(OnSegment(p,poly[i],poly[(i+1)%n]))return -1; //在边
125         界上
126         int k = dcmp(Cross(poly[(i+1)%n]-poly[i],p-poly[i]));
127         int d1 = dcmp(poly[i].y - p.y);
128         int d2 = dcmp(poly[(i+1)%n].y - p.y);
129         if(k > 0 && d1 <= 0 && d2 > 0)w++;
130         if(k < 0 && d2 <= 0 && d1 > 0)w--;
131     }
132     if(w != 0)return 1;
133     return 0;
134 }
135 //多边形有向面积
136 double PolygonArea(vector<Point> p){
137     int n = p.size();
138     double area = 0;
139     for(int i=1;i<n-1;i++){
140         area += Cross(p[i] - p[0],p[i+1]-p[0]);
141     }
142     return area/2;
143 }
144 //多边形周长
145 double PolygonZhouc(vector<Point> p){
146     int n = p.size();
147     if (!n) return 0.0;
148     double ans = 0;
149     for(int i=0;i<n-1;i++){
150         ans+= Length(p[i+1]-p[i]);
151     }
152     ans+=Length(p[0]-p[n-1]);
153     return ans;
154 }
155 double isint(double x){
156     return fabs(x - (int)(x+0.5))<EPS;
157 }
158 /*=====多边形面积等内容=====*/
159 bool OnLeft(Line L,Point P){
160     return Cross(L.v,P - L.P)>=0; //如果线上的点不
161     算就改成>
162 }
163 int HalfplaneIntersection(Line* L,int n,Point* poly){ //L
164     数组是从0开始
165     sort(L,L+n);
166     int first,last;
167     Point *p = new Point[n];
168     Line *q = new Line[n];
169     q[first = last = 0] = L[0];
170     for(int i=1;i<n;i++){
171         while(first<last && !OnLeft(L[i],p[last-1]))last--;
172         while(first<last && !OnLeft(L[i],p[first]))first++;
173         q[++last] = L[i];
174         if(fabs(Cross(q[last].v,q[last-1].v))<EPS){
175             last--;
176             if(OnLeft(q[last],L[i].P))q[last] = L[i];
177         }
178         if(first<last) p[last-1] = GetlineIntersection(q[last
179         -1],q[last]);
180     }
181     while(first<last && !OnLeft(q[first],p[last-1]))last --
182     ;
183     if(last-first<=1)return 0;
184     p[last] = GetlineIntersection(q[last],q[first]);
185     int m = 0;
186     for(int i=first;i<=last;i++)poly[m++] = p[i];
187     return m;
188 }
189 /*=====半平面交所需函数及主过程=====*/
190 vector<Point> ConvexHull(vector<Point> p){
191     sort(p.begin(),p.end());
192     //删除重复点
193     p.erase(unique(p.begin(),p.end()),p.end());
194     int n = p.size();
195     vector<Point> ch(n+1);
196     int m = 0;
197     for(int i=0;i<n;i++){
198         while(m>1 && dcmp(Cross(ch[m-1]-ch[m-2],p[i]-ch[m-2]))
199         <= 0)m--; //若需要把边线上的点也算上, 把等号
200         去掉
201         ch[m++] = p[i];
202     }
203     int k = m;
204     for(int i = n-2;i>=0;i--){
205         while(m > k && dcmp(Cross(ch[m-1] - ch[m-2] , p[i]-ch[
206         m-2] )) <= 0)m--;
207         ch[m++] = p[i];
208     }
209     if(n > 1)m--;
210     ch.resize(m);
211     return ch;
212 }
213 /*=====以上为凸包=====*/
214 double RotatingCalipers(const vector<Point>& p){
215     int n = p.size();
216     double ans = 0;
217     Point v;
218     int cur = 1;
219     for(int i=0;i<n;i++){
220         v = p[i]-p[(i+1)%n];
221     }

```

```

209     while(dcmp(Cross(v,p[(cur+1)%n]-p[cur]))<0)
210         cur = (cur+1)%n;
211     ans = max(ans,max(Length(p[i]-p[cur]),Length(p[(i+1)%n]-p[(cur+1)%n])));
212 }
213 return ans;
214 }//求凸包上两点间最远距离
215 /*=====以上为旋转卡壳=====*/
216 double earthdis(Point a,Point b){
217     double x1=PI*a.x/180.0;
218     double y1=PI*a.y/180.0;
219     double x2=PI*b.x/180.0;
220     double y2=PI*b.y/180.0;
221     return acos(cos(x1-x2)*cos(y1)*cos(y2)+sin(y1)*sin(y2));
222 }
223 /*=====给出经纬度，算出球体上两点之间的角度=====*/
224
225 //判断圆和直线交点，方程法
226 int getLineCircleIntersection(Line L, Circle C, double& t1
227 ,double& t2,vector<Point>& sol){
228     double a = L.v.x, b = L.p.x-C.c.x, c = L.v.y, d = L.p.y
229     - C.c.y;
230     double e = a*a+c*c,f = 2*(a*b+c*d),g = b*b-C.r*C.r;
231     double delta = f*f - 4*e*g; //判别式
232     if(dcmp(delta) < 0)return 0; //相离
233     if(dcmp(delta) == 0){ //相切
234         t1 = t2 = -f/(2*e);sol.push_back(L.point(t1));
235         return 1;
236     }
237     //相交
238     t1 = (-f - sqrt(delta)) / (2*e); sol.push_back(L.point(
239     t1));
240     t2 = (-f + sqrt(delta)) / (2*e); sol.push_back(L.point(
241     t2));
242     return 2;
243 }
244 //圆和直线交点，几何法
245 int getLineCircleIntersection(Line L, Circle C,vector<
246 Point>& sol){
247     double d = DistanceToLine(C.c, L);
248     if(dcmp(d - C.r)>0)return 0; //相离
249     Point ans = GetlineIntersection(L, Line(C.c,Normal(L.v))
250     );
251     if(dcmp(d - C.r) == 0){ //相切
252         sol.push_back(ans);
253         return 1;
254     }
255     //相交
256     double len = sqrt(C.r*C.r-d*d);
257     Vec v = L.v / Length(L.v);
258     sol.push_back(ans + v * len),sol.push_back(ans - v * len
259     );
260     return 2;
261 }
262 //判断两圆相交
263 int getCircleCircleIntersection(Circle C1, Circle C2,
264 vector<Point>& sol){
265     double d = Length(C1.c-C2.c);
266     if( dcmp(C1.r - C2.r)>0)
267         swap(C1,C2);
268     if(dcmp(d)==0){
269         if(dcmp(C1.r-C2.r)==0)return -1;//重合
270         return 0;
271     }
272     if(dcmp(C1.r + C2.r -d) < 0) return 0;//外离
273     if(dcmp(fabs(C1.r-C2.r)-d)>0)return 0;//内含
274     if(dcmp(C1.r + C2.r - d) == 0 || dcmp(fabs(C1.r - C2.r)-
275     d) == 0){
276         Vec p = C1.c-C2.c;
277         sol.push_back(C2.c + p / Length(p) * C2.r);
278         return 1;
279     }//外切或内切
280     double a = ang(C2.c - C1.c);
281     double da = acos((C1.r * C1.r+d*d-C2.r*C2.r)/(2*C1.r*d))
282     ;
283     Point p1 = C1.point(a-da),p2 = C1.point(a+da);
284     sol.push_back(p1);
285     sol.push_back(p2);
286     return 2;//相交
287 }
288 //过点p到圆C的切线
289 int getTangents(Point p,Circle C,vector<Line>& L){

```

