

Plotting the error bands for Off-Shell function was implemented successfully and some results are summarized as follows.

As the preliminary step, three types of fits were considered as follows.

- 1) CJ15 (In the original CJ15 work, the parameter x_1 was fixed by considering the constraint by quark sum rule)

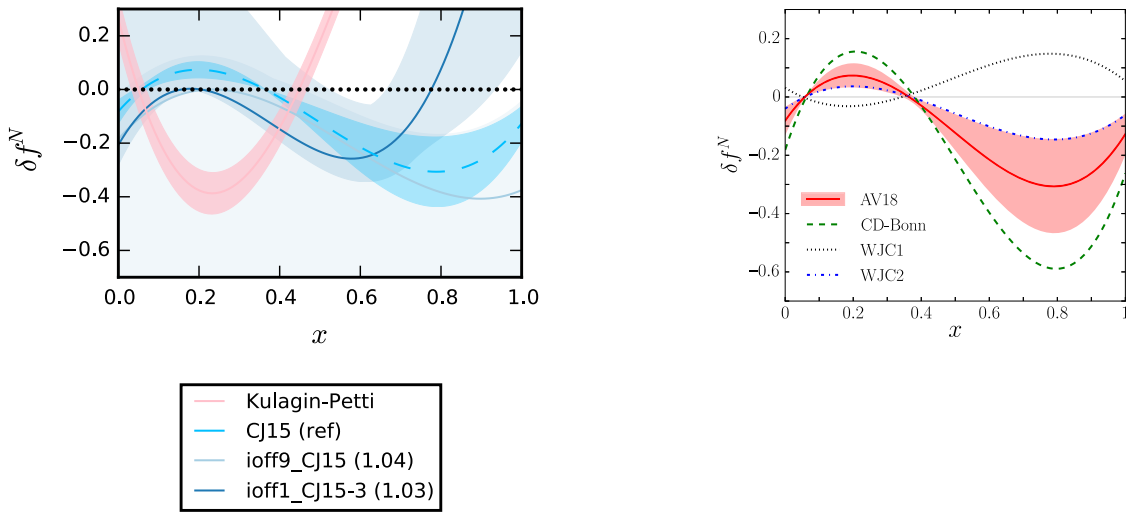
$$\delta f = N(x - x_0)(x - x_1)(1 + x_0 - x)$$

- 2) CJ15 with ioff9 (In this case, the parameter x_1 was kept free and purely determined by the fit) with same Off-Shell function as CJ15

$$\delta f = N(x - x_0)(x - x_1)(1 + x_0 - x)$$

- 3) CJ15 with ioff1 for 3-degree polynomial

$$\delta f_3 = N(x - x_0)(x - x_1)(x - x_2)$$



Observations:

- 1) CJ15 Off-Shell function's uncertainty band is reproduced
- 2) The uncertainty bands for ioff9 and ioff1 are not symmetrical because the parameters x_0 and x_1 are strongly correlated negatively. For example (correlation matrices for x_0 and x_1):

$$\text{i) ioff9} \quad \begin{pmatrix} 1.0 & -0.99682729722690833 \\ -0.99682729722690833 & 1.0000000000000002 \end{pmatrix}$$

$$\text{ii) ioff1} \quad \begin{pmatrix} 1.0000000000000002 & -0.97599951214758696 \\ -0.97599951214758696 & 1.0000000000000002 \end{pmatrix}$$

We can understand this asymmetry, using a generic function with negative linear correlation with a coefficient c near the solutions for x_0 and x_1 .

$$\delta f(\text{test}) = N(x - x_0 - c)(x - x_1 + c)$$

or

$$\delta f(\text{test}) = N(x - x_0 + c)(x - x_1 - c)$$