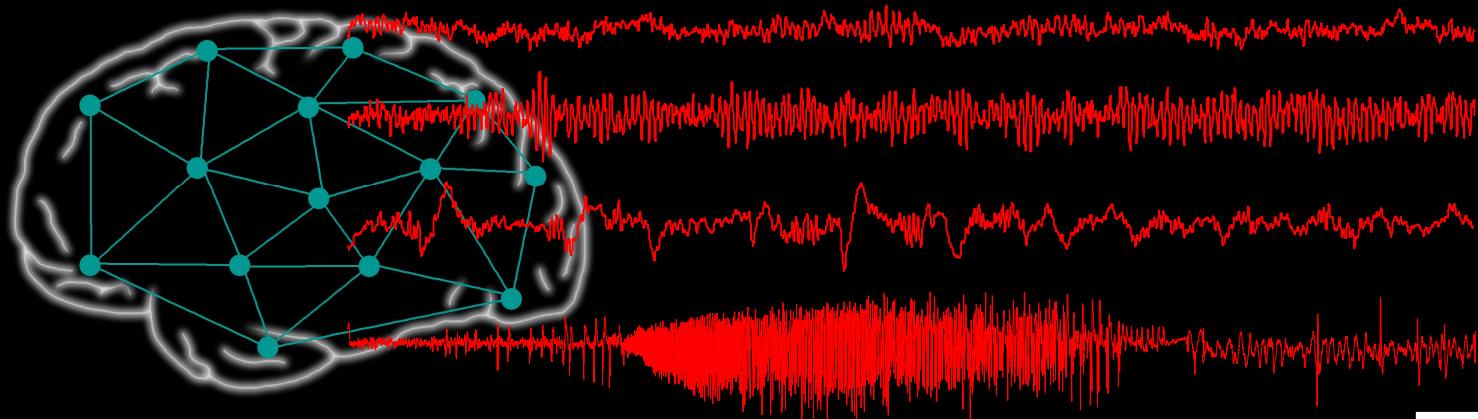


Long-term Dynamics of Large-scale Epileptic Brain Networks

Klaus Lehnertz



IZKS
Interdisciplinary Center
for Complex Systems



- Dept. of Epileptology
 - Neurophysics Group
- University of Bonn, Germany**



Helmholtz-Institute
for Radiation- and
Nuclear Physics



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Complex Network Brain

neurons: $\sim 10^{10}$

synapses/neuron: $\sim 10^3 - 10^4$

length of all connections: $\sim 10^7 - 10^9$ m

($\sim 2.5 \times$ distance earth-moon)

connectivity factor: $\sim 10^{-6}$ (adult)

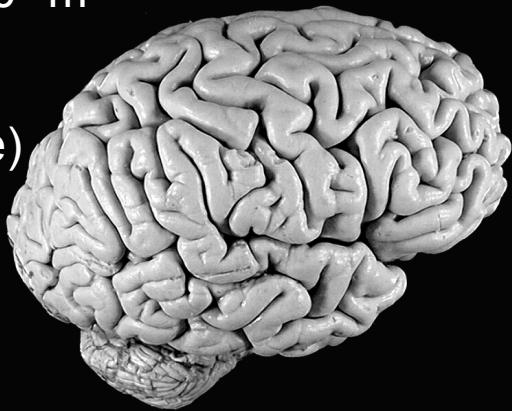
connectivity factor: $\sim 10^{-4}$ (juvenile)

ion channels / neuron: $\sim 10^2 - 10^3$

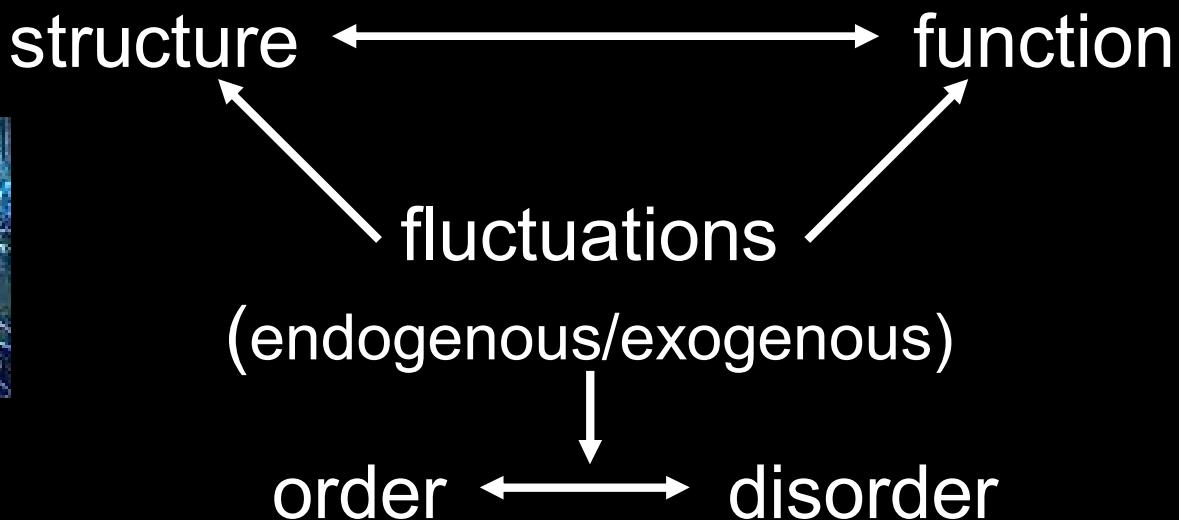
neurotransmitter &

other active substances: ~ 50

glia cells: ~ 3 -fold # neurons



control; movement;
perception; attention;
learning; memory;
knowledge; emotions;
motivation; language;
thinking; planning;
personality; self-identity;
consciousness; ...;
dysfunctions



Epilepsy

- Greek term for *seizure*; disease first mentioned ~ 1750 BC
- ~ 1 % of world population suffers from epilepsy
- famous people suffering from epilepsy:
Sokrates, Alexander the Great, Julius Caesar, Lenin,
Flaubert, Dostojevski, Carroll, Poe, Berlioz, Paganini,
Händel, van Gogh, Newton, Pascal, Helmholtz, Nobel

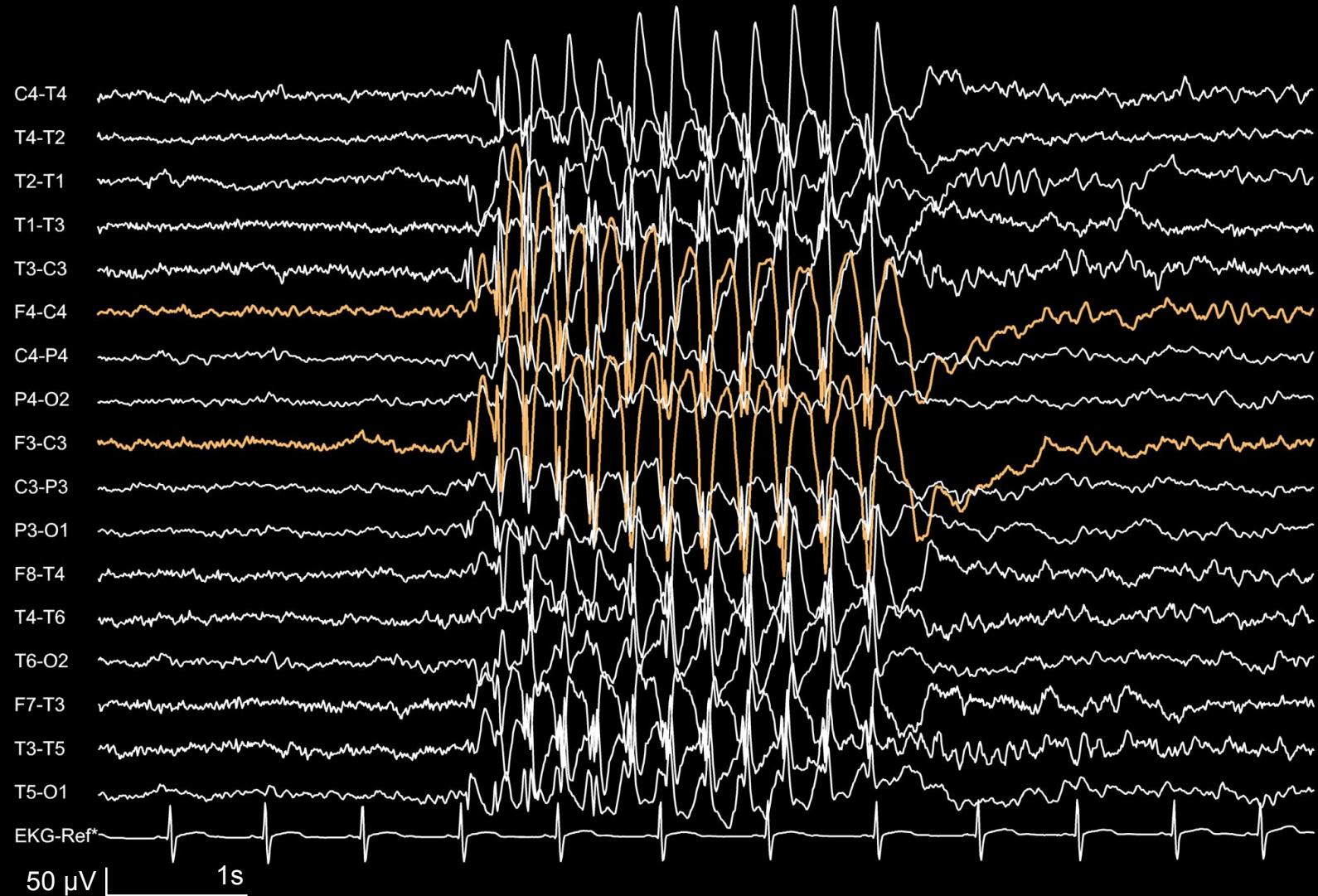
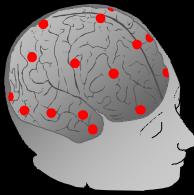


Extreme Event Epileptic Seizure

- frequency: ~ 3 szrs/month (max.: several 100 szrs/day)
- (apparently) non-predictable (exception: reflex epilepsies)
- duration: 1 – 2 min (exception: status epilepticus > 5 min)
- during the seizure: impaired mental functions, altered consciousness, loss of consciousness, involuntary movements, ...
- after the seizure: neurologic dysfunctions, depression, ...
- main seizure types:
 - focal seizure (with/without generalization)
 - generalized seizure (apparently instantaneous)

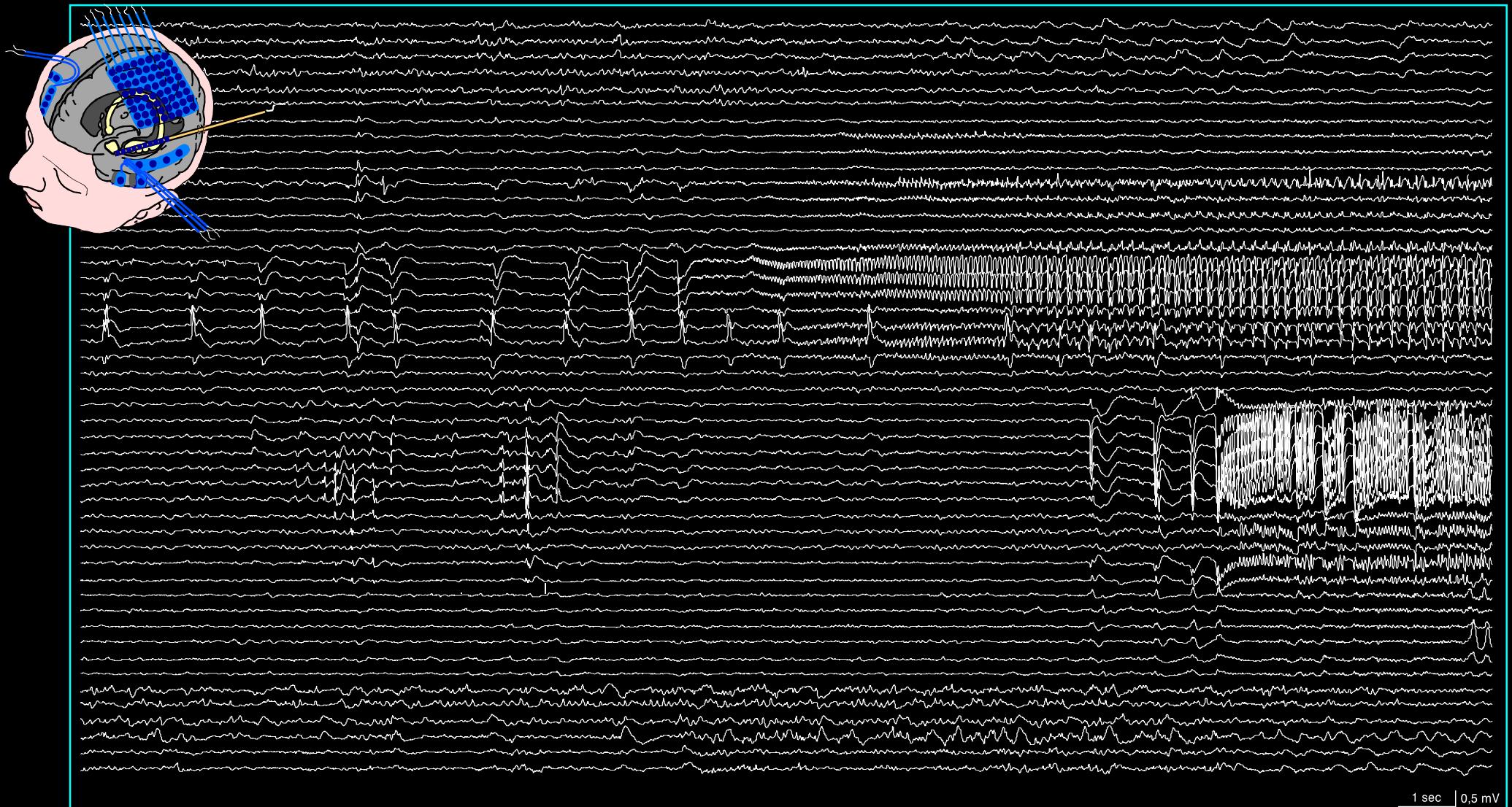


Epilepsy: Primary Generalized Seizure



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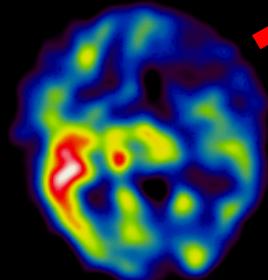
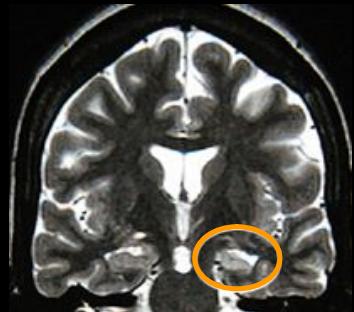
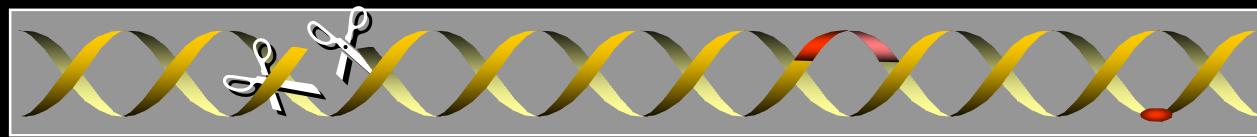
Epilepsy: Focal Seizure with spreading



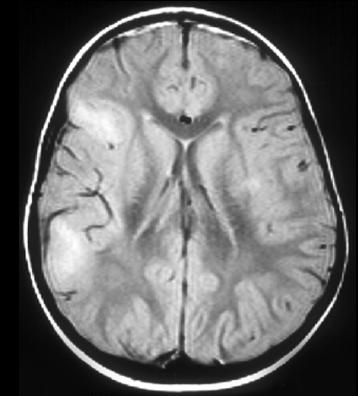
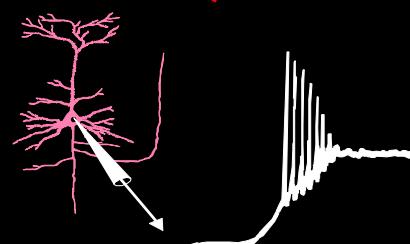
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1 sec | 0,5 mV

Epilepsy is network disease !