```

289     Vec u = C.c - p , temp;
290     double dist = Length(u);
291     if(dist < C.r) return 0;
292     else if(dcmp(dist - C.r) == 0){
293         temp = Normal(u);
294         L.push_back(Line(p,temp));
295         return 1;
296     }else {
297         double ang = asin(C.r/dist);
298         temp = Rotate(u,-ang),L.push_back(Line(p,temp));
299         temp = Rotate(u,+ang),L.push_back(Line(p,temp));
300         return 2;
301     }
302 }
303 //两圆公切线，返回切线条数，-1表示无穷多条
304 //注意，当两圆内切或者外切的时候，切点相同，均为p.
305 //sol里存的是切线，p为a上切点,p+v为b上切点
306 int getTangents(Circle A,Circle B,vector<Line>& sol){
307     int cnt = 0;
308     Point a,b;
309     if(dcmp(A.r - B.r) < 0)swap(A,B);
310     double d2 = (A.c.x - B.c.x) * (A.c.x - B.c.x) + (A.c.y -
311     B.c.y) * (A.c.y - B.c.y);
312     double rdiff = A.r - B.r;
313     double rsum = A.r + B.r;
314     if(dcmp(d2 - rdiff * rdiff) < 0) return 0;//内含
315
316     double base = atan2(B.c.y - A.c.y, B.c.x - A.c.x);
317     if(dcmp(d2)==0 && A.r == B.r)return -1;//重合，切线无限多
318     if(dcmp(d2-rdiff * rdiff)==0){//内切，一条切线
319         a = A.point(base),b = B.point(base);
320         sol.push_back(Line(a,Normal(A.c-B.c)));
321         return 1;
322     }
323     //有外切线
324     double ang = acos((A.r-B.r) / sqrt(d2));
325     a = A.point(base+ang),b = B.point(base+ang),sol.
326     push_back(Line(a,b-a)),cnt++;
327     a = A.point(base-ang),b = B.point(base-ang),sol.
328     push_back(Line(a,b-a)),cnt++;
329     if(dcmp(d2 - rsum * rsum)==0){
330         a = A.point(base),b = B.point(PI + base),sol.push_back
331         (Line(a,Normal(A.r-B.r))),cnt++;
332     }else if(dcmp(d2 - rsum * rsum)>0){
333         double ang2 = acos((A.r + B.r) / sqrt(d2));
334         a = A.point(base+ang2),b = B.point(PI+base+ang2),sol.
335         push_back(Line(a,b-a)),cnt++;
336         a = A.point(base-ang2),b = B.point(PI+base-ang2),sol.
337         push_back(Line(a,b-a)),cnt++;
338     }
339     return cnt;
340 }
341
342 /*=====以上为圆的常用函数及计算=====*/
343
344 //double RotatingCalipers(const vector<Point>& p){
345 int main(){
346     int n;
347     vector <Point> p;
348     double tx,ty;
349     while(~scanf("%d",&n)){
350         p.clear();
351         for(int i=1;i<=n;i++){
352             scanf("%lf%lf",&tx,&ty);
353             p.push_back(Point(tx,ty));
354         }
355         p=ConvexHull(p);
356         double goal=RotatingCalipers(p);
357         goal*=goal;
358         printf("%.f\n",goal);
359     }
360     return 0;
361 }

```

### 3.3 CGLines

```

1 struct Line {
2     // Ax + By = C
3     double A, B, C;
4     Line(double _A, double _B, double _C):A(_A),B(_B),C(_C)
5     {}
6     Line():A(0.0),B(0.0),C(0.0){}
7 };

```

```
7
8 Line getLineFromPoints(Point p1, Point p2) {
9     double A = p2.y-p1.y;
10    double B = p1.x-p2.x;
11    double C = A*p1.x + B*p1.y;
12    return Line(A,B,C);
13 }
14
15 // int = 0 无交点
16 // int = 1 一个交点
17 // int = 2 两直线重合
18 pair<Point, int> intersectPoint(Line l1, Line l2) {
19     double det = l1.A*l2.B - l2.A*l1.B;
20     if (dcmp(det) == 0) {
21         // 两直线平行 重合
22         if (dcmp(l1.A*l2.C - l2.A*l1.C) == 0 &&
23             dcmp(l1.B*l2.C - l2.B*l1.C) == 0)
24             return make_pair(Point(), 2);
25         else
26             return make_pair(Point(), 0);
27     }
28     else {
29         double x = (l2.B*l1.C - l1.B*l2.C) / det;
30         double y = (l1.A*l2.C - l2.A*l1.C) / det;
31         return make_pair(Point(x,y), 1);
32     }
33 }
```

### 3.4 CGkuangbin

### 3.5 CGpoints

```
1 struct Point {
2     double x, y;
3     Point(double _x, double _y):x(_x),y(_y){}
4     Point():x(0.0),y(0.0){}
5 };
6 typedef Point Vec;
7
8 void showPoint(Point A) {
9     printf("%.6f, %.6f\n", A.x, A.y);
10 }
11 const Vec operator + (Vec A, Vec B) {
12     return Vec(A.x+B.x, A.y+B.y);
13 }
14 const Vec operator - (Vec A, Vec B) {
15     return Vec(A.x-B.x, A.y-B.y);
16 }
17 const double operator * (Vec A, Vec B) {
18     return A.x*B.x + A.y*B.y;
19 }
20 // A*B = |A|*|B|*sin(theta)
21 // theta为 A,B 向量的夹角
22 // 如果 A 在 B 的顺时针方向180度内, 则theta取正值
23 // 向量叉乘
24 // 返回值为正时, 表示 A 在 B 的右侧180度内
25 // 返回值的绝对值等于以A,B向量为邻边的平行四边型的面积
26 const double operator ^ (Vec A, Vec B) {
27     return A.x*B.y - A.y*B.x;
28 }
29
30 double Lenth(Vec &v) {
31     return sqrt(v*v);
32 }
33
34
35 // 将点 A 绕 p 逆时针旋转 theta 角度(弧度制)
36 // 1. 平移坐标
37 // 2. 旋转
38 // 3. 平移坐标
39 Vec rotate(point A, point p, double theta) {
40     A = A-p;
41     point ret = point(A.x*cos(theta)-A.y*sin(theta), A.x*sin
42         (theta)+A.y*cos(theta)) + p;
43     return ret;
44 }
45
46 // 计算C到AB的距离
47 // isSeg = 1 : AB为线段
48 // isSeg = 0 : AB为直线
```

