Predicción de Abandono

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library(tidyverse)
library(data.table)
library(broom)
library(knitr)
library(lubridate)
library(RCT)
library(gamlr)
library(ranger)
library(tree)
library(tree)
library(typarallel)
library(tidymodels)
library(xgboost)

Contexto

Cell2Cell es una compañía de teléfonos celulares que intenta mitigar el abandono de sus usuarios. Te contratan para 1) Encontrar un modelo que prediga el abandono con acierto y para usar los insights de este modelo para proponer una estrategia de manejo de abandono.

Las preguntas que contestaremos son:

- 1. Se puede predecir el abandono con los datos que nos compartieron?
- 2. Cuáles son las variables que explican en mayor medida el abandono?
- 3. Qué incentivos da Cell2Cell a sus usarios para prevenir el abandono?
- 4. Cuál es el valor de una estrategia de prevención de abandono focalizada y cómo difiere entre los segmentos de los usuarios? Qué usuarios deberían de recibir incentivos de prevención? Qué montos de incentivos

Nota: Voy a evaluar las tareas con base en la respuesta a cada pregunta. Como hay algunas preguntas que no tienen una respuesta clara, al final ponderaré de acuerdo al poder predictivo de su modelo vs las respuestas sugeridas.

Datos

Los dotos los pueden encontrar en Cell2Cell.Rdata. En el archivo Cell2Cell-Database-Documentation.xlsx pueden encontrar documentación de la base de datos.

Cargemos los datos

```
load('Bases input/Cell2Cell.Rdata')
```

1. Qué variables tienen missing values? Toma alguna decisión con los missing values. Justifica tu respuesta

```
missings <- map_dbl(cell2cell %>% select_all(),
                   ~100*sum(is.na(.)/nrow(cell2cell)))
(missings<-missings[missings>0])
    revenue
                     mou
                            recchrge
                                         directas
                                                       overage
                                                                       roam
0.304024097 \ \ 0.304024097 \ \ 0.304024097 \ \ 0.304024097 \ \ 0.304024097 \ \ 0.304024097
    changem
                 changer
                              phones
                                           models
                                                       eqpdays
0.706574521 \ 0.706574521 \ 0.001407519 \ 0.001407519 \ 0.001407519 \ 1.750953594
       age2
1.750953594
# Revenue, mou, rcchrqe, directas, overage, roam, changem changer, phones, models w/zero
cell2cell <-
   cell2cell %>%
   mutate(across(names(missings[1:10]), ~if_else(is.na(.), 0, as.double(.))))
# eqpdays, age1, age2, quitar
cell2cell<-
   cell2cell %>%
   filter(!is.na(eqpdays), !is.na(age1), !is.na(age2))
```

2. Tabula la distribución de la variable churn. Muestra la frecuencia absoluta y relativa. Crees que se debe hacer oversampling/undersamping?

```
kable(cell2cell %>%
    group_by(churn) %>%
    summarise(n = n()) %>%
    mutate(share = 100*n/sum(n)), digits = 2)
```

churn	n	share
0	49534	70.96
1	20268	29.04

3. (2 pts) Divide tu base en entrenamiento y validación (80/20). Además, considera hacer oversampling (SMOTE) o undersampling. (Tip: Recuerda que el objetivo final es tener muestra ~balanceada en el traning set. En el validation la distribución debe ser la original)

La distribución esta 70% vs 30%. Si queremos construir un training set =80%. Dentro del training, hay que hacer el undersampling tal que se balanceen las clases.

```
set_validation <-</pre>
   treatment_assign(data = cell2cell,
                    share control = 0.8,
                    n_t = 1, strata_varlist = 'customer',
                    seed = 1908, key = 'customer')
Warning: Unknown or uninitialised column: `treat`.
Warning in if (missfits == "NA") {: the condition has length > 1 and only the
first element will be used
Warning in if (missfits == "global") {: the condition has length > 1 and only
the first element will be used
Warning: Unknown or uninitialised column: `treat`.
set_validation<-set_validation$data</pre>
cell2cell<-
   left_join(cell2cell, set_validation %>%
                ungroup %>%
                select(-c(strata, missfit)))
# Divido entre training y validation
cell2cell_V<-
   cell2cell %>%
  filter(treat == 1) %>%
  select(-treat)
rm(set_validation)
cell2cell T<-
  cell2cell %>%
  filter(treat==0) %>%
   select(-treat)
# Undersampling
cell2cell 1 T<-
   cell2cell_T %>%
  filter(churn==1)
undersampling<-
   treatment_assign(data = cell2cell_T %>% filter(churn==0),
                    share_control = 0.41,
                    n t = 1,
                    strata_varlist = 'customer', seed = 19987, key = 'customer')
Warning: Unknown or uninitialised column: `treat`.
Warning in if (missfits == "NA") {: the condition has length > 1 and only the
first element will be used
Warning in if (missfits == "global") {: the condition has length > 1 and only
the first element will be used
Warning: Unknown or uninitialised column: `treat`.
undersampling<-undersampling$data
```

Model estimation

Pondremos a competir 3 modelos:

- 1. Cross-Validated LASSO-logit
- 2. Prune Trees
- 3. Random Forest

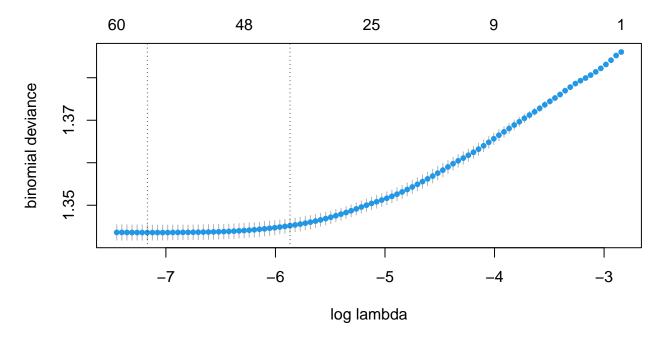
4.GBM

 $4~(2~\mathrm{pts}).$ Estima un cross validated LASSO. Muestra el la gráfica de CV Binomial Deviance vs Complejidad

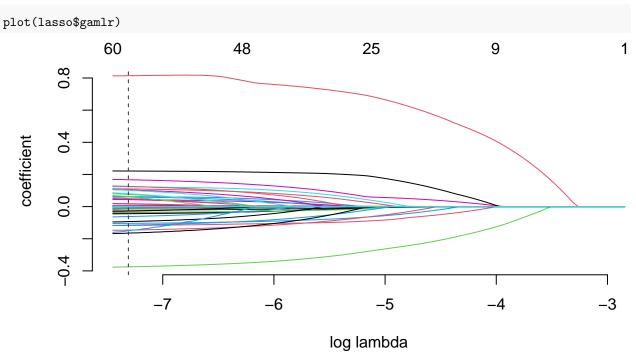
```
# Matriz de covariates
cell2cell_T$treat<-NULL</pre>
Χ<-
   cell2cell_T %>%
   ungroup() %>%
   select(-customer, -churn)
X<-sparse.model.matrix(~.+0, data = X)</pre>
dim(X)
[1] 32425
churn<-cell2cell_T$churn
# CV LASSO
detectCores()
Γ1 12
cl<-makeCluster(12)</pre>
inicio<-Sys.time()</pre>
lasso<-cv.gamlr(x = X, y = churn, verb = T, cl = cl, family = 'binomial')</pre>
fold done.
(tiempo<-Sys.time() - inicio)</pre>
```

```
stopCluster(cl)
save(lasso, file = 'Modelos/cv_lasso.Rdata')

# Plot del CV binomial dev
plot(lasso)
```



5. Grafica el Lasso de los coeficientes vs la complejidad del modelo.



6 (2 pts). Cuál es la λ resultante? Genera una tabla con los coeficientes que selecciona el CV LASSO. Cuántas variables deja iguales a cero? Cuales son las 3 variables más importantes para predecir el abandono? Da una explicación intuitiva a la última pregunta

Las variables más relevantes son:

- retcall [El usuario ya recibió una llamada del equipo de retención]: Esto puede indicar que el usuario está próximo a terminar contrato o que las llamadas del equipo de retención en verdad tienen un efecto contraproducente en términos de la supervivencia del usuario.
- creditaa [El usuario tiene la calificación crediticia más alta]: Esta disminuye la probabilidad de abandono. Muy útil en programas de pos-pago.
- refurb [El auricular del teléfono es reparado]: Esto podría indicar una experiencia negativa de uso de estos auriculares.

lasso\$lambda.min

[1] 0.0007696674

variable	coeficiente
retcall	0.8156834
creditaa	-0.3726389
refurb	0.2208763
uniqsubs	0.1647732
actvsubs	-0.1615133
refer	-0.1443873
retaccpt	-0.1378846
occcler	0.1226888
children	0.1220908
mailres	-0.1165030
credita	-0.1133504
prizmrur	0.1086174
webcap	-0.1034437
mcycle	0.1001941
creditcd	0.0959783
setprcm	-0.0905156
$\operatorname{occhmkr}$	0.0740675
occstud	0.0702888
phones	0.0610163
occret	-0.0597822
rv	0.0581167
intercept	0.0554109
retcalls	0.0516047
marryyes	0.0463030

variable	coeficiente
mailord	-0.0433610
prizmtwn	0.0427891
marryun	0.0412705
threeway	-0.0382060
prizmub	-0.0350963
travel	-0.0258979
callfwdv	-0.0221297
months	-0.0211867
newcelly	-0.0199876
pcown	0.0162476
models	0.0138686
income	-0.0111488
mailflag	-0.0094103
newcelln	-0.0089338
roam	0.0049909
dropvce	0.0049693
age1	-0.0041687
custcare	-0.0036080
changer	0.0023073
recchrge	-0.0021778
dropblk	0.0018898
eqpdays	0.0014490
directas	-0.0012966
overage	0.0011625
truck	0.0009712
age2	-0.0009244
incalls	-0.0008989
revenue	0.0004786
changem	-0.0004677
peakvce	-0.0003127
mou	-0.0002350
setprc	0.0002069
unansvce	0.0001318
outcalls	-0.0000402
blckvce	0.0000014

