

AVL Trees

AVL Tree is the perfectly balanced Binary Search Tree (BST). AVL is named after its two Soviet inventors, Georgy Adelson-Velsky & Evgenii Landis. If we have a BST and the nodes are in ascending / descending order the time complexity of searching / deletion will be $O(h)$ and if it is imbalance from left or right [left-heavy / Right-heavy], to make this more optimize we check balance factor [height of left sub tree - height of right sub tree] and if it is equal to $[-1, 0, 1]$ the tree is balanced if BF does not lies in that range Tree is imbalance to make tree balance we perform rotations.

→ Operations:

- (i) Insertion: The insertion in AVL Trees is same as BST compare data with root if greater insert in right if less insert in left.
- (ii) and after every insertion check BF if the node became imbalance perform rotation on critical node.
- The duplicates are not allowed in AVL Trees.

Deletion: The deletion in AVL Trees is also same as BST there are 3 cases:

Case 1:

Deleting leaf node: To delete a leaf node we make it null and check BF if it is imbalance perform rotation.

Case 2:

Possibility - I: Deleting node have only left child, we link left child to the parent of deleting node.

Possibility - II: Deleting node have right child, we link right child to parent of deleting node.

Case 3: The deleting node has both children then we find the inorder predecessor or ~~inorder~~ inorder successor of the deleting node and link it with parent of deleting node.

In last we check BF for performing rotation.

Rotation:

The rotation in AVL Trees is performed when any nodes of tree become imbalance which is checked by balance factor of every node. There are four rotations and rotations are performed on three nodes only:

1. LL (Left to Left) Rotation:

The LL Rotation is performed when any node is inserted in (left sub tree's left) or deleted that affect the height of the tree.

2. RR (Right to Right) Rotation:

The RR Rotation is performed when any node is inserted in (right sub tree's right) or deleted that affect the height of the tree.

For LL and RR Rotation:

We make a single rotation in LL and RR Rotation. In LL Rotation we rotate the nodes to the right and in RR Rotation we rotate to left. In LL Rotation middle node will be the root and upper node will be the right sub tree and lower will be left sub tree and in RR Rotation middle node will be the root and upper

node will be the left sub tree and lower will be right sub tree.

3- LR (Left to Right) Rotation:

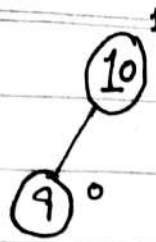
The LR Rotation is performed when any node is inserted in (right of left sub tree) or deleted that affects the height of the tree.

4- RL (Right to left) Rotation:

The RL Rotation is performed when any node is inserted in (left of right sub tree) or deleted that affects the height of the tree.

For LR and RL Rotation:

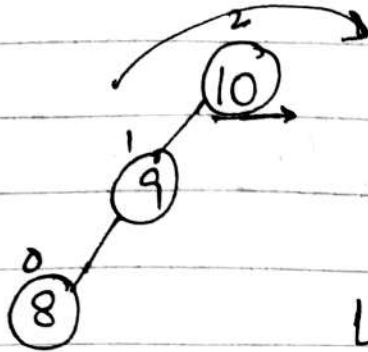
We make double rotations for LR ~~and~~ we perform right rotation first then left rotation and in RL rotation we perform left rotation first then right rotation.



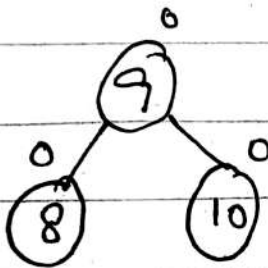
→ Binary Search Tree / AVL Tree

Balance Factor 0, 1.

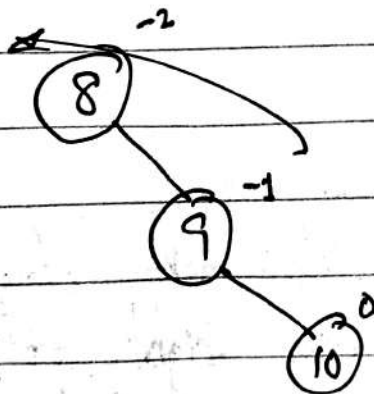
8 → inserting.



