

Disentangling respiratory, cardiogenic and vasomotor rhythms from dynamic infrared thermogram signals

Laboratoire Ondes et Matière d'Aquitaine, Bordeaux, France

Françoise Argoul

Alain Arneodo

Léo Delmarre

Alexandre Guillet

Etienne Harte

Stefano Polizzi

Ecole Normale Supérieure de Lyon, Lyon, France

Benjamin Audit

Stephane Roux

**Laboratoire MAST-IFFSTAR Champs sur Marne,
France**

Pierre Argoul

Institute of Continuous Media Mechanics, Perm, Russia

Evgeniya Gerasimova-Chechkina

Oleg Naimark

Perm State Academy of Medecine, Perm, Russia

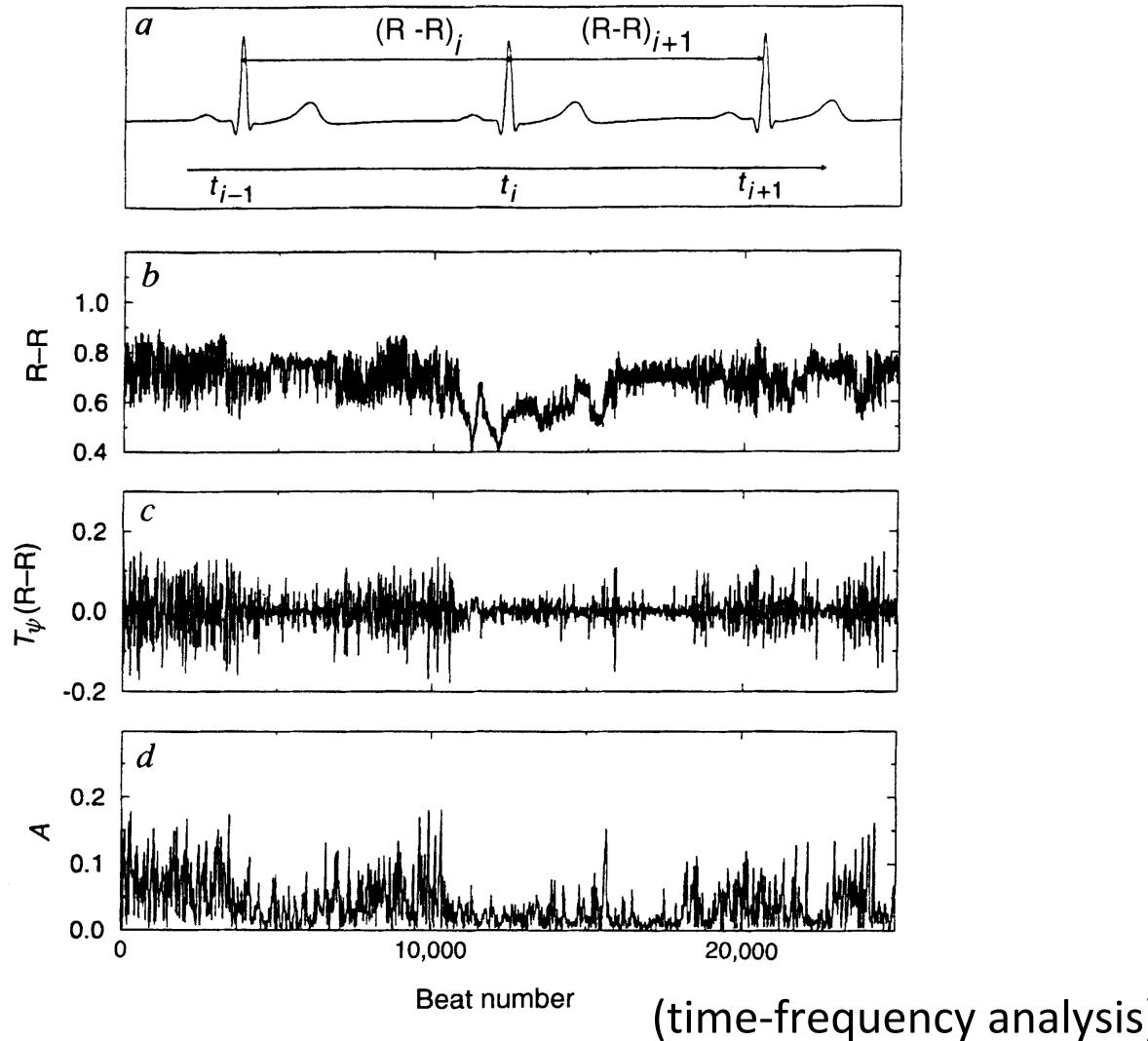
Olga Gileva

E. Gerasimova et al., EPL 104 (2013) 68011

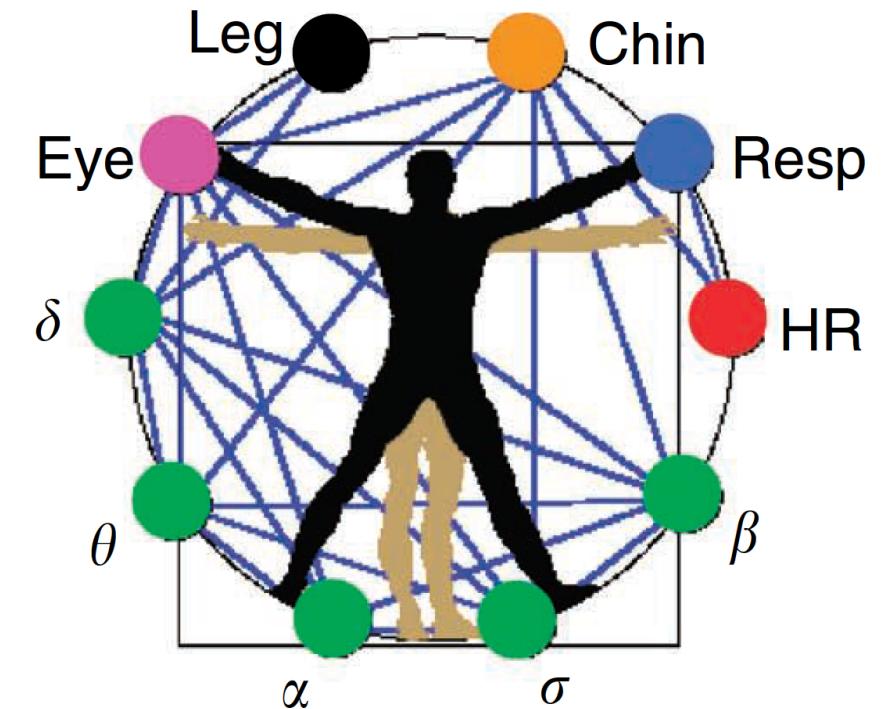
E. Gerasimova et al., Frontiers in Physiology 5 (2014) 176

Physiological networks : the inter-node dynamics complexity is the issue

Scaling behavior of heartbeat intervals
Ivanov et al. Nature **1996**



Network Physiology ->
Network Topology <-> Physiological Function
Bashan Nature Communications **2012**