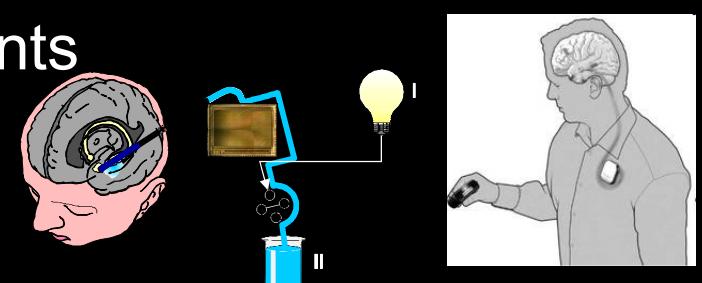
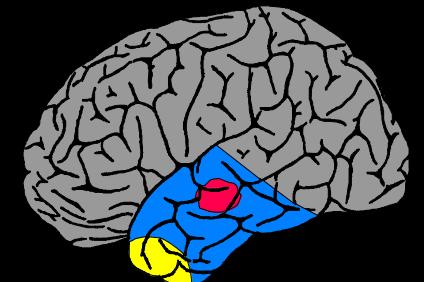


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Treatment of Epilepsy

- **antiepileptic drugs**; primary therapy; success: ~ 70 %
side effects, long-term treatment
- **epilepsy surgery**; option for ~ 5 – 10 % of patients
requirement: localize and delineate epileptic focus
from functionally relevant brain areas
success: ~ 60 % (15 % – 85 %)
long-term outcome, surgery-induced alterations?
- **alternative therapies**; for ~ 22 % of patients
seizure prediction, seizure control
success: ?



Epilepsy --- Unsolved Issues

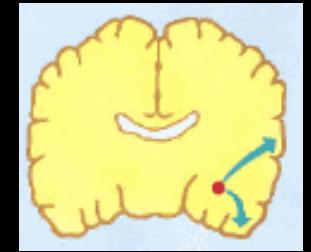
- basic mechanisms in humans
- where in the brain and when and why do seizures start ?
- seizure precursors ?
- where and why do seizures spread ? consistency ?
- when and why do seizure end ? consistency ?
- seizure-free interval: normal? pathologic?
- interactions epilepsy ↔ normal brain functioning (cognition)
- long-term (yrs) dynamics
- epileptic focus vs. epileptic network



Epileptic Focus vs. Epileptic Network

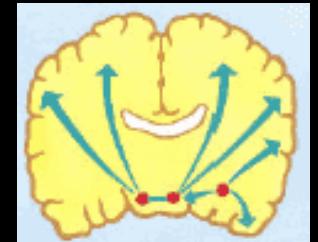
traditional concept: *epileptic focus*

- circumscribed area of the brain
- critical amount of neurons → epileptic seizures



recent evidence: *epileptic network*

- functionally and anatomically connected brain structures
- activity in any one part affects activity in all the others
- vulnerability to seizures in any one part of the network influenced by activity everywhere else in the network
- seizures may entrain large neural networks from any given part
- growing evidence from imaging, electrophysiological, and modeling studies



e.g. S. S. Spencer, *Epilepsia*, 43, 219, 2002

T. Berg & I. E. Scheffer, *Epilepsia*, 52, 1058, 2011

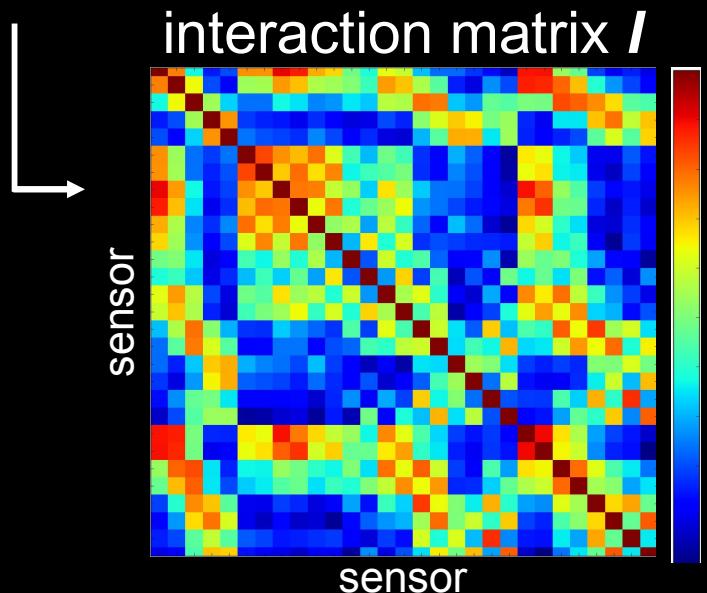
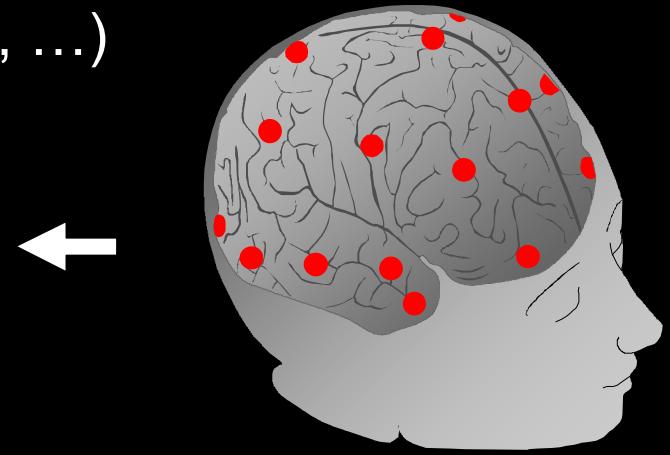
KL et al., *Physica D* 267, 7, 2014



First International Summer Institute on Network Physiology (ISINP)

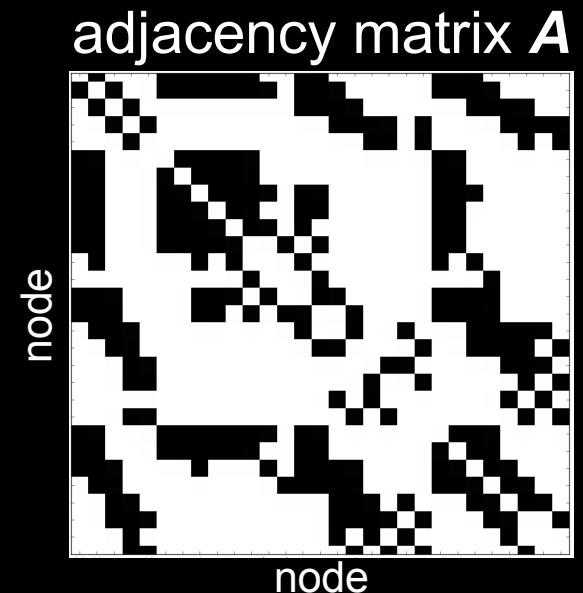
Inferring Functional (Interaction) Brain Networks

recordings of brain dynamics (EEG, MEG, fMRI, ...)



$$A = f(I)$$

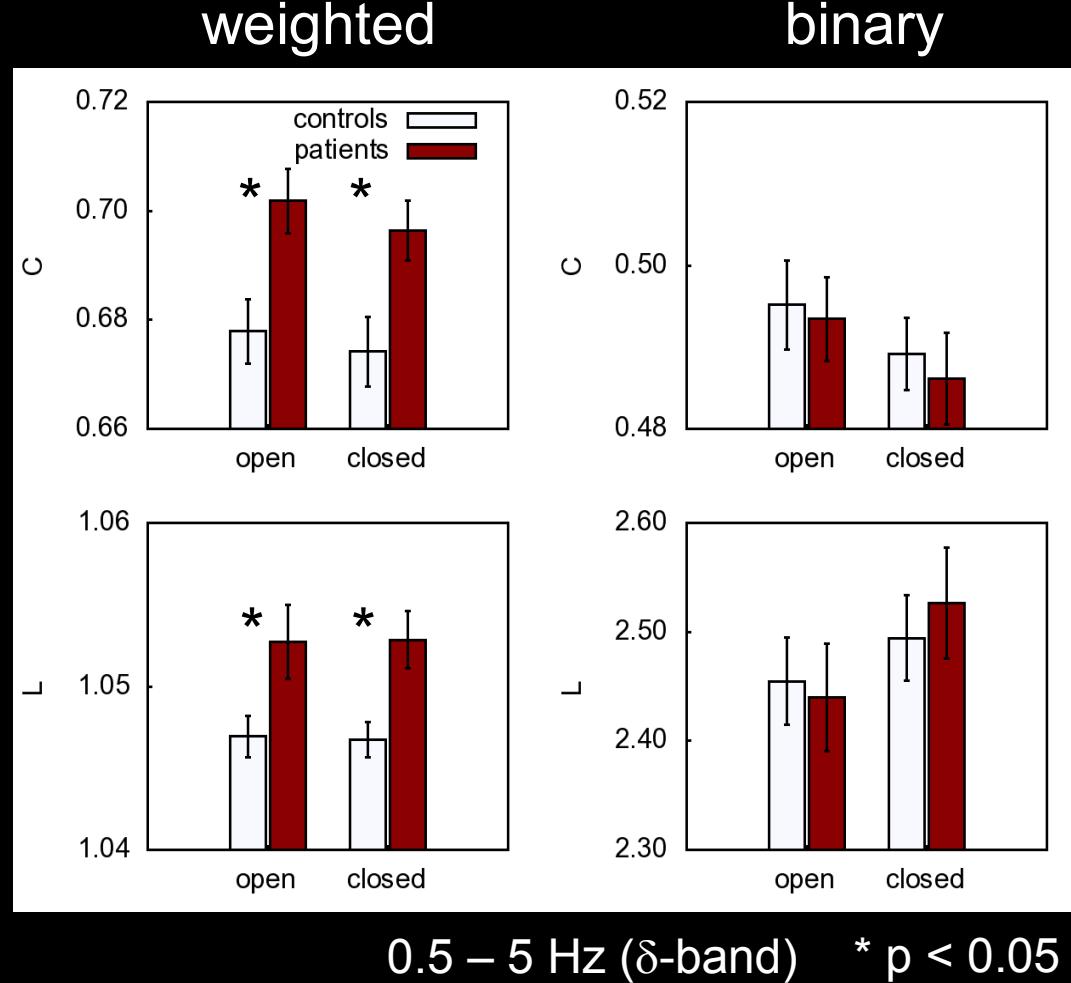
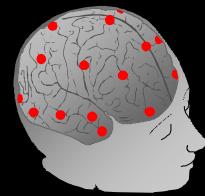
- thresholding
- significance testing
- ...



Functional Brain Networks: Epilepsy vs. Controls

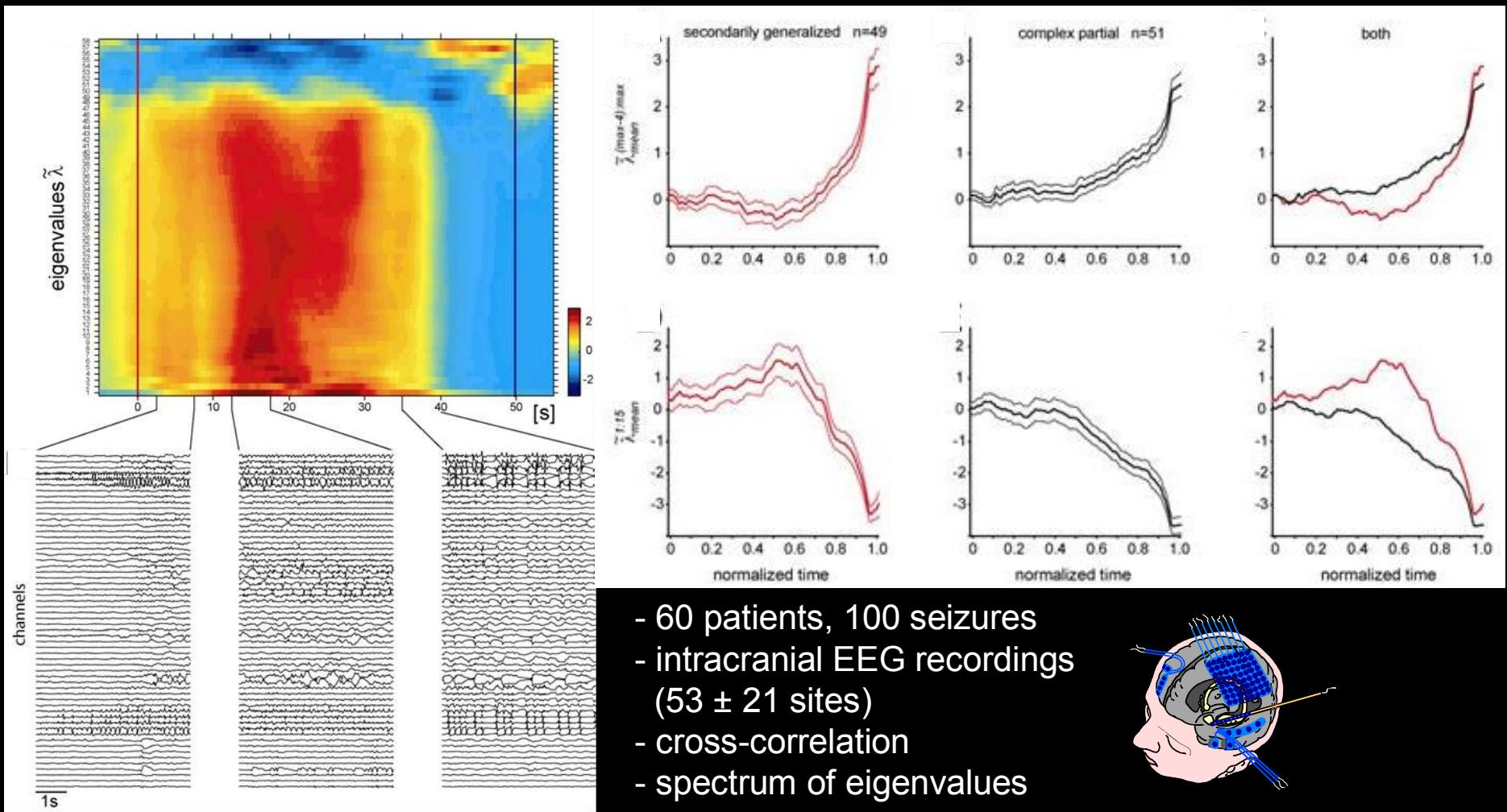
epileptic networks are more regular than healthy ones

- 21 patients, 23 controls
- scalp EEG recordings (29 sites)
- eyes-open (15 min)
- eyes-closed (15 min)
- mean phase coherence
(frequency-adaptive; -selective)
- binary networks
(fixed mean degree, thresholding)
- weighted networks
(different normalizations)
- clustering coefficient C
- average shortest path length L



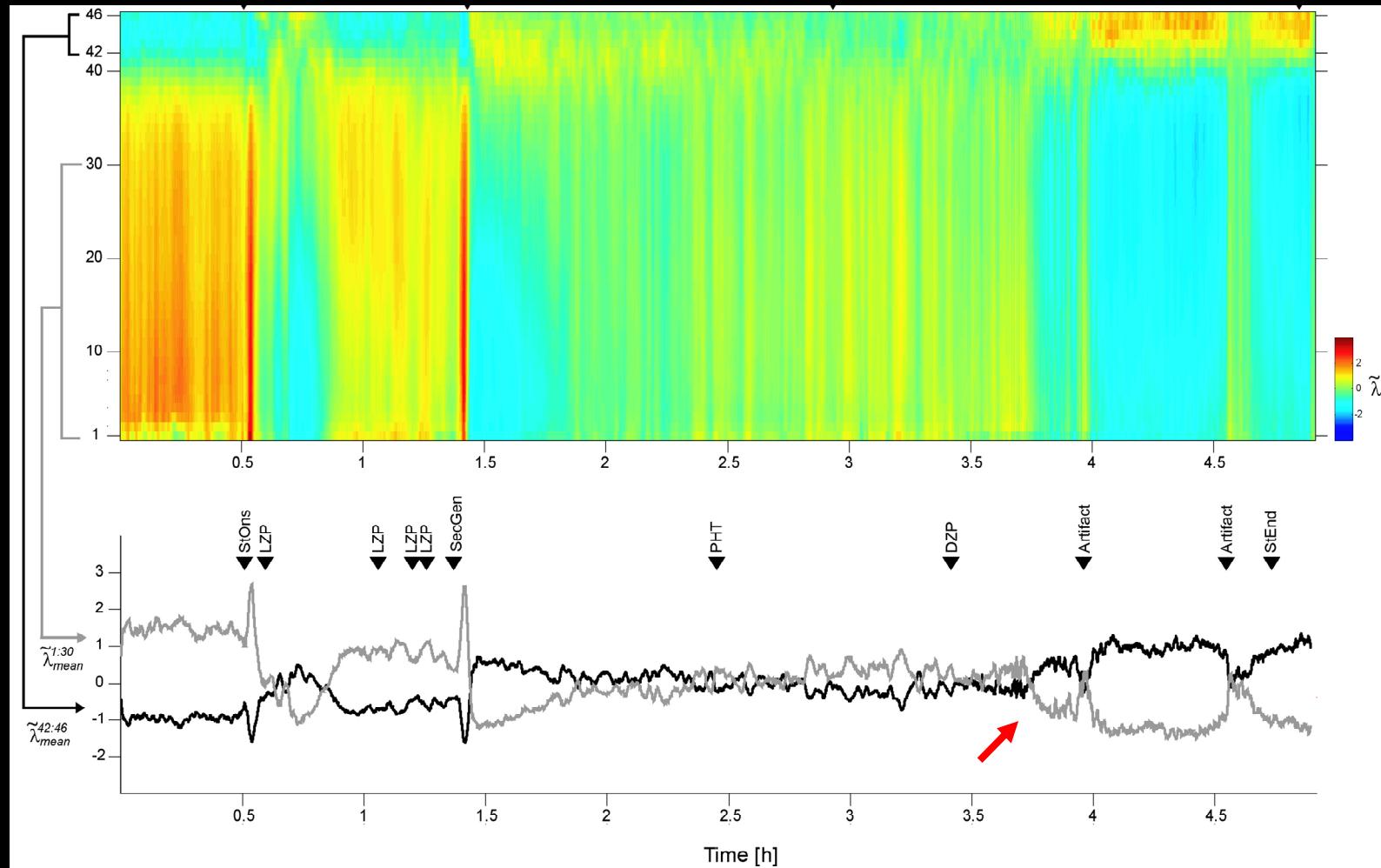
Epileptic Networks during Seizures

network sync: a mechanism for seizure termination?



