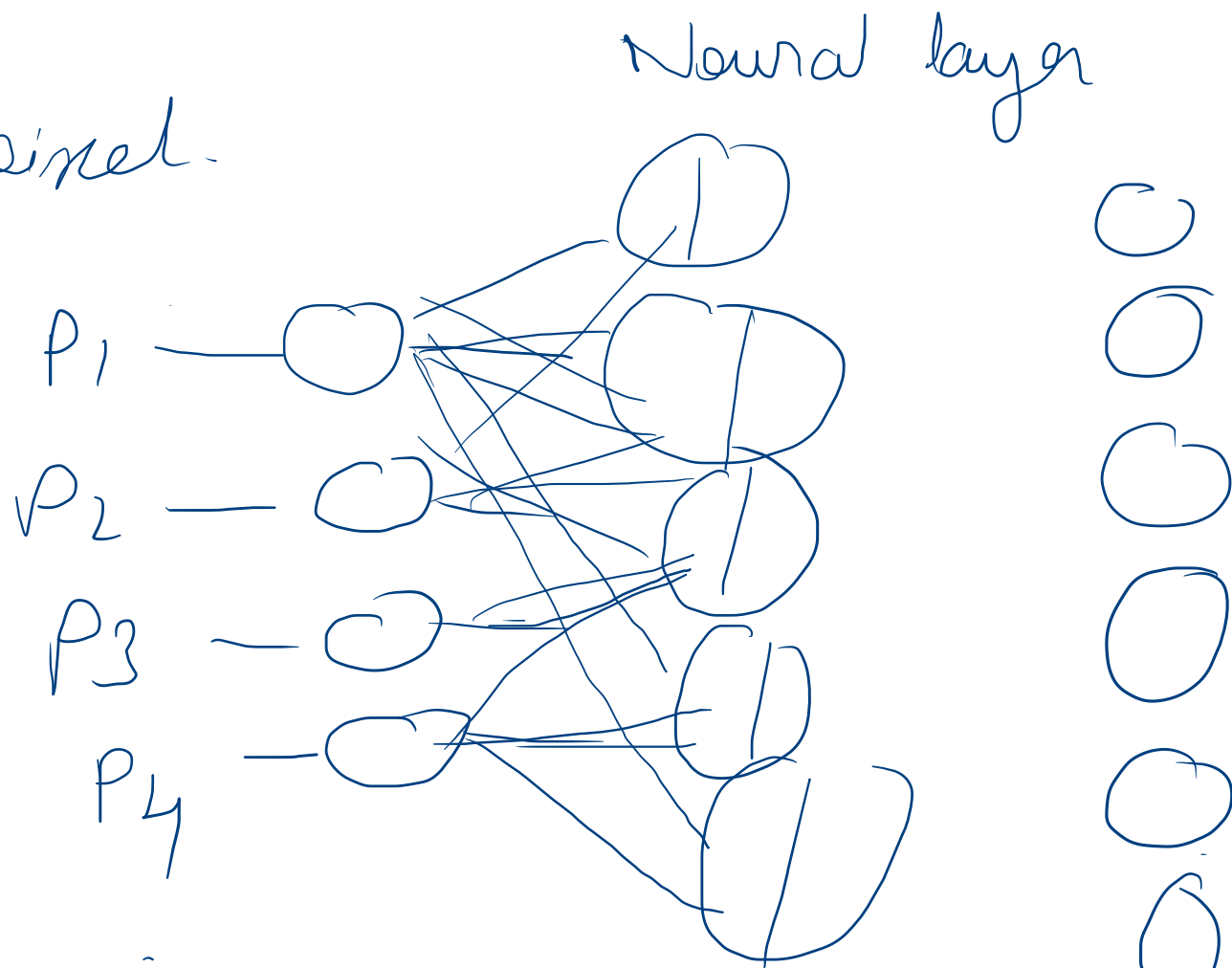
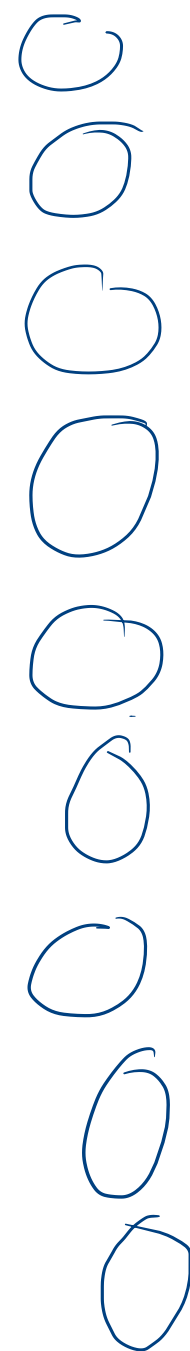