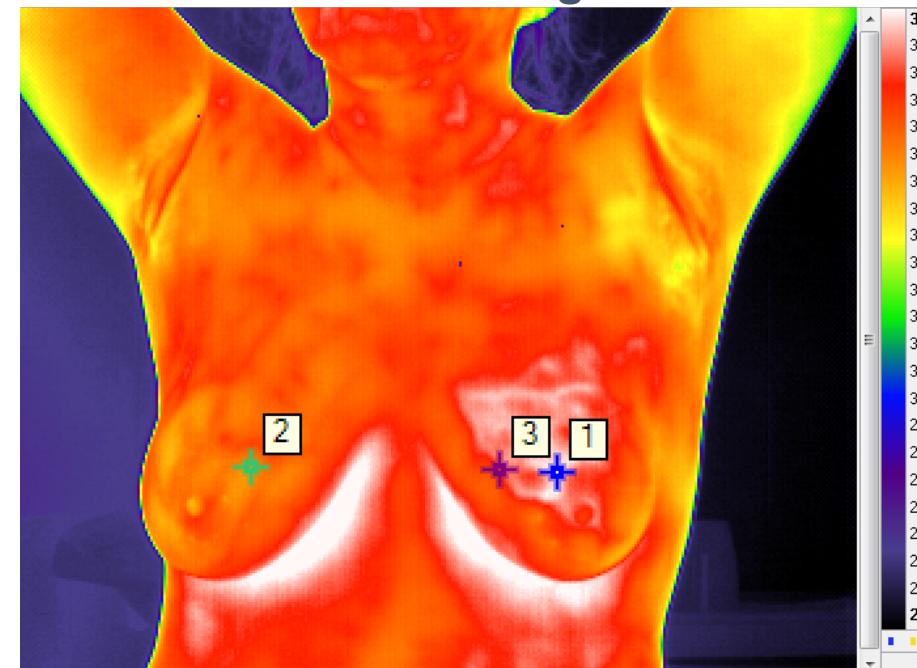


Infrared camera

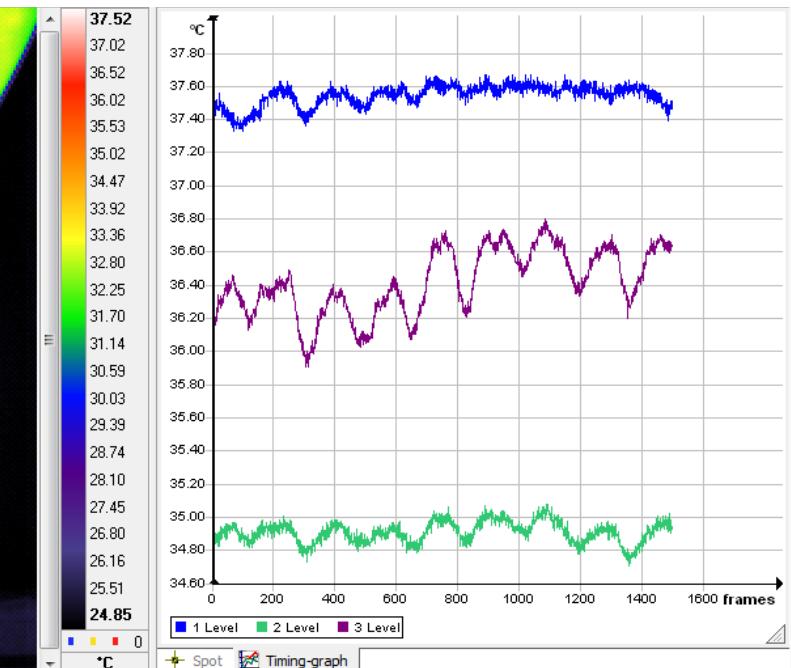


IR thermography to assist cancer diagnosis

Breast thermogram



Temperature time series



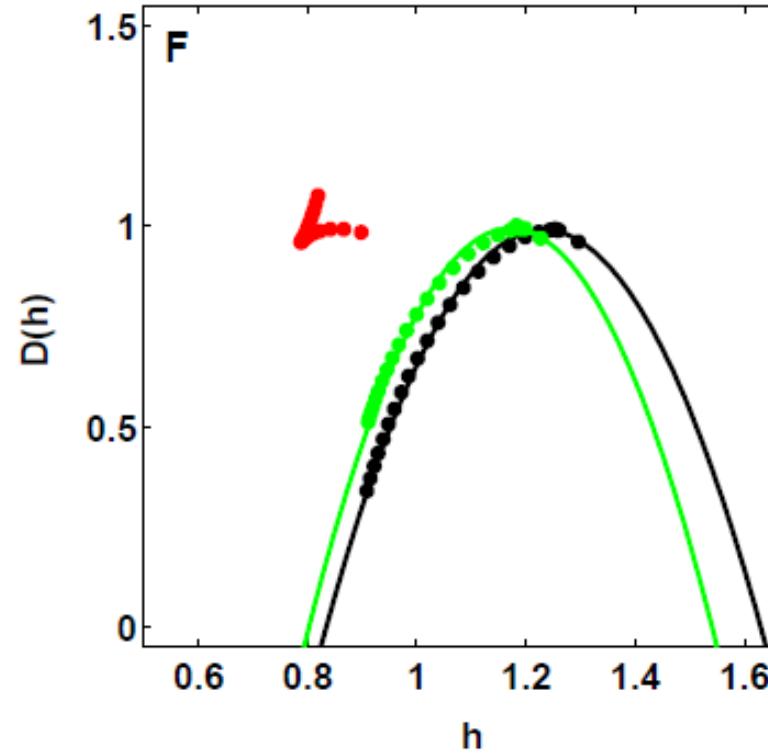
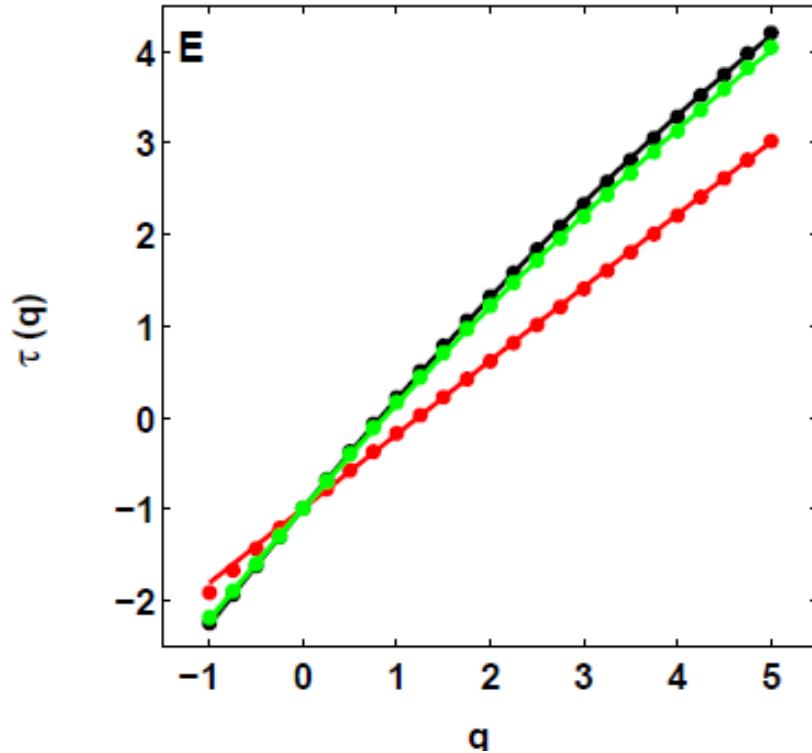
..... -> IR thermography video film