7. Genera un data frame (usando el validation set) que tenga: customer, churn y las predicciones del LASSO.

```
X<-
    cell2cell_V %>%
    select(-customer, -churn)

X<-sparse.model.matrix(~.+0, data = X)

table(cell2cell_V$churn)</pre>
```

0 1 9846 4115

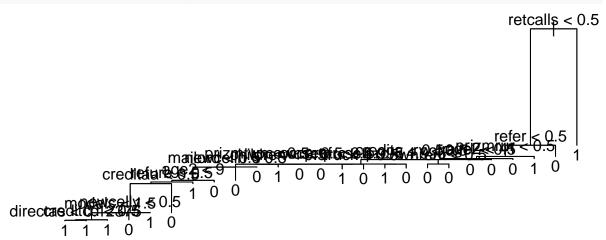
```
predicciones<-
   cell2cell_V %>%
   select(customer, churn) %>%
   mutate(lasso = drop(predict(lasso, newdata = X, select = 'min', type = 'response')))
```

8. Estima ahora tree. Usa mindev = 0.05, mincut = 1000 Cuántos nodos terminales salen? Muestra el summary del árbol

```
Classification tree:
tree(formula = churn ~ ., data = cell2cell_T %>% ungroup() %>%
   select(-customer), split = "gini", mindev = 0.05, mincut = 1000)
Variables actually used in tree construction:
 [1] "retcalls" "refer"
                          "prizmrur" "travel"
                                                "rv"
                                                           "credita"
[7] "truck"
                                     "children" "prizmtwn" "newcelln"
               "occprof" "pcown"
[13] "mailord" "age2"
                                     "creditaa" "newcelly" "models"
                          "refurb"
[19] "creditcd" "directas" "setprc"
                                     "ownrent"
Number of terminal nodes: 25
Residual mean deviance: 1.377 = 44630 / 32400
Misclassification error rate: 0.4661 = 15114 / 32425
```

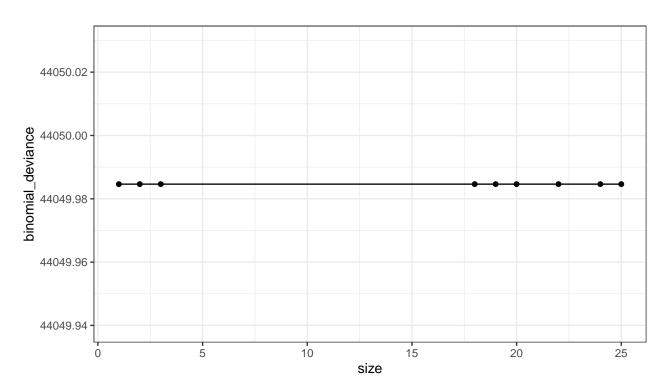
9. Grafica el árbol resultante

```
plot(arbol); text(arbol, pretty = 0)
```



10. Poda el árbol usando CV. Muestra el resultado. Grafica Tree Size vs Binomial Deviance. Cuál es el mejor tamaño del árbol? Mejora el Error?

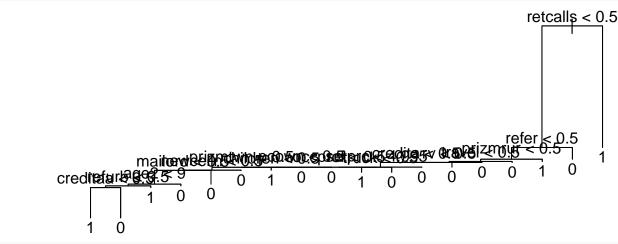
```
(cv_arbol<-cv.tree(arbol, K = 5))</pre>
$size
[1] 25 24 22 20 19 18 3 2 1
[1] 44049.98 44049.98 44049.98 44049.98 44049.98 44049.98 44049.98 44049.98
[9] 44049.98
$k
[1]
                  0.2889196
                               0.8183143
                                           5.6150824
                                                       5.8942294
                                                                   6.2601607
           -Inf
      6.4101217 17.6499275 183.3326909
$method
[1] "deviance"
attr(,"class")
[1] "prune"
                    "tree.sequence"
arbol_graf<-
   tibble(size = cv_arbol$size, binomial_deviance = cv_arbol$dev)
ggplot(arbol_graf, aes(size, binomial_deviance))+geom_point()+geom_path()+
   theme_bw()
```



11. Gráfica el árbol final. (Tip: Checa prune.tree)

save(arbol_prune, file = 'Modelos/arbol.Rdata')

```
arbol_prune<-prune.tree(arbol, best = 4)
plot(arbol_prune); text(arbol_prune, pretty = 0)</pre>
```



12. Genera las predicciones del árbol pruned. Guardalas en la base de predicciones. Guarda el score y la prediccion categorica en la misma data frame donde guardaste las predicciones

```
X<-
    cell2cell_V %>%
    select(-customer, -churn)

predicciones<-
    predicciones %>%
    mutate(arbol_class = drop(predict(arbol_prune, newdata = X, type = 'class')),
        arbol_prob = drop(predict(arbol_prune, newdata = X, type = 'vector'))[,2])
```

- 13 (4pts). Corre un Random Forest ahora. Cuál es la B para la que ya no ganamos mucho más en poder predictivo?
 - Corre para num.trees=100,200,300, 500, 700, 800
 - En cada caso, guarda únicamente el prediction.error
 - Recuerda fijar el parámetro probability-T para que el RF genere predicciones categoricas y sus probabilidades

```
X<-
    cell2cell_T %>%
    ungroup() %>%
    select(-customer, -churn)

X<-sparse.model.matrix(~.+0, data = X)
dim(X)</pre>
```

[1] 32425 66

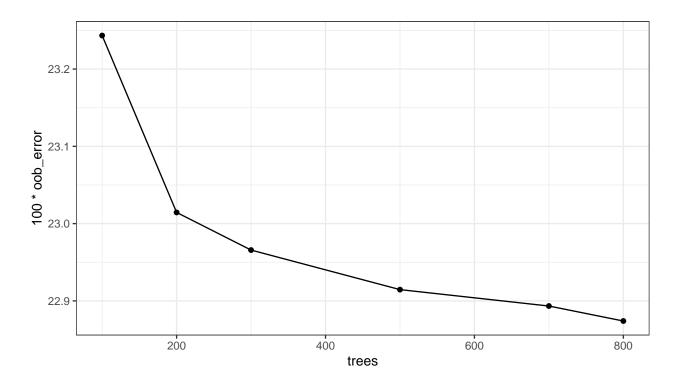
del LASSO

```
churn<-cell2cell_T$churn

# Grid de Random Forests
detectCores()</pre>
```

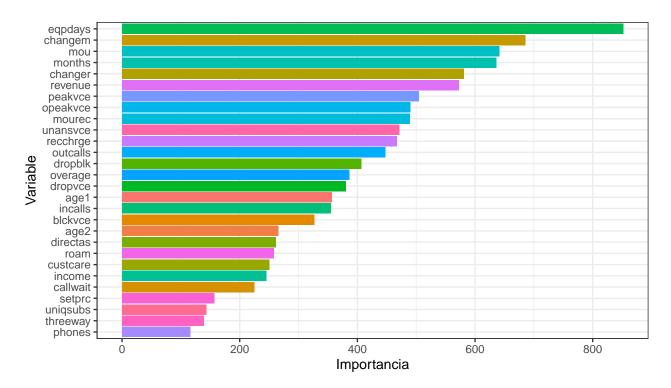
[1] 12

Time difference of 1.423926 mins



```
random_forest<-random_forest[[6]]
save(random_forest, file = 'Modelos/random_forest.Rdata')</pre>
```

14. Escoge un random forest para hacer las predicciones. Grafica la importancia de las variables. Interpreta



15. Genera las predicciones OOS para el random forest. Guardalas en la misma data.frame que los otros modelos

```
# predicciones continuas
X<-
    cell2cell_V %>%
    select(-customer, -churn)

X<-sparse.model.matrix(~.+0, data = X)</pre>
```

```
predicciones
predicciones %>%
  mutate(random_forest_prob = predict(random_forest, data = X)$predictions[,2])

rm(a, arbol, arbol_graf, arbol2, cl)

Warning in rm(a, arbol, arbol_graf, arbol2, cl): object 'a' not found

Warning in rm(a, arbol, arbol_graf, arbol2, cl): object 'arbol2' not found

save(predicciones, file = 'Bases output/predicciones.Rdata')
```