① $2 \times 2 = 4$ pixel.

$$\begin{array}{|c|c|} \hline P_1 & P_2 \\ \hline P_3 & P_4 \\ \hline \end{array}$$

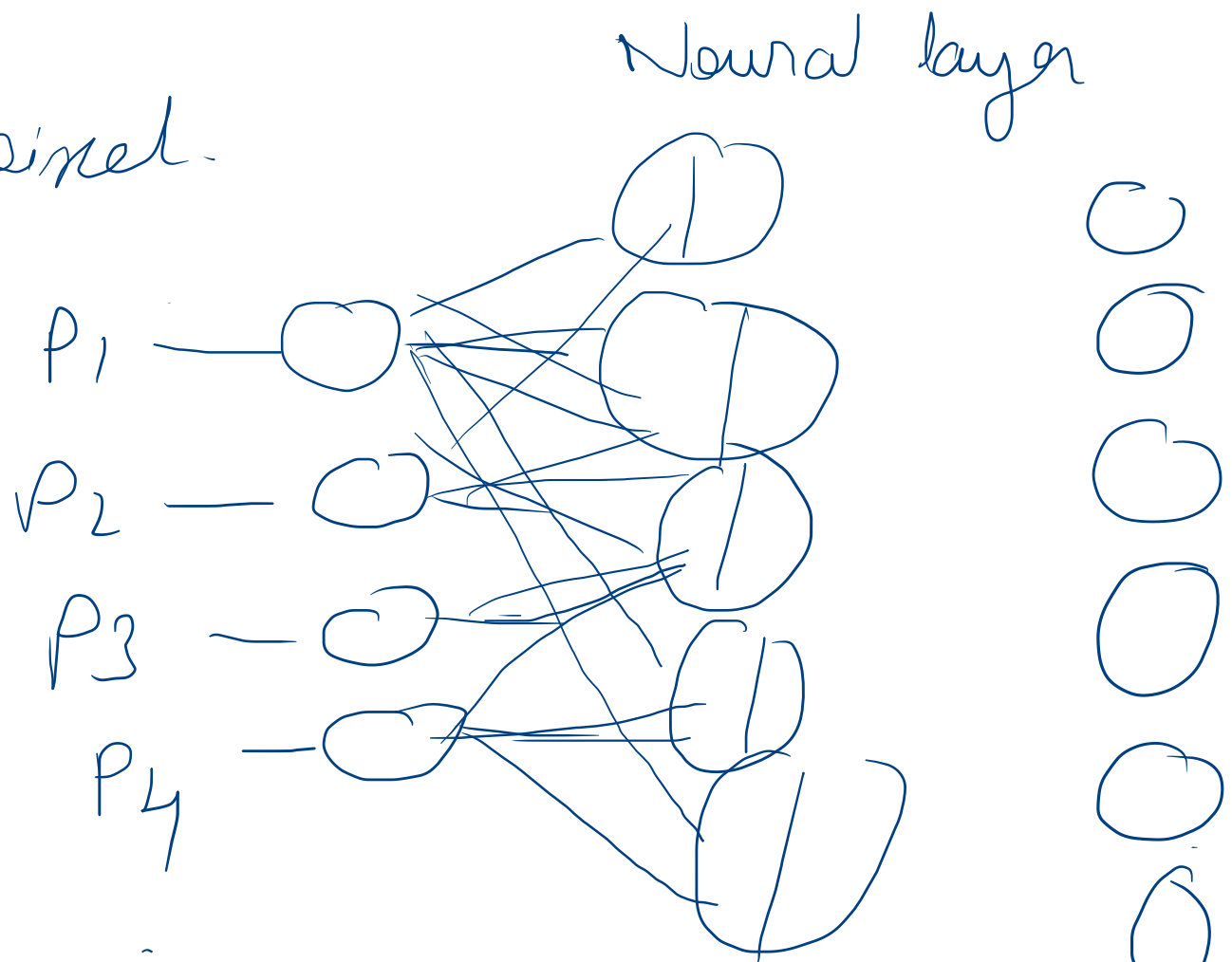


Input layer will have neurons
in same number as number of
features in dataset.

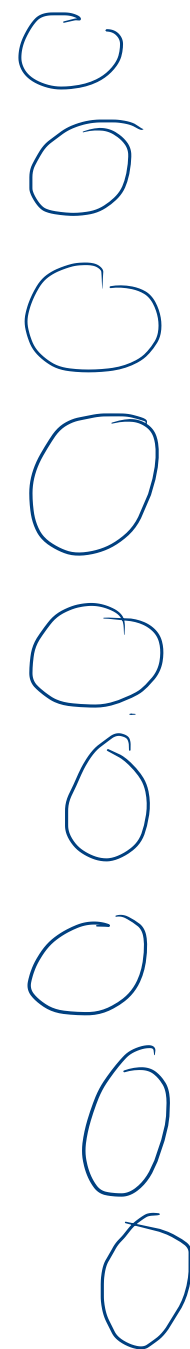


① $2 \times 2 = 4$ pixel.

$$\begin{array}{|c|c|} \hline P_1 & P_2 \\ \hline P_3 & P_4 \\ \hline \end{array}$$



Input layer will have neurons
in same number as number of
features in dataset.