PLAN OF THE PRESENTATION

- Characterization of the physiological noise of thermogram signals
 - singularity spectra computation based on the wavelet modulus maxima method in both healthy and cancer cases (local temperature averaged on 8x8 pixel squares)
- Disentangling respiratory, cardiogenic rhythms from thermogram signals
 - Respiratory and cardiogenic functions impact on both the spatial position and temperature
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Multifractal spectra of cumulative IR temperature time series

Average over 8x8 pixel²



$$\tau(q) = -c_0 + c_1 q - c_2 q^2 / 2$$
$$D(h) = c_0 - (h - c_1)^2 / 2c_2$$

Cancer

$[c_0, c_1, c_2] = [0.99, 0.81, 0.0044]$

Opposite

$[c_0, c_1, c_2] = [0.99, 1.23, 0.080]$

Healthy

$[c_0, c_1, c_2] = [0.99, 1.171, 0.069]$

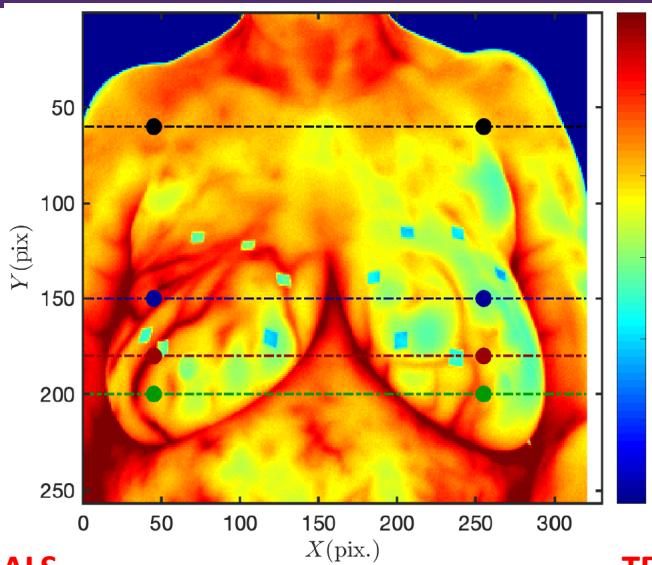
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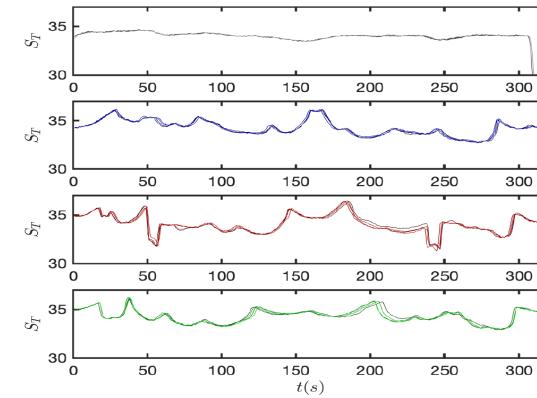
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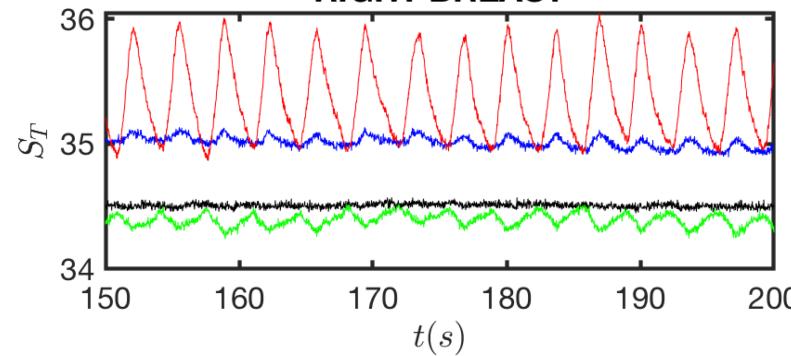
Respiratory and cardiogenic functions impact both the spatial tissue position and skin temperature



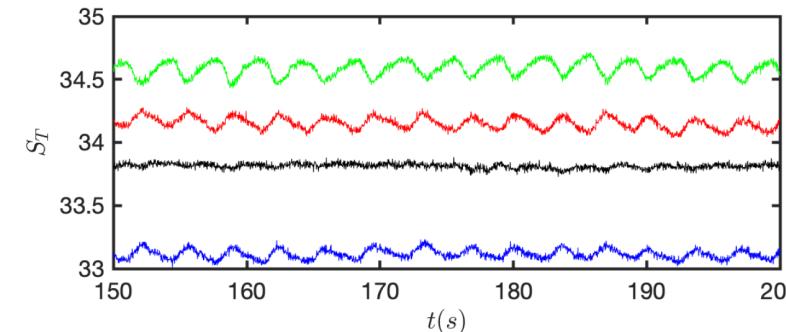
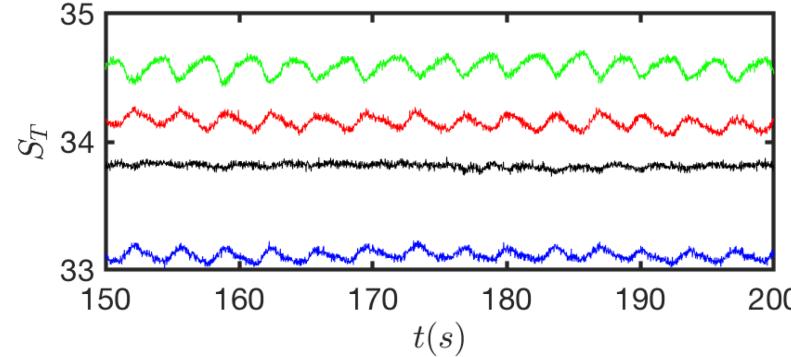
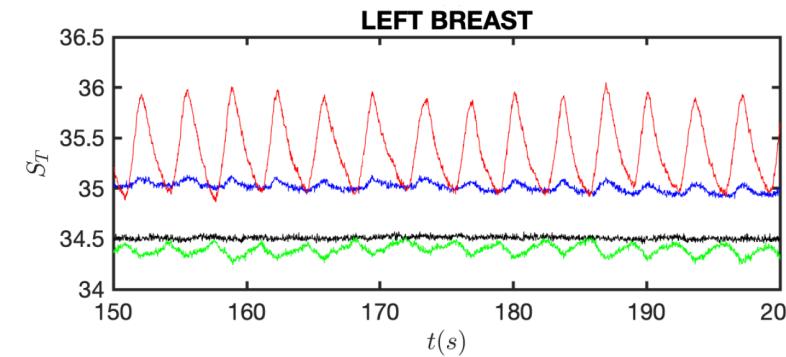
HORIZONTAL SECTIONS