```
double linePointDist(Point A, Point B, Point C, bool isSeg) {
    double dist = ((B-A)^(C-A)) / sqrt((B-A)*(B-A));
    if (isSeg) {
        double dot1 = (C-B)*(B-A);
        if (dcmp(dot1) > 0) return sqrt((B-C)*(B-C));
        double dot2 = (C-A)*(A-B);
        if (dcmp(dot2) > 0) return sqrt((A-C)*(A-C));
    }
    return fabs(dist);
}

// 判断线段的两个端点是否在直线的两侧
bool lineCrossSeg(Point p1, Point p2, Point ls, Point le) {
    Vec ver = ls-le, v1 = p1-ls, v2 = p2-ls;
    return dcmp((ver^v1)*(ver^v2)) <= 0;
}

// 判断点是否在线段上
// 叉积为 0 表示共线
bool pointOnSeg(point s1, point s2, point p, bool includeEnd) {
    if ((s1 == p || s2 == p) && !includeEnd) return false;
    s2 = s2-s1;
    p = p-s1;
    return dcmp(s2^p)==0 && dcmp(s2*p)>=0;
}

double minx = min(s1.x, s2.x);
double maxx = max(s1.x, s2.x);
double miny = min(s1.y, s2.y);
double maxy = max(s1.y, s2.y);

if ((s1 == p || s2 == p) && !includeEnd) return false;
if (p.x-minx>=0
    && maxx-p.x>=0
    && p.y-miny>=0
    && maxy-p.y>=0
    && ((s2-s1)^(p-s1)) == 0)
    return true;
else
    return false;
}

// 判断两条线段是否相交
// 两次跨立试验
typedef pair<Point, Point> seg;
bool segCrossSeg(seg a, seg b, bool includeEnd) {
    Vec ver = b.X-b.Y, v1 = a.X-b.X, v2 = a.Y-b.X;
    int tmp1 = dcmp((ver^v1)*(ver^v2));
    ver = a.X-a.Y, v1 = b.X-a.X, v2 = b.Y-a.X;
    int tmp2 = dcmp((ver^v1)*(ver^v2));
    if (includeEnd)
        return tmp1 <= 0 && tmp2 <= 0;
    else
        return tmp1 < 0 && tmp2 < 0;
}

double areaPoly(vector<Point> &P) {
    double area = 0.0;
    for (int i = 1, n = P.size(); i+1 < n; i++) {
        area += (P[i+1]-P[0])^(P[i]-P[0]);
    }
    return area / 2.0;
}
```

### 3.6 areaCircle2

```
double areaCircle2(double x1, double y1, double r1, double
x2, double y2, double r2) {
    double d = dist(x1, y1, x2, y2);
    if (r1+r2 < d-eps) return 0.0;
    if (fabs(r1-r2) > d-eps) {
        double tmp = min(r1, r2);
        return pi*tmp*tmp;
    }
    double ang1 = acos((r1*r1+d*d-r2*r2)/(2.0*r1*d));
    double ang2 = acos((r2*r2+d*d-r1*r1)/(2.0*r2*d));
    double ret = ang1*r1*r1+ang2*r2*r2-d*r1*sin(ang1);
    return ret;
}
```

### 3.7 closePair

```
1 bool cmp(Point a, Point b) {
2     if (a.x == b.x) return a.y < b.y;
3     return a.x < b.x;
4 }
5 bool cmpy(int a, int b) {
6     return p[a].y < p[b].y;
7 }
8
9 double closePair(int l, int r) {
10     if (l == r) return inf;
11     if (l+1 == r) return Lenth((p[l]-p[r]));
12     int mid =(l+r)/2;
13     double tdis = min(closePair(l, mid), closePair(mid+1, r)
14 );
15     int cnt = 0;
16     for (int i = l; i <= r; i++) if (fabs(p[i].x-p[i+1].x) <
17 tdis)
18         t[cnt++] = i;
19     sort(t, t + cnt, cmpy);
20     for (int i = 0; i < cnt; i++) {
21         for (int j = i+1; j < cnt && dcmp(p[t[j]].y-p[t[i]].y-
22 tdis) < 0; j++) {
23             double tmp = Lenth((p[t[i]]-p[t[j]]));
24             tdis = min(tdis, tmp);
25         }
26     }
27     return tdis;
28 }
```

### 3.8 convexHull

```
1 int n, s[maxn];
2 int top;
3 bool cmp(point a, point b) {
4     int tmp = (a-p[0])^(b-p[0]);
5     int dis1 = (a-p[0])*(a-p[0]);
6     int dis2 = (b-p[0])*(b-p[0]);
7     if (tmp > 0 || (tmp == 0 && dis1 > dis2)) return true;
8     return false;
9 }
10
11 int graham() {
12     for (int i = 0; i < n; i++) {
13         if (p[i].y < p[0].y || (p[i].y == p[0].y && p[i].x < p
14 [0].x))
15             swap(p[i], p[0]);
16     }
17     sort(p+1, p+n, cmp);
18     s[0] = 0;
19     s[1] = 1;
20     top = 1;
21     for (int i = 2; i < n; i++) {
22         // 注意是否包含边上的点
23         // while(top && ((p[i-1]-p[0])^(p[i]-p[0])) <= 0) top
24 —;
25         while(top && ((p[s[top]]-p[s[top-1]])^(p[i]-p[s[top
26 -1]])) < 0) top—;
27         s[++top] = i;
28     }
29
30     bool cmpxy(point a, point b) {
31         if (a.x == b.x) return a.y < b.y;
32         return a.x < b.x;
33     }
34     // 包含边上的点就将 <= 改为 <
35     int convexHull(Point *p, int n) {
36         sort(p, p + n, cmpxy);
37         int top = 0;
38         for (int i = 0; i < n; i++) {
39             while(top>1 && ((p[s[top-1]]-p[s[top-2]])^(p[i]-p[s[
40 top-2]])) <= 0) top—;
41             s[top++] = i;
42         }
43         int k = top;
44         for (int i=n-2;i>=0;i—) {
45             while(top>k && ((p[s[top-1]]-p[s[top-2]])^(p[i]-p[s[
46 top-2]])) <= 0) top—;
47             s[top++] = i;
48         }
49     }
```

