## **UC Irvine ISI-BUDS Day 13**

Zhaoxia Yu

7/27/2022

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Study Goals

Introduction

Correlated Data

Linear-Mixed Effects Model

LME Examples: Example 1

## **Study Goals**

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LME Examples: Example 1

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LME Examples: Example 1

- ► Introduction: Revisiting LM
- Correlated Data
  - Sources of correlation
  - The consequence of ignoring data dependence: a simulation study
- Model correlated data using linear mixed-effects model
- Examples of LME: Example 1
- ► The slides are based on my published work: https://doi.org/10.1016/j.neuron.2021.10.030 https://yu-zhaoxia.github.io/MM\_in\_Neuroscience/

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Adjustment for multiple comparisons

► Basic assumptions of LM

$$Y_i = \beta_0 + x_{i1} \times \beta_1 + \ldots + x_{ip} \times \beta_p + \epsilon_i, i = 1, \ldots, n$$

- $E(\epsilon_i) = 0$ , which is equivalent to  $E(Y_i|X_i) = \beta_0 + x_{i1} \times \beta_1 + \dots + x_{ip} \times \beta_p$
- $Var(\epsilon_i) = \sigma^2$ . Note, this is equivalent to say  $Var(Y_i|X_i) = \sigma^2$ .
- $(\epsilon_1, \cdots, \epsilon_n)$  are mutually independent
- Question: what if the observations are dependent?

### **Correlated Data**

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LME Examples: Example 1

- Clustered data: all fifth graders in the Irvine Unified School District
- ▶ Data with spatial correlation: today's highest temperatures of all cities in California
- Data with temporal correlation: hourly temperatures of Irvine within a day
- **•** . . .

### Sources of correlation

time<sub>0</sub> time<sub>1</sub> time<sub>2</sub> time<sub>0</sub>

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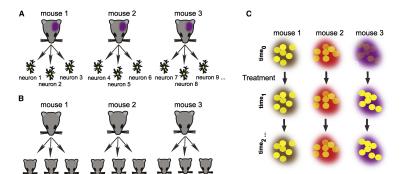
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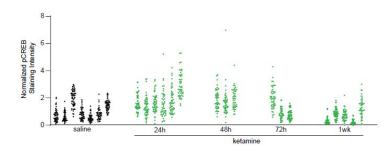
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**Figure 1:** Normalized pCREB staining intensity from 1,200 neurons. The values in each cluster were from one animal. In total, pCREB was measuredfrom 24 mice: saline (7 mice), 24h (6 mice), 48h (3 mice), 72h (3 mice), 1week (5 mice) after treatment.

Linear-Mixed Effects Model

LME Examples: Example 1

Adjustment for multiple comparisons

```
Ex1 = read.csv("https://www.ics.uci.edu/~zhaoxia/Data/BeyondT
#factor the treatment IDs
```

Ex1\$treatment idx = as.factor(Ex1\$treatment idx) dim(Ex1)# checking the dimensions of the dataset

## [1] 1200 3

names(Ex1)# checking the names of each column

```
## [1] "res"
                        "treatment idx" "midx"
```

```
table(Ex1$treatment_idx)
```

```
##
##
## 357 309 139 150 245
```

```
##
```

##

table(Ex1\$midx)

```
#table(Ex1$treatment, Ex1$midx)
```

8

53 49 56 52 46 47 54 52 54 54 47 53 49

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Linear-Mixed Effects Model

LME Examples: Example 1 Adjustment for multiple

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11 12 13 14 15 16 17 18 19

47 48 44 50 45 55 4

# Example 1: Ignore data dependence (incorrect analysis)

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LME Examples: Example 1

- ► A common analysis is to ignore data dependence
- Representative descriptions of inappropriate analyses
  - "t(28656) = 314 with  $p < 10^{-10}$  over a total of n=28657 neurons pooled across six mice,"
  - "n = 377 neurons from four mice, two-sided Wilcoxon signed rank test,"
  - "610 A cells, 987 B cells and 2584 C cells from 10 mice, oneway ANOVA and Kruskal–Wallis test,"
  - "two-sided paired t test, n=1597 neurons from 11 animals, d.f. = 1596,"