TEMPERATURE SIGNALS
RIGHT BREAST



TEMPERATURE SIGNALS



Wavelet transform for time-frequency analysis of rhythmic signals

$$\mathcal{W}_\psi[s](a, t; p) = \int_{-\infty}^{+\infty} s(t') a^{-\frac{1}{p}} \bar{\psi}\left(\frac{t' - t}{a}\right) dt'$$

ψ Wavelet function (in time variable)

(the bar corresponds to the complex conjugate)

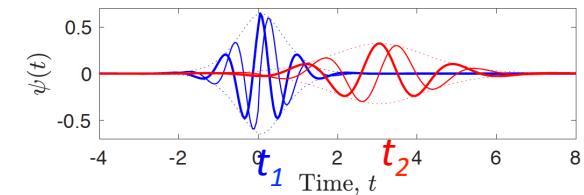
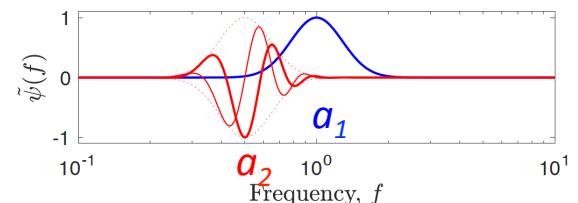
t translation parameter

a scale parameter ($a = f_0/f$)

p normalization exponent

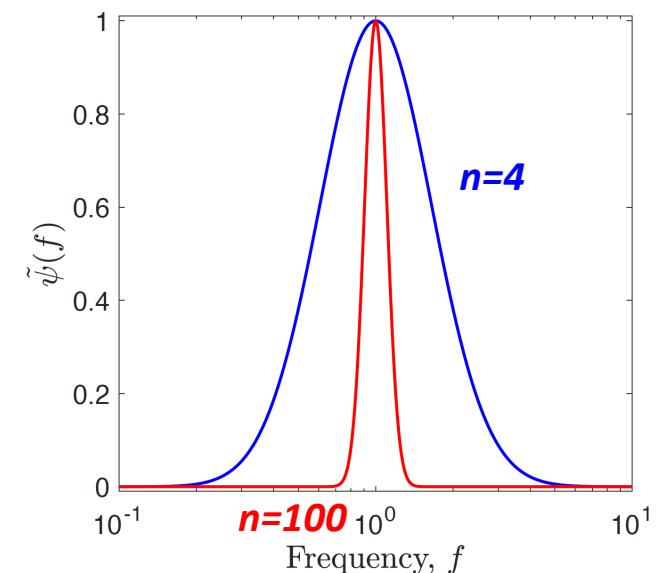
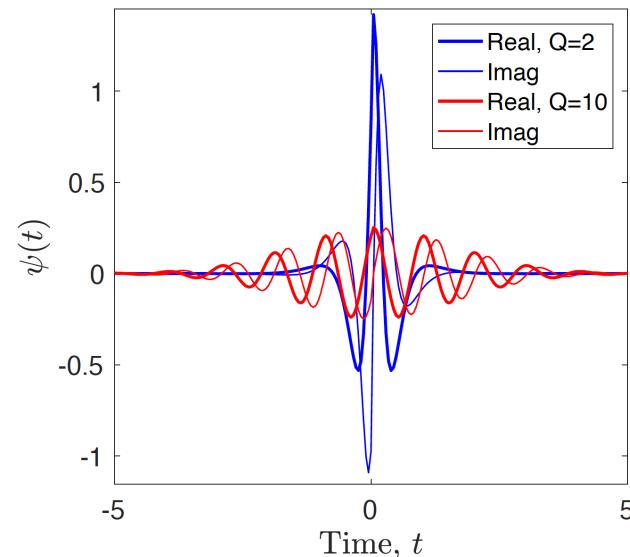
$Q = (n\gamma)^{1/2}$ quality factor