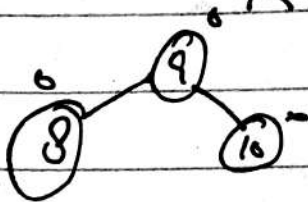
10 is critical node cause
BF is 2 we inserted in
left of left Sub-Tree
LL Rotation.



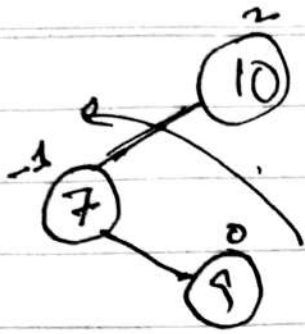
Tree Balanced.



RR Rotation.

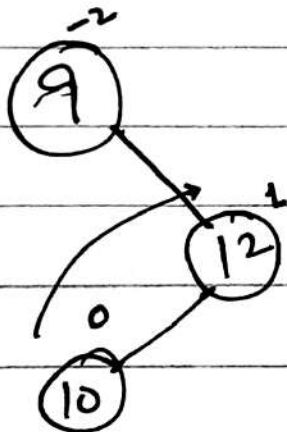
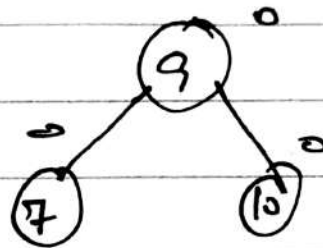
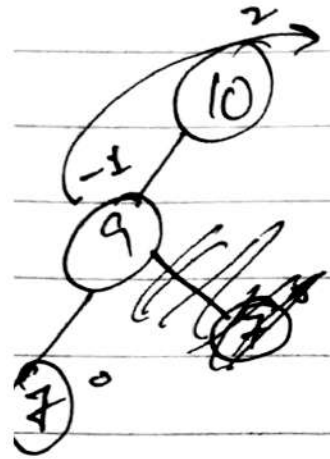


Balanced

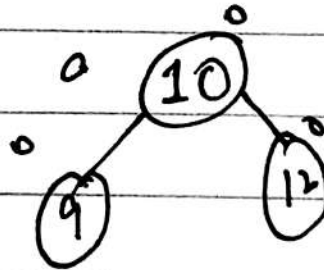
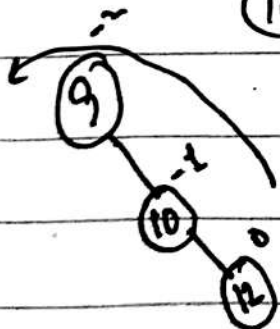


Inserted in Right of left Sub Tree.
Perform LR Rotation.

→ Double Rotation



Inserted in Right's left.
Perform RL Rotation
→ Double Rotation



Height Balanced.

