

$$1) T(n) = 2T\left(\frac{n}{2}\right) + n$$

Assignment 4

$$4) T(n) = 8T\left(\frac{n}{2}\right) + n^2$$

using master's theorem

$$a=8, b=2, k=2, p=0$$

$$\log_b a = \log_2 8 = \log_2 2^3 \Rightarrow 3$$

$$\log_b a < k \Rightarrow 3 < 2, \text{ and } p > 0$$

case 3a)

$$= \Theta(n^{k \log_b a + 1})$$

$$= \Theta(n^2 \log n)$$

$$\log_b a > k \Rightarrow 3 > 2$$

$$\text{case 1} \Rightarrow \Theta(n^{\log_b a})$$

$$\boxed{\Theta(n^3)}$$

Assignment 4

1) $T(n) = 2T(n/2) + n$

master's theorem

$$T(n) = aT(n/b) + f(n) \Rightarrow (n^k \log^p n)$$

$$a=2, b=2, k=1, p=0$$

$$\log_b a = k \Rightarrow \log_2 2 = 1 \Rightarrow \text{valid (case 2)}$$

$$p=0, p > -1 \rightarrow \Theta(n^k \log^{p+1} n)$$

$$\Theta(n \log n)$$

2) $T(n) = 2T(n/2) + n \log n$

using master's theorem

$$T(n) = aT(n/b) + (n^k \log^p n)$$

$$a=2, b=2, k=1, p=1$$

$$\text{case 2} \Rightarrow \log_b a = k$$

$$p=1, p > -1 \rightarrow \Theta(n^k \log^{p+1} n)$$

$$= \Theta(n \log^2 n)$$

3) $T(n) = 2T(n/2) + n^2$

$$a=2, b=2, k=2, \text{ case 3} \Rightarrow \log_b a < k$$

$$p \geq 0 \Rightarrow \Theta(n^k \log^p n) \Rightarrow \Theta(n^2 \log^0 n)$$

$$\Theta(n^2)$$

4) $T(n) = 8T(n/2) + n^2 \rightarrow a=8, b=2, k=2$