The larger Q , the sharper the wavelet
in frequency domain

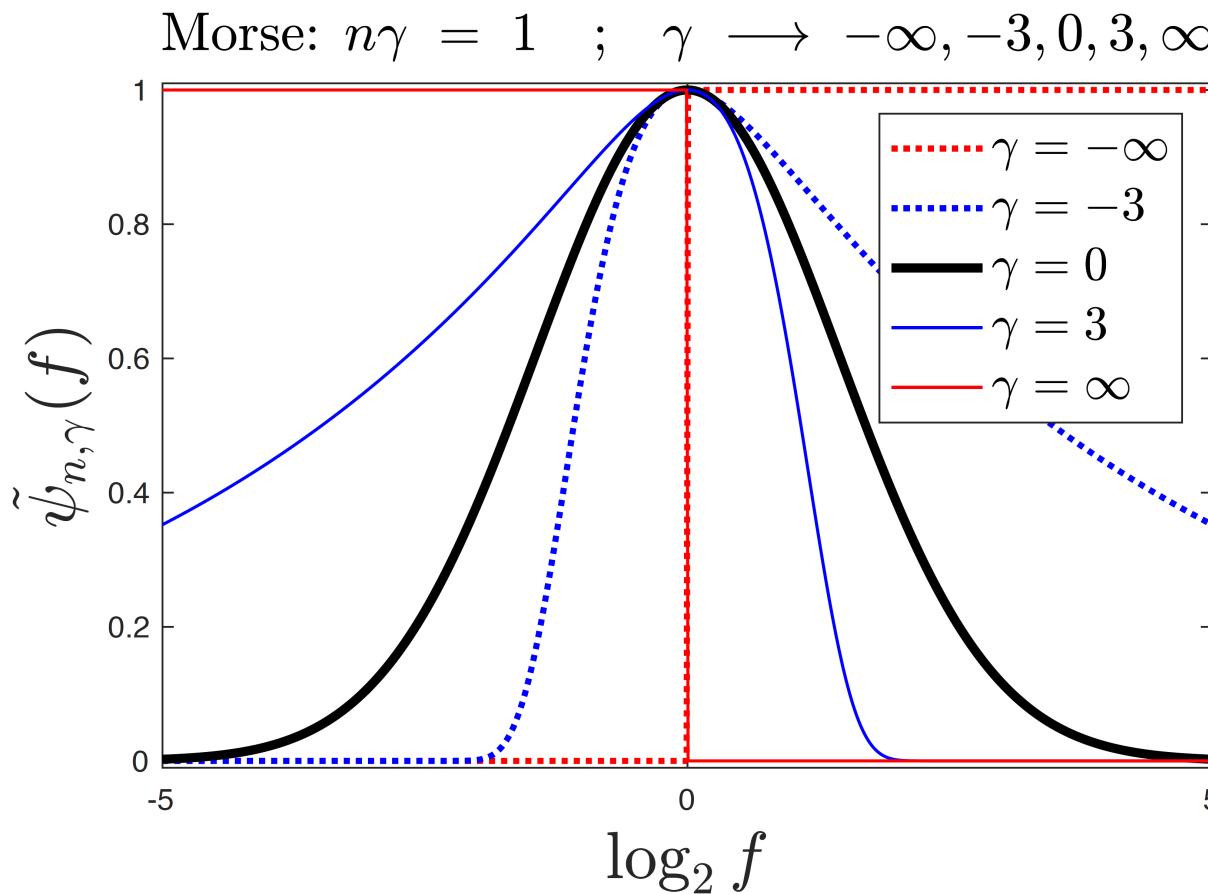


Morse wavelet

$$\tilde{\psi}_{n,\gamma}(f) \propto f^n e^{-f^\gamma} \quad \forall f > 0 ; \quad 0 \text{ if } f \leq 0$$



Wavelet transform for time-frequency analysis of rhythmic signals



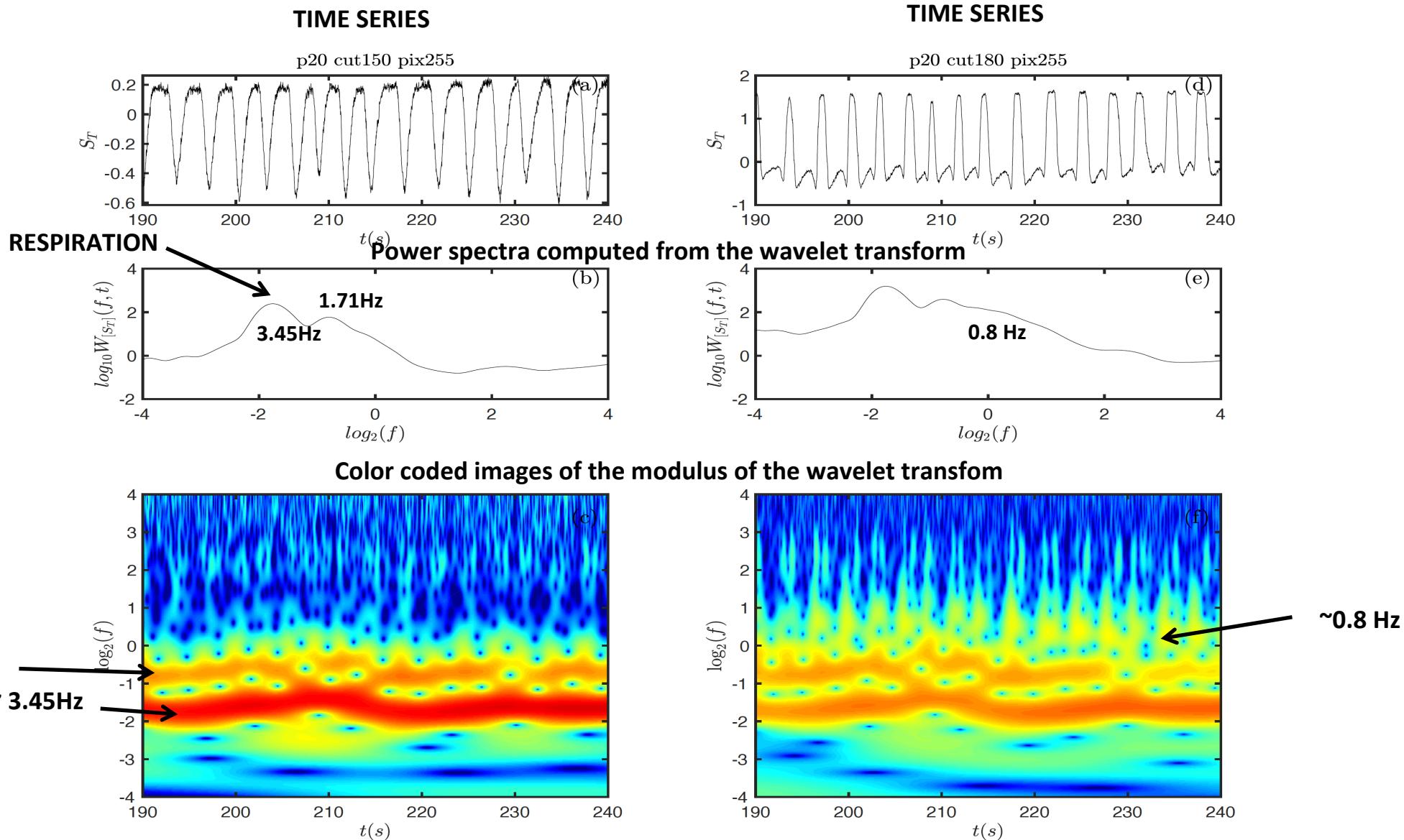
Log-normal Morse wavelet: $\gamma = 0, n\gamma = 1$

$$\tilde{\psi}_Q(f'/f) = e^{-\frac{1}{2}(Q \log f'/f)^2}$$

This wavelet is symmetric in frequency space
It is parametrized by the quality factor Q

Wavelet transform for time-frequency analysis of rhythmic signals

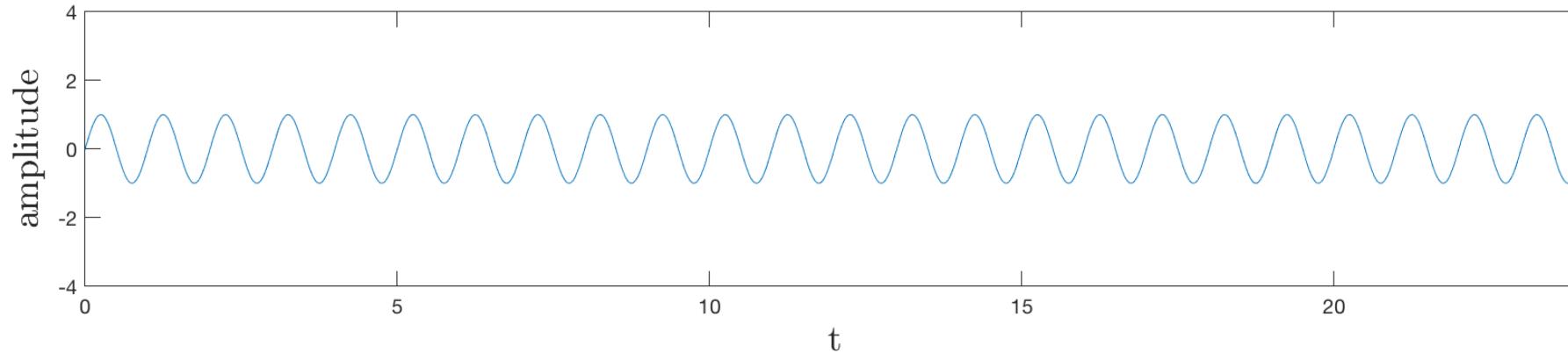
Wavelet:
Morse function
 $n=32, \gamma=1$
 $p=1$