AVLTreeImplementation.java - DSA - Visual Studio Code

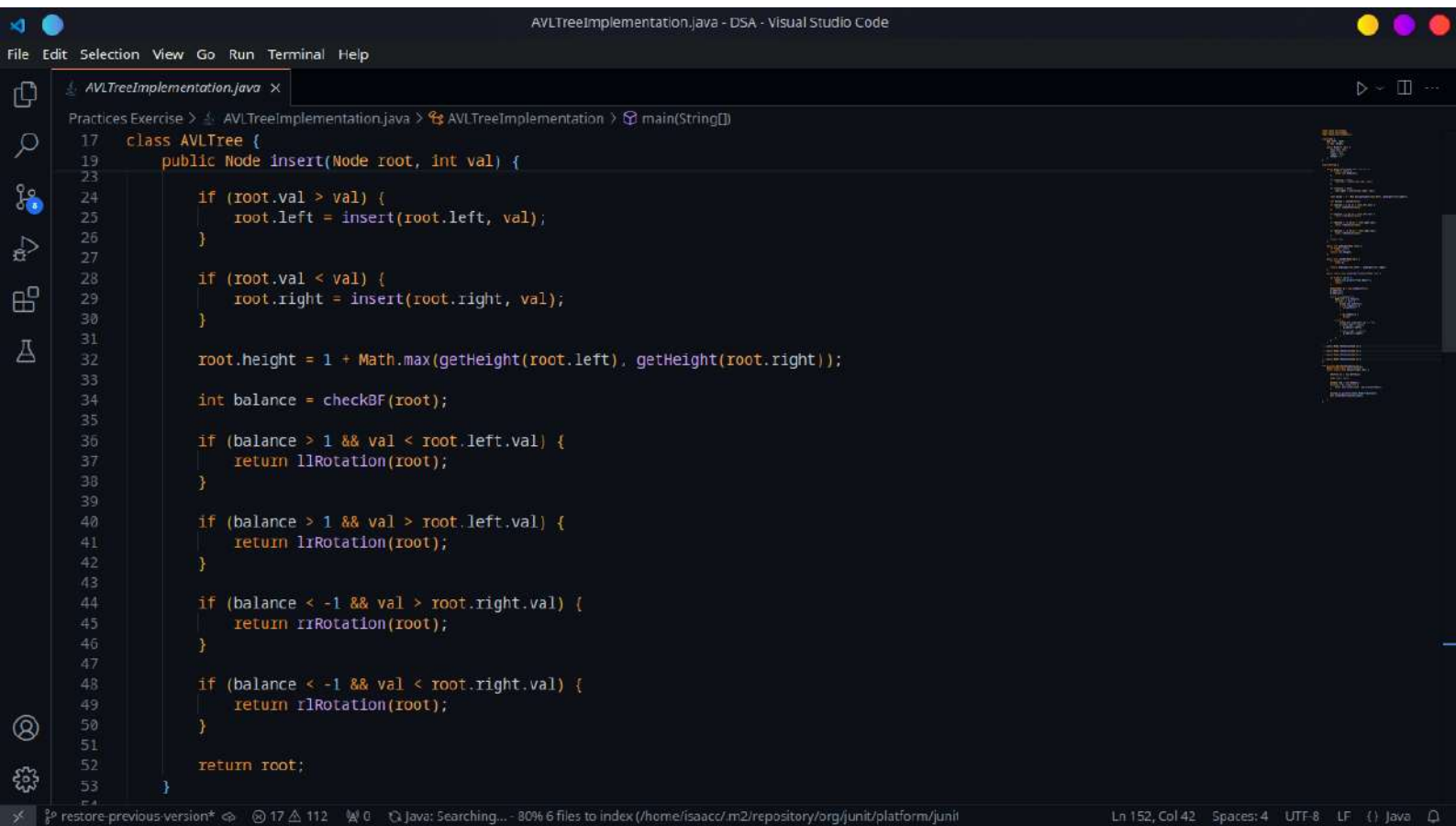
File Edit Selection View Go Run Terminal Help