```
    }
    if (n > 1) top—;
    return top;
}
```

### 3.9 halfPlane

```
1 struct Line {
2     Point p, v;
3     double ang;
4     Line(){}
5     Line(Point p, Vec v):p(p),v(v) {
6         ang = atan2(v.y, v.x);
7     }
8     bool operator < (const Line &L) const {
9         return ang < L.ang;
10     }
11 };
12 // 包含边上的点将 > 改为 >=
13 bool onLeft(Line L, Point p) {
14     return (L.v^(p-L.p)) > 0;
15 }
16 Point lineIntersection(Line a, Line b) {
17     Point u = a.p-b.p;
18     double t = (b.v^u)/(a.v^b.v);
19     return a.p+a.v*t;
20 }
21 int halfPlaneIntersection(Line *L, int n, Point *poly) {
22     sort(L, L+n);
23     int first, last;
24     Point *p = new Point[n];
25     Line *q = new Line[n];
26     q[first=last=0] = L[0];
27     for (int i = 1; i < n; i++) {
28         while(first < last && !onLeft(L[i], p[last-1])) last
29 —;
30         while(first < last && !onLeft(L[i], p[first])) first
31 ++;
32         q[++last] = L[i];
33         if (fabs(q[last].v^q[last-1].v) < eps) {
34             last—;
35             if (onLeft(q[last],L[i].p)) q[last] = L[i];
36         }
37         if (first < last) p[last-1] = lineIntersection(q[last
38 -1], q[last]);
39     }
40     while(first < last && !onLeft(q[first], p[last-1])) last
41 —;
42     // 删除无用平面
43     if (last - first <= 1) return 0; // empty
44     p[last] = lineIntersection(q[last], q[first]);
45     int m = 0;
46     for (int i = first; i <= last; i++) poly[m++] = p[i];
47     return m;
48 }
```

### 3.10 minCircleCover

```
1 void minCircleCover(int n, Point &c, double &r) {
2     random_shuffle(p, p+n); c = p[0]; r = 0;
3     for (int i = 1; i < n; i++) if (Lenth(p[i]-c) > r + eps)
4     {
5         c = p[i]; r = 0;
6         for (int j = 0; j < i; j++) if (Lenth(p[j]-c) > r +
7 eps) {
8             c.x = (p[i].x+p[j].x)/2.0;
9             c.y = (p[i].y+p[j].y)/2.0;
10             r = Lenth(p[j]-c);
11             for (int k = 0; k < j; k++) if (Lenth(p[k]-c) >
12 r + eps) {
13                 c = outerCircle(p[i].x,p[i].y,p[j].x,p[j].y,
14 p[k].x,p[k].y);
15                 r = Lenth(p[i]-c);
16             }
17         }
18     }
19 }
```

### 3.11 rotatingCaliper

```
// s 为保存有序的凸包点的下标的栈
// 此处的凸包点为顺时针的顺序
```

```
3 int rotatingCaliper(Point *p, int top) {
4     int q = 1;
5     int ans = 0;
6     s[top] = 0;
7     for (int i = 0; i < top; i++) {
8         while( ((p[s[i+1]]-p[s[i]])^(p[s[q+1]]-p[s[i]])) >
9                ((p[s[i+1]]-p[s[i]])^(p[s[q]] -p[s[i]])) )
10             q = (q+1)%top;
11         ans = max(ans, (p[s[i]]-p[s[q]])*(p[s[i]]-p[s[q]]));
12         // 处理两条边平行的情况
13         ans = max(ans, (p[s[i+1]]-p[s[q+1]])*(p[s[i+1]]-p[s[q+1]]));
14     }
15     return ans;
16 }
```

## 4 DataStructure

### 4.1 Ltree

```
1  /*
2   * 左倾树
3   * 多个优先队列，合并logn
4   *
5   */
6
7  int lc[maxn], rc[maxn];
8  int v[maxn], size[maxn], d[maxn];
9  int tot;
10 int merge(int x, int y) {
11     if (x==0||y==0) return x+y;
12     if (v[x] < v[y]) swap(x, y);
13     rc[x] = merge(rc[x], y);
14     size[x] = size[lc[x]]+size[rc[x]]+1;
15     if (d[rc[x]]>d[lc[x]]) swap(lc[x],rc[x]);
16     d[x] = d[rc[x]]+1;
17     return x;
18 }
19 int top(int x) {
20     return v[x];
21 }
22 int sz(int x) {
23     return size[x];
24 }
25 void pop(int &x) {
26     x = merge(lc[x], rc[x]);
27 }
28 int newHeap(int x) {
29     tot++;
30     v[tot] = x;
31     size[tot] = 1;
32     lc[tot]=rc[tot]=d[tot]=0;
33     return tot;
34 }
35 ll a[maxn];
36 int rt[maxn];
37 int L[maxn], R[maxn];
38 int n;
39 int main() {
40     scanf("%d", &n);
41     for (int i = 1; i <= n; i++) {
42         scanf("%d", &a[i]);
43         a[i]-=i;
44     }
45     tot = 0;
46     int cnt = 0;
47     for (int i = 1; i <= n; i++) {
48         cnt++;
49         rt[cnt] = newHeap(a[i]);
50         L[cnt] = R[cnt] = i;
51         while(cnt>1 && top(rt[cnt]) < top(rt[cnt-1])) {
52             rt[cnt-1] = merge(rt[cnt], rt[cnt-1]);
53             R[cnt-1] = R[cnt];
54             while(sz(rt[cnt-1]) > (R[cnt-1]-L[cnt-1]+2)/2)
55                 pop(rt[cnt-1]);
56             cnt--;
57         }
58     }
59     ll ans = 0;
60     for (int i = 1; i <= cnt; i++) {
61         for (int j = L[i]; j <= R[i]; j++)
62             ans += abs(top(rt[i]) - a[j]);
63     }
```

```
    }
    printf("%I64d\n", ans);
    return 0;
}
```

### 4.2 ST\_v2

```
const int maxn = 1e5+20;
int low[maxn][30];
void init(int *d) {
    for (int i = 1; i <= n; i++)
        low[i] = d[i];
    for (int j = 1; j <= 20; j++)
        for (int i = 1; i <= n; i++) if (i+(1<<j)-1 <= n)
            low[i][j] = min(low[i][j-1], low[i+(1<<(j-1))][j-1]);
}
int query(int s, int e) {
    int k = log2(e-s+1);
    return min(low[s][k], low[e-(1<<k)+1][k]);
}
```

### 4.3 Trie\_v2