obj.lm=lm(res~treatment idx, data=Ex1)

print(coef.table)

coef.table=summary(obj.lm)\$coefficients

row.names(coef.table)=c("Saline", "24h-S",

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```
Pr(>|t|)
##
            Estimate Std. Error
                                   t. value
## Saline
           1.0261907 0.03997259 25.672363
                                            4.064778e-116
## 24h-S
           0.7828564 0.05868406
                                 13.340189
                                             6.040147e-38
           0.8135287 0.07550847
                                 10.774006
                                             6.760583e-26
## 48h-S
## 72h-S
           0.1605790 0.07348870
                                  2.185084
                                             2.907634e-02
          -0.3604732 0.06265813 -5.753015
                                             1.112796e-08
## 1wk-S
```

## Example 1: Ignore data dependence

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Adjustment for multiple Pr(>F)

4 246.62 61.656 108.09 < 2.2e-16 \*\*\*

#The same analysis can be done by the "aov" function

0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 '

(incorrect analysis)

anova(obj.lm)

##

##

## ---

## Response: res

## treatment idx

## Signif. codes:

## Residuals

## Analysis of Variance Table

What is wrong with the analysis?

Df Sum Sq Mean Sq F value

1195 681.65 0.570

# Example 1: Understand the dependence in data

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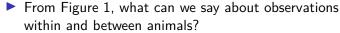
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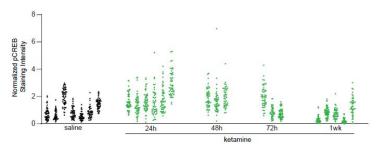
LME Examples:

LME Examples: Example 1

Adjustment for multiple comparisons



▶ Data are clustered in animals (mice)



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We use ICC to quantify the dependence due to clustering. It is defined as

$$ICC = \frac{\sigma_b^2}{\sigma_b^2 + \sigma_e^2},$$

### where

- $\sigma_b^2$  denotes the between-class variance  $\sigma_e^2$  denotes the within-class variance
- ► The ICC for naturally occurring clusters is often between 0 and 1
- ► ICC = 0: the data are uncorrelated
- ightharpoonup ICC = 1: all the observations in each cluster are identical

### load the ICC library

library(ICC)

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```
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```

```
### conduct ICC analysis by organizing all the information, in
icc.analysis=data.frame(n=rep(0,5), icc=rep(0,5), design_effe
effective.n=rep(0,5), M=rep(0,5), cells=rep(0,5))
```