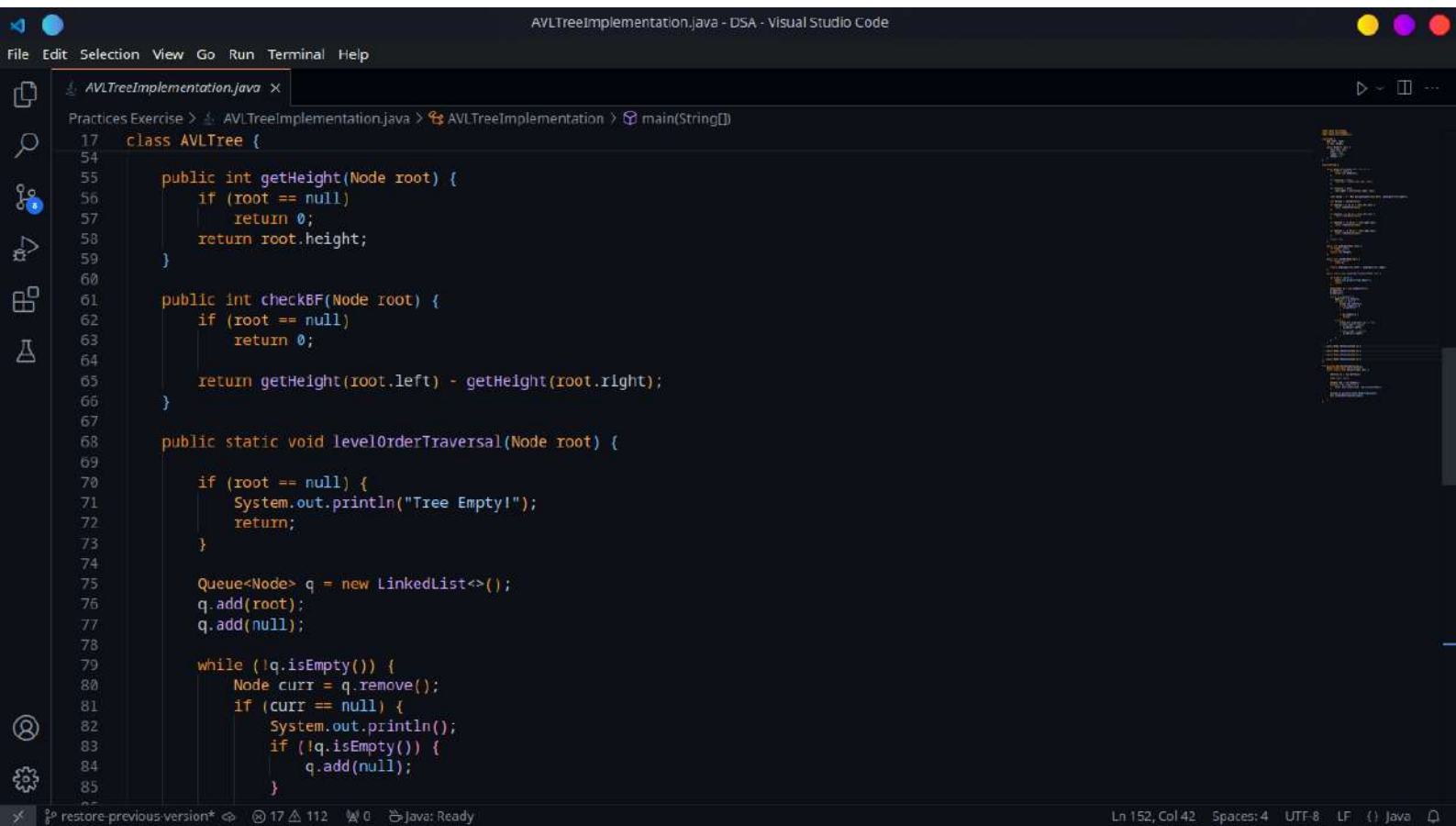
AVLTreeImplementation.java x

Practices Exercise > AVLTreeImplementation.java > AVLTreeImplementation > main(String[])

```
1 import java.util.Queue;
2 import java.util.Random;
3 import java.util.LinkedList;
4
5 class Node {
6     Node left, right;
7     int val, height;
8
9     public Node(int val) {
10         this.val = val;
11         left = null;
12         right = null;
13         height = 1;
14     }
15 }
16
17 class AVLTree {
18
19     public Node insert(Node root, int val) {
20         if (root == null) {
21             return new Node(val);
22         }
23
24         if (root.val > val) {
25             root.left = insert(root.left, val);
26         }
27
28         if (root.val < val) {
29             root.right = insert(root.right, val);
30         }
31
32         root.height = 1 + Math.max(getHeight(root.left), getHeight(root.right));
33     }
34 }
```

Ln 152, Col 42 Spaces: 4 UTF-8 LF Java





AVLTreeImplementation.java - DSA - Visual Studio Code

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AVLTreeImplementation.java x