Epileptic Networks during Status Epilepticus

network sync: a mechanism for seizure termination?



Epileptic Networks during Seizures

functional topology

from

more random

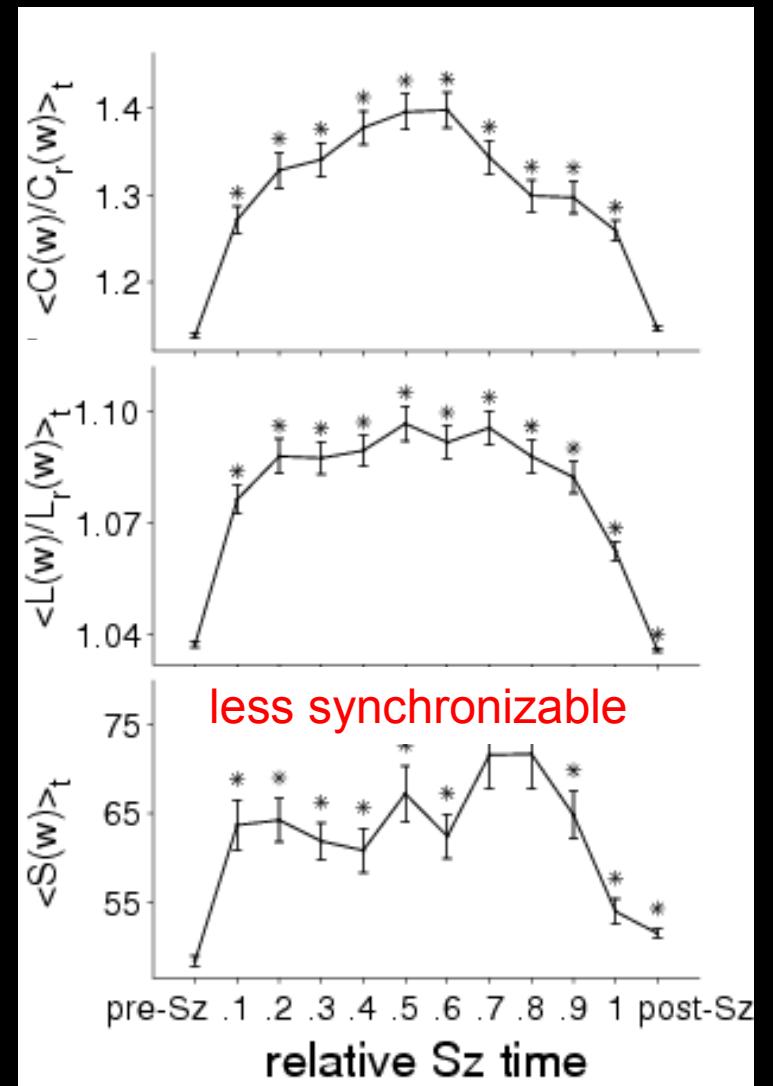
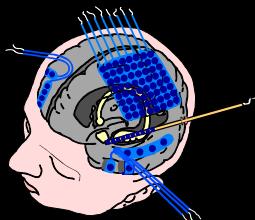
to

more regular

back to

more random

- 60 patients, 100 seizures
- intracranial EEG recordings (53 ± 21 sites)
- max. cross-correlation fct.
- thresholding (**A** fully connected)
- clustering coefficient C
- average shortest path length L
- *synchronizability* $S = \lambda_{\max}/\lambda_{\min}$ from Laplace matrix
- comparison with random networks (prescribed degree sequence)

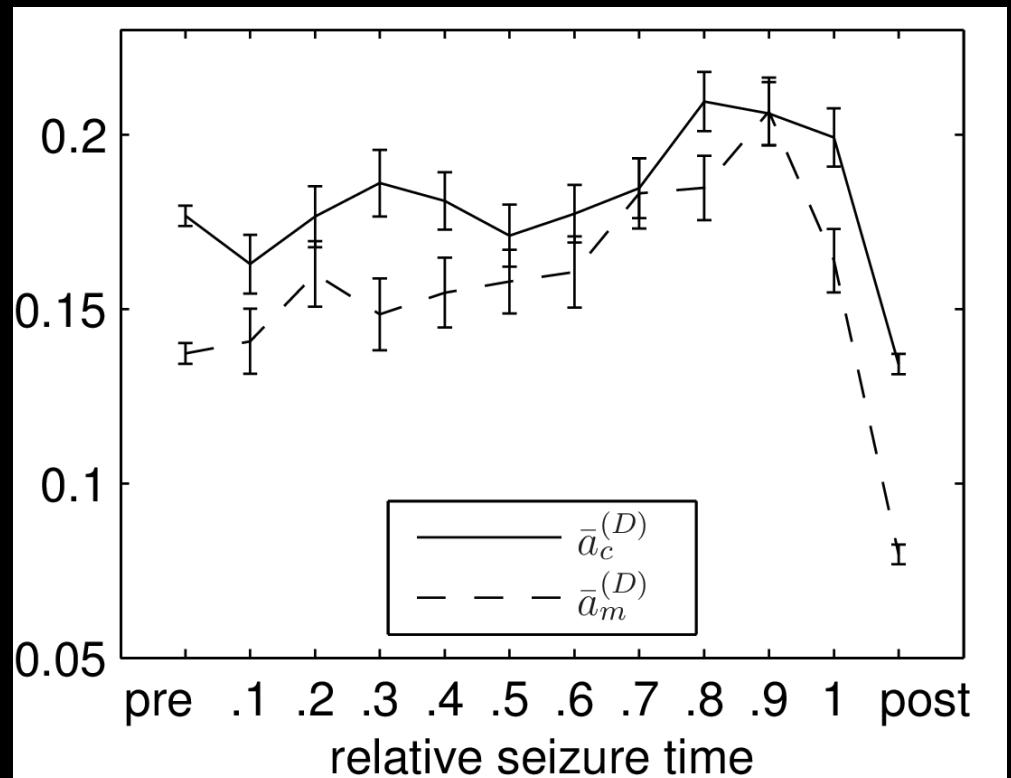
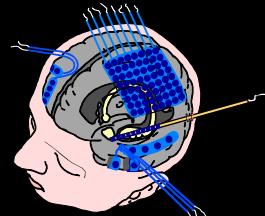


Epileptic Networks during Seizures

networks are assortative

- ***harder to synchronize***
- ***network disintegration***
- ***less vulnerable to attacks***

- 60 patients, 100 seizures
- intracranial EEG recordings (53 ± 21 sites)
- correlation coefficient
- max. of cross-correlation fct
- thresholding (**A** fully connected)
- assortativity coefficient a
- comparison with surrogate networks (based on IAAFT time series surrogates)

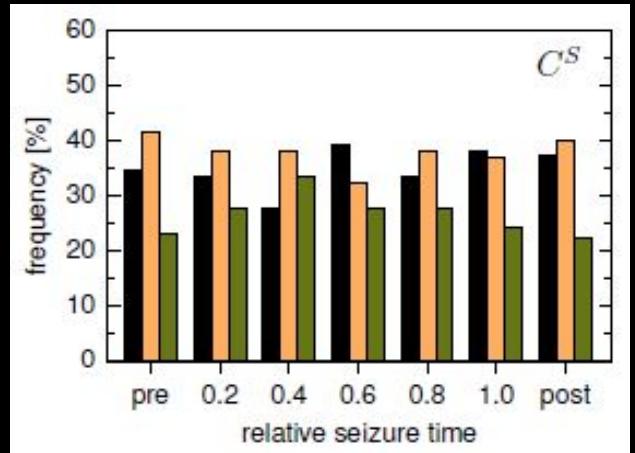
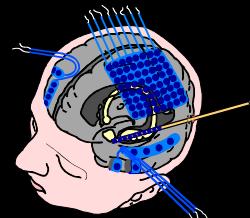


Epileptic Networks during Seizures

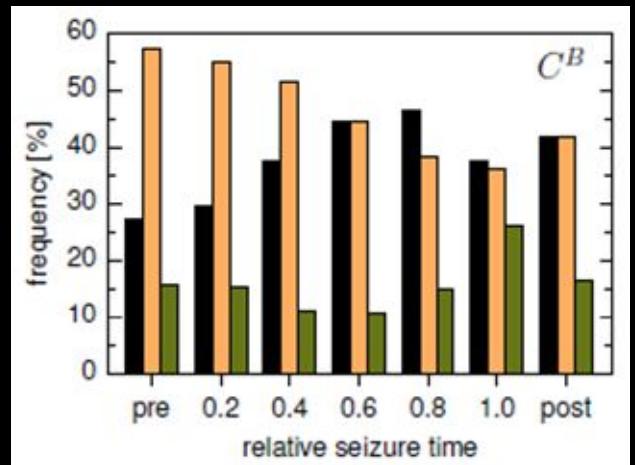
how important is the epileptic focus?

- ***important in only 35 % of cases***
- ***neighborhood more important (>50%)***
- ***neighborhood → bridge***
- ***improved prevention techniques?***

- 52 patients, 86 seizures
- intracranial EEG recordings (53 ± 21 sites)
- correlation coefficient
- max. of cross-correlation fct
- weighted networks (**A** normalized)
- various centrality indices:
strength (C^S), eigenvector, closeness, betweenness (C^B)
- comparison with surrogate networks
(based on IAAFT time series surrogates)



similar findings with eigenvector centrality

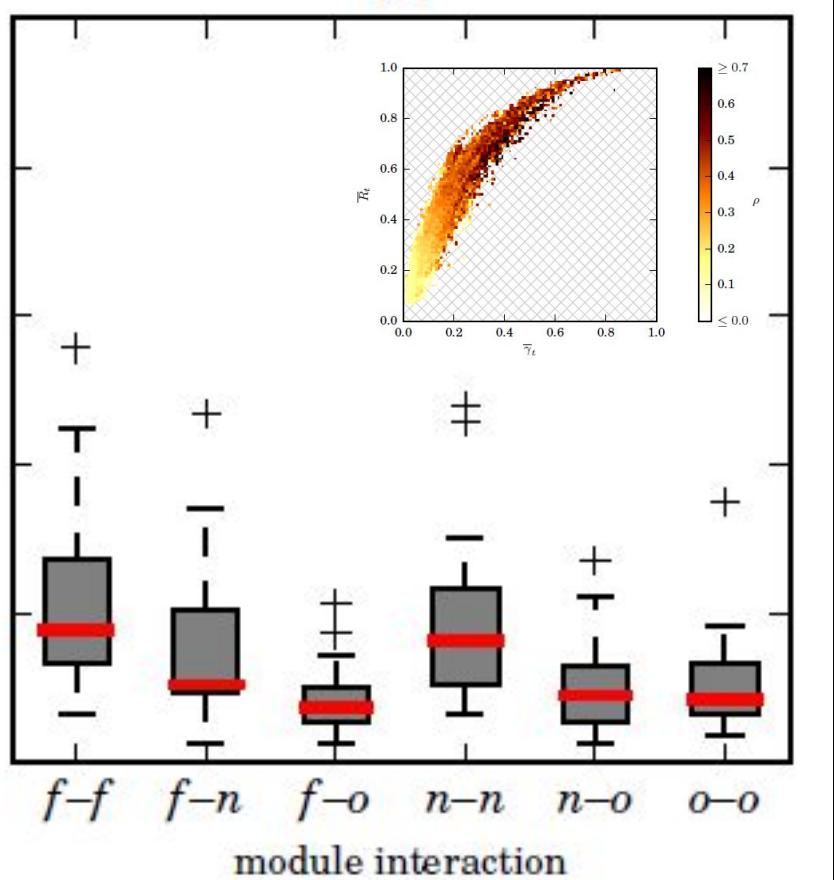
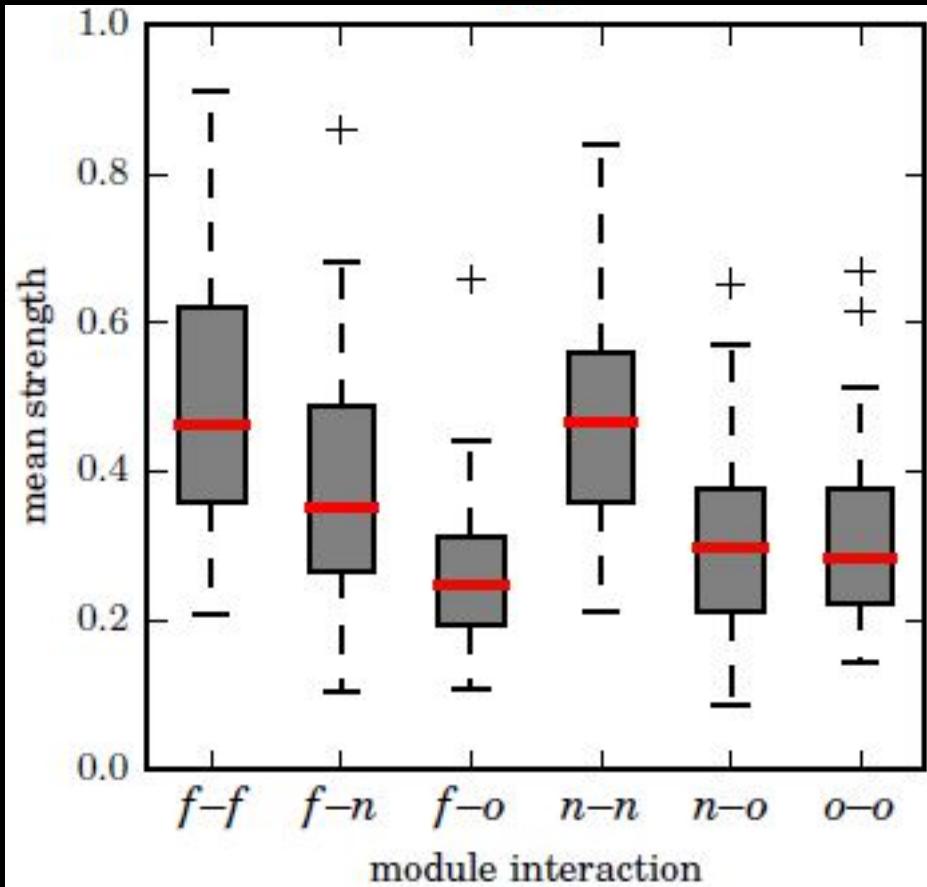