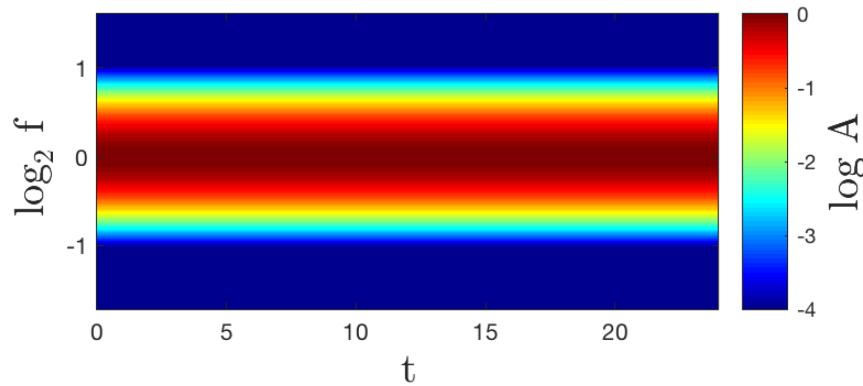
Wavelet transform analysis of model signals

PERIODIC SIGNAL (pure sinus)

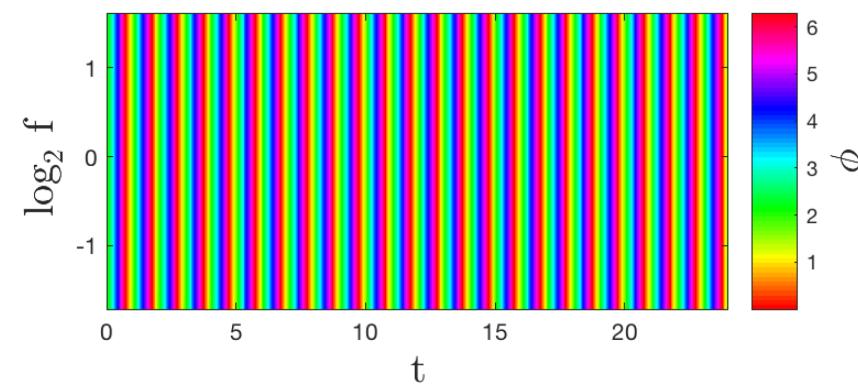
Sine wave



Modulus of the CWT

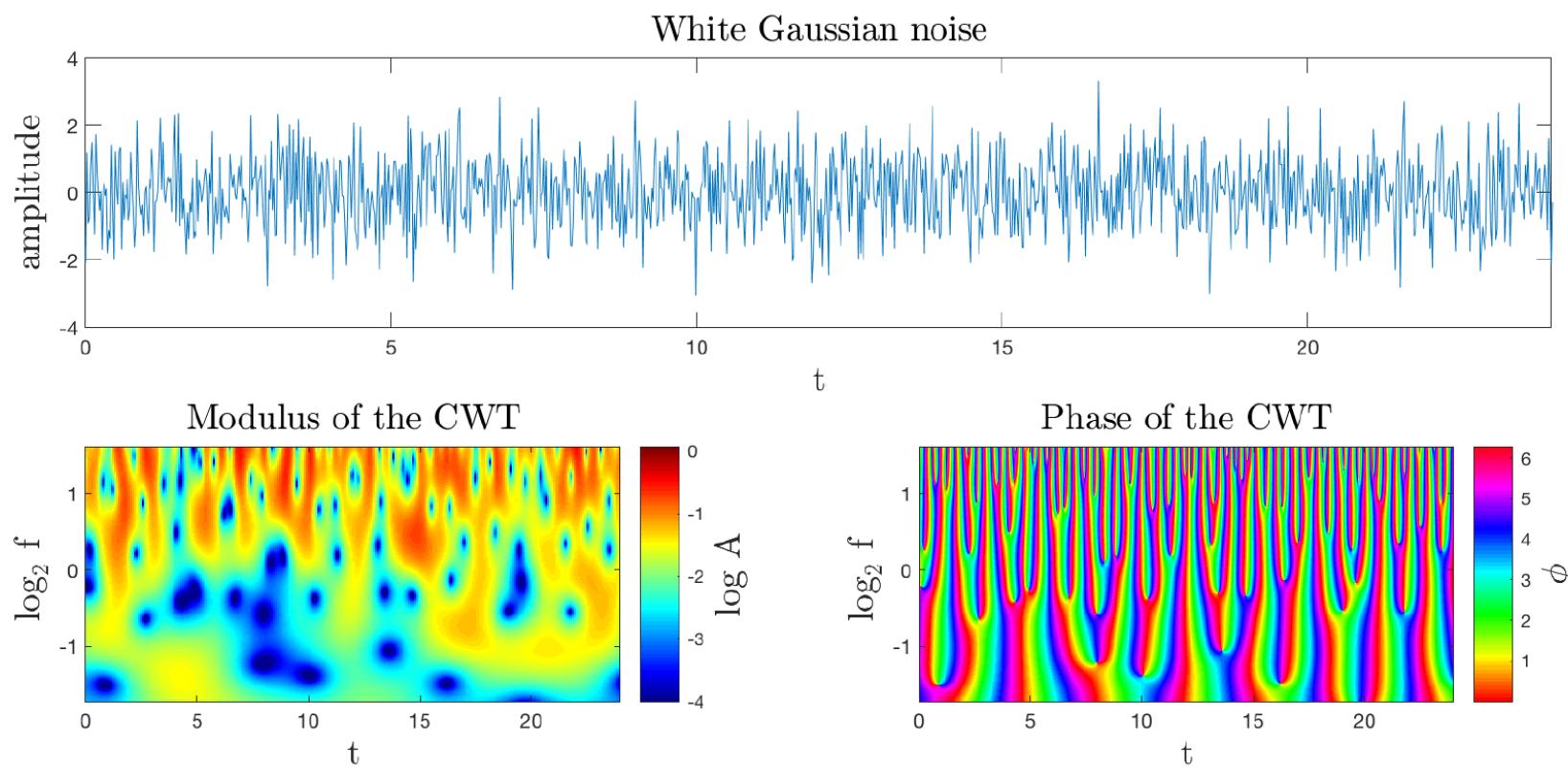


Phase of the CWT



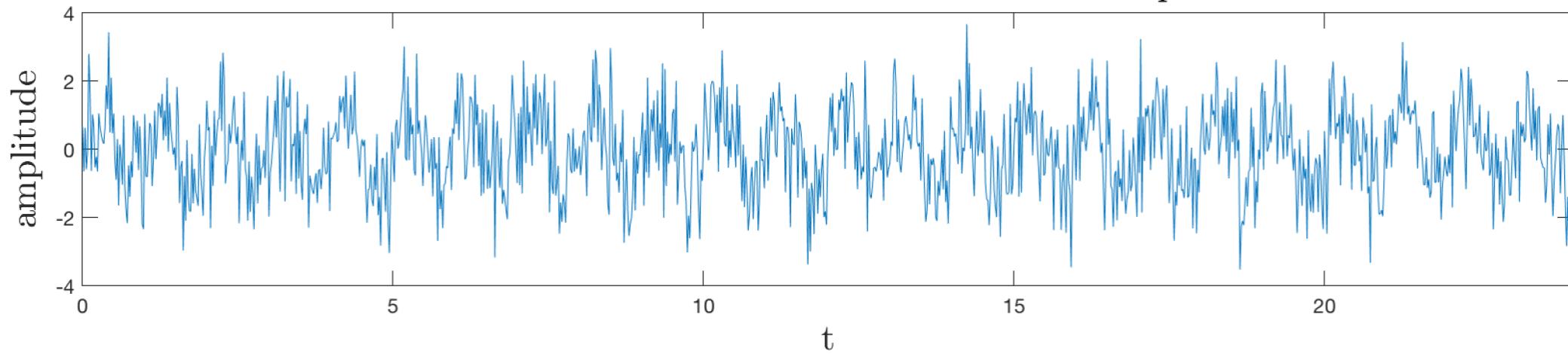