16. Estima un GBM.

- Encuenta el número de boosting rounds ideal B
- ullet Encuentra la profundidad de los árboles d
- Estima un grid de modelos para calibrar los dos hiperparametros

```
library(tidymodels)
library(xgboost)
X<-
   cell2cell_T %>%
   select(-customer, -churn)
X<-sparse.model.matrix(~.+0, data = X)</pre>
churn<-as.numeric(cell2cell_T$churn)-1</pre>
# Creating the grid that covers must of the hyper space
xgb_grid<-grid_latin_hypercube(</pre>
                 tree_depth(),
                 loss_reduction(),
                 sample_size = sample_prop(),
                 learn_rate(),
                 mtry(c(1,ncol(X))),
                 size = 15)
# XGBOOST matrix
training<-xgb.DMatrix(data = X, label = churn)</pre>
# Validation
X<-
   cell2cell_V %>%
   select(-customer, -churn)
X<-sparse.model.matrix(~.+0, data = X)</pre>
```

```
churn<-cell2cell_V$churn</pre>
validation<-xgb.DMatrix(data = X, label = churn)</pre>
# Watchlist
watchlist<-list(training = training, validation = validation)</pre>
# names(watchlist$validation)<- names(watchlist$training)</pre>
# transforming xgb_grid to have proper names
xgb_grid<-xgb_grid %>%
                rename(max_depth = tree_depth,
                       gamma = loss_reduction,
                       subsample = sample_size,
                       eta = learn rate,
                       colsample_bytree = mtry) %>%
                mutate(eval_metric = 'auc',
                       colsample_bytree = colsample_bytree/66)
# Modelo
listas<-map(1:15, ~as.list(xgb_grid[.,]))</pre>
a<-Sys.time()
xgb<-map(listas,</pre>
             function(x) {
               xgb.train(params = x,
                         data = training,
                         nrounds = 300,
                         objective = "binary:logistic",
                         early_stopping_rounds = 5,
                         verbose = 1,
                         watchlist = watchlist) })
[1] training-auc:0.647920 validation-auc:0.638442
Multiple eval metrics are present. Will use validation_auc for early stopping.
Will train until validation_auc hasn't improved in 5 rounds.
[2] training-auc:0.655253 validation-auc:0.643946
[3] training-auc:0.657465 validation-auc:0.646606
[4] training-auc:0.658609 validation-auc:0.647244
[5] training-auc:0.658525 validation-auc:0.647490
[6] training-auc:0.659565 validation-auc:0.647864
[7] training-auc:0.661414 validation-auc:0.649330
[8] training-auc: 0.661174
                            validation-auc:0.648968
[9] training-auc: 0.661262
                           validation-auc:0.649123
Γ107
       training-auc:0.661270
                                validation-auc:0.649535
[11]
       training-auc: 0.661469 validation-auc: 0.650153
       training-auc:0.661386 validation-auc:0.650080
Γ12]
[13]
       training-auc:0.661811 validation-auc:0.650208
       training-auc:0.662852 validation-auc:0.650594
[14]
[15]
       training-auc: 0.662729 validation-auc: 0.651047
       training-auc:0.662641 validation-auc:0.651204
[16]
[17]
       training-auc:0.662802 validation-auc:0.651015
[18]
       training-auc:0.663154 validation-auc:0.651188
```

```
[19]
        training-auc:0.663069
                                 validation-auc:0.651122
[20]
        training-auc:0.663149
                                 validation-auc:0.651502
        training-auc:0.663263
[21]
                                 validation-auc:0.651613
[22]
        training-auc:0.663768
                                 validation-auc:0.652130
[23]
        training-auc:0.663836
                                 validation-auc:0.652415
[24]
        training-auc:0.663840
                                 validation-auc:0.652376
[25]
        training-auc:0.663643
                                 validation-auc:0.652292
「26]
        training-auc:0.663836
                                 validation-auc:0.652258
[27]
        training-auc:0.663979
                                 validation-auc:0.652459
[28]
        training-auc:0.664070
                                 validation-auc:0.652422
[29]
        training-auc:0.663840
                                 validation-auc:0.652308
[30]
                                 validation-auc:0.652356
        training-auc:0.663807
[31]
                                 validation-auc:0.652489
        training-auc:0.663781
[32]
        training-auc:0.663771
                                 validation-auc:0.652291
[33]
        training-auc:0.663985
                                 validation-auc:0.652656
[34]
        training-auc:0.663969
                                 validation-auc:0.652700
[35]
        training-auc:0.664020
                                 validation-auc:0.652723
[36]
        training-auc:0.663987
                                 validation-auc:0.652704
[37]
        training-auc:0.664079
                                 validation-auc:0.653017
                                 validation-auc:0.653062
[38]
        training-auc:0.664021
[39]
        training-auc:0.664016
                                 validation-auc:0.653084
Γ407
        training-auc:0.664064
                                 validation-auc:0.653089
Γ417
                                 validation-auc:0.653071
        training-auc:0.664134
[42]
        training-auc:0.664210
                                 validation-auc:0.653074
[43]
        training-auc:0.664368
                                 validation-auc:0.653172
[44]
        training-auc:0.664401
                                 validation-auc:0.653275
[45]
        training-auc:0.664708
                                 validation-auc:0.653372
[46]
        training-auc:0.664720
                                 validation-auc:0.653368
[47]
                                 validation-auc:0.653394
        training-auc:0.664666
[48]
                                 validation-auc:0.653433
        training-auc:0.664707
[49]
                                 validation-auc:0.653481
        training-auc:0.664770
[50]
        training-auc:0.664743
                                 validation-auc:0.653389
[51]
                                 validation-auc:0.653390
        training-auc:0.664765
[52]
        training-auc:0.664742
                                 validation-auc:0.653485
                                 validation-auc:0.653568
[53]
        training-auc:0.664889
[54]
        training-auc:0.664816
                                 validation-auc:0.653567
[55]
        training-auc:0.664720
                                 validation-auc:0.653495
[56]
        training-auc:0.664863
                                 validation-auc:0.653574
[57]
        training-auc:0.664857
                                 validation-auc:0.653628
[58]
        training-auc:0.664827
                                 validation-auc:0.653604
[59]
        training-auc:0.664953
                                 validation-auc:0.653751
[60]
        training-auc:0.664934
                                 validation-auc:0.653604
[61]
        training-auc:0.664982
                                 validation-auc:0.653627
[62]
        training-auc:0.664951
                                 validation-auc:0.653560
[63]
        training-auc:0.664955
                                 validation-auc:0.653586
                                 validation-auc:0.653683
[64]
        training-auc:0.665043
Stopping. Best iteration:
[59]
        training-auc:0.664953
                                 validation-auc:0.653751
```

[1] training-auc:0.648573 validation-auc:0.626451 Multiple eval metrics are present. Will use validation_auc for early stopping. Will train until validation_auc hasn't improved in 5 rounds.

[2] training-auc:0.658551 validation-auc:0.638188

```
[3] training-auc:0.673811
                            validation-auc:0.648961
[4] training-auc:0.680175
                            validation-auc:0.651717
[5] training-auc:0.683983
                            validation-auc:0.653528
[6] training-auc:0.686979
                            validation-auc:0.655199
[7] training-auc:0.688592
                            validation-auc:0.655133
[8] training-auc: 0.690215
                            validation-auc:0.659423
[9] training-auc: 0.691342
                            validation-auc:0.659476
Γ107
        training-auc:0.693692
                                validation-auc:0.660160
Γ117
        training-auc:0.693783
                                 validation-auc:0.660417
[12]
        training-auc:0.695530
                                validation-auc:0.662007
[13]
        training-auc:0.695325
                                validation-auc:0.662112
[14]
                                validation-auc:0.661996
        training-auc:0.697257
[15]
        training-auc:0.697271
                                validation-auc:0.661977
[16]
        training-auc:0.697071
                                validation-auc:0.662162
[17]
        training-auc:0.696962
                                validation-auc:0.662839
[18]
        training-auc:0.696560
                                validation-auc:0.663050
[19]
        training-auc:0.698394
                                validation-auc:0.664661
[20]
        training-auc:0.698551
                                validation-auc:0.664938
[21]
        training-auc:0.697970
                                validation-auc:0.665033
[22]
        training-auc:0.697595
                                validation-auc:0.665110
[23]
        training-auc:0.698105
                                validation-auc:0.665915
Γ241
        training-auc:0.697995
                                validation-auc:0.665842
[25]
        training-auc:0.697583
                                validation-auc:0.666012
Γ261
        training-auc:0.697163
                                validation-auc:0.665882
                                validation-auc:0.665384
[27]
        training-auc:0.696865
[28]
        training-auc:0.697029
                                validation-auc:0.665428
                                validation-auc:0.664922
[29]
        training-auc:0.696834
[30]
        training-auc:0.696657
                                validation-auc:0.665057
Stopping. Best iteration:
[25]
        training-auc:0.697583
                                validation-auc:0.666012
[1] training-auc:0.629092
                            validation-auc:0.603514
Multiple eval metrics are present. Will use validation_auc for early stopping.
Will train until validation_auc hasn't improved in 5 rounds.
[2] training-auc:0.645093
                            validation-auc:0.605765
[3] training-auc:0.657370
                            validation-auc:0.610515
[4] training-auc:0.666984
                            validation-auc:0.619186
[5] training-auc:0.677609
                            validation-auc:0.626551
[6] training-auc:0.682118
                            validation-auc:0.633533
[7] training-auc:0.681807
                            validation-auc:0.629833
[8] training-auc:0.683806
                            validation-auc:0.628657
[9] training-auc:0.687251
                            validation-auc:0.628631
[10]
        training-auc:0.691523
                                validation-auc:0.630434
[11]
        training-auc:0.691946
                                validation-auc:0.632968
Stopping. Best iteration:
[6] training-auc:0.682118
                            validation-auc:0.633533
[1] training-auc:0.500000
                            validation-auc:0.500000
Multiple eval metrics are present. Will use validation_auc for early stopping.
Will train until validation_auc hasn't improved in 5 rounds.
[2] training-auc:0.500000
                            validation-auc:0.500000
[3] training-auc:0.500000
                            validation-auc:0.500000
```

```
[5] training-auc:0.500000
                            validation-auc:0.500000
[6] training-auc:0.500000
                            validation-auc:0.500000
Stopping. Best iteration:
[1] training-auc:0.500000
                            validation-auc:0.500000
[1] training-auc:0.500000
                            validation-auc:0.500000
Multiple eval metrics are present. Will use validation_auc for early stopping.
Will train until validation_auc hasn't improved in 5 rounds.
[2] training-auc:0.500000
                            validation-auc:0.500000
[3] training-auc:0.500000
                            validation-auc:0.500000
[4] training-auc:0.500000
                            validation-auc:0.500000
[5] training-auc:0.500000
                            validation-auc:0.500000
[6] training-auc:0.500000
                            validation-auc:0.500000
Stopping. Best iteration:
[1] training-auc:0.500000
                            validation-auc:0.500000
[1] training-auc:0.663945
                            validation-auc:0.623688
Multiple eval metrics are present. Will use validation_auc for early stopping.
Will train until validation_auc hasn't improved in 5 rounds.
[2] training-auc:0.684106
                            validation-auc:0.628627
[3] training-auc:0.706486
                            validation-auc:0.636827
[4] training-auc:0.710539
                            validation-auc:0.642265
[5] training-auc:0.720622
                            validation-auc:0.648821
[6] training-auc:0.719707
                            validation-auc:0.648780
[7] training-auc:0.725983
                            validation-auc:0.648488
[8] training-auc:0.732200
                            validation-auc:0.648082
[9] training-auc:0.737685
                            validation-auc:0.651266
[10]
        training-auc:0.740657
                                validation-auc:0.653223
[11]
        training-auc:0.743273
                                validation-auc:0.651995
[12]
       training-auc:0.745803
                                validation-auc:0.656492
[13]
       training-auc:0.747093
                                validation-auc:0.657539
[14]
       training-auc:0.748437
                                validation-auc:0.657553
Г15]
       training-auc:0.748987
                                validation-auc:0.657411
Г16Т
       training-auc:0.749284
                               validation-auc:0.657144
Γ17]
       training-auc:0.750866
                                validation-auc:0.656295
       training-auc:0.751530
Г187
                                validation-auc:0.655156
        training-auc:0.751486
[19]
                                validation-auc:0.656547
Stopping. Best iteration:
Γ147
       training-auc:0.748437
                                validation-auc:0.657553
[1] training-auc:0.614566
                            validation-auc:0.608029
Multiple eval metrics are present. Will use validation_auc for early stopping.
Will train until validation_auc hasn't improved in 5 rounds.
[2] training-auc:0.634041
                            validation-auc:0.628428
[3] training-auc:0.638050
                            validation-auc:0.631636
[4] training-auc:0.647608
                            validation-auc:0.639205
[5] training-auc:0.655020
                            validation-auc:0.644668
[6] training-auc:0.654699
                            validation-auc:0.644758
[7] training-auc:0.658061
                            validation-auc:0.646269
[8] training-auc:0.658935
                            validation-auc:0.647123
```