similar findings with closeness centrality

Strength of Interactions in Epileptic Networks

phase-based approach

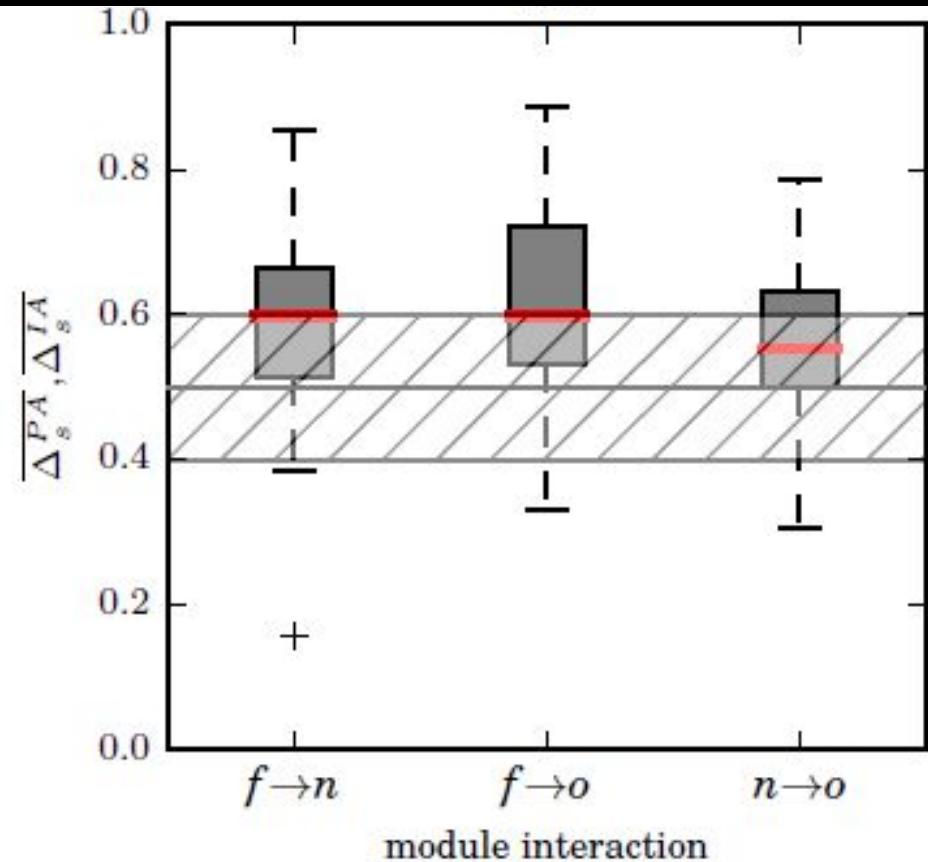
information-theoretic approach



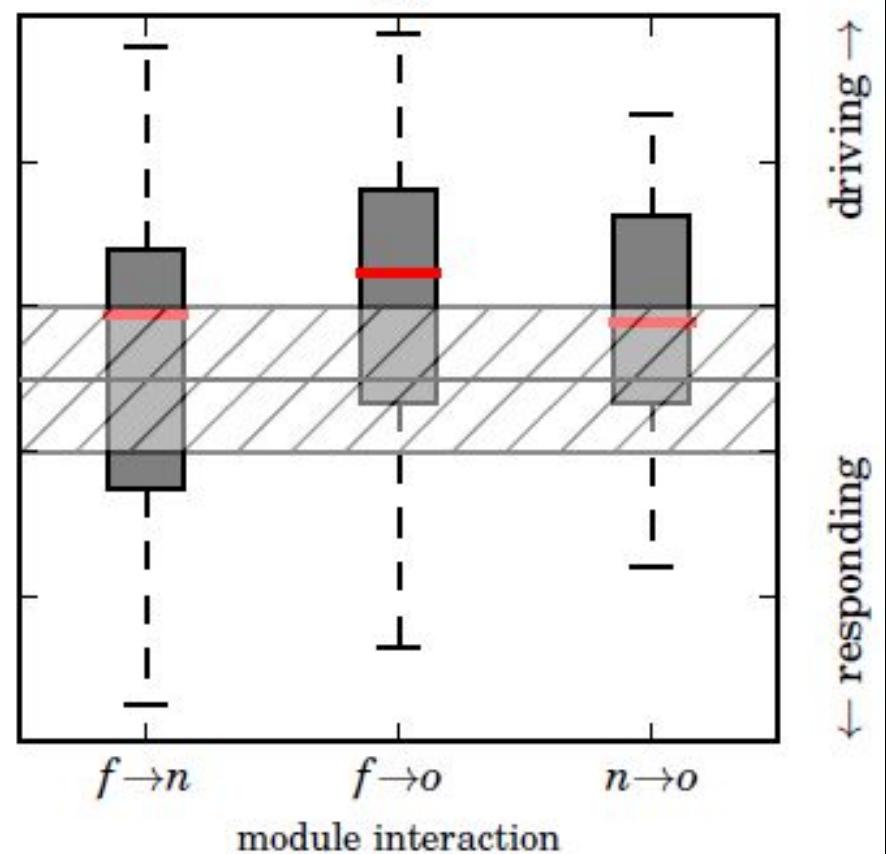
35 patients; Ø 51 sites; Ø 114 hrs iEEG recording; szr-free interval only

Direction of Interactions in Epileptic Networks

phase-based approach



information-theoretic approach



35 patients; Ø 51 sites; Ø 114 hrs iEEG recording; szr-free interval only

Strength and Direction of Interactions

patient group:

- highest strength of interactions within the epileptic focus
(gradually declines with increasing distance)
- epileptic focus “drives” all other brain areas
- largely unaffected by physiological activities
(e.g. circadian rhythms)

single patient

- very high variability (... reasons?)

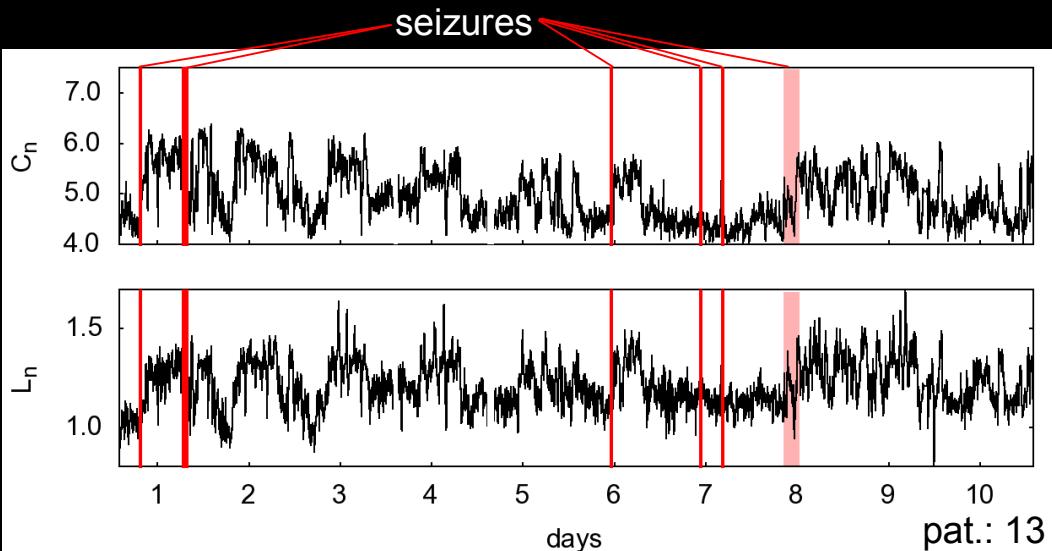
similar findings (phase-based vs information-theoretic approaches)

- what kind of synchronization phenomena ?
(phase, generalized, ...) ?
- confounding variables ?

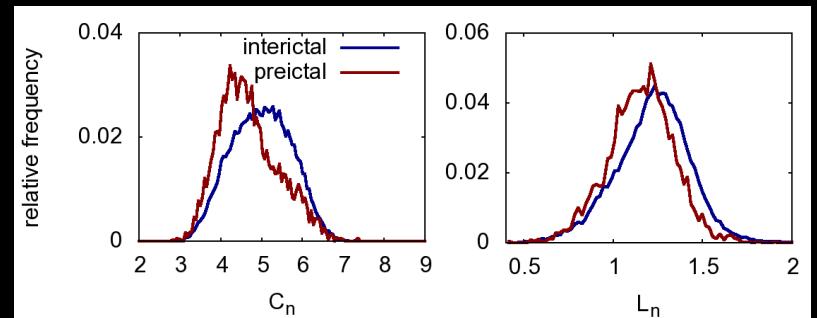


Long-Term Dynamics of Epileptic Networks (C , L)

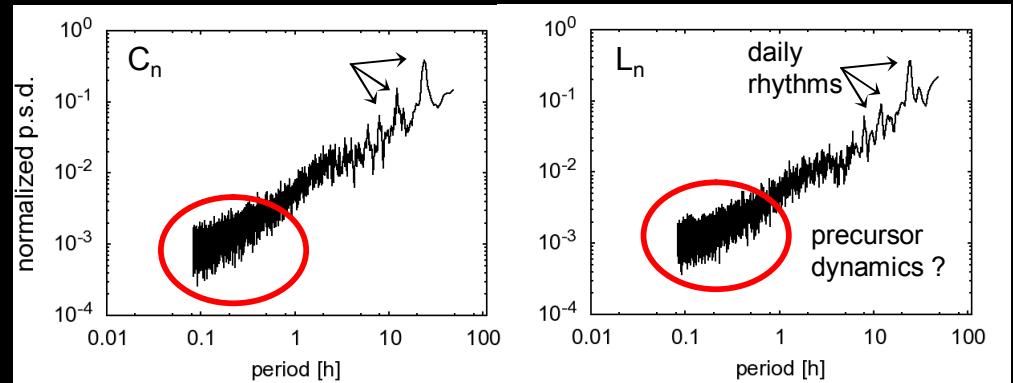
mainly reflects daily rhythms, epileptic process only marginally



exemplary frequency distributions



power spectral density estimates
(grand average)

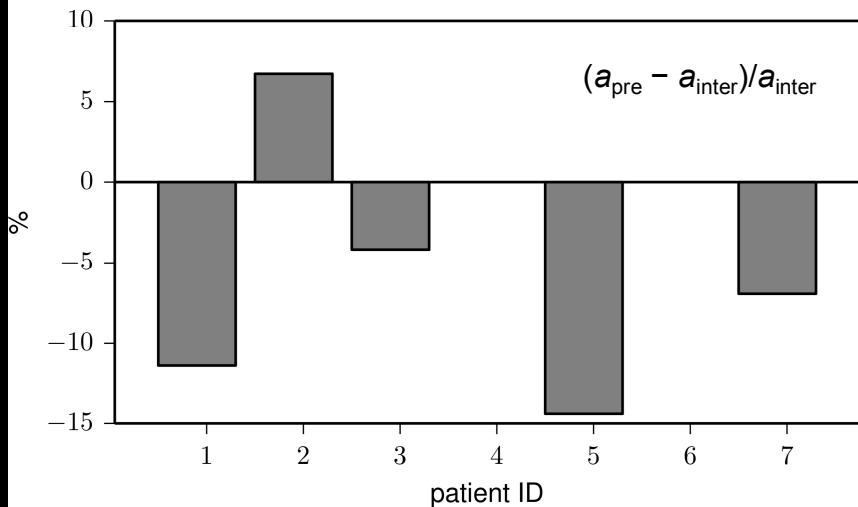
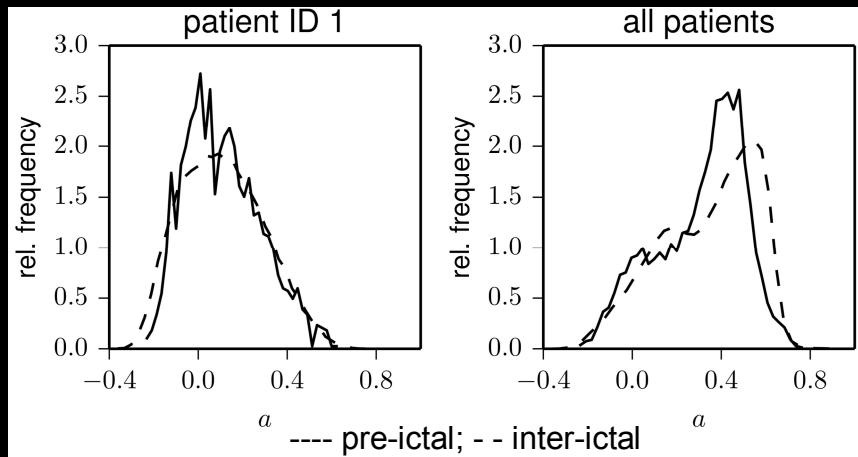
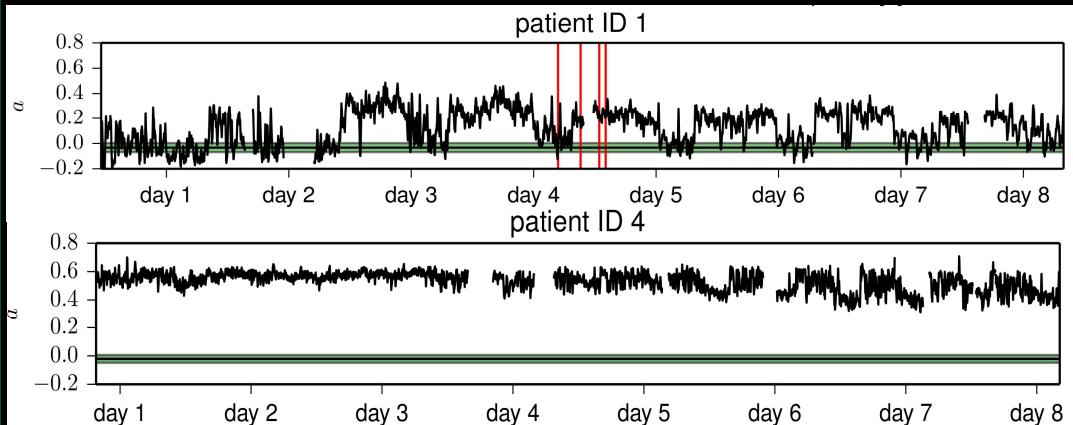


- 13 patients, 75 seizures
- intracranial EEG recordings (> 2100 h)
(56 sites, range: 24-72)
- mean phase coherence (frequency-adaptive)
- thresholding (fixed mean degree)
- clustering coefficient C
- average shortest path length L



Long-Term Dynamics of Epileptic Networks (a)

mainly reflects daily rhythms, easier to synchronize pre-ictally?

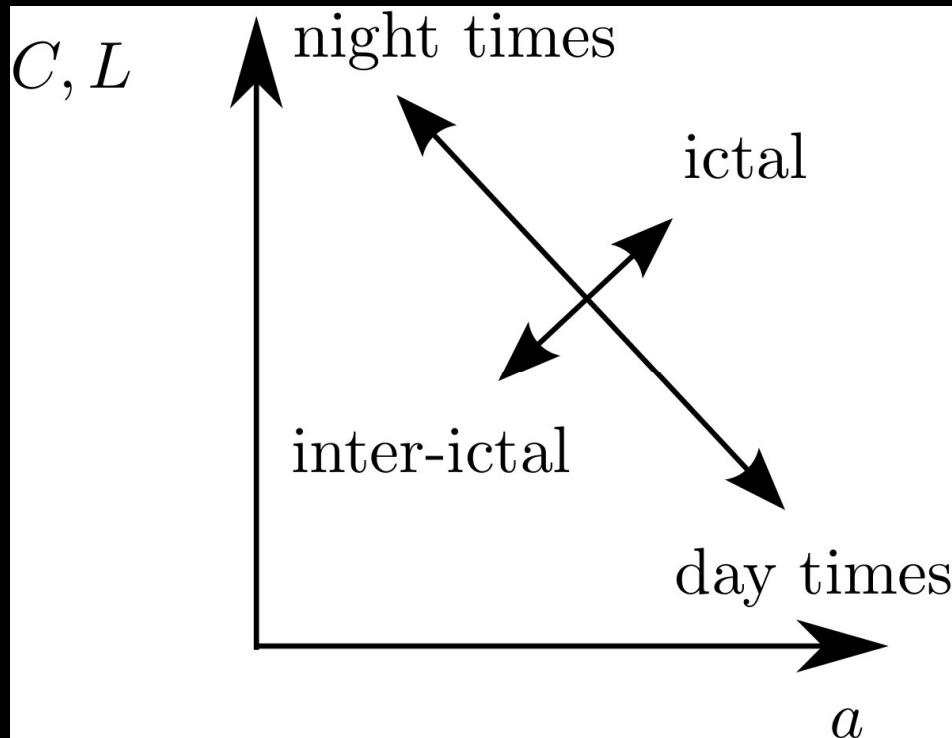


- 7 patients, 16 seizures
- intracranial EEG recordings (> 1000 h)
(90 sites, range: 44-90)
- mean phase coherence (frequency-adaptive)
- thresholding (pre-def. link density)
- assortativity a
- comparison with surrogate networks