```
# The ICC is computed as follows (code won't show in slides)
```

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Table 1. ICC, design effect, and effective sample size for the 5 groups in example 1

	Saline (7 mice)	24 h (6 mice)	48 h (3 mice)	72 h (3 mice)	1 week (5 mice)
No. cells	357	209	139	150	245
ICC	0.61	0.33	0.02	0.63	0.54
Design effect	32.0	17.7	1.8	31.8	26.8
Effective sample size	11.1	17.5	76.9	4.7	9.1

ICC and the design effect were the lowest at 48 h, when the data were relatively homogeneous across animals. At baseline and 72 h, the data were noticeably heterogeneous across animals, leading to high ICC.

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- ► The dependency due to clustering is substantial
- the 1,200 neurons should not be treated as 1,200 independent cells
- ▶ Design effect:  $D_{eff} = 1 + (M 1)ICC$ , where M is the average cluster size
- ► Effective sample size:  $n_{eff} = n/D_{eff}$ .

# The consequence of ignoring data dependence: a simulation study

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- ▶ We generated 1000 data sets
  - each follows the same ICC structure of Example 1
  - data are simulated under the assumptino of no difference between the five treatments/conditions
  - each data set is analyzed with the regular LM/ANOVA, without accounting for the data dependence.
  - **>** significance level is set at  $\alpha = 0.05$ .
- Let's guess: What is the type I error rate (proportion of times rejecting the null hypothesis wrongly)?

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LME Examples: Example 1

- A Type I error (false positive): rejecting the null hypothesis when it is true
- ► A Type II error (false negative): failing to reject the null hypothesis when it is false
- ▶ Significance level  $\alpha$ :
- If the null hypothesis is true and  $\alpha = 0.05$ , the type I error rate of a valid test should be 0.05

# The consequence of ignoring data dependence: a simulation study

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source("https://www.ics.uci.edu/~zhaoxia/Data/BeyondTand/

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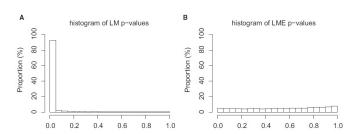


Figure 3. Histograms of p values using simulated data that assume (1) no treatment effects and (2) the same sample sizes and correlation structure with example 1

(A) Histogram of the p values from the inappropriate method (linear model) shows that ignoring the correlation structure of the data led to a surprisingly high type I error rate (90%) at significance level x = 0.05.

(B) Histogram of the p values from IME.

### **Linear-Mixed Effects Model**

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## A Motivating Example of LME: Example 1 (the wrong model)

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LME Examples:

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► The model without accounting for dependence:

$$Y_{ij} = \beta_0 + x_{ij,1}\beta_1 + \dots + x_{ij,4}\beta_4 + \epsilon_{ij}, i = 1, \dots, 24; j = 1, \dots, n_{i,i,i,i,j}$$

### where

- $\triangleright$   $n_i$  is the number of observations from the *i*th mouse and  $\sum_{i=1}^{24} n_i = 1200$
- $ightharpoonup \epsilon_{ii}$  represents the deviation in pCREB immunoreactivity of observation (cell) *j* in mouse *i* from the mean pCREB immunoreactivity of mouse i. We assume that the errors  $\epsilon_{ii}$ 's are i.i.d. from  $N(0, \sigma^2)$ .

# A Motivating Example of LME: Example 1 (the wrong model)

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► The model without accounting for dependence:

$$Y_{ij} = \beta_0 + x_{ij,1}\beta_1 + \cdots + x_{ij,4}\beta_4 + \epsilon_{ij}, i = 1, \cdots, 24; j = 1, \cdots, n$$

where the coefficients  $\beta_0, \beta_1, \beta_2, \beta_3, \beta_4$  are assumed to be fixed but unknown parameters

- $\triangleright$   $\beta_0$  is the intercept (the mean of the baseline)
- $\triangleright$   $\beta_1$  is the effect (change) at 24h, compared to the baseline
- $\triangleright$   $\beta_2$  is the effect (change) at 48h, ...
- $\triangleright$   $\beta_3$  is the effect (change) at 72h, ...
- $\triangleright$   $\beta_4$  is the effect (change) at 1wk, ...

## A Motivating Example of LME: Example 1 (the wrong model)

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Example 1

Adjustment for comparisons

► The model without accounting for dependence:

$$Y_{ij} = \beta_0 + x_{ij,1}\beta_1 + \cdots + x_{ij,4}\beta_4 + \epsilon_{ij}, i = 1, \cdots, 24; j = 1, \cdots, n$$

- We use four dummy variables to denote treatments/conditions, which are the time after treatment
  - $x_{ii,1} = 1$  for 24 hours and 0 otherwise
  - $x_{ii,2} = 1$  for 48 hours and 0 otherwise