validation-auc:0.500000

[4] training-auc:0.500000

```
[9] training-auc:0.659997
                             validation-auc:0.648829
Γ107
        training-auc:0.660484
                                 validation-auc:0.650840
Г117
        training-auc:0.660658
                                 validation-auc:0.651289
[12]
        training-auc:0.662519
                                 validation-auc: 0.652941
Г137
        training-auc:0.663265
                                 validation-auc:0.653585
Г147
        training-auc:0.663574
                                 validation-auc:0.653462
Γ15]
        training-auc:0.663964
                                 validation-auc:0.653454
[16]
                                 validation-auc:0.654178
        training-auc:0.665201
Γ17]
        training-auc:0.665830
                                 validation-auc:0.655301
[18]
        training-auc:0.667497
                                 validation-auc:0.656995
[19]
        training-auc:0.667794
                                 validation-auc:0.656945
[20]
        training-auc:0.668790
                                 validation-auc:0.657901
        training-auc:0.669108
[21]
                                 validation-auc:0.658255
[22]
        training-auc:0.669187
                                 validation-auc:0.658380
[23]
        training-auc:0.669596
                                 validation-auc:0.658363
[24]
                                 validation-auc:0.658333
        training-auc:0.669648
[25]
        training-auc:0.669956
                                 validation-auc:0.658288
[26]
                                 validation-auc:0.658914
        training-auc:0.670361
[27]
        training-auc:0.670364
                                 validation-auc:0.658673
[28]
                                 validation-auc:0.659023
        training-auc:0.671016
[29]
        training-auc:0.671208
                                 validation-auc:0.658989
[30]
        training-auc:0.671198
                                 validation-auc:0.659562
Γ317
        training-auc:0.671241
                                 validation-auc:0.659865
「32]
        training-auc:0.671295
                                 validation-auc:0.659683
                                 validation-auc:0.659953
[33]
        training-auc:0.671398
[34]
        training-auc:0.672051
                                 validation-auc:0.660451
[35]
        training-auc:0.672464
                                 validation-auc:0.660640
[36]
        training-auc:0.672239
                                 validation-auc:0.660781
[37]
        training-auc:0.672234
                                 validation-auc:0.661186
[38]
        training-auc:0.672709
                                 validation-auc:0.661432
[39]
                                 validation-auc:0.661737
        training-auc:0.673040
Γ401
        training-auc:0.673820
                                 validation-auc:0.662073
[41]
        training-auc:0.674090
                                 validation-auc:0.662178
[42]
        training-auc:0.674080
                                 validation-auc:0.662351
[43]
        training-auc:0.673888
                                 validation-auc:0.662315
[44]
        training-auc:0.673764
                                 validation-auc:0.662189
[45]
        training-auc:0.673681
                                 validation-auc:0.662261
[46]
        training-auc:0.674046
                                 validation-auc:0.662658
Γ47]
                                 validation-auc:0.662912
        training-auc:0.674255
Γ487
        training-auc:0.674389
                                 validation-auc:0.663028
[49]
        training-auc:0.674862
                                 validation-auc:0.663665
[50]
                                 validation-auc:0.664101
        training-auc:0.675665
[51]
        training-auc:0.675414
                                 validation-auc:0.664126
[52]
        training-auc:0.675493
                                 validation-auc:0.664072
[53]
        training-auc:0.675966
                                 validation-auc:0.664574
[54]
                                 validation-auc:0.664660
        training-auc:0.676288
[55]
                                 validation-auc:0.664765
        training-auc:0.676500
[56]
        training-auc:0.676546
                                 validation-auc:0.664658
[57]
                                 validation-auc:0.664882
        training-auc:0.676660
[58]
        training-auc:0.676850
                                 validation-auc:0.664964
[59]
        training-auc:0.677068
                                 validation-auc:0.664974
[60]
                                 validation-auc:0.665183
        training-auc:0.677428
[61]
        training-auc:0.677749
                                 validation-auc:0.665345
[62]
        training-auc:0.677700
                                 validation-auc:0.665397
```

```
[63]
        training-auc:0.678041
                                 validation-auc:0.665452
[64]
        training-auc:0.678134
                                 validation-auc:0.665755
[65]
        training-auc:0.678334
                                 validation-auc:0.665813
[66]
        training-auc:0.678567
                                 validation-auc:0.665990
[67]
        training-auc:0.678699
                                 validation-auc:0.665920
[68]
        training-auc:0.678699
                                 validation-auc:0.665920
[69]
        training-auc:0.678748
                                 validation-auc:0.665996
[70]
        training-auc:0.679208
                                 validation-auc:0.666306
[71]
        training-auc:0.679443
                                 validation-auc:0.666380
[72]
        training-auc:0.679442
                                 validation-auc:0.666380
[73]
        training-auc:0.679529
                                 validation-auc:0.666374
[74]
                                 validation-auc:0.666374
        training-auc:0.679529
Γ75]
                                 validation-auc:0.666374
        training-auc:0.679529
[76]
        training-auc:0.679589
                                 validation-auc:0.666518
[77]
        training-auc:0.679684
                                 validation-auc:0.666589
[78]
        training-auc:0.679684
                                 validation-auc:0.666589
[79]
        training-auc:0.679753
                                 validation-auc:0.666688
[80]
        training-auc:0.680191
                                 validation-auc:0.666915
[81]
        training-auc:0.680306
                                 validation-auc:0.666901
[82]
                                 validation-auc:0.667159
        training-auc:0.680497
[83]
        training-auc:0.680497
                                 validation-auc:0.667159
[84]
        training-auc:0.680648
                                 validation-auc:0.667155
[85]
                                 validation-auc:0.667208
        training-auc:0.680862
[86]
        training-auc:0.680862
                                 validation-auc:0.667208
[87]
        training-auc:0.681315
                                 validation-auc:0.667459
[88]
        training-auc:0.681316
                                 validation-auc:0.667459
[89]
        training-auc:0.681809
                                 validation-auc:0.667621
[90]
        training-auc:0.681982
                                 validation-auc:0.667927
[91]
                                 validation-auc:0.668047
        training-auc:0.682085
[92]
                                 validation-auc:0.668321
        training-auc:0.682385
[93]
                                 validation-auc:0.668321
        training-auc:0.682385
[94]
        training-auc:0.682605
                                 validation-auc:0.668288
[95]
                                 validation-auc:0.668288
        training-auc:0.682605
[96]
        training-auc:0.682664
                                 validation-auc:0.668295
                                 validation-auc:0.668611
[97]
        training-auc:0.683014
[98]
        training-auc:0.683014
                                 validation-auc:0.668611
[99]
        training-auc:0.683308
                                 validation-auc:0.668705
Γ1007
        training-auc:0.683529
                                 validation-auc:0.669074
Γ1017
        training-auc:0.683668
                                 validation-auc:0.669007
[102]
                                 validation-auc:0.669291
        training-auc:0.683903
[103]
        training-auc:0.684203
                                 validation-auc:0.669513
[104]
        training-auc:0.684294
                                 validation-auc:0.669410
Γ105]
        training-auc:0.684294
                                 validation-auc:0.669410
[106]
        training-auc:0.684294
                                 validation-auc:0.669410
[107]
        training-auc:0.684294
                                 validation-auc:0.669410
                                 validation-auc:0.669402
        training-auc:0.684247
[108]
Stopping. Best iteration:
[103]
        training-auc:0.684203
                                 validation-auc:0.669513
```

[1] training-auc:0.500000 validation-auc:0.500000 Multiple eval metrics are present. Will use validation_auc for early stopping. Will train until validation_auc hasn't improved in 5 rounds.