```
struct Trie{
    int next[26], cnt;
    void clear() {
        memset(next,0,sizeof(next));
    }
}trie[maxn];
int tot;
void insert(char *s)
{
    int cur = 1;
    for(int i = 0; s[i]; i++)
    {
        if(!trie[cur].next[s[i]-'a']) {
            trie[cur].next[s[i]-'a'] = ++tot;
            trie[tot].clear();
        }
        cur = trie[cur].next[s[i]-'a'];
    }
    trie[cur].cnt++;
}
int query(char *s) {
    int cur = 1;
    for (int i=0;s[i];i++) {
        if (trie[cur].next[s[i]-'a'])
            cur = trie[cur].next[s[i]-'a'];
        else
            return 0;
    }
    return trie[cur].cnt;
}
```

### 4.4 bit

```
struct bit {
    int s[maxn];
    int num;
    void add(int x, int z) {
        for (int i=x;i<=num;i+=(i&-i)) s[i]+=z;
    }
    int ask(int x) {
        int tmp=0;
        for (int i=x;i; i--=(i&-i)) tmp+=s[i];
        return tmp;
    }
    void clear(int n) {
        num=n;
        memset(s,0,sizeof(s));
    }
};
```

### 4.5 segtree\_v2

```
#define lson l, m, rt<<1
#define rson m+1, r, rt<<1|1
typedef long long ll;
const int maxn = 1e5+20;
using namespace std;
```

```

6 ll segsum[maxn<<2], lazy[maxn<<2];
7 void pushup(int rt) {
8     segsum[rt] = segsum[rt<<1] + segsum[rt<<1|1];
9 }
10 void build(int l, int r, int rt) {
11     if(l == r) {
12         scanf("%lld",&segsum[rt]);
13         return;
14     }
15     int m = (l+r)>>1;
16     build(lson); build(rson);
17     pushup(rt);
18 }
19 void pushdown(int rt, int m) {
20     lazy[rt<<1] += lazy[rt];
21     lazy[rt<<1|1] += lazy[rt];
22     segsum[rt<<1] += lazy[rt]*(m-(m>>1));
23     segsum[rt<<1|1] += lazy[rt]*(m>>1);
24     lazy[rt] = 0;
25 }
26 void update(int L, int R, int c, int l, int r, int rt) {
27     if(L <= l && r <= R) {
28         lazy[rt] += c;
29         segsum[rt] += (r - l + 1) * c;
30         return;
31     }
32     if(lazy[rt] != 0)
33         pushdown(rt, r - l + 1);
34     int m = (l + r) >> 1;
35     if(L <= m) update(L, R, c, lson);
36     if(R > m) update(L, R, c, rson);
37     pushup(rt);
38 }
39 ll querysum(int L, int R, int l, int r, int rt) {
40     if(L <= l && R >= r)
41         return segsum[rt];
42     if(lazy[rt] != 0)
43         pushdown(rt, r - l + 1);
44     int m = (l+r)>>1;
45     ll tmp = 0;
46     if(L <= m) tmp += querysum(L, R, lson);
47     if(R > m) tmp += querysum(L, R, rson);
48     return tmp;
49 }

```

## 5 Graph

### 5.1 Dijkstra

```

1  /*
2   * Dijkstra shortest path and minimal cost
3   */
4  #define maxn 1020
5  #define INF 0x7f7f7f7f
6  using namespace std;
7  typedef pair<int, int> PII;
8  struct Edge
9  //l 为边的长度， c为费用
10 {
11     int u, v, l, c;
12     Edge(){}
13     Edge(int u,int v, int l, int c):u(u),v(v),l(l),c(c){}
14 };
15 struct Node
16 //Node 用于 priority_queue 的记录
17 //v: node id
18 //l: length from start
19 //c: mincost
20 {
21     int v, l, c;
22     Node(){}
23     Node(int v, int l, int c):v(v),l(l),c(c){}
24     bool operator < (const Node &a) const
25     //priority_queue 的优先级和 < 相反
26     {
27         if(l == a.l) return c > a.c;
28         return l > a.l;
29     }
30 };
31 vector<Edge>G[maxn];
32 priority_queue<Node>pq;
33 int dist[maxn],cost[maxn],vis[maxn],tot;

```

```

void add_edge(int u, int v, int l, int c)
{
    G[u].push_back(Edge(u, v, l, c));
}
PII dijkstra(int s, int d)
//start s, dest d
{
    memset(dist, INF, sizeof(dist));
    memset(cost, INF, sizeof(cost));
    memset(vis, 0, sizeof(vis));
    while(!pq.empty()) pq.pop();
    pq.push(Node(s, 0, 0));
    while(!pq.empty())
    {
        const Node nd = pq.top();
        pq.pop();
        if(vis[nd.v]) continue;
        vis[nd.v] = true;
        dist[nd.v] = nd.l;
        cost[nd.v] = nd.c;
        if(nd.v == d) return make_pair(dist[d], cost[d]);
        for(int i = 0, len = G[nd.v].size(); i < len; i++)
        {
            Edge& e = G[nd.v][i];
            if(!vis[e.v])
            {
                pq.push(Node(e.v, nd.l + e.l, nd.c+e.c));
            }
        }
    }
    //dist[d]: shortest distance
    //cost[d]: mincost
    return make_pair(dist[d], cost[d]);
}

```

### 5.2 Dinic

```

#define ll long long
#define maxn 320
using namespace std;
int G[maxn][maxn], layer[maxn];
int m, n;
bool vis[maxn];
bool countLayer()
{
    queue<int>q;
    memset(layer, 0xff, sizeof(layer));
    layer[1] = 0;q.push(1);

    while(!q.empty())
    {
        int v = q.front();q.pop();
        for(int j = 1; j <= n; j++)
            if(G[v][j] > 0 && layer[j] == -1)
            {
                layer[j] = layer[v] + 1;
                if(j == n) return true;
                else q.push(j);
            }
    }
    return false;
}
int Dinic()
{
    int i;
    int maxflow = 0;
    deque<int> q;
    while(countLayer())
    {
        q.push_back(1);
        memset(vis, 0, sizeof(vis));
        vis[1] = true;
        while(!q.empty())
        {
            int nd = q.back();
            if(nd == n)
            {
                int minc = 1000000000;
                int minstart;
                for(i = 1; i < q.size();i++)
                {
                    int vs = q[i-1];
                    int ve = q[i];

```

```

47         if(G[vs][ve] > 0 && minc > G[vs][ve])
48         {
49             minc = G[vs][ve];
50             minstart = vs;
51         }
52     }
53     maxflow += minc;
54     for(i = 1; i < q.size(); i++)
55     {
56         int vs = q[i-1];
57         int ve = q[i];
58         G[vs][ve] -= minc;
59         G[ve][vs] += minc;
60     }
61     while(!q.empty() && q.back() != minstart)
62     {
63         vis[q.back()] = false;
64         q.pop_back();
65     }
66 }else{
67     for(i = 1; i <= n; i++)
68     if(G[nd][i] > 0 && layer[i] == layer[nd] + 1 && !vis[i])
69     {
70         vis[i] = true;
71         q.push_back(i);
72         break;
73     }
74     if(i > n) q.pop_back();
75 }
76 }
77 }
78 }
79 }
80 return maxflow;
81 }
82
83 int main()
84 {
85     while(scanf("%d%d", &m, &n) != EOF)
86     {
87         int s, e, c;
88         memset(G, 0, sizeof(G));
89         for(int i = 0; i < m; i++)
90         {
91             scanf("%d%d%d", &s, &e, &c);
92             G[s][e] += c;
93         }
94         printf("%d\n", Dinic());
95     }
96     return 0;
97 }

```

### 5.3 MaxFlowMinCost