Wavelet transform analysis of model signals

RANDOM SIGNAL (no rhythms)

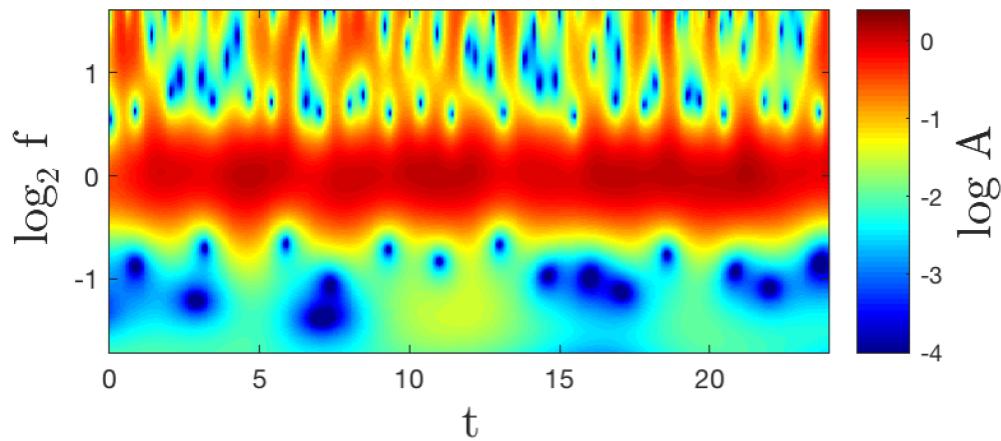


Wavelet transform analysis of model signals

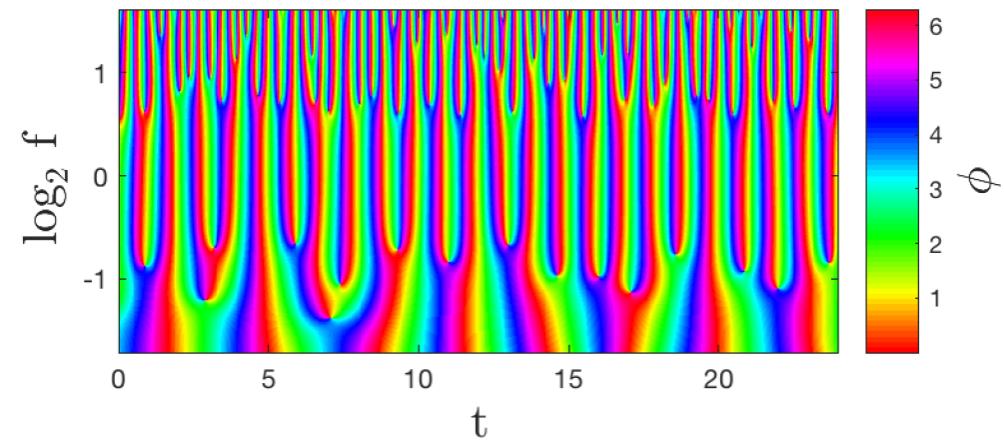
Sine wave + white Gaussian noise with same amplitude