[2] training-auc:0.503100 validation-auc:0.502011

```
[3] training-auc: 0.532068
                             validation-auc:0.516896
[4] training-auc:0.547334
                             validation-auc:0.520366
[5] training-auc:0.560379
                             validation-auc:0.526087
[6] training-auc:0.576267
                             validation-auc:0.529007
[7] training-auc:0.590902
                             validation-auc:0.536152
[8] training-auc:0.609945
                             validation-auc:0.546864
[9] training-auc: 0.618699
                             validation-auc:0.552446
Γ107
        training-auc:0.632552
                                 validation-auc:0.553571
Γ117
        training-auc:0.655997
                                 validation-auc:0.568075
[12]
        training-auc:0.663971
                                 validation-auc:0.569939
[13]
        training-auc:0.681185
                                 validation-auc:0.584985
[14]
                                 validation-auc:0.595802
        training-auc:0.694639
Γ15]
                                 validation-auc:0.604924
        training-auc:0.706450
[16]
        training-auc:0.716179
                                 validation-auc:0.612662
[17]
        training-auc:0.725371
                                 validation-auc:0.616712
[18]
        training-auc:0.730459
                                 validation-auc:0.620873
[19]
        training-auc:0.736406
                                 validation-auc:0.625043
[20]
        training-auc:0.740149
                                 validation-auc:0.623717
[21]
        training-auc:0.742613
                                 validation-auc:0.626264
[22]
                                 validation-auc:0.627191
        training-auc:0.746250
[23]
        training-auc:0.748279
                                 validation-auc:0.630074
[24]
        training-auc:0.748519
                                 validation-auc:0.629617
Γ251
                                 validation-auc:0.633663
        training-auc:0.752711
[26]
        training-auc:0.755323
                                 validation-auc:0.636267
[27]
        training-auc:0.755298
                                 validation-auc:0.636627
[28]
        training-auc:0.758794
                                 validation-auc:0.638982
[29]
        training-auc:0.761441
                                 validation-auc:0.641330
[30]
        training-auc:0.761851
                                 validation-auc:0.643343
[31]
                                 validation-auc:0.643524
        training-auc:0.764211
[32]
                                 validation-auc:0.644518
        training-auc:0.766918
[33]
                                 validation-auc:0.645344
        training-auc:0.767048
[34]
        training-auc:0.768362
                                 validation-auc:0.646397
[35]
                                 validation-auc:0.647493
        training-auc:0.770991
[36]
        training-auc:0.770740
                                 validation-auc:0.647263
                                 validation-auc:0.645355
[37]
        training-auc:0.771850
[38]
        training-auc:0.772314
                                 validation-auc:0.646153
[39]
        training-auc:0.772749
                                 validation-auc:0.645808
Γ407
        training-auc:0.775939
                                 validation-auc:0.648417
Γ417
        training-auc:0.776478
                                 validation-auc:0.648451
[42]
                                 validation-auc:0.649713
        training-auc:0.778214
[43]
        training-auc:0.778406
                                 validation-auc:0.649726
[44]
        training-auc:0.779017
                                 validation-auc:0.649891
[45]
        training-auc:0.777539
                                 validation-auc:0.649808
[46]
        training-auc:0.778601
                                 validation-auc:0.650148
[47]
        training-auc:0.779790
                                 validation-auc:0.649535
[48]
        training-auc:0.781595
                                 validation-auc:0.650610
[49]
                                 validation-auc:0.649615
        training-auc:0.782084
[50]
        training-auc:0.782346
                                 validation-auc:0.649302
[51]
        training-auc:0.781317
                                 validation-auc:0.649404
[52]
        training-auc:0.781628
                                 validation-auc:0.650248
[53]
        training-auc:0.783109
                                 validation-auc:0.649046
Stopping. Best iteration:
Γ487
        training-auc:0.781595
                                 validation-auc:0.650610
```

[1] training-auc:0.671824 validation-auc:0.578347
Multiple eval metrics are present. Will use validation_auc for early stopping.
Will train until validation auc hasn't improved in 5 rounds.

```
[2] training-auc:0.721618
                             validation-auc:0.596732
[3] training-auc:0.738992
                             validation-auc:0.612206
[4] training-auc:0.754698
                             validation-auc:0.618252
[5] training-auc:0.765397
                             validation-auc:0.625754
[6] training-auc:0.776044
                             validation-auc:0.629548
[7] training-auc:0.784051
                             validation-auc:0.630608
[8] training-auc:0.793233
                             validation-auc:0.631904
[9] training-auc:0.799366
                             validation-auc:0.632434
Γ107
                                 validation-auc:0.635421
        training-auc:0.803522
[11]
        training-auc:0.811694
                                 validation-auc:0.640965
Γ12]
        training-auc:0.813147
                                 validation-auc:0.642789
[13]
        training-auc:0.819084
                                 validation-auc:0.646209
[14]
        training-auc:0.823247
                                 validation-auc:0.648552
[15]
        training-auc:0.826908
                                 validation-auc:0.650113
Г167
        training-auc:0.830234
                                 validation-auc:0.652743
                                 validation-auc:0.653623
[17]
        training-auc:0.832979
Г187
        training-auc:0.833169
                                 validation-auc:0.655173
Г197
        training-auc:0.839412
                                 validation-auc:0.656432
[20]
        training-auc:0.839454
                                 validation-auc:0.657433
[21]
        training-auc:0.843898
                                 validation-auc:0.658163
[22]
        training-auc:0.844791
                                 validation-auc:0.658067
[23]
        training-auc:0.845992
                                 validation-auc:0.657969
[24]
        training-auc:0.846515
                                 validation-auc:0.658228
[25]
        training-auc:0.849269
                                 validation-auc:0.658195
[26]
                                 validation-auc:0.658440
        training-auc:0.849974
[27]
                                 validation-auc:0.659193
        training-auc:0.849406
[28]
                                 validation-auc:0.659285
        training-auc:0.851525
[29]
        training-auc:0.852148
                                 validation-auc:0.659212
[30]
                                 validation-auc:0.659243
        training-auc:0.851778
[31]
        training-auc:0.853762
                                 validation-auc:0.660593
                                 validation-auc:0.660710
[32]
        training-auc:0.853819
[33]
        training-auc:0.853484
                                 validation-auc:0.660573
Γ341
        training-auc: 0.853578
                                 validation-auc:0.660637
[35]
        training-auc:0.855520
                                 validation-auc:0.660169
[36]
        training-auc:0.855312
                                 validation-auc:0.660038
[37]
                                 validation-auc:0.661258
        training-auc:0.856179
[38]
        training-auc:0.855076
                                 validation-auc:0.661391
[39]
        training-auc:0.855091
                                 validation-auc:0.661585
Γ407
        training-auc:0.855020
                                 validation-auc:0.661655
[41]
        training-auc:0.856638
                                 validation-auc:0.661856
[42]
        training-auc:0.857477
                                 validation-auc:0.661449
[43]
                                 validation-auc:0.661366
        training-auc:0.857326
[44]
                                 validation-auc:0.661812
        training-auc:0.857875
[45]
        training-auc:0.857420
                                 validation-auc:0.662242
[46]
        training-auc:0.857682
                                 validation-auc:0.662037
[47]
        training-auc:0.858287
                                 validation-auc:0.662430
[48]
        training-auc:0.858250
                                 validation-auc:0.662654
[49]
        training-auc:0.857834
                                 validation-auc:0.662644
[50]
        training-auc:0.857512
                                 validation-auc:0.662692
[51]
                                 validation-auc:0.662229
        training-auc:0.856965
```

```
[52]
        training-auc:0.856732
                                 validation-auc:0.662404
[53]
        training-auc:0.857129
                                 validation-auc:0.662731
        training-auc:0.856986
[54]
                                 validation-auc:0.663115
[55]
        training-auc:0.858363
                                validation-auc:0.663905
[56]
        training-auc:0.858477
                                 validation-auc:0.664221
[57]
        training-auc:0.858276
                                 validation-auc:0.663917
[58]
        training-auc:0.858463
                                 validation-auc:0.664230
[59]
        training-auc:0.857999
                                 validation-auc:0.664402
[60]
        training-auc:0.858186
                                 validation-auc:0.664644
[61]
        training-auc:0.859537
                                 validation-auc:0.664912
[62]
        training-auc:0.860054
                                 validation-auc:0.665084
[63]
                                 validation-auc:0.665304
        training-auc:0.860158
[64]
        training-auc:0.859811
                                 validation-auc:0.664926
[65]
        training-auc:0.859695
                                 validation-auc:0.664707
[66]
        training-auc:0.859564
                                 validation-auc:0.664583
[67]
        training-auc:0.860285
                                 validation-auc:0.664894
[68]
        training-auc:0.860196
                                 validation-auc:0.664855
Stopping. Best iteration:
[63]
        training-auc:0.860158
                                 validation-auc:0.665304
[1] training-auc:0.547003
                            validation-auc:0.540599
Multiple eval metrics are present. Will use validation_auc for early stopping.
Will train until validation_auc hasn't improved in 5 rounds.
[2] training-auc: 0.617976
                            validation-auc:0.613925
[3] training-auc: 0.623669
                             validation-auc:0.617871
[4] training-auc:0.626762
                            validation-auc:0.619665
[5] training-auc:0.639286
                            validation-auc:0.632621
[6] training-auc:0.641047
                            validation-auc:0.635096
[7] training-auc:0.640405
                             validation-auc:0.633811
[8] training-auc:0.640897
                             validation-auc:0.632769
[9] training-auc:0.639814
                             validation-auc:0.634788
[10]
        training-auc:0.639821
                                 validation-auc:0.634170
[11]
        training-auc:0.640547
                                 validation-auc:0.633455
Stopping. Best iteration:
[6] training-auc:0.641047
                            validation-auc:0.635096
[1] training-auc:0.585406
                            validation-auc:0.573614
Multiple eval metrics are present. Will use validation_auc for early stopping.
Will train until validation_auc hasn't improved in 5 rounds.
[2] training-auc:0.597084
                            validation-auc:0.587823
[3] training-auc: 0.602515
                             validation-auc:0.592376
[4] training-auc:0.605622
                             validation-auc:0.593560
[5] training-auc:0.602263
                            validation-auc:0.588977
[6] training-auc:0.600952
                            validation-auc:0.588109
[7] training-auc:0.601757
                             validation-auc:0.588495
[8] training-auc: 0.623748
                             validation-auc:0.609997
[9] training-auc: 0.625773
                             validation-auc:0.611136
[10]
                                validation-auc:0.607579
        training-auc:0.625019
[11]
        training-auc:0.624568
                                 validation-auc:0.607400
[12]
        training-auc:0.622750
                                 validation-auc:0.606632
Г137
        training-auc:0.629835
                                validation-auc:0.614774
Γ147
        training-auc:0.630680
                                validation-auc:0.616947
```

```
[16]
        training-auc:0.628835
                                 validation-auc:0.615976
        training-auc:0.626721
                                 validation-auc:0.613869
Γ17]
        training-auc:0.633982
                                 validation-auc:0.621505
[18]
Г197
        training-auc:0.633225
                                 validation-auc:0.620730
[20]
        training-auc:0.633390
                                 validation-auc:0.620630
[21]
        training-auc:0.632704
                                 validation-auc:0.619253
Γ221
        training-auc:0.636093
                                 validation-auc:0.621830
[23]
        training-auc:0.636262
                                 validation-auc:0.621777
[24]
        training-auc:0.635337
                                 validation-auc:0.619971
[25]
        training-auc:0.639376
                                 validation-auc:0.624753
[26]
                                 validation-auc:0.623343
        training-auc:0.637931
[27]
        training-auc:0.640452
                                 validation-auc:0.626098
[28]
        training-auc:0.639933
                                 validation-auc:0.625260
[29]
        training-auc:0.640607
                                 validation-auc:0.626167
[30]
        training-auc:0.641784
                                 validation-auc:0.627031
[31]
        training-auc:0.642006
                                 validation-auc:0.627501
[32]
        training-auc:0.643331
                                 validation-auc:0.629144
[33]
        training-auc:0.642559
                                 validation-auc:0.628225
                                 validation-auc:0.629540
Γ341
        training-auc:0.643204
[35]
        training-auc:0.642423
                                 validation-auc:0.628244
[36]
        training-auc:0.642294
                                 validation-auc:0.628030
[37]
        training-auc:0.642639
                                 validation-auc:0.628405
[38]
        training-auc:0.642987
                                 validation-auc:0.629336
[39]
        training-auc:0.642655
                                 validation-auc:0.628579
Stopping. Best iteration:
[34]
        training-auc:0.643204
                                 validation-auc:0.629540
                            validation-auc:0.500000
[1] training-auc:0.500000
Multiple eval metrics are present. Will use validation_auc for early stopping.
Will train until validation_auc hasn't improved in 5 rounds.
[2] training-auc:0.500000
                             validation-auc:0.500000
[3] training-auc:0.500000
                             validation-auc:0.500000
[4] training-auc:0.500000
                             validation-auc:0.500000
[5] training-auc:0.500000
                            validation-auc:0.500000
[6] training-auc:0.500000
                            validation-auc:0.500000
Stopping. Best iteration:
[1] training-auc:0.500000
                            validation-auc:0.500000
[1] training-auc:0.500000
                            validation-auc:0.500000
Multiple eval metrics are present. Will use validation_auc for early stopping.
Will train until validation_auc hasn't improved in 5 rounds.
[2] training-auc:0.500000
                             validation-auc:0.500000
[3] training-auc:0.505887
                            validation-auc:0.504918
[4] training-auc:0.532905
                             validation-auc:0.516533
[5] training-auc:0.561320
                             validation-auc:0.525615
[6] training-auc:0.584028
                             validation-auc:0.537137
[7] training-auc:0.613069
                             validation-auc:0.545386
[8] training-auc:0.644133
                             validation-auc:0.556239
[9] training-auc:0.671772
                             validation-auc:0.571911
Γ107
        training-auc:0.697755
                                 validation-auc:0.584741
Γ117
                                validation-auc:0.594233
        training-auc:0.716735
```