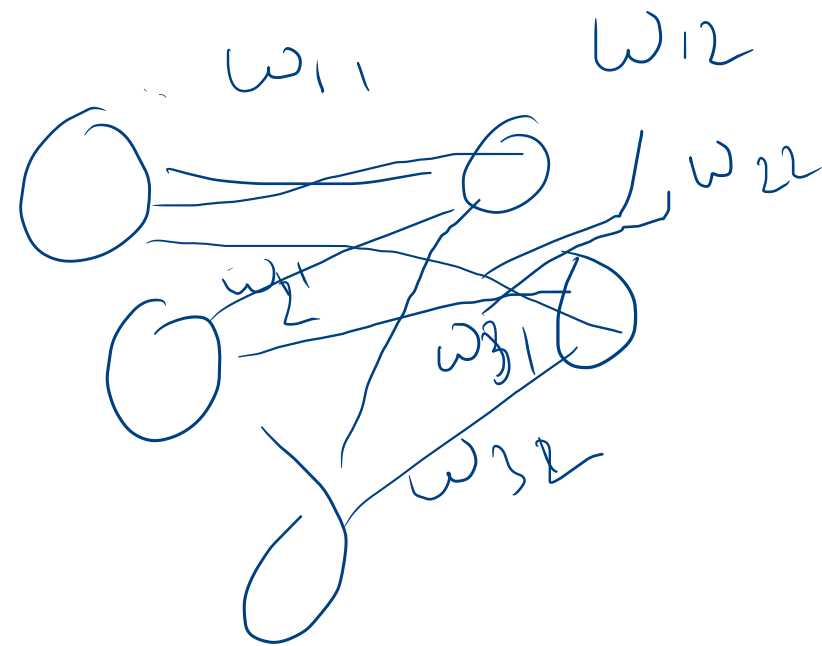
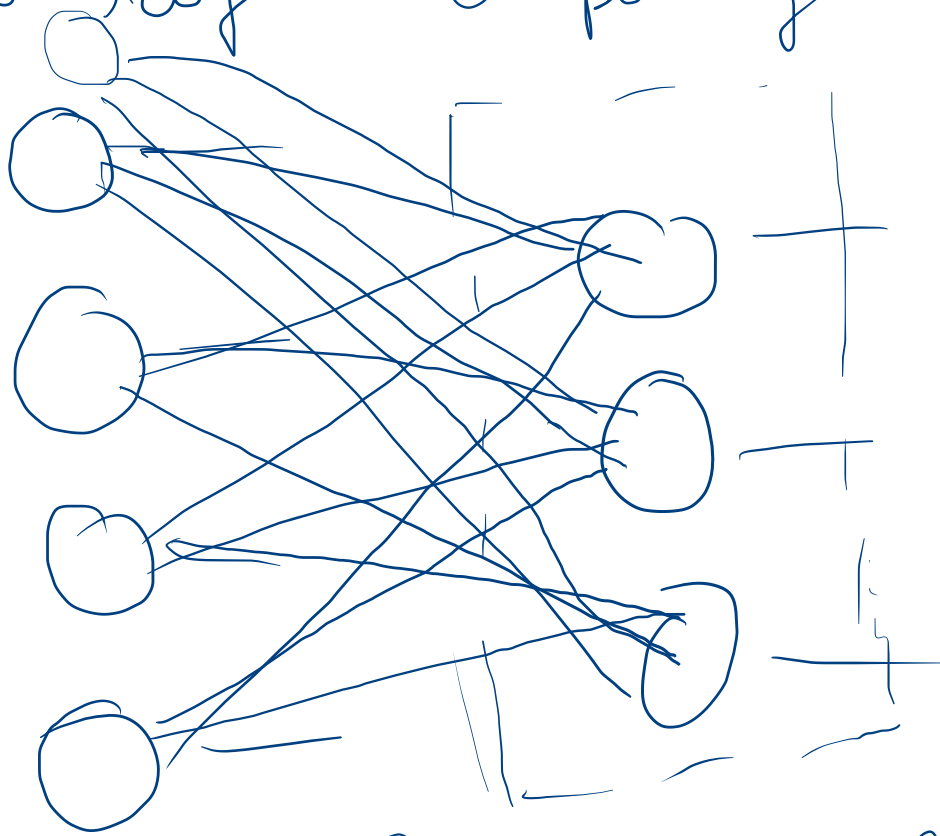


iris = input parameters (4)

Perceptron

output class (3)

