

HW 3

ISHMEET KAUR

2015042

ques 1. No. XOR is not linearly separable.
Neural network with linear activation can't classify it

$$y = f(w_1 w_1 x + b_1) + b_2 \Rightarrow \text{svm with linear function}$$

$$\begin{aligned} f(x) &= B(Ax + a) + b \\ &= \underbrace{BA}_{\text{const}} x + \underbrace{Ba + b}_{\text{const}} \end{aligned}$$

$$\therefore f(x) = c_1 x + c_2$$

ques 2

ReLU : performs better than sigmoid

- large gradient results in update weight that gradient flowing could be 0.
- this kills neurons
- So, keep the learning rate low.

Sigmoid : when sigmoid neuron's activation saturates at 0/1, gradient $\rightarrow 0$
i.e. sigmoid saturation and gradients killed
: no flow through neurons

- : initialise weight by extra 1
- : start with low weights

ques 3.

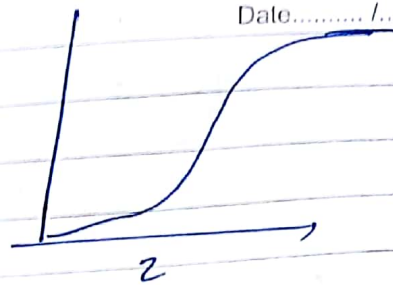
for quadratic, error \uparrow , Learning rate \downarrow

$$C = \frac{(y - a)^2}{2}$$

$$a = \sigma(z)$$

$$\frac{\partial C}{\partial w} = (a - y) \sigma'(z) x = a \sigma'(z)$$

$$\frac{\partial C}{\partial b} = a \sigma'(z)$$



$\therefore \frac{\partial C}{\partial w}, \frac{\partial C}{\partial b}$ are v. low (slow learning)

cross entropy cost

$$C = -\frac{1}{n} \sum_x [y \ln a + (1-y) \ln (1-a)]$$

I. $C > 0$

II. output closer to actual value then entropy $\rightarrow 0$.

$$\begin{aligned} \Rightarrow \frac{\partial C}{\partial w_j} &= -\frac{1}{n} \sum \left(\frac{y}{\sigma(z)} - \frac{(1-y)}{1-\sigma(z)} \right) \sigma'(z) y \\ &= \frac{1}{n} \sum_x x_j (\sigma(z) - y) \end{aligned}$$

\therefore learning rate of weights = $\sigma(z) - y$
large error \Rightarrow more learning !!