validation-auc:0.615225

[15]

training-auc:0.628477

```
[12]
        training-auc:0.731382
                                 validation-auc:0.603349
[13]
        training-auc:0.742693
                                 validation-auc:0.610279
Γ147
        training-auc:0.754901
                                 validation-auc:0.616778
Г157
        training-auc:0.765559
                                 validation-auc: 0.621645
Г167
        training-auc:0.772621
                                 validation-auc:0.625780
Γ17]
        training-auc:0.779824
                                 validation-auc:0.628205
Г187
        training-auc:0.786830
                                 validation-auc:0.633695
Г197
                                 validation-auc:0.635470
        training-auc:0.794678
[20]
        training-auc:0.797672
                                 validation-auc:0.636909
[21]
        training-auc:0.801385
                                 validation-auc:0.639978
[22]
        training-auc:0.805242
                                 validation-auc:0.642608
[23]
        training-auc:0.809638
                                 validation-auc:0.643680
[24]
                                 validation-auc:0.643840
        training-auc:0.812309
[25]
        training-auc:0.815227
                                 validation-auc:0.646268
[26]
        training-auc:0.818476
                                 validation-auc:0.645846
[27]
                                 validation-auc:0.647049
        training-auc:0.820612
[28]
        training-auc:0.821932
                                 validation-auc:0.649685
[29]
                                 validation-auc:0.649469
        training-auc:0.824255
[30]
        training-auc:0.826379
                                 validation-auc:0.649871
Γ317
                                 validation-auc:0.652003
        training-auc: 0.827747
[32]
        training-auc:0.829904
                                 validation-auc:0.650957
[33]
        training-auc:0.830664
                                 validation-auc:0.653805
「347
        training-auc:0.832300
                                 validation-auc:0.652645
[35]
        training-auc:0.834222
                                 validation-auc:0.656071
                                 validation-auc:0.656241
[36]
        training-auc:0.835559
[37]
        training-auc:0.837454
                                 validation-auc:0.657901
[38]
        training-auc:0.839575
                                 validation-auc:0.658169
[39]
        training-auc:0.840138
                                 validation-auc:0.657762
[40]
        training-auc:0.840486
                                 validation-auc:0.656847
[41]
                                 validation-auc:0.658313
        training-auc:0.841740
[42]
                                 validation-auc:0.658804
        training-auc:0.843041
[43]
        training-auc:0.844536
                                 validation-auc:0.658791
[44]
        training-auc:0.844752
                                 validation-auc:0.659862
[45]
        training-auc:0.845801
                                 validation-auc:0.660843
[46]
        training-auc:0.846381
                                 validation-auc:0.659555
                                 validation-auc:0.659646
[47]
        training-auc:0.847726
[48]
        training-auc:0.848617
                                 validation-auc:0.660147
[49]
        training-auc:0.849370
                                 validation-auc:0.661999
[50]
                                 validation-auc:0.661885
        training-auc:0.848635
[51]
        training-auc:0.848699
                                 validation-auc:0.662804
[52]
        training-auc:0.849414
                                 validation-auc:0.664328
[53]
                                 validation-auc:0.666040
        training-auc:0.849850
Γ541
        training-auc:0.850318
                                 validation-auc:0.666407
[55]
        training-auc:0.850340
                                 validation-auc:0.667227
[56]
        training-auc:0.851390
                                 validation-auc:0.666734
[57]
                                 validation-auc:0.668139
        training-auc:0.851721
[58]
                                 validation-auc:0.666802
        training-auc:0.851843
[59]
        training-auc:0.852775
                                 validation-auc:0.667668
[60]
                                 validation-auc:0.667989
        training-auc:0.853172
[61]
        training-auc:0.853466
                                 validation-auc:0.667483
Γ62]
        training-auc:0.853285
                                 validation-auc:0.667054
Stopping. Best iteration:
[57]
        training-auc:0.851721
                                 validation-auc:0.668139
```