Input layer output layer



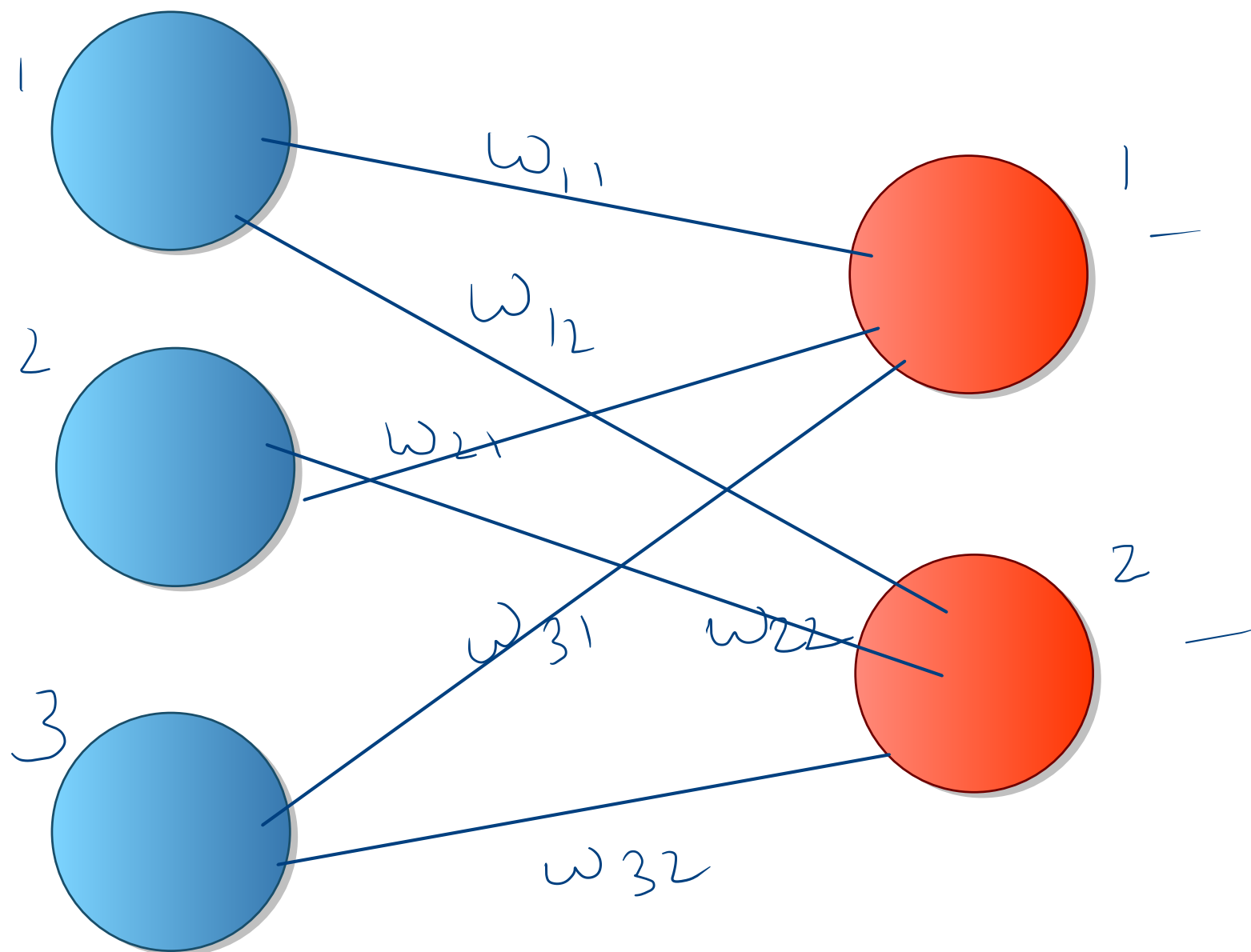
Perceptron model

random
1 →
2
3

150

for instance

2)



~

$$\theta_{\text{next step}} = \theta - \eta \nabla_{\theta} \text{MSE}(\theta)$$

$$y = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_3$$

Vector = $y = \underline{\underline{\theta^T}} X$

$$\theta^T = \begin{bmatrix} \theta_0 \\ \theta_1 \\ \theta_2 \\ \vdots \\ \theta_n \end{bmatrix}$$

$$X = \begin{bmatrix} 1, x_1, x_2, \dots, x_n \end{bmatrix}$$

$$\theta_0 \times 1 + \theta_1 x_1 + \theta_2 x_2 + \dots + \theta_n x_n$$

$$\theta_{\text{next step}} = \theta - \eta \nabla_{\theta} \text{MSE}(\theta)$$

$$y = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_3$$

Vector = $y = \underline{\underline{\theta^T}} X$

$$\theta^T = \begin{bmatrix} \theta_0 \\ \theta_1 \\ \theta_2 \\ \vdots \\ \theta_n \end{bmatrix} \quad X = \begin{bmatrix} 1, x_1, x_2, \dots, x_n \end{bmatrix}$$

$$\theta_0 \times 1 + \theta_1 x_1 + \theta_2 x_2 + \dots + \theta_n x_n$$

$$\hat{\theta} = (X^T \cdot X)^{-1} \cdot X^T \cdot y$$

best fit

To solve this equation how much time is req. is governed by $(X^T \cdot X)^{-1}$ size of matrix. = y ~~* is~~ have n feature Data

The Time / Computational complexity =

$O(n^{2.4})$ or $O(n^3)$

If I double the number of pages
then time taken be 8 times.