  - $x_{ii,3} = 1$  for 72 hours and 0 otherwise
  - $x_{ii.4} = 1$  for 1 week and 0 otherwise after ketamine treatments, respectively.

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Adjustment for multiple comparisons

Cells from the same animal share the same environment

$$Y_{ij} = \beta_0 + x_{ij,1}\beta_1 + \ldots + x_{ij,4}\beta_4 + \frac{\mathbf{u}_i}{\mathbf{u}_i} + \epsilon_{ij}, i = 1, \ldots, 24; j = 1, \ldots$$

- We add the subject-specific effect u<sub>i</sub> into the LM
  - $(u_1, \dots, u_{24})$  are assumed to be independent and identically distributed (i.i.d.) from  $N(0, \sigma_b^2)$
  - In addition,  $(u_1, \dots, u_{24})$  are assumed to be independent from the random errors  $\epsilon_{ii}$ 's.

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LME Examples: Example 1

Adjustment for multiple comparisons

$$Y_{ij} = \beta_0 + x_{ij,1}\beta_1 + \ldots + x_{ij,4}\beta_4 + u_i + \epsilon_{ij}, i = 1, \ldots, 24; j = 1, \ldots, n_i$$

\* We call this model a mixed-effects model because there are two types of coefficients +  $(u_1, \cdots, u_{24})$  are random-effect coefficients +  $(\beta_0, \cdots, \beta_4)$  are fixed-effect coefficients

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Including the random coefficients introduces correlation between two observations from the same cluster:

• for 
$$j \neq j'$$
,  $cov(Y_{ij}, Y_{ij'}) = ... = \sigma_b^2$ 

## A Better Representation of the model

- Introduce dummy variables for the animals: let the vector  $(z_{ij,1},\ldots,z_{ij,24})$  be the dummy variables for the cluster/animal memberships such that  $z_{ij,k}=1$  for i=k and 0 otherwise.
- Then the LME can be rewritten to

$$Y_{ij} = \beta_0 + x_{ij,1}\beta_1 + \ldots + x_{ij,4}\beta_4 + z_{ij,1}u_1 + \ldots + z_{ij,24}u_{24} + \epsilon_{ij},$$
  

$$i = 1, \ldots, 24; j = 1, \ldots, n_i;$$

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LME Examples: Example 1

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LME Examples: Example 1

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▶ A more compact form of the model presented in the previous slide:

$$Y = \mathbf{1}\beta_0 + X\beta + \mathbf{Z}\mathbf{u} + \epsilon$$

Remark 1: Example 1 includes treatment effects as fixed effects. Similar to LM and GLM, when available and sensible, other covariates should be added

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LME Examples: Example 1

- Remark 2: You might wonder why do we treat  $u_i$ 's as random, rather than fixed effects.
- Fixed-effects: typically, a fixed effect captures a parameter at the population level
- ► Random-effects:
  - ► A random effect captures cluster-specific effects (e.g., due to cells clustered in animals)
  - ▶ In many situations, the number of clusters (e.g., patients in a longitudinal study) is large. There would be too many parameters to estimate if we treat *u<sub>i</sub>*'s as fixed.
  - Subject-specific effects are typically of no direct scientific interest
- Remark 3: Other random effects might also be necessary. e.g., we will discuss random slopes in an

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LME Examples: Example 1

Adjustment for multiple comparisons

▶ The parameters need to be estimated:

$$\beta_0, \beta_1, \cdots, \beta_p, \sigma^2, \sigma_b^2$$

- Two methods to estimated parameters
  - Maximum likelihood estimation
  - REML: restricted/residual maximum likelihood estimates
  - Two main packages:
    - ▶ nlme: lme
    - Ime4: Imer (doesn't provide p-value) and glmm

## Fit an LME model: relevant packages

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LME Examples: Example 1

Table 5. Selected R packages and functions for mixed-effects modeling and statistical inference				
Package name	Functions related to mixed-effect modeling			
nlme	Ime: fit a linear mixed-effects model			
lme4	Imer: fit a linear mixed-effects model			
	glmm: fit a generalized linear mixed-effects model			
brms	It can conduct Bayesian mixed-effects modeling			
<i>ImerTest</i>	It can perform hypothesis testing on fixed and random effects based on models from Ime4::Imer			
emmeans	It can provide adjusted p values for pairwise and treatments versus control comparisons			
pbkrtest	It can perform the F-test (Kenward-Roger and Satterthwaite type) and parametric bootstrap test			
car	car::Anova provides large-ample Wald test or F-test with Kenward-Roger denominator degrees of freedom			
sjPlot	It can provide visualization and create manuscript-style tables			

## LME Examples: Example 1

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LME Examples: Example 1

# Example 1: evaluate the overall significance of a factor with nlme::lme