Long-Term Dynamics of Epileptic Networks

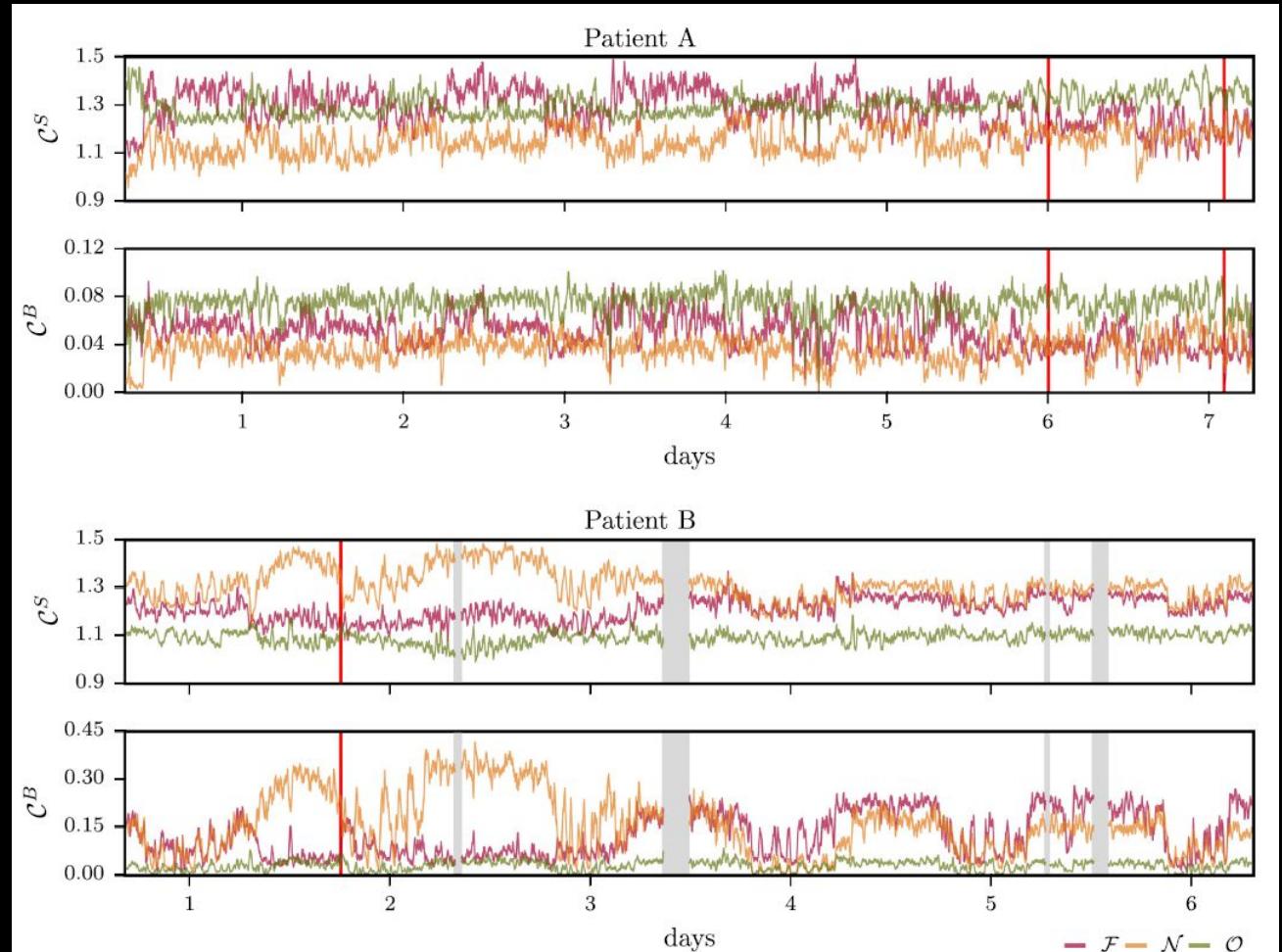
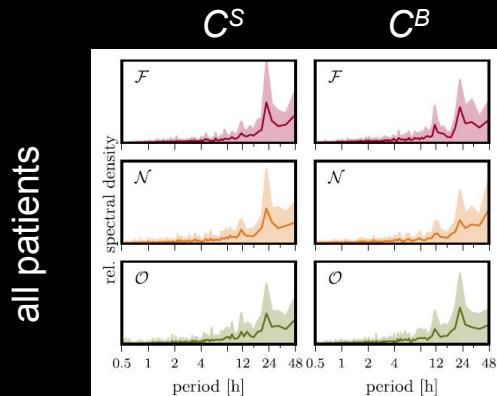
how epileptic brain networks explore the space (a, C, L) of accessible network topologies



Long-Term Node Importance in Epileptic Networks

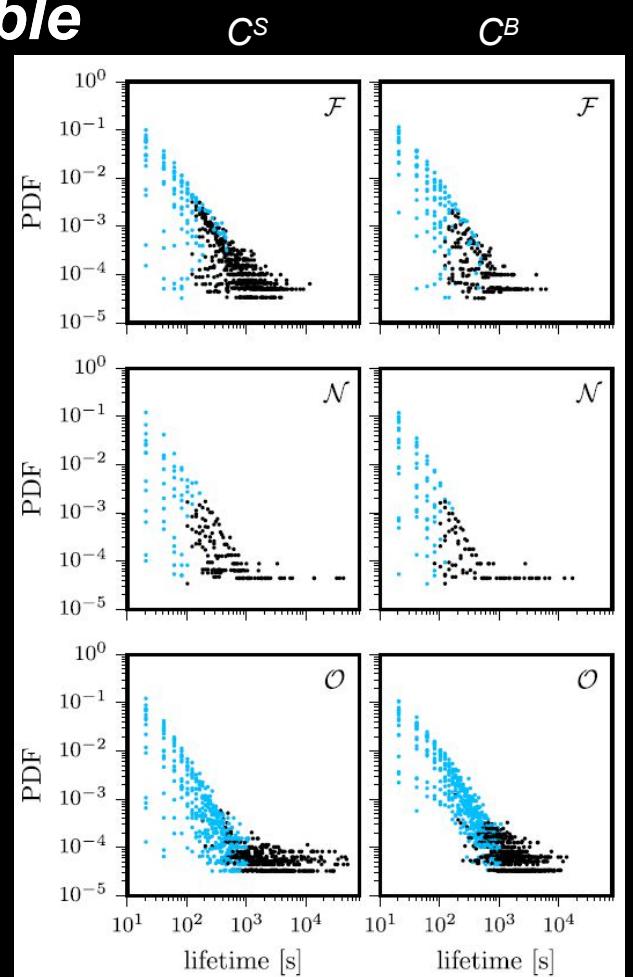
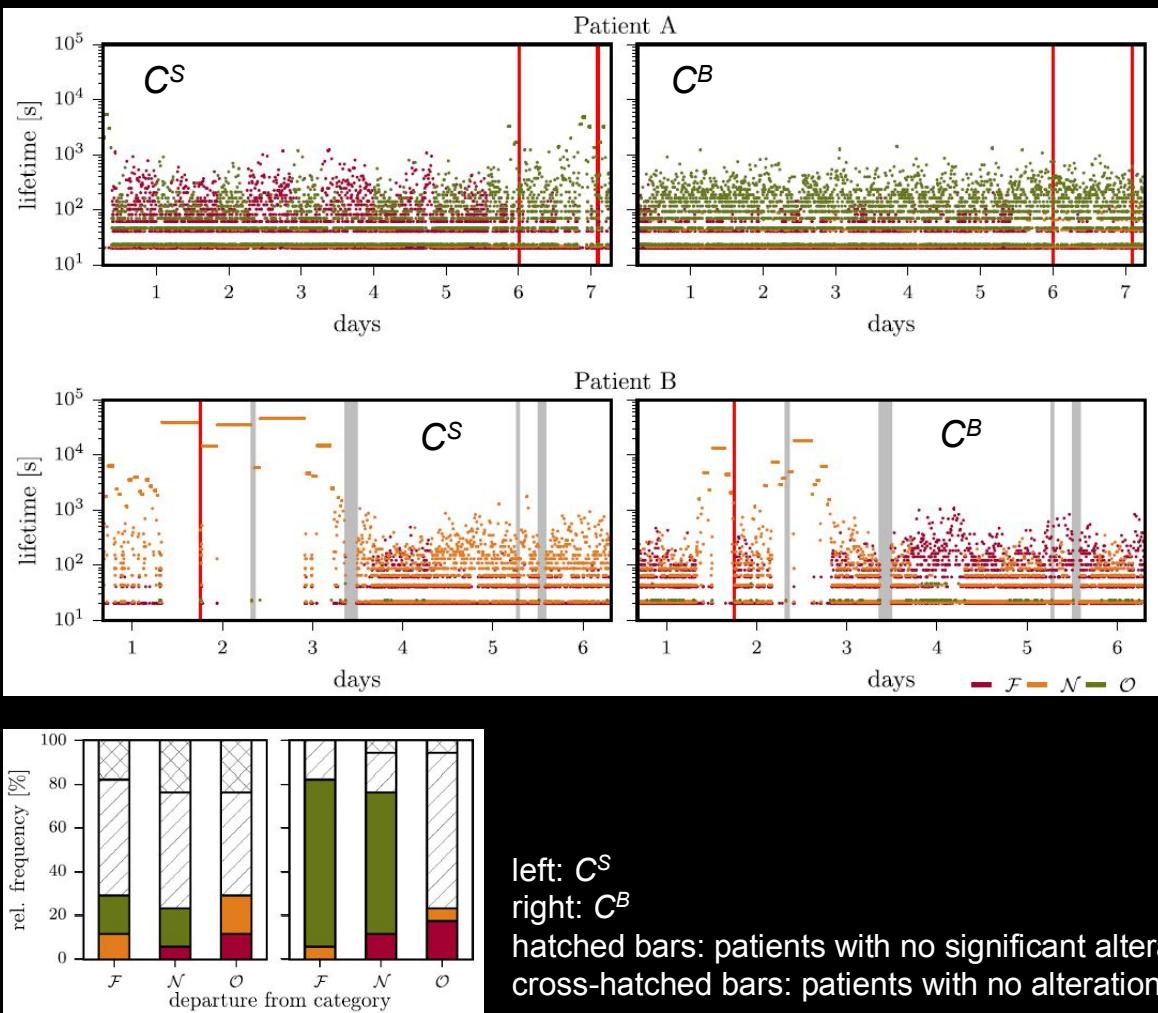
importance of brain regions is highly variable

- 17 patients, 83 seizures
- intracranial EEG recordings (> 2100 h; sites range: 16-64)
- mean phase coherence (frequency-adaptive)
- normalized weighted networks
- strength and betweenness centrality (C^S , C^B) and relationship to focus (F), neighborhood (N), other brain areas (O)



Long-Term Node Importance in Epileptic Networks

importance of brain regions is highly variable



blue dots: epochs with lifetimes shorter than expected
under null hypothesis: occurrence probabilities determined by population densities of F, N, O



Seizure Prediction and Prevention

prediction feasible, but ...

- ... not in all patients
- ... not in all seizures

unsolved issues:

- **when to prevent**
- **where to prevent**
- **how to disturb
an adaptive system?**

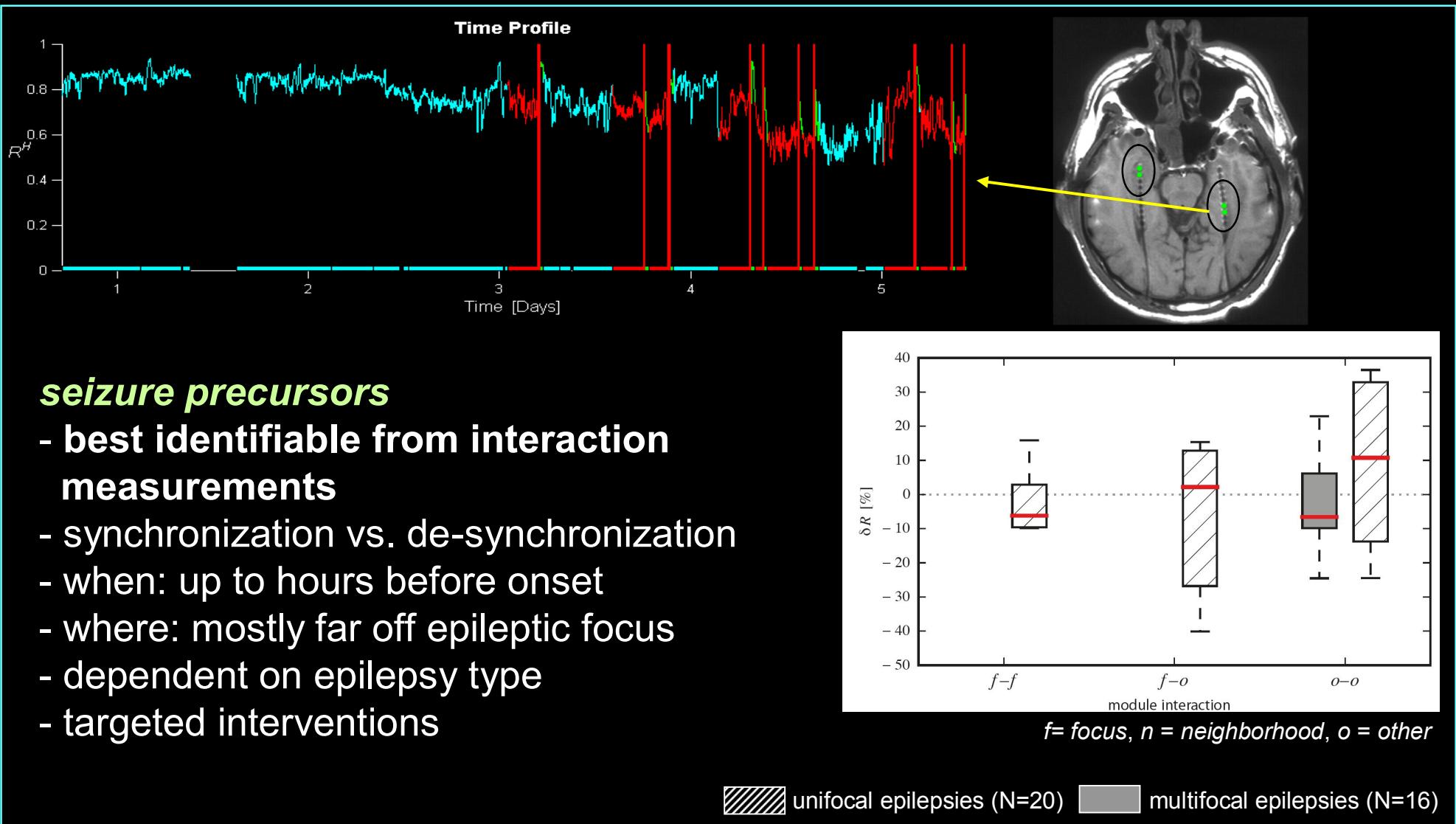


from: Cook et al., Lancet Neurol 2013; 12: 563



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Searching for Seizure Precursors

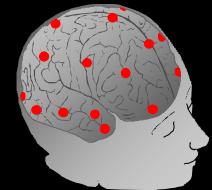


Cognition modifies Functional Brain Networks

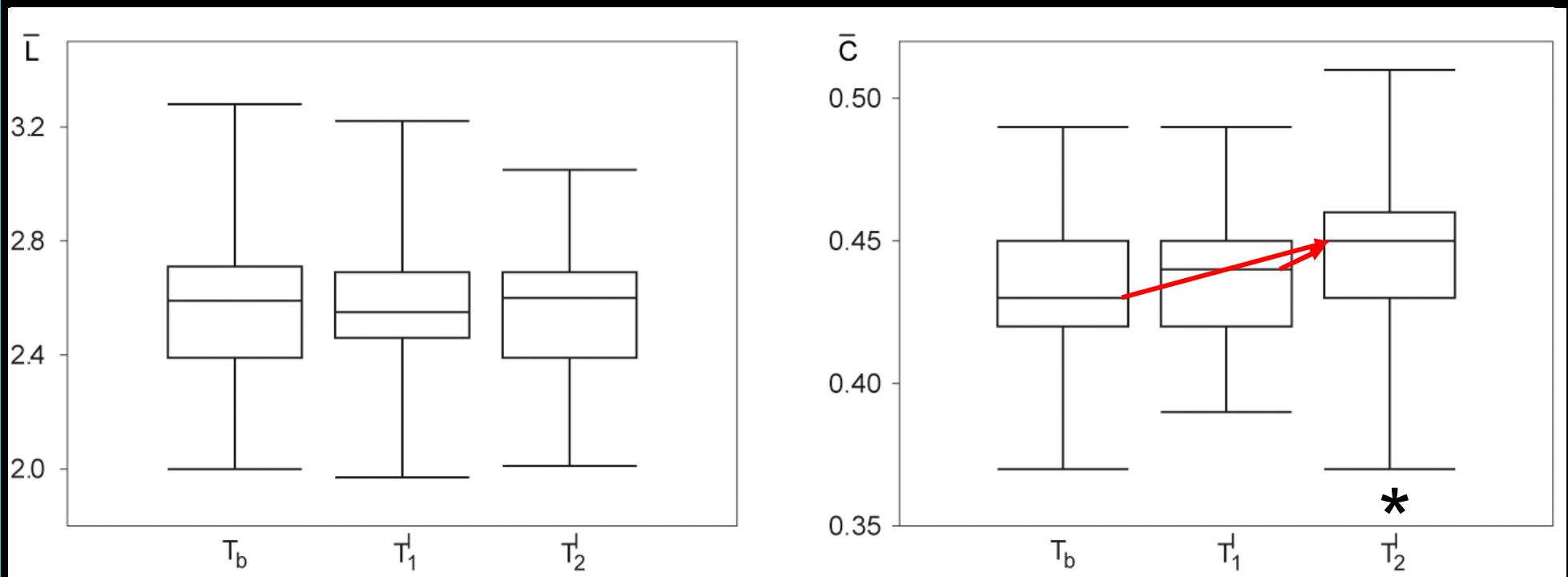
incidental					intentional				
rest	T_1^I	FF	rest	T_1^r	rest	T_2^I	FF	rest	T_2^r
5 min	3 min	1 min	3 min	3 min	5 min	3 min	1 min	3 min	3 min

Learning- and memory-related processes

- incidental vs. intentional learning; free recall of learned material
- number of recalled words N_1, N_2
- 13 patients, 20 healthy controls; non-invasive EEG, 29 sites
- mean phase coherence
- binary networks (thresholding)
- clustering coefficient C
- average shortest path length L



