Plotting the error bands for Off-Shell function was implemented successfully and some results are summarized as follows.

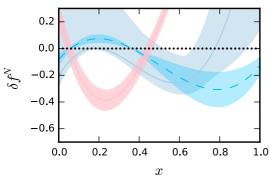
As the preliminary step, three types of fits were considered as follows.

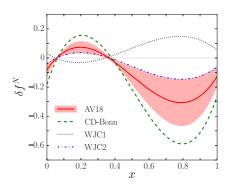
1) CJ15 (In the original CJ15 work, the parameter  $x_1$  was fixed by considering the constraint by quark sum rule)

$$\delta f = N(x - x_0)(x - x_1)(1 + x_0 - x)$$

2) CJ15 with ioff1 for 3-degree polynomial

$$\delta f 3 = N(x - x_0)(x - x_1)(x - x_2)$$





Kulagin-PettiCJ15 (ref)ioff1\_CJ15-3 (1.03)

## Observations:

- 1) CJ15 Off-Shell function's uncertainty band is reproduced
- 2) The uncertainty bands for ioff1 is not symmetrical because the parameters  $x_0$  and  $x_1$  are strongly correlated negatively. For example (correlation matrices for  $x_0$  and  $x_1$ ):

ioff1 
$$\begin{pmatrix} 1.000 & -0.976 \\ -0.976 & 1.000 \end{pmatrix}$$

The parameters for ioff1 are the following.

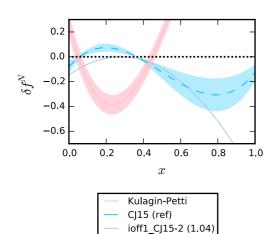
$$N = 8.2851 \pm 5.2739$$

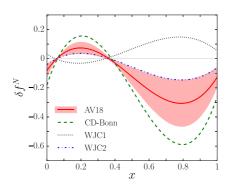
$$x_0 = 0.20480 \pm 0.39590$$

$$x_1 = 0.15685 \pm 0.37412$$

$$x_2 = 0.77609 \pm 0.11280$$

3) CJ15 with ioff1 2-degree polynomial  $\delta f = N(x - x_0)(x - x_1)$ 





Observations:

Correlation matrix for  $x_0$  and  $x_1$  in ioff1 2-degree polynomial is the following.

$$\begin{pmatrix}
1.000 & -0.999 \\
-0.999 & 1.000
\end{pmatrix}$$

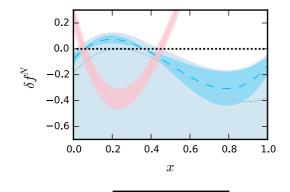
The parameters for ioff1 2D are the following.  $N=-1.9052\pm1.0349$ 

$$x_0 = 0.27550 \pm 9.0427$$

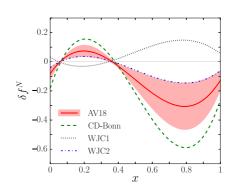
$$x_1 = 0.28029 \pm 9.0625$$

4) CJ15 with ioff9 (In this case, the parameter  $x_1$  was kept free and purely determined by the fit) with same Off-Shell function as CJ15

$$\delta f = N(x - x_0)(x - x_1)(1 + x_0 - x)$$



Kulagin-Petti



— CJ15 (ref) — ioff9\_CJ15 (1.04)

Observations:

Correlation matrix for  $x_0$  and  $x_1$  in ioff9 is the following.

$$\begin{pmatrix} 1.000 & -0.997 \\ -0.997 & 1.000 \end{pmatrix}$$

The parameters for ioff9 are the following.

$$N = -2.7758 \pm 5.3158$$

$$x_0 = 0.22976 \pm 1.3858$$

$$x_1 = 0.23625 \pm 1.3608$$

## 5) CJ15 ioff1 with Vs without JLab data (Simona + BoNuS)

$$\delta f 3 = N(x - x_0)(x - x_1)(x - x_2)$$

### With JLab Data

## 0.2 0.0 -0.2 -0.4 -0.6 0.0 0.2 0.4 0.6 0.8 1.0

# Kulagin-PettiCJ15 (ref)ioff1\_CJ15-3 (1.03)

 $\boldsymbol{x}$ 

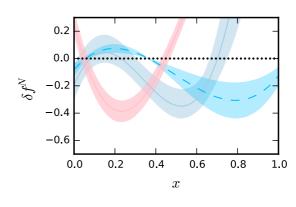
$$N = 8.2851 \pm 5.2739$$

$$x_0 = 0.20480 \pm 0.39590$$

$$x_1 = 0.15685 \pm 0.37412$$

$$x_2 = 0.77609 \pm 0.11280$$

### Without JLab data



Kulagin-PettiCJ15 (ref)ioff1\_CJ15-3-NoJLabData (1.03)

$$N = 15.027 \pm 5.773$$

$$x_0 = 0.080580 \pm 0.071163$$

$$x_1 = 0.229570 \pm 0.086896$$

$$x_2 = 0.701960 \pm 0.039769$$

Correlation matrix for N,  $x_0$ ,  $x_1$  and  $x_2$ :

$$\begin{pmatrix} N & x_0 & x_1 & x_2 \\ 1.000 & 0.460 & -0.503 & -0.816 \\ 0.460 & 1.000 & -0.976 & -0.235 \\ -0.503 & -0.976 & 1.000 & 0.307 \\ -0.816 & -0.235 & 0.307 & 1.000 \end{pmatrix}$$

$$\begin{pmatrix} N & x_0 & x_1 & x_2 \\ 1.000 & -0.391 & 0.452 & -0.606 \\ -0.391 & 1.000 & -0.753 & 0.225 \\ 0.452 & -0.753 & 1.000 & -0.178 \\ -0.606 & 0.225 & -0.178 & 1.000 \end{pmatrix}$$