```
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```

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Adjustment for multiple comparisons

```
#Wald F-test from an lme object
obj.lme=lme(res~treatment_idx, data= Ex1, random =
anova(obj.lme) #Wald F-tes
```

```
## numDF denDF F-value p-value
## (Intercept) 1 1176 142.8589 <.0001
## treatment idx 4 19 4.6878 0.0084
```

#### Example 1: evaluate the overall significance of a factor with nlme::lme

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```
# notice the argument of the option "method"
# which calls for using ML instead of REML
obj.lme0.ml=lme(res~1, data= Ex1, random = ~ 1|midx, agmethod="
obj.lme.ml=lme(res~treatment_idx, data= Ex1, random compariso1s|mid
```

#Likelihood ratio test from lme objects

anova(obj.lme0.ml, obj.lme.ml)

```
Model df
##
                           AIC
                                    BIC
                                           logLik
                                                   Test
                  1 3 2281.441 2296.712 -1137.721
## obj.lme0.ml
```

## obj.lme.ml 2 7 2272.961 2308.592 -1129.481 1 vs 2 16

#### **Example 1:** evaluate the overall significance of a factor with nlme::lme

```
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```

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```
#equivalently, one can conduct LRT using drop1
drop1(obj.lme.ml, test="Chisq")
```

## Single term deletions

```
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```

```
## res ~ treatment idx
```

0.001

LRT Pr(>Chi)

0.01

```
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```

```
2273.0
## treatment_idx 4 2281.4 16.48 0.002438 **
##
```

AIC

Df

```
0.05
```

##

##

## Model ·

## <none>

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LME Example Example 1

Adjustment for multiple comparisons

#### Compare LM and LME

Table 2. p values for comparing pCREB immunoreactivity at each time point (24 h, 48 h, 72 h, and 1 week) after ketamine treatment to the baseline (saline)

	Overall	24 h	48 h	72 h	1 week
Linear model (ANOVA)	1.2 × 10 <sup>-78</sup>	6.0 × 10 <sup>-38</sup>	6.8 × 10 <sup>-26</sup>	0.0291	1.1 × 10 <sup>-8</sup>
LME	0.0029	0.0049	0.0164	0.5601	0.2525

The "Overall" column corresponds to the null hypothesis of no difference among the 5 groups (example 1). The LME p values are based upon the *lme* function in the *nlme* package, in which the denominator degrees of freedom are determined by the animal grouping level (Pinheiro et al., 2007). The methods for obtaining more accurate p values with adjustments for multiple comparisons can be found in the supplemental information.

#### Example 1: use Ime4::Imer

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library(lme4) #load the lme4 library obj.lmer=lmer(res ~ treatment\_idx+(1|midx), data=Ex1) | data=Ex1)

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```
library(lmerTest)
```

##

##

```
## Warning: package 'lmerTest' was built under R version 4.1.
```

```
## Attaching package: 'lmerTest'

## The following object is masked from 'package:lme4'justment for multiple to the standard of the standard o
```

```
## lmer
## The following object is masked from 'package:stats':
```

```
## step
```

obj.lmer=lmerTest::lmer(res ~ treatment\_idx+(1|midx), data=Ex

#### Example 1: use Ime4::Imer

## lmerModLmerTestl

Data: Ex1

##

##

##

##

##

summary(obj.lmer, ddf="Kenward-Roger")