For eg: $1 = \text{time} \cdot 0.1 \text{ sec}$

$$2 = 0.1 \times 8 = 0.8$$

$$4 = 0.8 \times 8 = 6.4$$

$$8 = 6.4 \times 8 = 51.2$$

$$16 = 51.2 \times 8 = 409.6$$

Method called gradient descent. $Q_i = 1$

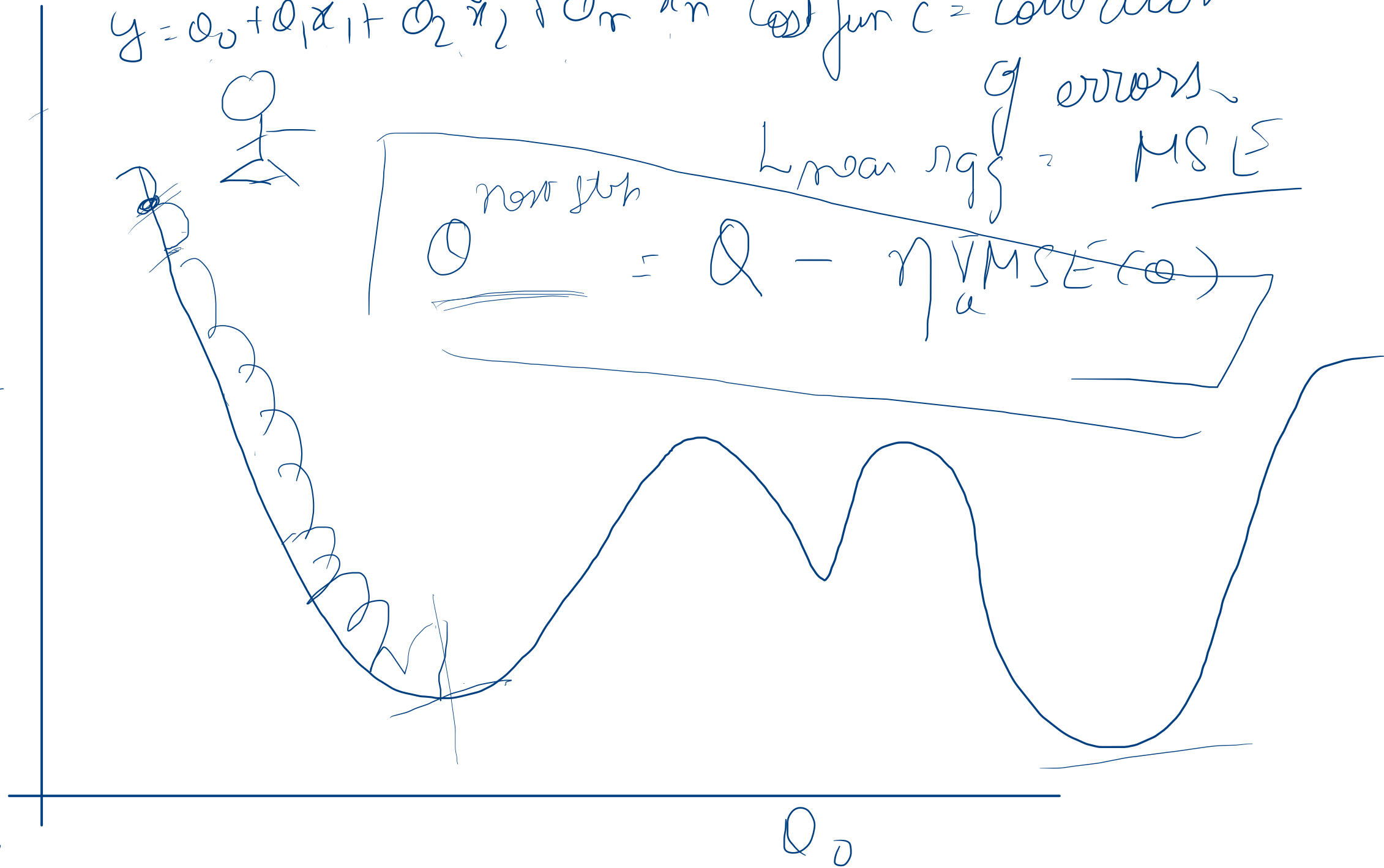
$y = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \dots + \theta_n x_n$ Cost fun $C =$ collection of errors