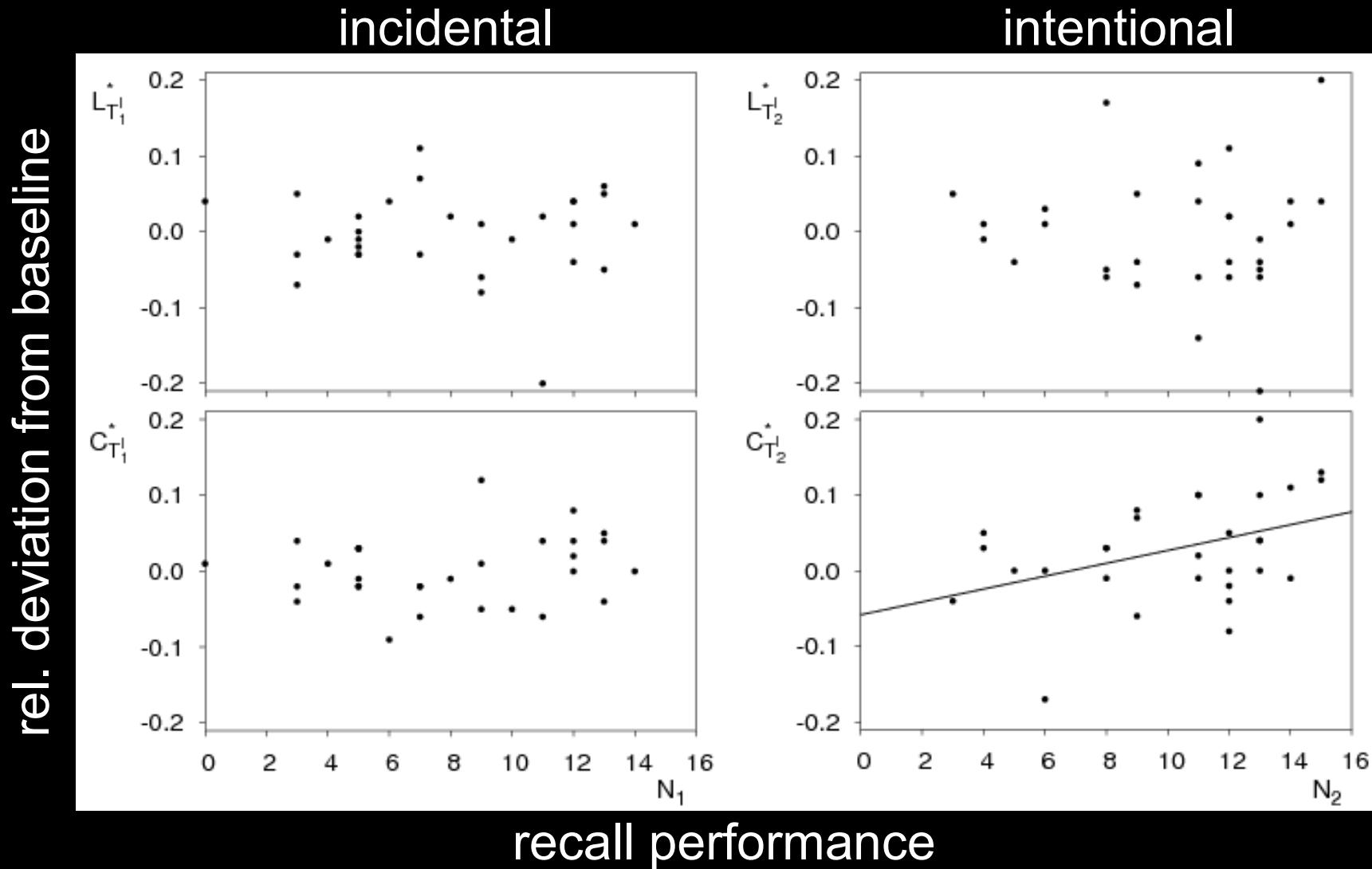
Cognition modifies Functional Brain Networks



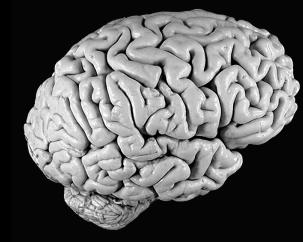
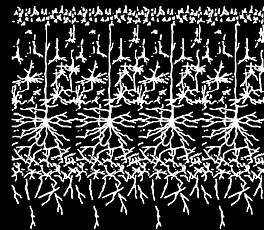
group statistics:

- clustering coefficient: slightly larger ($p<0.05$) during intentional learning T_2 than during incidental learning T_1 or during baseline T_b
- average shortest path length: no significant change

Cognition modifies Functional Brain Networks



Modeling the Epileptic Process: On which Scales ?



integrate-and-fire
FitzHugh-Nagumo
Morris-Lecar
Hodgkin-Huxley

ion channels
neurotransmitter
synapses

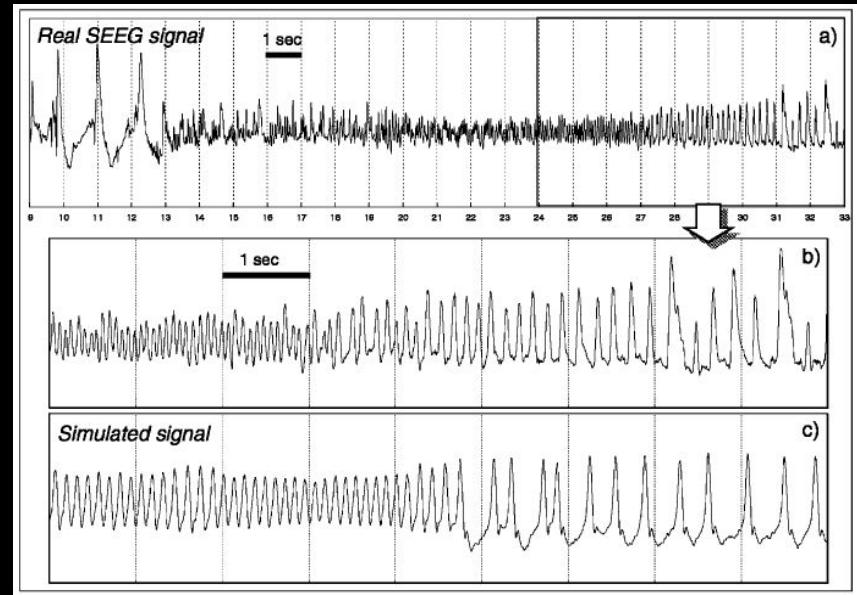
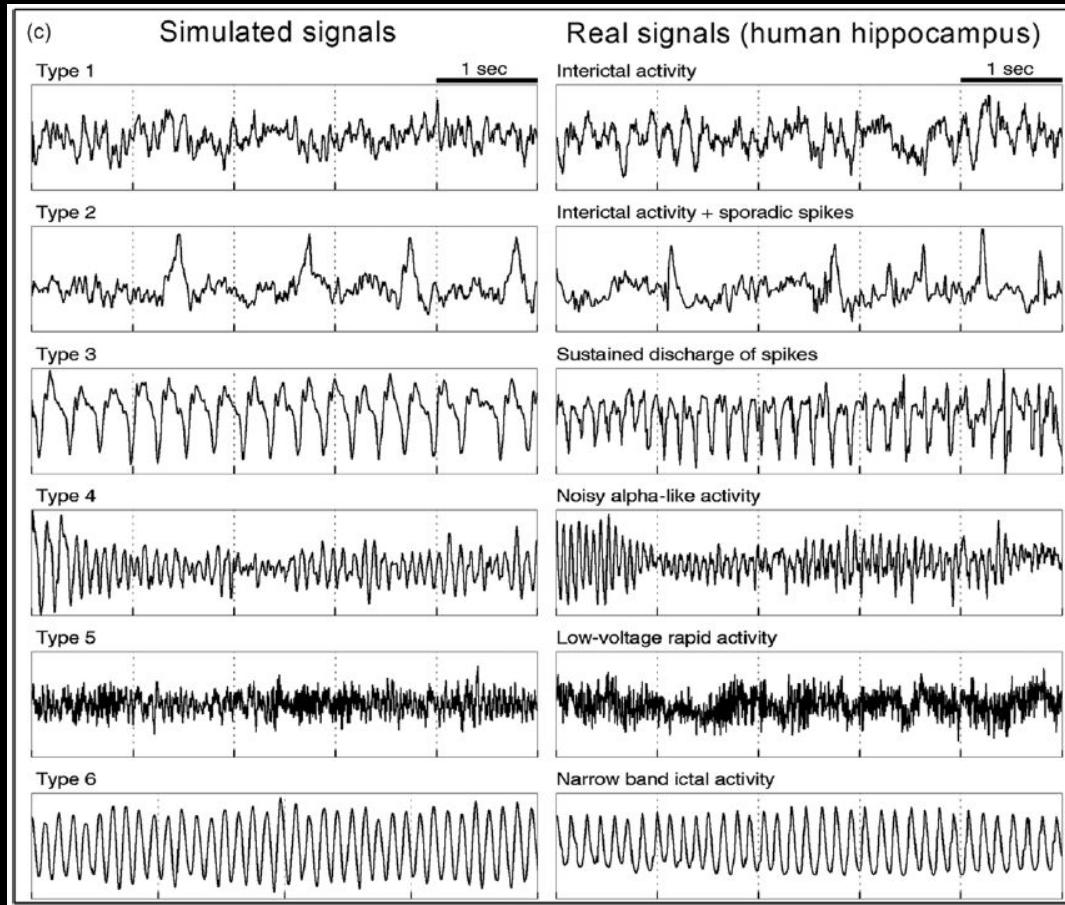
branching structure

single cell models
distributed neuronal networks
network size ($\sim 10^5$)
connectivity
inhibition/excitation
feed back/ feed forward coupling
interneurons / glia cells

neuronal population models
NDE, SDE, coupled ODEs,
(s)PDE, NODE,
lumped parameter,
mean field approaches
EEG phenomena
transitions
- bistability
- parameter changes, noise



Modeling the Epileptic Process: Neural Mass Models



- + models able to “seize”
- + transition to seizure-like activity
- + spread of seizure-like activity

- no self-termination of activity
- mostly noise driven
- time dependent control parameter



Modeling Epileptic Network Dynamics

The Journal of Neuroscience, September 15, 2004 • 24(37):8075–8083 • 8075

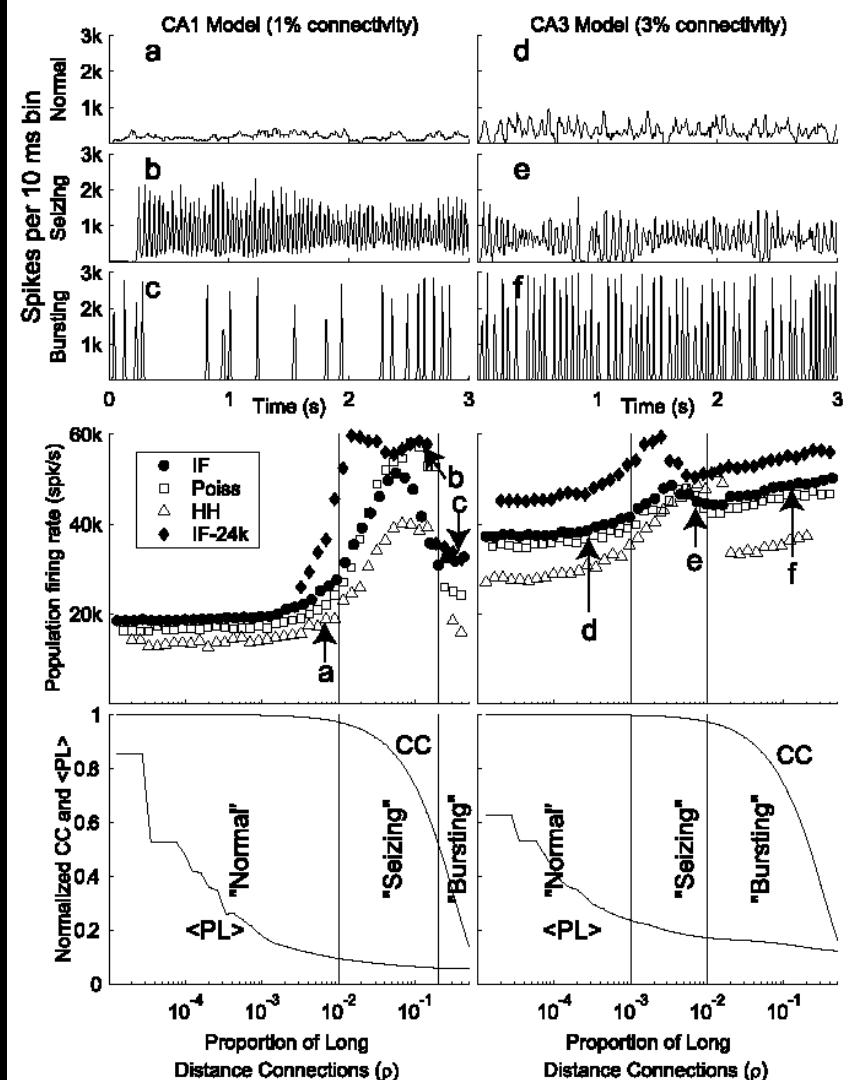
Neurobiology of Disease

Epilepsy in Small-World Networks

Theoden I. Netoff,^{1,3} Robert Clewley,^{2,3} Scott Arno,^{1,3} Tara Keck,^{1,3} and John A. White^{1,3}

¹Department of Biomedical Engineering, ²Department of Mathematics and ³Center for BioDynamics and Center for Memory and Brain, Boston University, Boston, Massachusetts 02215

“By **changing parameters** such as the synaptic strengths, number of synapses per neuron, proportion of local versus long-distance connections, we induced normal, seizing, and bursting behaviors. [...] explains how **specific changes in the topology or synaptic strength** in the model cause **transitions from normal to seizing and then to bursting**. These behaviors appear to be general properties of excitatory networks.”



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Modeling Epileptic Network Dynamics

PHYSICAL REVIEW E 76, 021920 (2007)

Internetwork and intranetwork communications during bursting dynamics: Applications to seizure prediction

S. Feldt,^{1,*} H. Osterhage,^{2,3} F. Mormann,^{2,4} K. Lehnertz,^{2,3,5} and M. Żochowski^{1,6}

¹*Department of Physics, University of Michigan, Ann Arbor, Michigan 48109, USA*

²*Department of Epileptology, University of Bonn, Bonn, Germany*

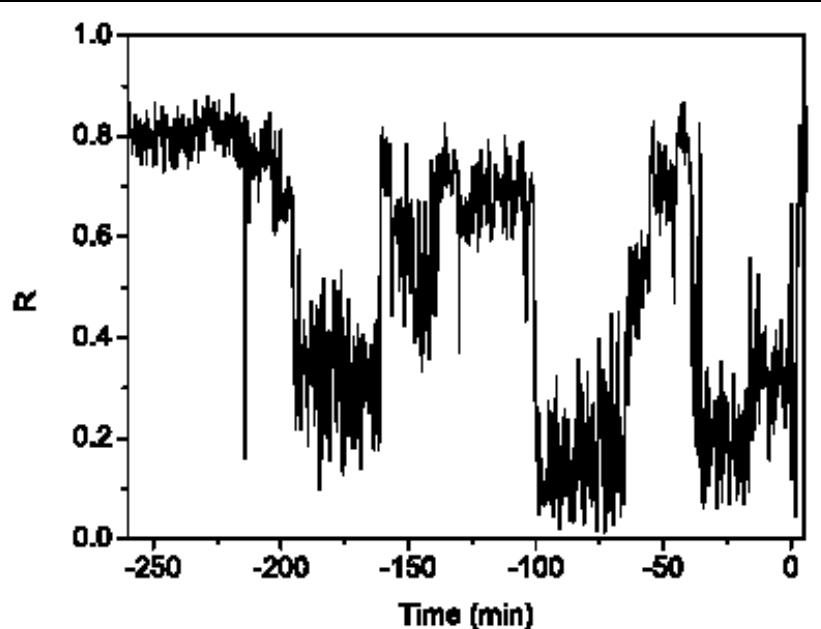
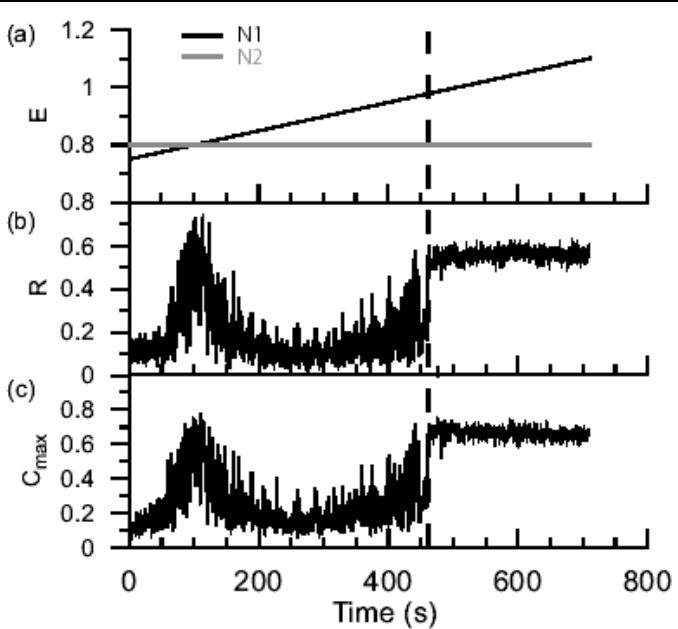
³*Helmholtz-Institute for Radiation and Nuclear Physics, University of Bonn, Bonn, Germany*