```

1  const int maxn=120;
2  const int oo = 0x3f3f3f3f;
3  struct Edge
4  {
5      int u, v, cap, flow, cost;
6      Edge(int u, int v, int cap, int f, int cost):u(u), v(v),
7          cap(cap), flow(f), cost(cost) {}
8  };
9  struct MCMF
10 {
11     int n, m, s, t;
12     vector<Edge> edge;
13     vector<int> G[maxn];
14     int inq[maxn], d[maxn], p[maxn], a[maxn];
15     void init(int n)
16     {
17         this->n=n;
18         for(int i=0; i<=n; i++)G[i].clear();
19         edge.clear();
20     }
21     void AddEdge(int u, int v, int cap, int cost)
22     {
23         edge.push_back(Edge(u, v, cap, 0, cost));
24         edge.push_back(Edge(v, u, 0, 0, -cost));
25         m=edge.size();
26         G[u].push_back(m-2);
27         G[v].push_back(m-1);
28     }
29 }

```

```

bool SPFA(int s, int t, int& flow, int& cost)
{
    memset(d, 0x3f, sizeof d);
    memset(inq, 0, sizeof inq);
    d[s]=0, inq[s]=1, p[s]=0, a[s]=oo;

    queue<int> q;
    q.push(s);
    while(!q.empty())
    {
        int u=q.front();
        q.pop();
        inq[u]=0;
        for(int i=0; i<G[u].size(); i++)
        {
            Edge& e=edge[G[u][i]];
            if(e.cap>e.flow && d[e.v]>d[u]+e.cost)
            {
                d[e.v]=d[u]+e.cost;
                p[e.v]=G[u][i];
                a[e.v]=min(a[u], e.cap-e.flow);
                if(!inq[e.v])
                {
                    q.push(e.v);
                    inq[e.v]=true;
                }
            }
        }
    }
    if(d[t]==oo)return false;
    flow+=a[t];
    cost+=d[t]*a[t];
    int u=t;
    while(u!=s)
    {
        edge[p[u]].flow+=a[t];
        edge[p[u]^1].flow-=a[t];
        u=edge[p[u]].u;
    }
    return true;
}

int Mincost(int s, int t, int& cost)
{
    int flow=0;
    while(SPFA(s, t, flow, cost))
    ;
    return flow;
}

} net;

int ord[55][55], sto[55][55];
int main()
{
    int n, m, k;
    while(~scanf("%d%d%d", &n, &m, &k) && n+m+k)
    {
        for(int i=1; i<=n; i++)
            for(int j=1; j<=k; j++)
                scanf("%d", &ord[i][j]);
        for(int i=1; i<=m; i++)
            for(int j=1; j<=k; j++)
                scanf("%d", &sto[i][j]);
        int S=0, T=n+m+2;
        int cost=0;
        for(int p=1; p<=k; p++)
        {
            int sum=0;
            net.init(n+m+10);
            for(int i=1; i<=n; i++)
            {
                net.AddEdge(i, T, ord[i][p], 0);
                sum+=ord[i][p];
            }
            for(int i=1; i<=m; i++)
                net.AddEdge(S, i+n, sto[i][p], 0);
            for(int i=1; i<=n; i++)
                for(int j=1; j<=m; j++)
                {
                    int x;
                    scanf("%d", &x);
                    net.AddEdge(n+j, i, oo, x);
                }
            if(-cost && net.Mincost(S, T, cost)<sum)

```

```
111     cost=-1;
112 }
113 printf("%d\n", cost);
114 }
115 return 0;
116 }
```

### 5.4 floyed

```
1 const int maxn=110;
2 const int INF=10000000;
3 int dist[maxn][maxn], G[maxn][maxn];
4 int n, m, num, minc;
5 void floyd()
6 {
7     minc=INF;
8     // 求最小环
9     for(int k=1; k<=n; k++)
10     {
11         for(int i=1; i<k; i++)
12             for(int j=i+1; j<k; j++)
13             {
14                 int ans=dist[i][j]+G[i][k]+G[k][j];
15                 if(ans<minc) //找到最优解
16                 {
17                     minc=ans;
18                 }
19             }
20         for(int i=1; i<=n; i++)
21             for(int j=1; j<=n; j++)
22             {
23                 if(dist[i][j]>dist[i][k]+dist[k][j])
24                 {
25                     dist[i][j]=dist[i][k]+dist[k][j];
26                 }
27             }
28     }
29 }
```

### 5.5 hungary

```
1 #define __maxNodes 4020
2 using namespace std;
3 struct Edge
4 {
5     int from,to,weight;
6     Edge(int f, int t, int w):from(f), to(t), weight(w) {}
7 };
8 vector<Edge> G[__maxNodes]; /* G[i] 存储顶点 i 出发的边的
9 编号 */
10 int matching[__maxNodes]; /* 存储求解结果 */
11 int check[__maxNodes];
12 int n, m, sum;
13 /*DFS*/
14 bool dfs(int u)
15 {
16     for (int i = 0; i < G[u].size(); i++) {
17         int v = G[u][i].to;
18         if (!check[v]) { // 要求不在交替路中
19             check[v] = true; // 放入交替路
20             if (matching[v] == -1 || dfs(matching[v])) {
21                 // 如果是未盖点，说明交替路为增广路，则交换路径，
22                 // 并返回成功
23                 matching[v] = u;
24                 matching[u] = v;
25                 return true;
26             }
27         }
28     }
29     return false; // 不存在增广路，返回失败
30 }
31 int hungarian()
32 {
33     int ans = 0;
34     memset(matching, -1, sizeof(matching));
35     for (int u=1; u <= n; ++u) {
36         if (matching[u] == -1) {
37             memset(check, 0, sizeof(check));
38             if (dfs(u)) ++ans;
39         }
40     }
41 }
```