[1] training-auc:0.650557 validation-auc:0.574586
Multiple eval metrics are present. Will use validation_auc for early stopping.
Will train until validation auc hasn't improved in 5 rounds.

```
[2] training-auc:0.715705
                             validation-auc:0.604836
[3] training-auc:0.743575
                             validation-auc:0.617012
[4] training-auc:0.767385
                             validation-auc:0.627971
[5] training-auc:0.778021
                             validation-auc:0.639153
[6] training-auc:0.788293
                             validation-auc:0.639248
[7] training-auc:0.797726
                             validation-auc:0.645065
[8] training-auc:0.803255
                             validation-auc:0.646696
[9] training-auc:0.806047
                             validation-auc:0.650041
Γ107
        training-auc:0.811731
                                 validation-auc:0.654138
[11]
        training-auc:0.815468
                                 validation-auc:0.654327
Γ12]
        training-auc:0.817084
                                 validation-auc:0.657988
[13]
        training-auc:0.816929
                                 validation-auc:0.657789
[14]
        training-auc:0.816994
                                 validation-auc:0.659188
[15]
        training-auc:0.817936
                                 validation-auc:0.660417
Г167
        training-auc:0.819505
                                 validation-auc:0.661701
                                 validation-auc:0.660650
[17]
        training-auc: 0.823850
Г187
        training-auc:0.826763
                                 validation-auc:0.661821
Г197
        training-auc:0.828928
                                 validation-auc:0.661897
[20]
        training-auc:0.829287
                                 validation-auc:0.663855
[21]
        training-auc:0.831157
                                 validation-auc:0.664204
[22]
        training-auc:0.832326
                                 validation-auc:0.664082
[23]
        training-auc:0.833083
                                 validation-auc:0.664511
[24]
        training-auc:0.833610
                                 validation-auc:0.665054
[25]
        training-auc:0.834233
                                 validation-auc:0.665765
[26]
                                 validation-auc:0.665856
        training-auc:0.834135
[27]
                                 validation-auc:0.666064
        training-auc:0.834332
[28]
                                 validation-auc:0.666393
        training-auc:0.835369
[29]
        training-auc:0.836663
                                 validation-auc:0.666567
[30]
                                 validation-auc:0.666625
        training-auc:0.837001
[31]
        training-auc:0.838512
                                 validation-auc:0.667472
                                 validation-auc:0.667684
[32]
        training-auc:0.838879
[33]
        training-auc:0.839682
                                 validation-auc:0.668037
Γ341
        training-auc:0.839276
                                 validation-auc:0.668107
[35]
        training-auc:0.840069
                                 validation-auc:0.668416
[36]
        training-auc:0.840515
                                 validation-auc:0.668781
[37]
                                 validation-auc:0.668989
        training-auc:0.840807
[38]
        training-auc:0.840999
                                 validation-auc:0.669797
[39]
        training-auc:0.840963
                                 validation-auc:0.669565
Γ407
        training-auc:0.841488
                                 validation-auc:0.670211
[41]
        training-auc:0.841918
                                 validation-auc:0.670455
[42]
        training-auc:0.841428
                                 validation-auc:0.670724
[43]
                                 validation-auc:0.670831
        training-auc:0.841461
[44]
                                 validation-auc:0.670727
        training-auc:0.841228
[45]
        training-auc:0.841436
                                 validation-auc:0.670781
[46]
        training-auc:0.841154
                                 validation-auc:0.671008
[47]
        training-auc:0.841282
                                 validation-auc:0.670595
[48]
        training-auc:0.841348
                                 validation-auc:0.671076
[49]
        training-auc:0.841635
                                 validation-auc:0.670968
[50]
        training-auc:0.842650
                                 validation-auc:0.671142
[51]
                                 validation-auc:0.671181
        training-auc: 0.842758
```

```
[52]
        training-auc:0.842624
                                 validation-auc:0.670992
[53]
        training-auc:0.843204
                                 validation-auc: 0.671195
        training-auc:0.843658
                                 validation-auc:0.671335
Γ541
[55]
        training-auc:0.843617
                                 validation-auc:0.671415
[56]
        training-auc:0.843446
                                 validation-auc:0.671658
[57]
        training-auc:0.843458
                                 validation-auc:0.672030
[58]
        training-auc:0.843359
                                 validation-auc:0.671796
[59]
        training-auc:0.843125
                                 validation-auc:0.672021
[60]
        training-auc:0.843650
                                 validation-auc:0.672454
[61]
        training-auc:0.843900
                                 validation-auc:0.672362
[62]
        training-auc:0.844091
                                 validation-auc:0.672525
[63]
                                 validation-auc:0.672318
        training-auc:0.843884
[64]
                                 validation-auc:0.672385
        training-auc:0.843995
[65]
        training-auc:0.843899
                                 validation-auc:0.672775
[66]
        training-auc:0.843980
                                 validation-auc:0.672770
[67]
        training-auc:0.844146
                                 validation-auc:0.672561
[68]
        training-auc:0.844169
                                 validation-auc:0.672739
[69]
        training-auc:0.844322
                                 validation-auc:0.672704
        training-auc:0.844621
[70]
                                 validation-auc:0.673138
                                 validation-auc:0.673236
[71]
        training-auc:0.844682
[72]
        training-auc:0.844807
                                 validation-auc:0.673297
[73]
        training-auc:0.844944
                                 validation-auc:0.673582
[74]
        training-auc:0.845171
                                 validation-auc:0.673613
[75]
        training-auc:0.844974
                                 validation-auc:0.673522
[76]
        training-auc:0.844989
                                 validation-auc:0.673888
[77]
        training-auc:0.845176
                                 validation-auc:0.673840
[78]
        training-auc:0.845776
                                 validation-auc:0.673942
[79]
        training-auc:0.845659
                                 validation-auc:0.673831
[80]
                                 validation-auc:0.673903
        training-auc:0.845358
[81]
                                 validation-auc:0.673891
        training-auc:0.845467
[82]
                                 validation-auc:0.673869
        training-auc:0.845308
[83]
        training-auc:0.845213
                                 validation-auc:0.673968
[84]
                                 validation-auc:0.674235
        training-auc:0.845338
[85]
        training-auc:0.845499
                                 validation-auc:0.674265
                                 validation-auc:0.674021
[86]
        training-auc:0.845421
[87]
        training-auc:0.845186
                                 validation-auc:0.674195
[88]
        training-auc:0.845142
                                 validation-auc:0.673978
[89]
        training-auc:0.845190
                                 validation-auc:0.673859
[90]
        training-auc:0.845124
                                 validation-auc:0.674085
Stopping. Best iteration:
        training-auc:0.845499
                                 validation-auc:0.674265
```

[1] training-auc:0.573126 validation-auc:0.576189
Multiple eval metrics are present. Will use validation_auc for early stopping.
Will train until validation_auc hasn't improved in 5 rounds.

```
[2] training-auc:0.599735
                            validation-auc:0.600864
[3] training-auc:0.608227
                            validation-auc:0.609918
[4] training-auc: 0.606751
                            validation-auc:0.607534
[5] training-auc:0.608457
                            validation-auc:0.610620
[6] training-auc:0.608774
                            validation-auc:0.610362
[7] training-auc:0.607766
                            validation-auc:0.608712
[8] training-auc:0.613957
                            validation-auc:0.615430
[9] training-auc:0.617968
                            validation-auc:0.618522
```

```
[10]
         training-auc:0.619291
                                    validation-auc:0.620146
Γ117
         training-auc:0.615331
                                    validation-auc:0.616558
         training-auc:0.616702
[12]
                                    validation-auc:0.617512
[13]
         training-auc:0.610980
                                    validation-auc:0.610975
[14]
         training-auc:0.617599
                                    validation-auc:0.617873
[15]
         training-auc:0.616563
                                    validation-auc:0.616662
Stopping. Best iteration:
[10]
         training-auc:0.619291
                                    validation-auc:0.620146
Sys.time() -a
Time difference of 56.67389 secs
save(xgb, xgb_grid, training, watchlist, file = "Modelos/xgb.Rdata")
# Winning combination
params xgb<-map dfr(xgb, ~.$params)</pre>
params_xgb<-bind_cols(params_xgb, auc = map_dbl(xgb, function(x) x$best_score))</pre>
params_xgb$model_number<-seq(1:15)</pre>
# tabla
kable(params_xgb)
\max_{dep} dep_{de} de
                  subsample
                              eta
                                   colsample by texed metrio bjective
                                                                       validate parametersic
                                                                                              model number
                                                                                                     1
        0.000000000.85718600.0000778 0.8939394
                                                           binary:logisticTRUE
                                                                                      0.653751
                                                auc
        0.0529435\, 0.75549470.0000020\ 0.6060606
                                                           binary:logisticTRUE
                                                                                                     2
                                                                                      0.666012
                                                auc
        0.0001262\, 0.6849654 0.0132164\ 0.1666667
                                                           binary:logisticTRUE
                                                                                                     3
                                                auc
                                                                                      0.633533
    9
        0.0000022\,0.61348570.0000000\,\,\,0.6969697
                                                           binary:logisticTRUE
                                                                                                     4
                                                auc
                                                                                      0.500000
    15
        0.20041570.80691700.00000000\ 0.0757576
                                                auc
                                                           binary:logisticTRUE
                                                                                      0.500000
                                                                                                     5
    8
        0.0002120\, 0.93512260.0002485\, 0.3484848
                                                           binary:logisticTRUE
                                                                                                     6
                                                                                      0.657553
                                                auc
                                                                                                     7
    5
        13.823486 0.32742630.0687369 0.4393939
                                                auc
                                                           binary:logisticTRUE
                                                                                      0.669513
    13
        4.9568172\, 0.38439210.0000000\,\, 0.2575758
                                                           binary:logisticTRUE
                                                                                                     8
                                                auc
                                                                                      0.650610
                                                                                                     9
    12
        0.0000155\, 0.4180194 0.0000195\,\, 0.4848485
                                                           binary:logisticTRUE
                                                                                      0.665304
                                                auc
    3
        0.0000000\,0.52504370.0037858\,\, 0.3030303
                                                auc
                                                           binary:logisticTRUE
                                                                                      0.635096
                                                                                                    10
    3
        0.01805370.11689340.0008345\ 0.1363636
                                                           binary:logisti&RUE
                                                                                                    11
                                                                                      0.629540
                                                auc
    10
        0.000000000.18838170.0000000000.6515152
                                                           binary:logisticTRUE
                                                                                                    12
                                                auc
                                                                                      0.500000
                                                                                      0.668139
    14
        0.0000004\, 0.2629531 \\ 0.0000000\,\, 0.9545455
                                                           binary:logisticΓRUE
                                                                                                    13
                                                auc
        0.0000000\,0.46505650.0000002\,\,0.7424242
                                                           binary:logisticTRUE
    11
                                                                                      0.674265
                                                                                                    14
                                                auc
                                                                                      0.620146
        0.00103330.99023040.00000050.8333333
                                                           binary:logisticTRUE
                                                                                                    15
                                                auc
# Quedandome con el ganador
a<-pull(params_xgb %>% arrange(desc(auc)) %>% dplyr::slice(1) %>% select(model_number))
xgb<-xgb[[1]]
# Predicting
# Validation
X<-
   cell2cell_V %>%
```

select(-customer, -churn)

