

Homework Quiz 7

Due 10 Nov at 6:00	Points 180	Questions 18
Available 3 Nov at 6:00 - 10 Nov at 6:00	Time limit None	

This quiz was locked 10 Nov at 6:00.

Attempt history

	Attempt	Time	Score
LATEST	Attempt 1	5,807 minutes	170 out of 180

Score for this quiz: **170** out of 180
Submitted 9 Nov at 1:30
This attempt took 5,807 minutes.

Correct!

Question 1

10 / 10 pts

If the columns of an $n \times n$ matrix A are linearly independent, then the columns of A span \mathbb{R}^n .

☒ True

☐ False

Question 2

10 / 10 pts

If the equation $Ax = b$ has at least one solution for each b in \mathbb{R}^n , then the solution is unique for each b .

Note: The matrix A is $n \times n$.

Correct!

☒ True

☐ False

Question 3

10 / 10 pts

If the linear transformation $x \rightarrow Ax$ maps \mathbb{R}^n to \mathbb{R}^n , then A always has n pivot positions.

Note: The matrix A is $n \times n$.

☐ True

Correct!

☒ False

Question 4

10 / 10 pts

If there is a b in \mathbb{R}^n such that the equation $Ax = b$ is inconsistent (i.e. has no solution), then the transformation $x \rightarrow Ax$ is not one-to-one.

Note: The matrix A is $n \times n$.

☒ True

Correct!

☐ False

Question 5

10 / 10 pts

The inverse of the matrix: $\begin{bmatrix} 4 & 3 \\ 7 & 5 \end{bmatrix}$

is $\begin{bmatrix} -5 & x \\ 7 & -4 \end{bmatrix}$

What is x ?

(Write your answer as an integer, no spaces or decimals.)

Correct!

Correct Answers

3

Question 6

10 / 10 pts

The inverse of the matrix: $\begin{bmatrix} 1 & -1 & 2 \\ 2 & -1 & 0 \\ 3 & 0 & -5 \end{bmatrix}$

is: $\begin{bmatrix} 5 & -5 & 2 \\ 10 & -11 & 4 \\ 3 & -3 & x \end{bmatrix}$

What is x ?

(Write your answer as an integer. No spaces or decimals.)

Correct!

Correct Answers

1

Question 7**10 / 10 pts**

A product of invertible $n \times n$ matrices is invertible, and the inverse of the product is the product of their inverses in the same order.

☐ True☒ False**Correct!****Question 8****10 / 10 pts**

If a matrix A is invertible, then the inverse of A^{-1} is A itself.

☒ True☐ False**Correct!****Question 9****10 / 10 pts**

If $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ and $ad = bc$, then A is invertible.

☐ True☒ False**Correct!****Question 10****10 / 10 pts**

If a matrix A can be row reduced to the identity matrix, then A must be invertible.

Correct!

☒ True

☐ False

Question 11

0 / 10 pts

If a matrix A is invertible, then the same elementary row operations that reduce A to the identity I also reduce A^{-1} to I .

You Answered

☒ True

Correct answer

☐ False

See Theorem 7

Question 12

10 / 10 pts

Suppose A , B , and C are invertible $n \times n$ matrices and $C^{-1}(A + X)B^{-1} = I$.

What is X ?

☐ $X = C^{-1}X^{-1} - A$

Correct!

☒ $X = CB - A$

☐ $X = B^{-1}C^{-1} - A$

☐ $X = BC - A$

☐ This equation does not have a solution for X .

Question 13

10 / 10 pts

Which of the following are invertible?

(You should first determine if they are invertible by hand--and find the inverse where applicable. You can check your work with MATLAB.)

☐ $\begin{bmatrix} 1 & -2 & -4 \\ 0 & 3 & 6 \end{bmatrix}$

Correct!

☒ $\begin{bmatrix} 1 & 6 & 1 & 4 \\ 0 & 1 & 2 & 3 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 1 \end{bmatrix}$

Correct!

☒ $\begin{bmatrix} -2 & 2 \\ -5 & 4 \end{bmatrix}$

☐ $\begin{bmatrix} 0 & 2 & 8 \\ 0 & 1 & -1 \\ 0 & 3 & 7 \end{bmatrix}$

Question 14

10 / 10 pts

If there is an $n \times n$ matrix D such that $AD = I$, then $DA = I$.

Note: The matrix A is $n \times n$.

Correct!

☒ True

☐ False

Question 15

10 / 10 pts

In order for the linear system, $A\mathbf{x} = \mathbf{b}$ to have a solution, the vector \mathbf{b} must be in the null space.

☐ True

☒ False

Correct!

Question 16

10 / 10 pts

The difference between a set of vectors spanning a subspace in \mathbb{R}^n , and a basis for the same subspace in \mathbb{R}^n , is

☐ a basis will always contain more vectors than the span.

☐ There is no difference between a span and a basis.

☒ a basis will always contain linearly independent vectors.

☐ a basis will contain the zero vector, a span will not.

Correct!

Question 17

10 / 10 pts

Which one of the following is true for a matrix A having column vectors

$\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3, \mathbf{v}_4, \mathbf{v}_5$ and row echelon form

$$\begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

Correct!

☒ $\mathbf{v}_1, \mathbf{v}_3$, and \mathbf{v}_5 form a basis for the column space of A.

☐ $\mathbf{v}_1, \mathbf{v}_3$, and \mathbf{v}_4 form a basis for the column space of A.

☐ $\mathbf{v}_1, \mathbf{v}_2$, and \mathbf{v}_4 form a basis for the column space of A.

☐ Cannot be determined without knowing the entries of A

☐ $\mathbf{v}_2, \mathbf{v}_3$, and \mathbf{v}_4 form a basis for the column space of A.

Question 18

10 / 10 pts

Does the vector $\begin{bmatrix} 2 \\ 4 \\ 1 \end{bmatrix}$ belong to the null space of the matrix

$$\begin{bmatrix} -2 & 3 & -8 \\ -3 & -3 & 18 \end{bmatrix}$$

Correct!

☒ Yes

☐ No

Quiz score: **170** out of 180