```
return ans;
}
```

### 5.6 kruskal

```
1 struct Edge
2 {
3     int u, v, c;
4     Edge(){}
5     Edge(int u, int v, int c):u(u),v(v),c(c){}
6     bool operator < (const Edge &e) const {
7         return c < e.c;
8     }
9 };
10 vector<Edge> ve;
11 int n, m;
12 int R[10020];
13 // dsj 1
14 int root(int x)
15 {
16     while(R[x] != x)
17         x = R[x] = R[R[x]];
18     return R[x];
19 }
20 // dsj 2
21 int root(int x)
22 {
23     if(R[x] == -1) return x;
24     if(R[x] != -1) R[x] = root(R[x]);
25     return R[x];
26 }
27 int main()
28 {
29     scanf("%d%d", &n, &m);
30     int u, v, c;
31     for (int i = 1; i <= m; i++)
32     {
33         scanf("%d%d%d", &u,&n,&c);
34         ve.push_back(Edge(u,n,c));
35     }
36     // for (int i = 1; i <= n; i++)
37     //     R[i] = i;
38     memset(R, -1, sizeof(R));
39     sort(ve.begin(), ve.end());
40     int ans = 0;
41     int Ru, Rv;
42     for (int i = 0, len = ve.size(); i < len; i++)
43     {
44         Edge &now = ve[i];
45         Ru = root(now.u);
46         Rv = root(now.v);
47         if(Ru != Rv)
48         {
49             ans += now.c;
50             R[Ru] = Rv;
51         }
52     }
53     printf("%d\n", ans);
54     return 0;
55 }
```

### 5.7 prim

```
1 struct Edge
2 {
3     int u, v, c;
4     Edge(){}
5     Edge(int u, int v, int c):u(u),v(v),c(c){}
6 };
7 vector<Edge> G[10020];
8 void addedge(int u, int v, int c)
9 {
10     G[u].push_back(Edge(u,v,c));
11     G[v].push_back(Edge(v,u,c));
12 }
13 int n, m;
14 int vis[10020];
15 int dist[10020];
16 int prim()
17 {
18     int ans = 0;
19     memset(vis, 0, sizeof(vis));
```



```

20 memset(dist, 0x3f, sizeof(dist));
21 vis[1] = 1;
22 int minid, minc;
23 int now = 1;
24 for (int t = 1; t < n; t++)
25 {
26     for (int i = 0, len = G[now].size(); i < len; i++)
27     {
28         int to = G[now][i].v, c = G[now][i].c;
29         if(vis[to] == 1) continue;
30         if(dist[to] > c)
31             dist[to] = c;
32     }
33     minid = -1;
34     minc = 0x3f3f3f3f;
35     for (int i = 1; i <= n; i++) if(!vis[i] && dist[i] <
        minc)
36     {
37         minid = i;
38         minc = dist[i];
39     }
40     ans += minc;
41     vis[minid] = 1;
42     now = minid;
43 }
44 return ans;
45 }
46
47 int main()
48 {
49     scanf("%d%d", &n, &m);
50     int u,v,c;
51     for (int i = 0; i < m; i++)
52     {
53         scanf("%d%d%d", &u,&v,&c);
54         addedge(u,v,c);
55     }
56     printf("%d\n" ,prim());
57     return 0;
58 }

```

```

        //dfn[i] not low[i];
        low[u] = min(low[u], dfn[to]);
    }
}
if (dfn[u] == low[u])
{
    strongcnt++;
    do
    {
        to = stk[top-];
        instack[to] = false;
        belong[to] = strongcnt;
        strongsize[strongcnt]++;
    } while (to != u);
}
}
int main()
{
    for (int i = 1; i <= n; ++i)
    {
        if (!dfn[i])
        {
            tarjan(i);
        }
    }
    int to;
    for(int i = 1; i <= n; i++)
    {
        for (int j = 0; j < v[i].size(); ++j)
        {
            to = v[i][j];
            if(belong[i] != belong[to]){
                outde[belong[i]]++;
                inde[belong[to]]++;
            }
        }
    }
    return 0;
}

```

## 5.8 tarjan

```

1  #define maxn 100020
2  using namespace std;
3  vector<int>v[maxn];
4  bool instack[maxn];
5  int dfn[maxn], low[maxn];
6  int n, m;
7  int depth, strongcnt;
8  int belong[maxn], strongsize[maxn];
9  int stk[maxn], top;
10 int inde[maxn], outde[maxn];
11
12 void clear(){
13     memset(dfn, 0, sizeof(dfn));
14     memset(low, 0, sizeof(low));
15     memset(instack, 0, sizeof(instack));
16     memset(belong, 0, sizeof(belong));
17     memset(strongsize, 0, sizeof(strongsize));
18     memset(inde, 0, sizeof(inde));
19     memset(outde, 0, sizeof(outde));
20     depth = 0;
21     strongcnt = 0;
22     for (int i = 1; i <= n; ++i)
23     {
24         v[i].clear();
25     }
26 }
27
28 void tarjan(int u){
29     dfn[u] = low[u] = ++depth;
30     instack[u] = true;
31     stk[++top] = u;
32     int to;
33     for (int i = 0; i < v[u].size(); ++i)
34     {
35         to = v[u][i];
36         if(!dfn[to]){
37             tarjan(to);
38             low[u] = min(low[to], low[u]);
39         }else if (instack[to])
40         {

```

## 6 ToolsTricks

### 6.1 ConvexHullTrick

```

/*
 * The ConvexHull Trick
 * CF 244 div2 E
 * 斜率需要按升序排序
 * 求对应 x 的最大的 y 值
 * nlogn
 */
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
struct Line
{
    ll a, b;
    ll cal(ll x) { return a*x+b; }
    Line(ll a, ll b):a(a),b(b){}
    Line(){}
};
struct ConvexHull
{
    int size;
    Line *hull;
    ConvexHull(int maxsize)
    {
        hull = new Line[++maxsize], size = 0;
    }
    bool isbad(ll cur, ll pre, ll ne)
    {
        Line c = hull[cur], p = hull[pre], n = hull[ne];
        return (c.b - n.b) * (c.a - p.a) <= (p.b - c.b) * (n.a
            - c.a);
    }
    void addLine(ll a, ll b)
    {
        hull[size++] = Line(a,b);
        while (size > 2 && isbad(size - 2, size - 3, size - 1)
        )

```

