Problem 134

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1 Definition

Given the positive integers, x, y, and z, are consecutive terms of an arithmetic progression, the least value of the positive integer, n, for which the equation, $x^2 - y^2 - z^2 = n$, has exactly two solutions is n = 27:

$$34^2 - 27^2 - 20^2 = 12^2 - 9^2 - 6^2 = 27 (1)$$

It turns out that n = 1155 is the least value which has exactly ten solutions.

How many values of n less than one million have exactly ten distinct solutions?

2 Solution(s) and proof

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