⁴*California Institute of Technology, Division of Biology, 216-76, Pasadena, CA 91125, USA*

⁵*Interdisciplinary Center for Complex Systems, University of Bonn, Bonn, Germany*

⁶*Biophysics Research Division, University of Michigan, Ann Arbor, Michigan 48109, USA*

(Received 9 March 2007; revised manuscript received 23 May 2007; published 20 August 2007)



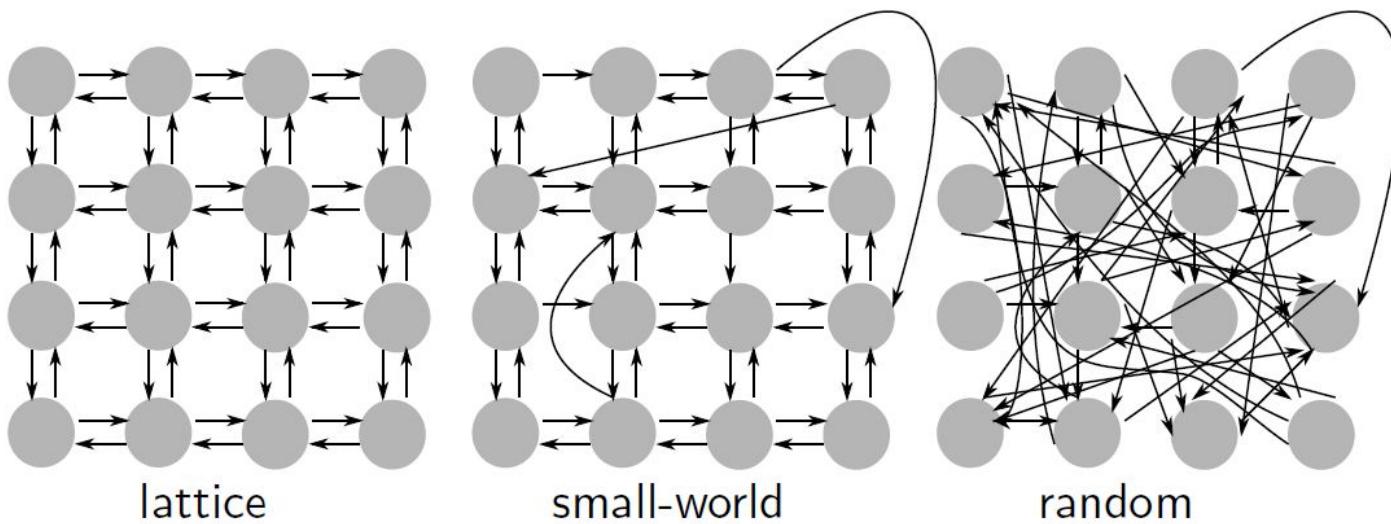
- two interacting networks
- IF neurons (N=225)
- small-world topology

- EEG data
- MTLE patient



Self-Initiation and -Termination of Sz-like Events

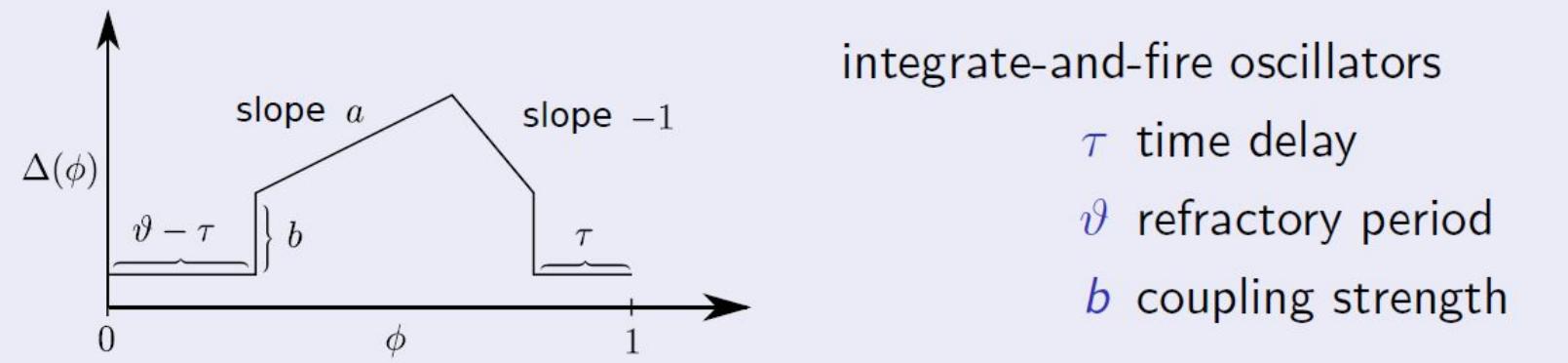
- $N \times N$ oscillators
- connect each oscillator to its m nearest neighbors
- cyclic boundary conditions (torus)
- replace fraction p of connections by connections between randomly chosen oscillators



Self-Initiation and -Termination of Sz-like Events

pulse-coupled phase oscillators (IF neurons)

- intrinsic dynamics: $\dot{\phi}_n = 1, \phi_n \in (0, 1]$
- oscillator n fires ($\phi_n(t_f) = 1$)
 - ▶ excite all oscillators n' connected to n
 $\phi_j(t_f^+) = R(\phi_{n'}(t_f)) = \Delta(\phi_{n'}(t_f)) + \phi_{n'}(t_f)$
 - ▶ reset oscillator n : $\phi_n(t_f^+) = 0$

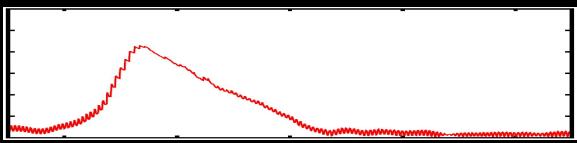
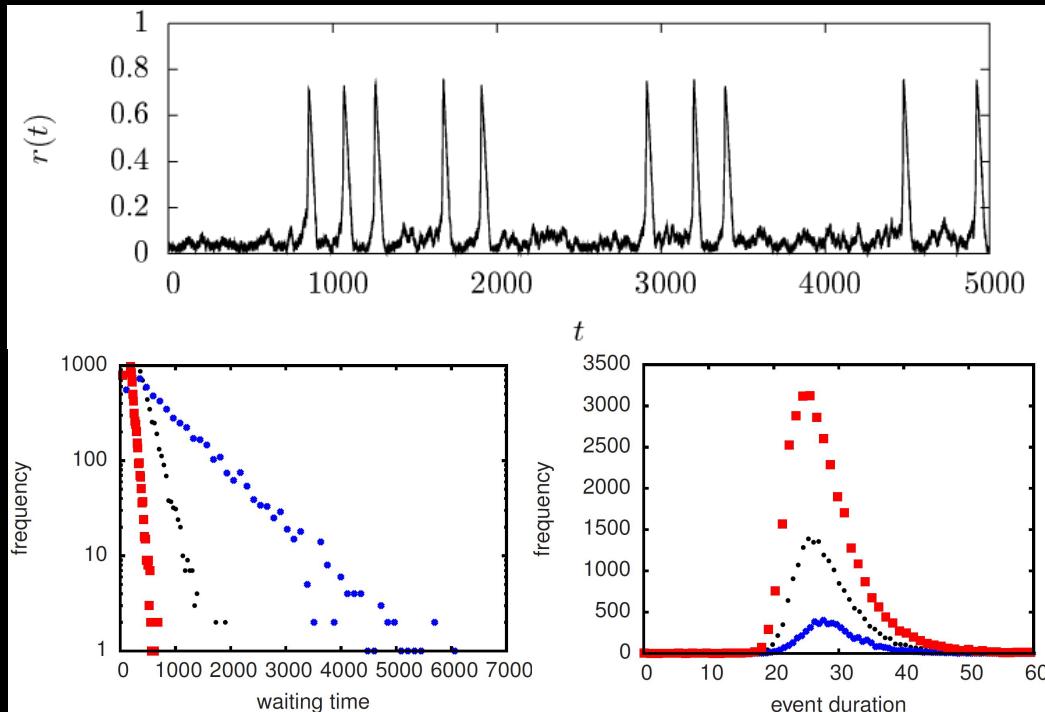


Measuring synchrony with Kuramoto's order parameter: $r(t) = 1/|N| \left| \sum_{n \in N} e^{2\pi i \phi_n(t)} \right|$



Self-Initiation and -Termination of Sz-like Events

$N = 500 \times 500, m = 50, \tau = 0.01, b = 0.01, \text{various } v$



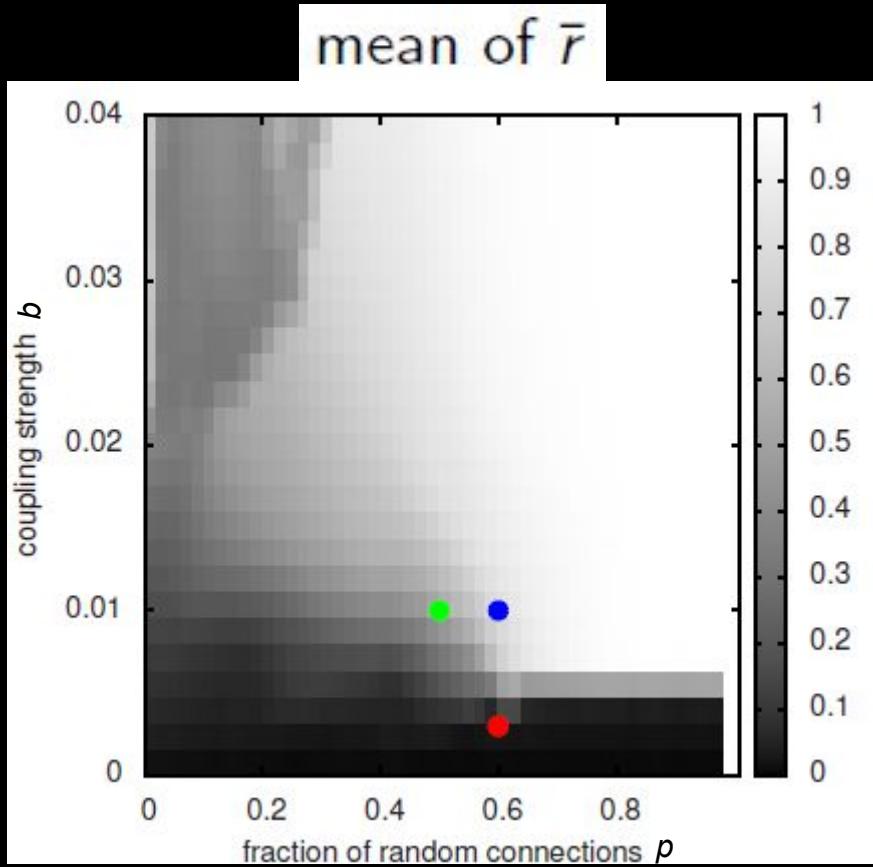
$N = 500 \times 500, m = 50, \tau = 0.01, b = 0.01, v = 0.05$

1
φ
0

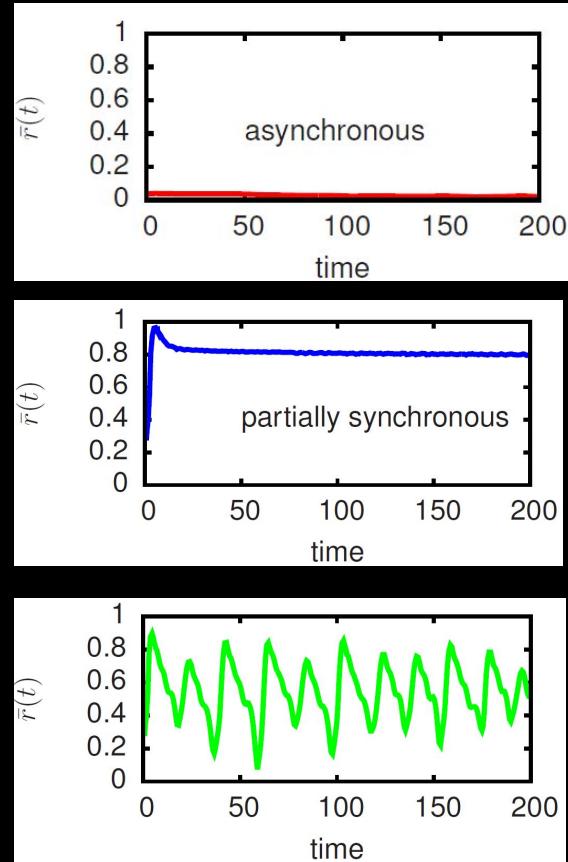


Self-Initiation and -Termination of Sz-like Events

$$r(t) = 1/N \left| \sum_n e^{2\pi i \phi_n(t)} \right|, \quad \bar{r}(t) \text{ local maxima of } r(t)$$

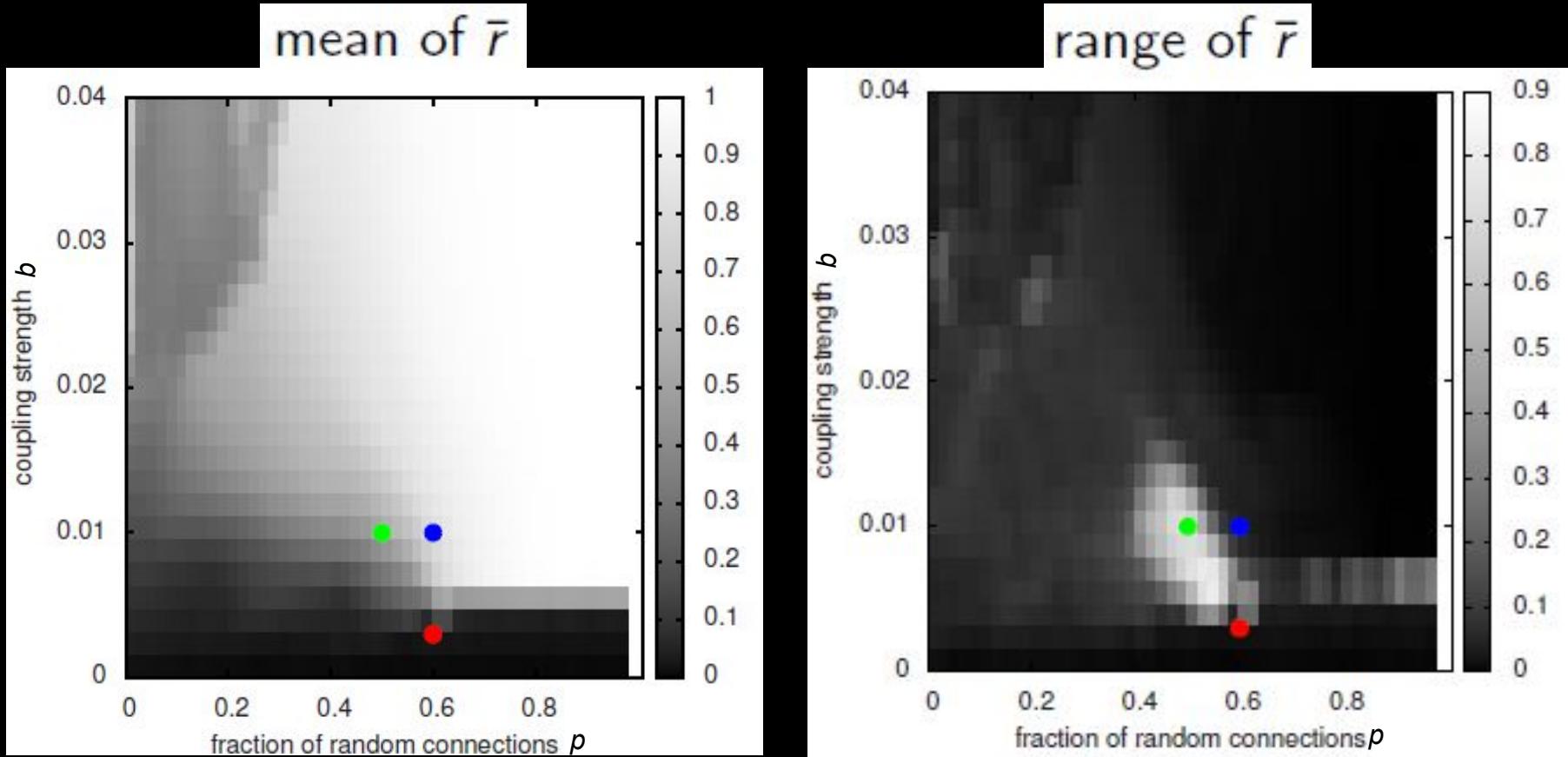


$N = 500 \times 500, m = 50, \tau = 0.01, \vartheta = 0.05;$



Self-Initiation and -Termination of Sz-like Events

$$r(t) = 1/N \left| \sum_n e^{2\pi i \phi_n(t)} \right|, \quad \bar{r}(t) \text{ local maxima of } r(t)$$