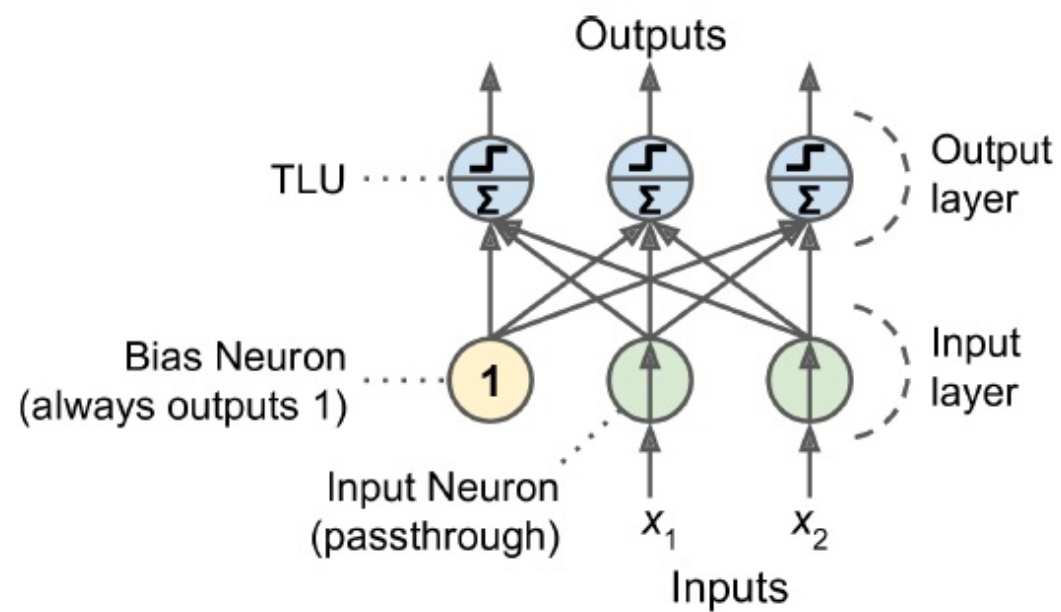
Linear reg \rightarrow MSE

new step

$$\underline{\underline{\theta}} = \underline{\underline{\theta}} - \eta \nabla_{\underline{\underline{\theta}}} \text{MSE}(\underline{\underline{\theta}})$$

Cost function





$$w_{i,j}^{(\text{next step})} = w_{i,j} + \eta(y_j - \hat{y}_j)x_i$$

- $w_{i,j}$ is the connection weight between the i^{th} input neuron and the j^{th} output neuron.
- x_i is the i^{th} input value of the current training instance.
- \hat{y}_j is the output of the j^{th} output neuron for the current training instance.
- y_j is the target output of the j^{th} output neuron for the current training instance.
- η is the learning rate.

The decision boundary of each output neuron is linear, so Perceptrons are incapable of learning complex patterns (just like Logistic Regression classifiers). However, if the training instances are linearly separable, Rosenblatt demonstrated that this algorithm would converge to a solution.⁷ This is called the *Perceptron convergence theorem*.

Scikit-Learn provides a `Perceptron` class that implements a single TLU network. It can be used pretty much as you would expect—for example, on the iris dataset (introduced in [Chapter 4](#)):

