

1.

A	B	C	D	Out
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

AB \ CD	CD			
	00	01	11	10
00	0	1	0	0
01	0	1	0	0
11	0	1	1	0
10	0	1	1	1

2.

To minimize the given Boolean expression using the four-variable Karnaugh map, follow these steps:

Step 1: Create the Karnaugh map with rows and columns representing all possible combinations of A, B, C, and D.

		CD			
AB		00	01	11	10
00					
01					
11					
10					

Step 2: Fill in the K-map with the given minterms (1, 5, 6, 12, 13, 14) and don't cares (2, 4).

CD					
AB	00	01	11	10	

00	1				

01		1			

11			1		

10				1	

Step 3: Group adjacent 1s in powers of 2 (1, 2, 4, 8, etc.) to form groups in the K-map.

CD					
AB	00	01	11	10	

00	1	1	1		

01		1	1		

11		1	1		

10	1			1	

Step 4: Determine the simplified expressions for each group.

Group 1: AB = 00

Minterms: 1, 5, 6, 12

For $AB = 00$, the value of C and D can be either 00 , 01 , 11 , or 10 . In this case, the output is always 1 . So the simplified expression for this group is simply 1 .

Group 2: $AB = 01$

Minterms: $13, 14$

For $AB = 01$, the value of C and D can be 00 or 01 . In this case, the output is always 1 . So the simplified expression for this group is also 1 .

Group 3: $AB = 10$

Minterm: 10

For $AB = 10$, the value of C and D can be 00 or 10 . In this case, the output is always 1 . So the simplified expression for this group is 1 .

Group 4: $AB = 11$

Minterm: None

There are no minterms for $AB = 11$. It means that this group does not contribute to the output.

Step 5: Write down the minimized Boolean expression.

$$F(A, B, C, D) = \sum m(1, 5, 6, 12) + \sum m(13, 14) + \sum m(10)$$

$$\text{Simplified: } F(A, B, C, D) = 1$$

The minimized Boolean expression for the given function $F(A, B, C, D)$ is simply $F(A, B, C, D) = 1$.