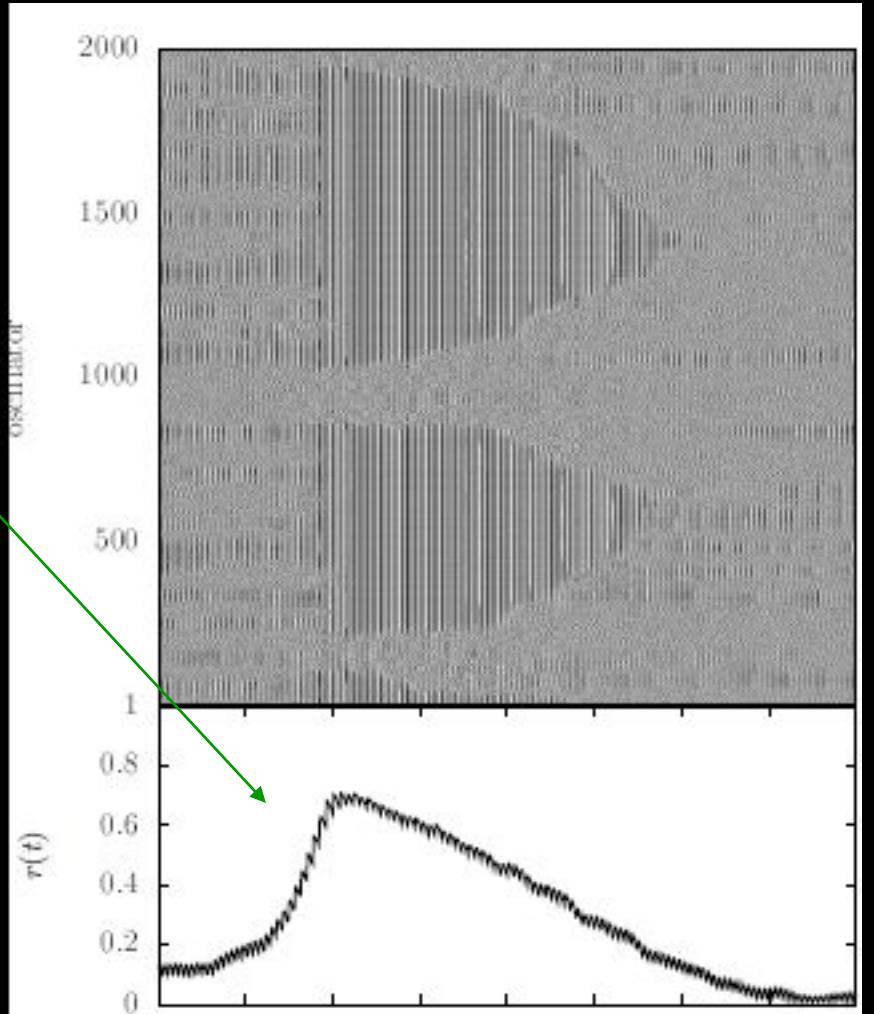
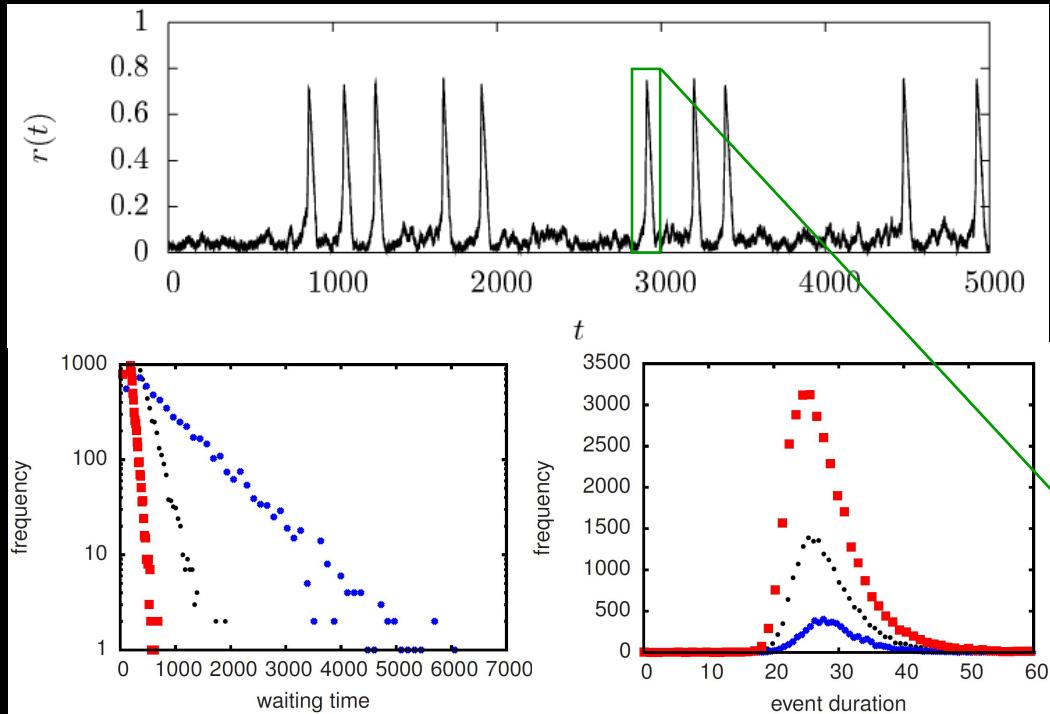


$N = 500 \times 500, m = 50, \tau = 0.01, \vartheta = 0.05;$



Self-Initiation and -Termination of Sz-like Events

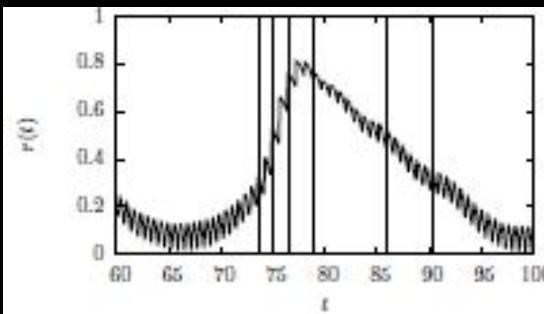
$N = 500 \times 500$, $p = 0.5$, $m = 50$, $\tau = 0.01$, $b = 0.01$, various v



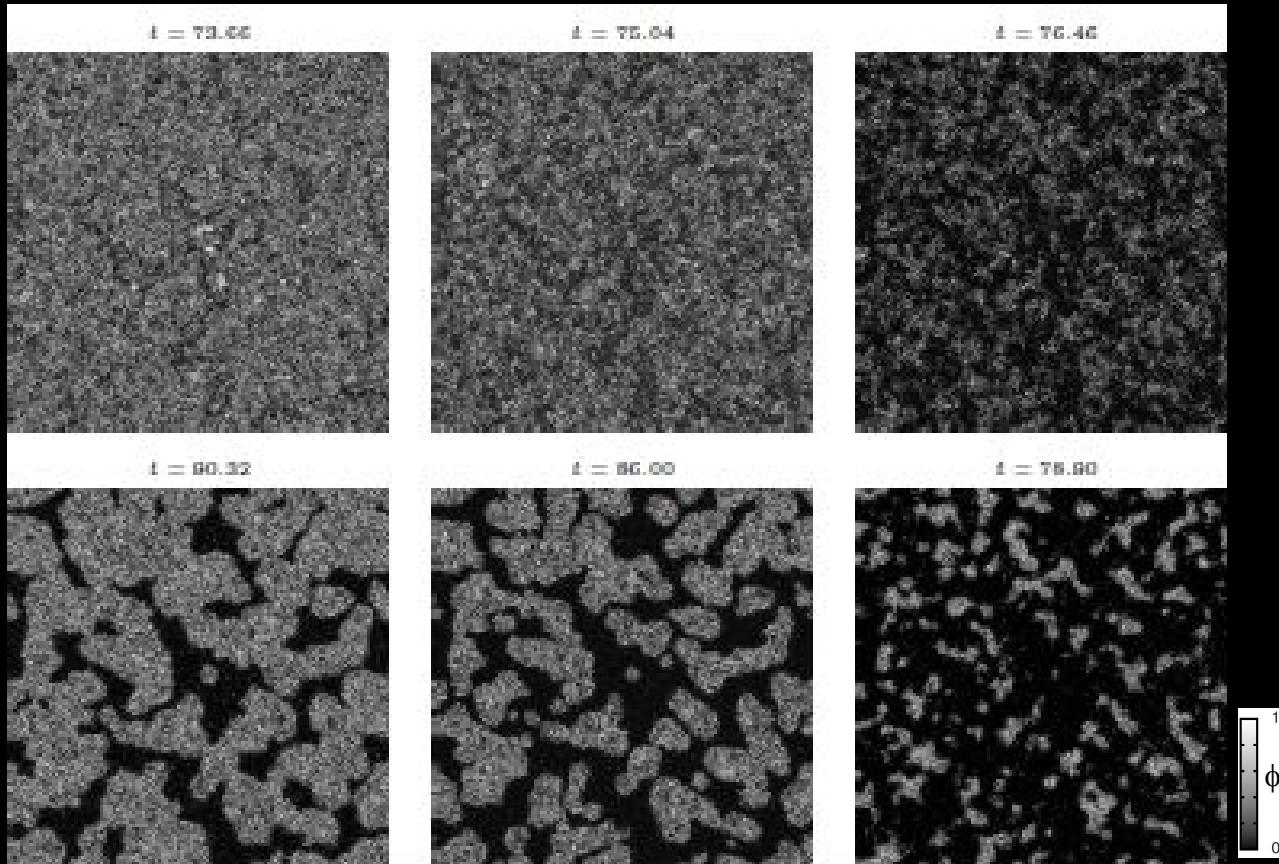
- small-amplitude oscillations with average phase velocity of oscillators
- non-converging macroscopic behavior, network-generated rhythms



Self-Initiation and -Termination of Sz-like Events



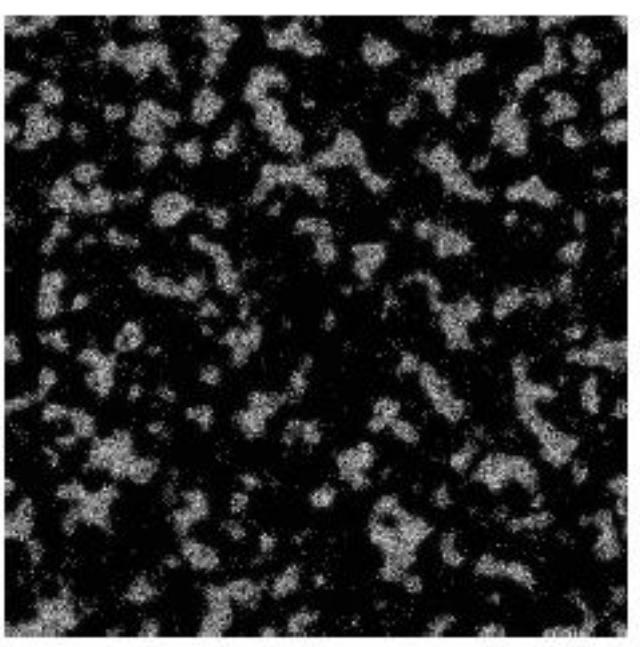
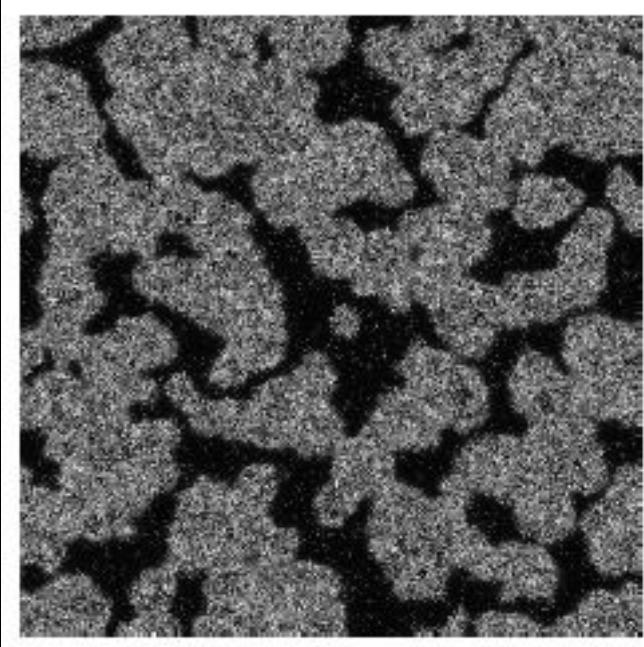
$N = 500 \times 500, m = 50, \tau = 0.01, b = 0.01, v = 0.05$



- comparable values of $r(t)$ during ascending and descending part of event
- distributed asynchronous regions during ascending part
- connected asynchronous regions during descending part



Self-Initiation and -Termination of Sz-like Events



mechanisms:

- stability of asynchronous regions
- stability of synchronous regions
- growing of asynchronous regions
- shrinking of asynchronous regions

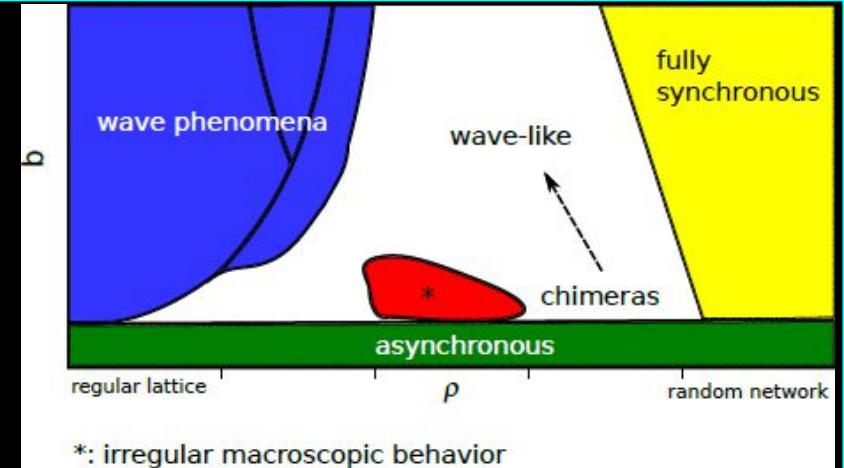
long-range connections

short-range connections



Self-Initiation and -Termination of Sz-like Events

- ***no inhibition***
- ***no pacemaker***
- ***rhythm is network phenomenon***



- irregular macroscopic dynamics and sz-like events due to self-organized generation of chimera states
- cumulative size of asynchronous regions determined by control parameters
- event initiation via long-range connections
- even termination via short-range connections

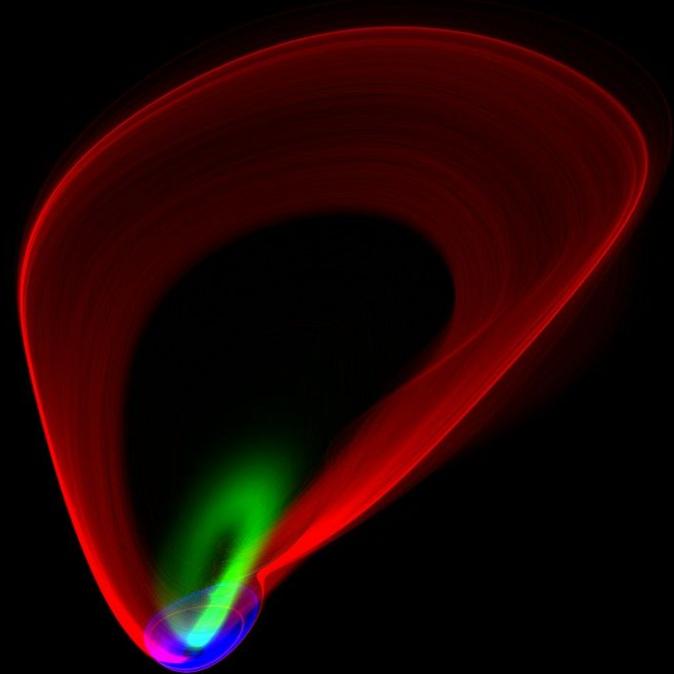
- importance of complex coupling topology



Self-Initiation and -Termination of Sz-like Events

FitzHugh-Nagumo oscillators

$$\begin{aligned}\dot{x}_i &= x_i(a - x_i)(x_i - 1) - y_i + k \sum_{j=1}^n A_{ij}(x_j - x_i), \\ \dot{y}_i &= b_i x_i - c y_i.\end{aligned}\tag{1}$$



- small-world network based on $n = 100 \times 100$ lattice
- weak coupling ($k \sim 10^{-3}$)
- cyclic boundary conditions
- 60 nearest neighbors
- rewiring probability of $p = 0.2$
- a, b_i, c fixed
- observable: spatial mean of x
- “critical mass”
- channel-like structures
- mixed-mode oscillations



Conclusions

- epilepsy: disorder of large-scale neuronal networks
(structure & function)
- paradigm shift: epileptic focus → epileptic network
- seizure self-termination through synchronization
→ new therapeutic options?
- characterization of individual epileptic network
→ individualized treatment?