```
36     hull[size-2] = hull[size-1], size--;
37 }
38 ll query(ll x)
39 {
40     int l = -1, r = size - 1;
41     while (r - l > 1)
42     {
43         int m = (l + r) / 2;
44         if (hull[m].cal(x) <= hull[m+1].cal(x))
45             l = m;
46         else
47             r = m;
48     }
49     return hull[r].cal(x);
50 }
51 };
52
53 int const maxn = (int)2e5+1;
54 int n, a[maxn];
55 ll sum[maxn], ans, dans;
56
57 int main()
58 {
59     scanf("%d", &n);
60     ConvexHull ch = ConvexHull(n);
61     sum[0] = 0;
62     for (int i = 1; i <= n; i++)
63     {
64         scanf("%d", &a[i]);
65         sum[i] = sum[i-1] + a[i];
66         ans += (ll)a[i] * i;
67     }
68     ch.size = 0;
69     for (int r = 2; r <= n; r++)
70     {
71         ch.addLine(r-1, -sum[r-2]);
72         dans = max(dans, ch.query(a[r]) + sum[r-1]-(ll)a[r]*r)
73         ;
74     }
75     ch.size = 0;
76     for (int l = n - 1; l >= 1; l--)
77     {
78         ch.addLine(-(l+1), -sum[l+1]);
79         dans = max(dans, ch.query(-a[l]) + sum[l] - (ll)a[l]*1
80         );
81     }
82     printf("%I64d\n", ans + dans);
83     return 0;
84 }
```

## 6.2 cantor

```
1  /*
2   * 康拓展开
3   * 元素个数 len
4   * 元素0-9
5   * 0-based count
6   * last edit : 2015/9/25
7   */
8  int fact[10] = {1,1,2,6,24,120,720,5040,40320,362880};
9  int cantor(int* a,int len)
10 {
11     int ret = 0;
12     for(int i = 0; i < len; i++)
13     {
14         int tmp = 0;
15         for(int j = i+1; j < len; j++)if(a[i] > a[j]) tmp++;
16         ret += tmp * fact[len-i-1];
17     }
18     return ret;
19 }
20
21 void cantorrev(int* a,int d, int len)
22 {
23     int vis[10] = {0}, tmp, tt;
24     for(int i = 0; i < len; i++)
25     {
26         tmp = d / fact[len-i-1];
27         d %= fact[len-i-1];
28         //the min
29         tt = 0;
30         while(tmp || vis[tt])
31         {
```

```
        if(vis[tt] == 0)
            tmp--;
            tt++;
        }
        vis[tt] = 1;
        a[i] = tt;
    }
}
```

## 6.3 merge\_sort\_reverse

```
int arr[1000200], tarr[1000200];
int cnt;
void merge(int low, int mid, int high)
{
    int i, j, k;
    for (i = low, j = mid + 1, k = 0; i <= mid && j <= high
    ;)
    {
        if(arr[i] < arr[j])
            tarr[k++] = arr[i++];
        else
        {
            tarr[k++] = arr[j++];
            cnt += mid - i + 1;
        }
    }
    while(i <= mid) tarr[k++] = arr[i++];
    while(j <= high) tarr[k++] = arr[j++];

    for (k = 0; low <= high; low++, k++)
        arr[low] = tarr[k];
}
void mergesort(int low, int high)
{
    if(low == high) return;
    int mid = (low + high) / 2;
    mergesort(low, mid);
    mergesort(mid + 1, high);
    merge(low, mid, high);
}
int main()
{
    int n;
    scanf("%d", &n);
    for (int i = 0; i < n; i++)
        scanf("%d", &arr[i]);
    cnt = 0;
    mergesort(0, n-1);
    printf("%d\n", cnt);
    return 0;
}
```

## 6.4 stl

```
/*
 * bool next_permutation(a, a + n);
 * true: has next permutation and
 * change a[n] into the next permutation
 * false: the a[n] now is the last permutation
 */

//sample code:
sort(a, a + len);
do {
    for (int i = 0; i < len; i++)
        cout << a[i];
    cout << endl;
} while(next_permutation(a, a + len));
```

## 7 Game

### 7.1 Wythoff

```
//Wythoff Game
//A first
//B second
//当 n 过大时需要用高精度处理，和精确的黄金比例数
int main()
{
    int T;
```

```
8   scanf("%d", &T);
9   while(T--)
10  {
11      int a, b;
12      scanf("%d%d", &a, &b);
13      if(a > b) swap(a, b);
14
15      int k = b - a;
16      if(a == (int)((k)*(1+sqrt(5.0))/2.0)) cout << "B" << endl;
17      else cout << "A" << endl;
18  }
19  return 0;
20 }
```

## 8 BigInt

### 8.1 Java

```
1  /*
2  //将r进制保存的 string 转化为10进制的数
3  Integer.parseInt(String, radian);
4
5  //将10进制的数转化为对应进制的字符串
6  Integer.toBinaryString(n);
7  Integer.toOctalString(n);
8  Integer.toHexString(n);
9  */
10
11 import java.io.OutputStream;
12 import java.io.IOException;
13 import java.io.InputStream;
14 import java.io.PrintWriter;
15 import java.util.StringTokenizer;
16 import java.io.IOException;
17 import java.io.BufferedReader;
18 import java.io.InputStreamReader;
19 import java.io.InputStream;
20
21 /**
22  * Built using CHelper plug-in
23  * Actual solution is at the top
24  */
25 public class Main {
26     public static void main(String[] args) {
27         InputStream inputStream = System.in;
28         OutputStream outputStream = System.out;
29         InputReader in = new InputReader(inputStream);
30         PrintWriter out = new PrintWriter(outputStream);
31         TaskA solver = new TaskA();
32         solver.solve(1, in, out);
33         out.close();
34     }
35
36     static class TaskA {
37     public void solve(int testNumber, InputReader in,
38         PrintWriter out) {
39         int n = in.nextInt();
40         int l = in.nextInt();
41         int v1 = in.nextInt();
42         int v2 = in.nextInt();
43         int k = in.nextInt();
44         double gain = 1.0 / v1 - 1.0 / v2;
45         double together = 1.0 / (v1 + v2);
46         double left = 0;
47         double right = 1 / (double) v1;
48         while (right - left > 1e-7 * Math.max(1.0,
49             right)) {
50             double middle = (left + right) / 2;
51             double needBus = (1 / (double) v1 - middle
52                 ) / gain;
53             double time = 0;
54             for (int first = 0; first < n; first += k)
55             {
56                 if (first + k < n)
57                     time += 2 * needBus * together;
58                 else
59                     time += needBus / v2;
60             }
61             if (time <= middle) {
62                 right = middle;
63             } else {
64                 left = middle;
65             }
66             out.println((left + right) / 2);
67         }
68     }
69
70     static class InputReader {
71     public BufferedReader reader;
72     public StringTokenizer tokenizer;
73
74     public InputReader(InputStream stream) {
75         reader = new BufferedReader(new
76             InputStreamReader(stream), 32768);
77         tokenizer = null;
78     }
79
80     public String next() {
81         while (tokenizer == null || !tokenizer.
82             hasMoreTokens()) {
83             try {
84                 tokenizer = new StringTokenizer(reader
85                     .readLine());
86             } catch (IOException e) {
87                 throw new RuntimeException(e);
88             }
89         }
90         return tokenizer.nextToken();
91     }
92
93     public int nextInt() {
94         return Integer.parseInt(next());
95     }
96     }
97 }
```

```
60
61
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90
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92
93
```