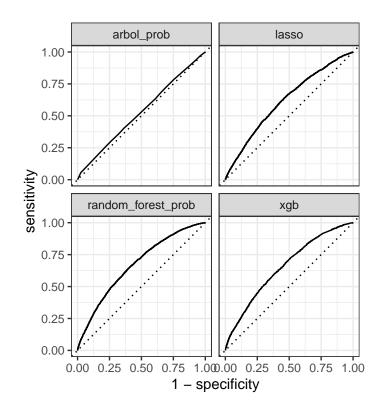
X<-sparse.model.matrix(~.+0, data = X)</pre>

```
predicciones<-
  predicciones %>%
  mutate(xgb = predict(xgb, newdata = X))

save(predicciones, file = 'Bases output/predicciones.Rdata')
```

17 (4 pts). Genera graficas de las curvas ROC para los 4 modelos. Cual parece ser mejor?

```
# Factor truth
predicciones<-
  predicciones %>%
  mutate(churn = factor(churn, levels = c('1', '0')))
# ROC para cada una
predicciones1<-
  predicciones %>%
  pivot_longer(cols = c("lasso", "arbol_prob", "random_forest_prob", "xgb"),
                names_to = 'modelo',
                values_to = 'pred')
bases<-predicciones1 %>% split(.$modelo)
rocs < -map2_dfr(.x = bases,
               y = names(bases),
               function(x,y) roc_curve(data = x, churn, pred) %>%
                  mutate(modelo = y))
ggplot(rocs, aes(1-specificity, y = sensitivity))+
   geom_path()+
   geom_abline(lty =3)+coord_equal()+theme_bw()+
  facet_wrap(~modelo)
```



18. Genera una tabla con el AUC ROC. Cuál es el mejor modelo?

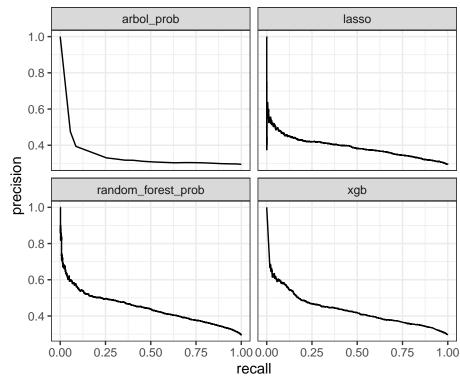
El random forest marginalmente sobre el XGB

.metric	.estimator	.estimate	modelo
roc_auc roc_auc roc_auc roc_auc	binary	0.6174667	arbol_prob lasso random_forest_prob xgb

19 (2 pts). Genera las gráficas de las curvas precission recall para los 4 modelos. Cuál parece ser mejor ahora?

Ahora el XGB parece ser mejor que el random forest

```
geom_path()+
coord_equal()+theme_bw()+
facet_wrap(~modelo)
```



.metric	.estimator	.estimate	modelo
pr_auc	binary	0.3445663	arbol_prob
pr_auc	binary	0.3890416	lasso
pr_auc	binary	0.4445194	$random_forest_prob$
pr_auc	binary	0.4338018	xgb

20 (2pts). Escoge un punto de corte para generar predicciones categoricas para el LASSO basado en la Curva ROC. Genera las matrices de confusión para cada modelo. Compáralas. Qué tipo de error es mas pernicioso?

```
# Cortes usando ROC
cortes<-
   rocs %>%
   group_by(modelo) %>%
   filter(sensitivity >= 0.80) %>%
   arrange(desc(specificity)) %>%
   dplyr::slice(1)
```

Table 6: Matriz de Confusión LASSO

	0	1
0 1	0.34 0.66	0.2

kable(prop.table(table(predicciones\$arbol_class, as.numeric(as.character(predicciones\$churn))), margin

Table 7: Matriz de Confusión Prune Tree

	0	1
0	0.64	0.6
_	0.00	0.1

kable(prop.table(table(predicciones\$rf_cat, as.numeric(as.character(predicciones\$churn))), margin = 2),

Table 8: Matriz de Confusión RF

	0	1
0 1	0.42 0.58	0.2
1	0.00	0.0

kable(prop.table(table(predicciones\$xgb_cat, as.numeric(as.character(predicciones\$churn))), margin = 2)

Table 9: Matriz de Confusión XGB

	0	1
0	0.39	0.2
1	0.61	0.8

21 (4pts). Construye una lift table. Esto es, para 20 grupos del score predecido de manera decreciente, genera 1) El promedio de las predicciones, 2) el promedio del churn rate observado. Estima el lift:

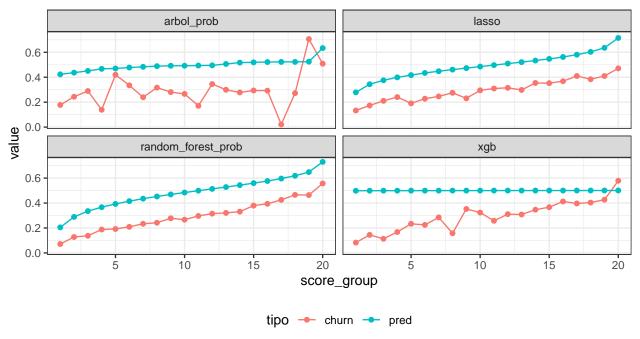
$$lift_k = \frac{churn \ rate_k}{churn \ rate \ promedio}$$

Donde churn rate promedio es el promedio global. Muesta la tabla. Que te dice el lift intuitivamente

Intuitivamente, el lift me dice si el nivel de churn observado es más alto en scores más altos o no. Esperarías ver una relación monotónica entre el lift y el score promedio

```
# ROC para cada una
predicciones1<-
  predicciones %>%
  pivot_longer(cols = c("lasso", "arbol_prob", "random_forest_prob", "xgb"),
                names to = 'modelo',
                values_to = 'pred')
predicciones1<-
  predicciones1 %>%
  group_by(modelo) %>%
  mutate(score_group = ntile(x = pred, 20)) %>%
  group_by(modelo, score_group) %>%
   summarise(pred = mean(pred),
             churn = mean(as.numeric(as.character(churn))))
base_grafica<-
  predicciones1 %>%
  pivot_longer(cols = c(pred, churn), names_to = 'tipo', values_to = 'value')
ggplot(base_grafica, aes(score_group, value, fill = tipo, color = tipo))+
  geom_point()+geom_line()+
  facet_wrap(~modelo)+
   theme_bw()+
  labs(title = 'Relación Score realidad')+
  theme(legend.position = 'bottom')
```

Relación Score realidad



22 (4pts). Construye un Gain table. Esto es: Cuántas personas detectarías con el modelo del total de churned users al buscar al x% de la población? Como se compara esto para una selección aleatoria?

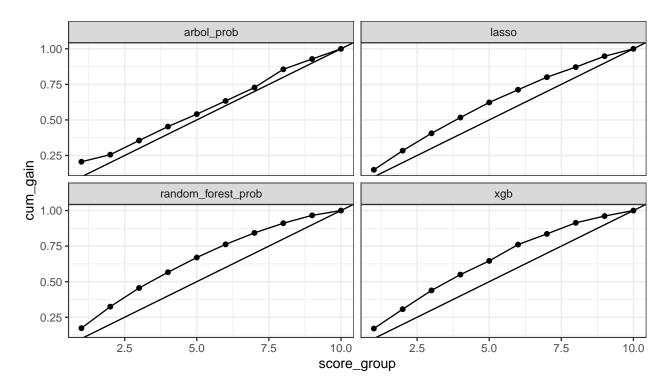
Ejemplo: Si tengo 10% de churn y tengo 10 grupos:

- Si focalizo al 10% aleatoriamente, voy a obtener el 10% de la población churned.
- Si focalizo al 20% aleatoriamente, voy a obtener el 20% de la población churned.
- Si focalizo al 10% usando al 10% de la población con score predecido mas alto, que porcentaje obtengo?
- Como se compara tu modelo vs el modelo aleatorio

```
# Gain
predicciones1<-
  predicciones %>%
  pivot_longer(cols = c("lasso", "arbol_prob", "random_forest_prob", "xgb"),
                names_to = 'modelo',
                values_to = 'pred')
gain<-
  predicciones1 %>%
  group_by(modelo) %>%
  mutate(score_group = ntile(x = pred, 10),
          total churn = sum(as.numeric(as.character(churn)))) %>%
  ungroup() %>%
   group_by(modelo, score_group) %>%
   summarise(gain = sum(as.numeric(as.character(churn)))) %>%
  group_by(modelo) %>%
  mutate(total_churn = sum(gain),
         score_group = abs(score_group-10)+1,
         gain = gain/total_churn) %>%
```

```
group_by(modelo) %>%
arrange(score_group) %>%
mutate(cum_gain = cumsum(gain))

# Graficas
ggplot(gain, aes(score_group, cum_gain))+geom_point()+geom_line()+
    geom_abline(intercept = 0 ,slope = 1/10)+facet_wrap(~modelo)+
    theme_bw()
```



23 (2pts). Calcula el AUC Gain del mejor modelo. Interpreta

[1] 0.5998177

```
library(pracma)
bases <- gain %>% split(.$modelo)
map(bases, ~trapz(.$score_group, .$cum_gain)/10)

$arbol_prob
[1] 0.5353949

$lasso
[1] 0.5736817

$random_forest_prob
[1] 0.6085541

$xgb
```

24. Concluye. Que estrategia harías con este modelo? Cómo generarías valor a partir de el?

Haría una estrategia focalizada de prevencion de churn con el modelo usando el Random Forest. Se que estaré atacando al 80% de los casos (recall) y que la gente que ataque tendré una precisión de $\sim 34\%$. Al ser una estrategia que no genera dolor, no hay problema con tener baja precisión. Así mismo, puedo ver que con sólo tratar al 30% de la base, puedo capturar al $\sim 50\%$ de la base de churn users!!!