Practices Exercise > AVLTreeImplementation.java > AVLTreeImplementation > main(String[])

```
17 class AVLTree {
68     public static void levelOrderTraversal(Node root) {
71         System.out.println("Tree Empty!");
72         return;
73     }
74
75     Queue<Node> q = new LinkedList<>();
76     q.add(root);
77     q.add(null);
78
79     while (!q.isEmpty()) {
80         Node curr = q.remove();
81         if (curr == null) {
82             System.out.println();
83             if (!q.isEmpty()) {
84                 q.add(null);
85             }
86
87             if (q.isEmpty()) {
88                 break;
89             }
90         } else {
91             System.out.print(curr.val + " ");
92             if (curr.left != null) {
93                 q.add(curr.left);
94             }
95             if (curr.right != null) {
96                 q.add(curr.right);
97             }
98         }
99     }
100 }
101 }
```

Ln 152, Col 42 Spaces: 4 UTF-8 LF {} Java

AVLTreeImplementation.java - DSA - Visual Studio Code

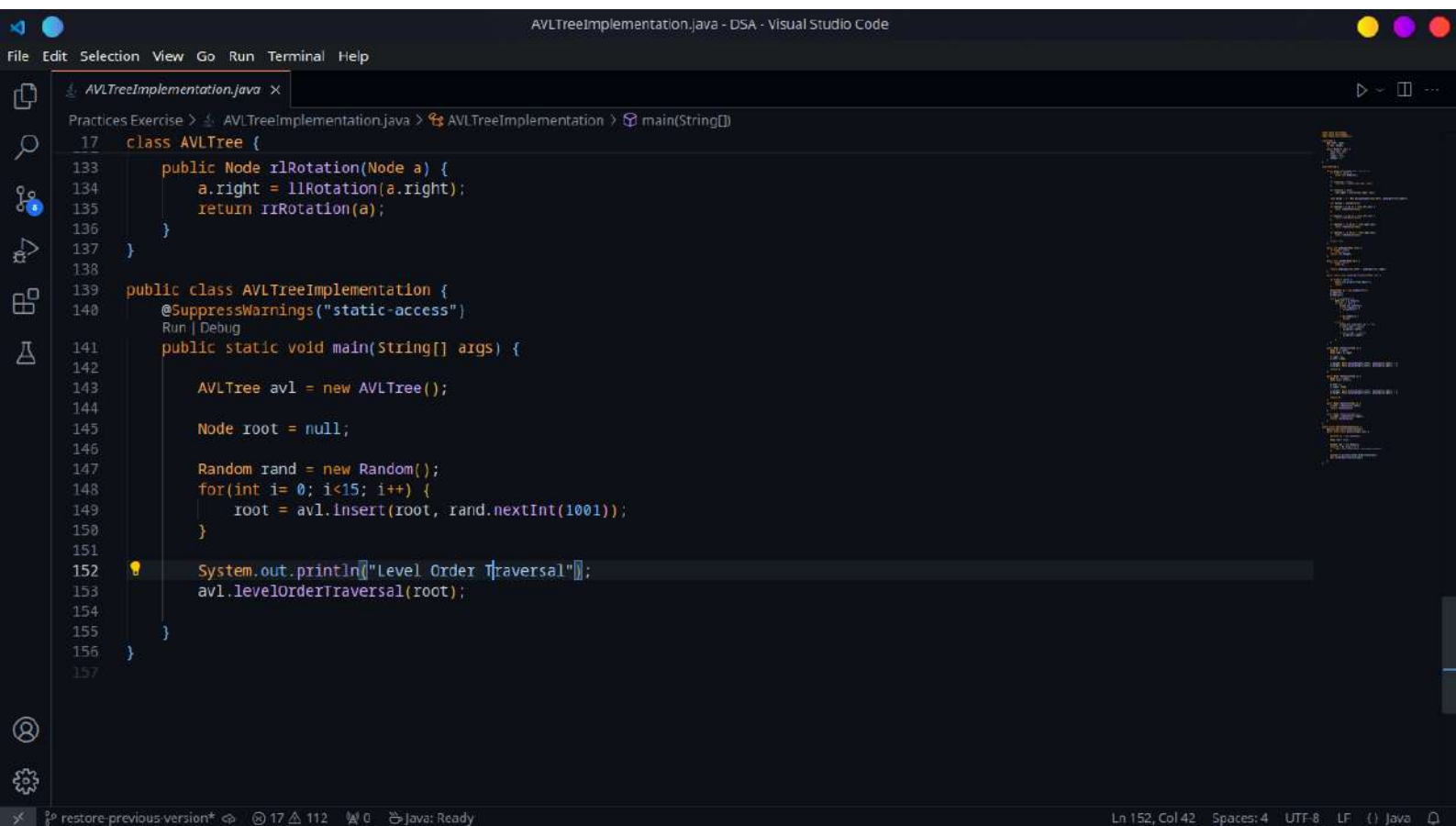
File Edit Selection View Go Run Terminal Help

