

Tutorial 2.

Solution 1:

i	j	No. of times loop is running be K .
0	1	$S_K = 1+3+6+10+\dots+T_K$
1	2	
3	3	$S_{K-1} = 1+3+6+\dots+T_{K-1}$
6	4	subtracting both
10	5	
		$S_K - S_{K-1} = 1+2+3+4+\dots+(K-1)$
		$T_K = (K-1)K/2$.

Given that K^{th} term is n .

$$T_K = n$$

$$K(K-1)/2 = n \Rightarrow K^2/2 - K/2 = n \quad \text{ignoring lower order terms and constants.}$$

$$\Rightarrow K^2 = n$$

$$K = \lceil \sqrt{n} \rceil$$

$$T(n) = O(\lceil \sqrt{n} \rceil)$$

=

Solution 2:

$$T(n) = T(n-1) + T(n-2) + O(1)$$

For recursive fibonaci solution

No. of times function is running will be sum of the series.

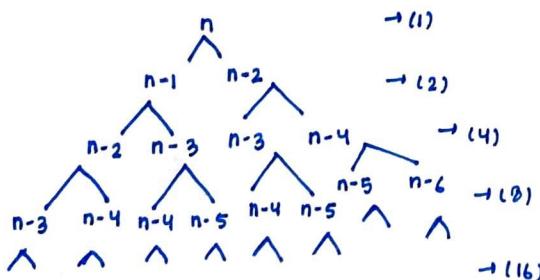
$$S = 1+2+4+\dots+2^n$$

$$= 2^{n+1} - 1 / 2 - 1 = 2^{n+1} - 1$$

Time complexity

$$T(n) = O(2^n)$$

after removing constants



$$\underline{\text{solution 4:}} \quad T(n) = T(n/4) + T(n/2) + cn^2$$

Ignoring lower order terms:

$$T(n) = T(n/2) + cn^2$$

Using Master Theorem:

$$a=1, b=2 \quad \rightarrow f(n) = n^2$$

$$c = \frac{\log a}{\log b} = \frac{\log 1}{\log 2} = 0$$

$$\boxed{0 < n^2} \quad \text{true.}$$

$$\Rightarrow \boxed{T(n) = O(n^2)} =$$

Solution 3: code having time complexity

$O(n \log n) =$

```
for (int i=1; i<=n; i++)  
    for (int j=1; j<n; j=j*2)  
        printf ("Hello");
```

$O(n^3) :$

```
for (int i=0; i<n; i++)  
    for (int j=0; j<n; j++)  
        for (int k=0; k<n; k++)  
            printf ("Hello");
```

$O(\log(\log n)) :$

```
for (int i=2; i<n; i=pow(i,3))  
    printf ("Hello");
```

Solution 5:

i	j	Time complexity will be sum of series
1	n	$S = n/1 + n/2 + n/3 + \dots$
2	$n/2$	$= \sum_{i=1}^n (n/i)$
3	$n/3$	
4	$n/4$	Complexity = $n \times \sum_{i=1}^n (n/i)$
⋮	⋮	$\boxed{T(n) = n \log n} =$