## Formula: res ~ treatment idx + (1 | midx)

## REML criterion at convergence: 2264.5

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```
## Linear mixed model fit by REML. t-tests use Kenward-Roger'
                                                         Linear-Mixed
```

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Adjustment for multiple comparisons

```
## Scaled residuals:
      Min
          1Q Median
                               3Q
                                      Max
## -2.5388 -0.5761 -0.1129 0.4721 8.8601
## Random effects:
                        Variance Std.Dev.
   Groups
            Name
```

```
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obj.lmer.ml=lme4::lmer(res ~ treatment_idx+(1|midx), data=Ex1
obj.lmer0.ml=lme4::lmer(res ~ 1+(1|midx), data=Ex1,
```

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Adjustment for multiple comparisons

## obj.lmer.ml: res ~ treatment\_idx + (1 | midx) npar AIC BIC logLik deviance Chisq Df

## obj.lmer0.ml 3 2281.4 2296.7 -1137.7 2275.4

## obj.lmer.ml 7 2273.0 2308.6 -1129.5 2259.0 16.48 4

0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 '

#likelihood ratio test

## Data: Ex1 ## Models:

##

## ---

## Signif. codes:

anova(obj.lmer0.ml, obj.lmer.ml)

## obj.lmer0.ml: res ~ 1 + (1 | midx)

## Adjustment for multiple comparisons

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Adjustment for multiple comparisons

Introduction

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LME Examples: Example 1

Adjustment for multiple comparisons

- What is the issue of multiple comparisons
- Suppose the null hypothesis is true. What is the type I error rate if we conduct a test with  $\alpha = 0.05$ ?
- Suppose M null hypotheses are true. What is the probability of making at least one mistake if we use  $\alpha = 0.05$  for each test?
  - ▶ This probability is called the family wise error rate
- ► Mathematical derivation or simulation will show that the family wise error rate is much greater than 0.05
- ► Procedures have been developed to control for the family wise error rate and other types error rate (e.g., false discovery rate)

### Adjustment for multiple comparisons

contrast estimate

##

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LME Examples: Example 1

Adjustment for multiple comparisons

```
-0.8194 0.289 19.0
##
    1 - 2
                                    -2.835
                                            0.0704
##
    1 - 3
               -0.8429 0.359 19.1
                                    -2.349
                                            0.1727
##
              -0.1898 0.359 19.0
                                    -0.529
                                            0.9832
                                     1.051
    1 - 5
                0.3200 0.304 19.0
                                            0.8283
##
##
    2 - 3
              -0.0235 0.368 19.0
                                    -0.064
                                            1,0000
    2 - 4
                0.6296 0.367 19.0
                                     1.713
                                            0.4496
##
    2 - 5
                1.1394 0.315 19.0
                                     3.621
                                            0.0138
##
##
    3 - 4
                0.6531 0.425 19.0
                                     1.538
                                            0.5517
    3 - 5
                1.1629 0.380 19.1
                                     3.062
                                            0.0447
##
##
    4 - 5
                0.5098 0.380 19.0
                                     1.343
                                            0.6690
##
```

SE

df t.ratio p.value

## Degrees-of-freedom method: kenward-roger
## P value adjustment: tukey method for comparing a family of

```
Effects Model
LME Examples:
Example 1
```

```
##
    contrast estimate
                        SE
                             df t.ratio p.value
   2 - 1
               0.819 0.289 19.0
                                  2.835
                                         0.0364
##
## 3 - 1
               0.843 0.359 19.1
                                  2.349 0.0965
   4 - 1
               0.190 0.359 19.0
                                0.529 0.9219
##
   5 - 1
              -0.320 0.304 19.0
##
                                 -1.051
                                         0.6613
##
```

contrast(emmeans(obj.lmer, specs="treatment\_idx"),

Degrees-of-freedom method: kenward-roger

## P value adjustment: dunnettx method for 4 tests