AVLTreeImplementation.java x

Practices Exercise > AVLTreeImplementation.java > AVLTreeImplementation > main(String[])

```
17 class AVLTree {
101
102     public Node llRotation(Node a) {
103         Node b = a.left;
104         Node temp = b.right;
105
106         b.right = a;
107         a.left = temp;
108
109         a.height = Math.max(getHeight(a.left), getHeight(a.right)) + 1;
110         b.height = Math.max(getHeight(b.left), getHeight(b.right)) + 1;
111
112         return b;
113     }
114
115     public Node rrRotation(Node a) {
116         Node b = a.right;
117         Node temp = b.left;
118
119         b.left = a;
120         a.right = temp;
121
122         a.height = Math.max(getHeight(a.left), getHeight(a.right)) + 1;
123         b.height = Math.max(getHeight(b.left), getHeight(b.right)) + 1;
124
125         return b;
126     }
127
128     public Node lrRotation(Node a) {
129         a.left = rrRotation(a.left);
130         return llRotation(a);
131     }
132
133     public Node rlRotation(Node a) {
```

Ln 152, Col 42 Spaces: 4 UTF-8 LF () Java



AVLTreeImplementation.java - DSA - Visual Studio Code

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RUN AND DEBUG

RUN

Run and Debug

To customize Run and Debug create a launch.json file.

Show all automatic debug configurations.

AVLTreeImplementation.java

```
139 public class AVLTreeImplementation {
140     @SuppressWarnings("static-access")
141     public static void main(String[] args) {
142
143         AVLTree avl = new AVLTree();
144
145         Node root = null;
146
147         Random rand = new Random();
148         for(int i= 0; i<15; i++) {
149             root = avl.insert(root, rand.nextInt(1001));
150         }
151
152         System.out.println("Level Order Traversal");
153         avl.levelOrderTraversal(root);
154
155     }
```

PROBLEMS 129 OUTPUT DEBUG CONSOLE TERMINAL PORTS

isaacc@IsaacNewton: ~/DSA\$ /usr/bin/env /usr/lib/jvm/java-21-openjdk-21.0.5.0.11-1.fc40.x86_64/bin/java -agentli
b:jdwp=transport=dt_socket,server=n,suspend=y,address=localhost:36643 -XX:+ShowCodeDetailsInExceptionMessages -cp
/home/isaacc/.config/Code/User/workspaceStorage/ae23cd8fd9f7848aca7cd9bb7fd6e787/redhat.java/jdt_ws/DSA_a9d721ce
/bin AVLTreeImplementation
Level Order Traversal
269
208 848
17 216 397 918
13 172 265 284 433 859
276 335
isaacc@IsaacNewton: ~/DSA\$

BREAKPOINTS

Uncaught Exceptions

Caught Exceptions

restore-previous-version* 17 112 0 Java: Ready Ln 152, Col 42 Spaces: 4 UTF-8 LF {} Java