Modulus of the CWT

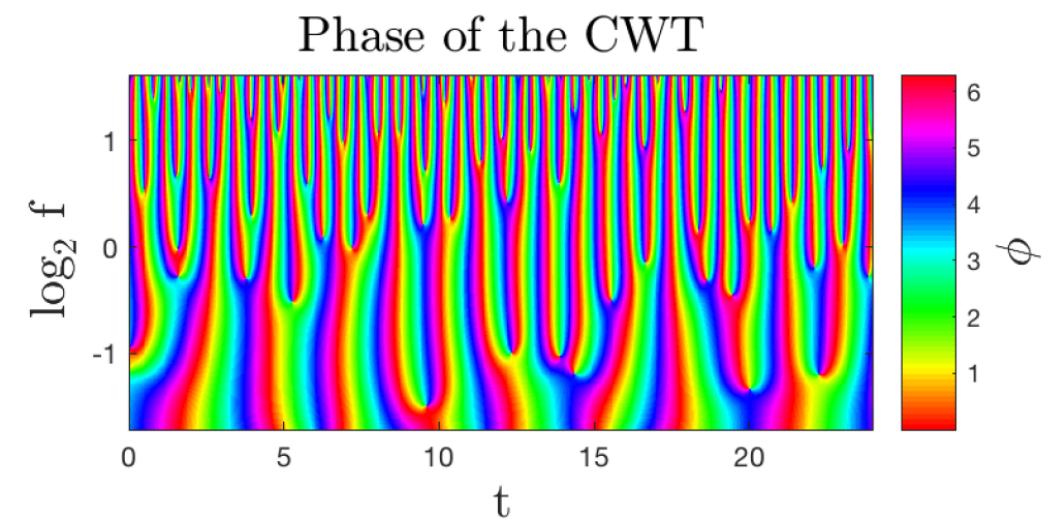
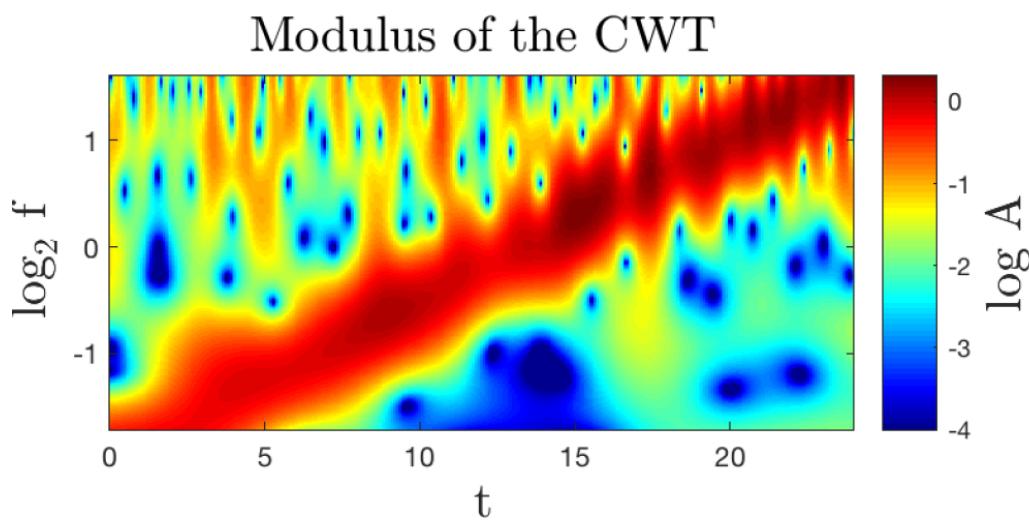
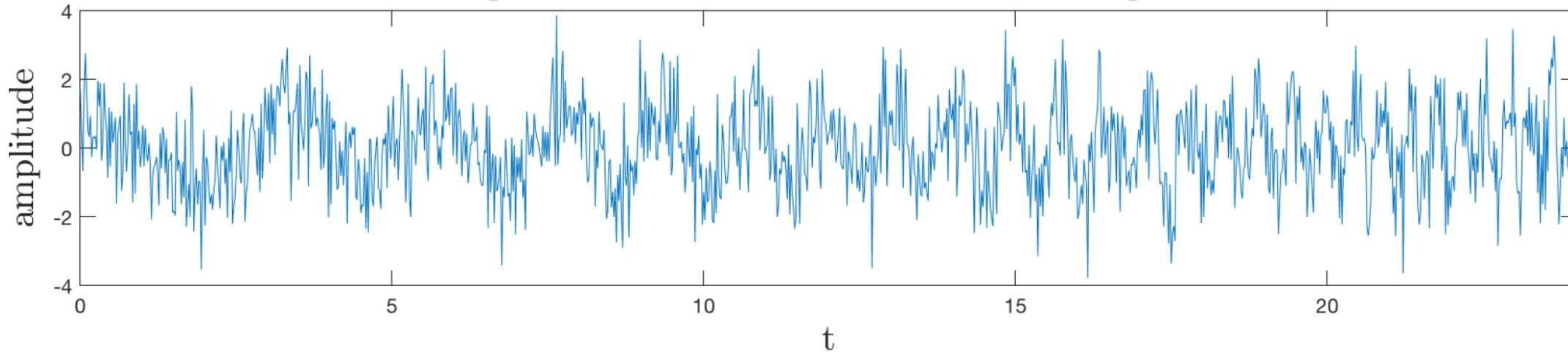


Phase of the CWT



Wavelet transform analysis of model signals

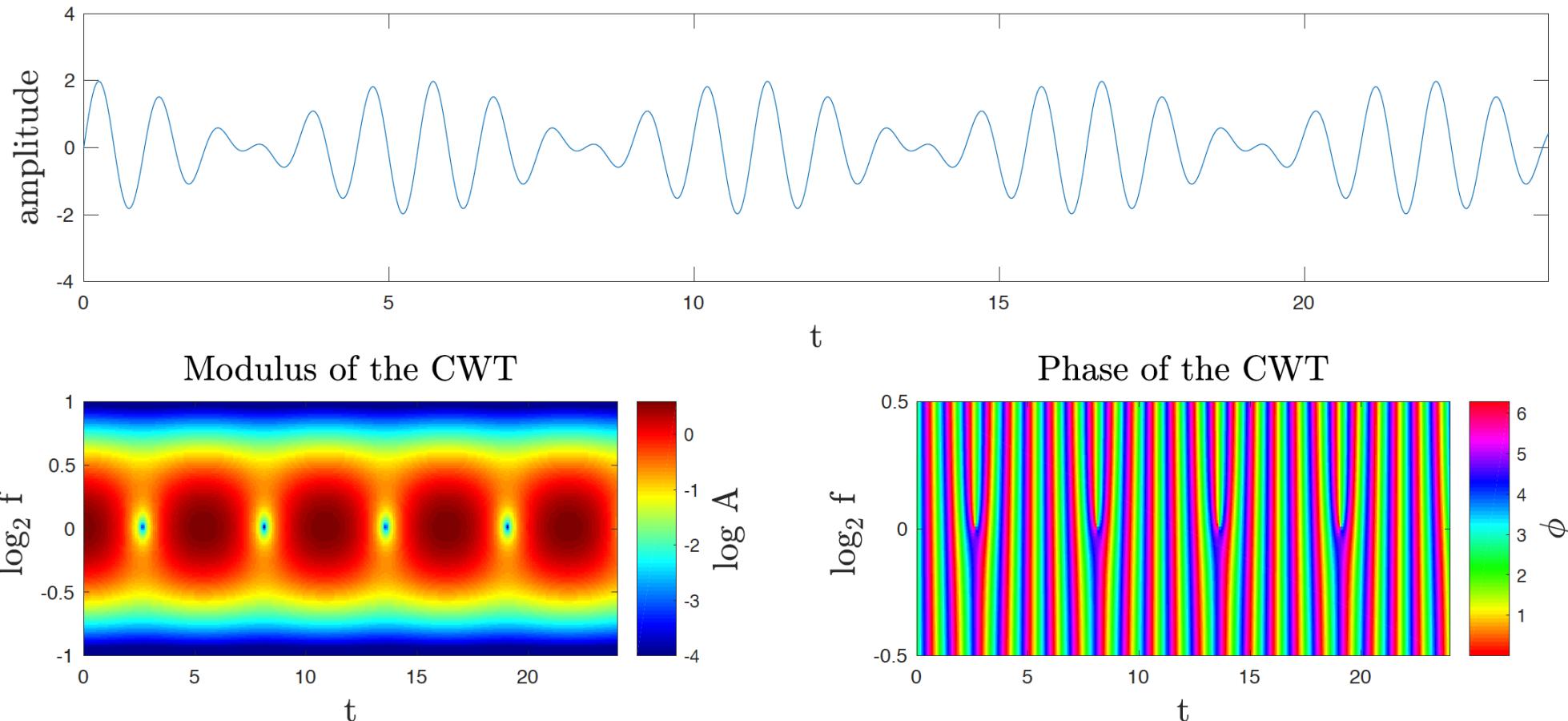
Chirp + white Gaussian noise with same amplitude



Wavelet transform analysis of model signals: frequency duets

$$S(t) = \sin(ft) + \sin((f+\delta f)t)$$

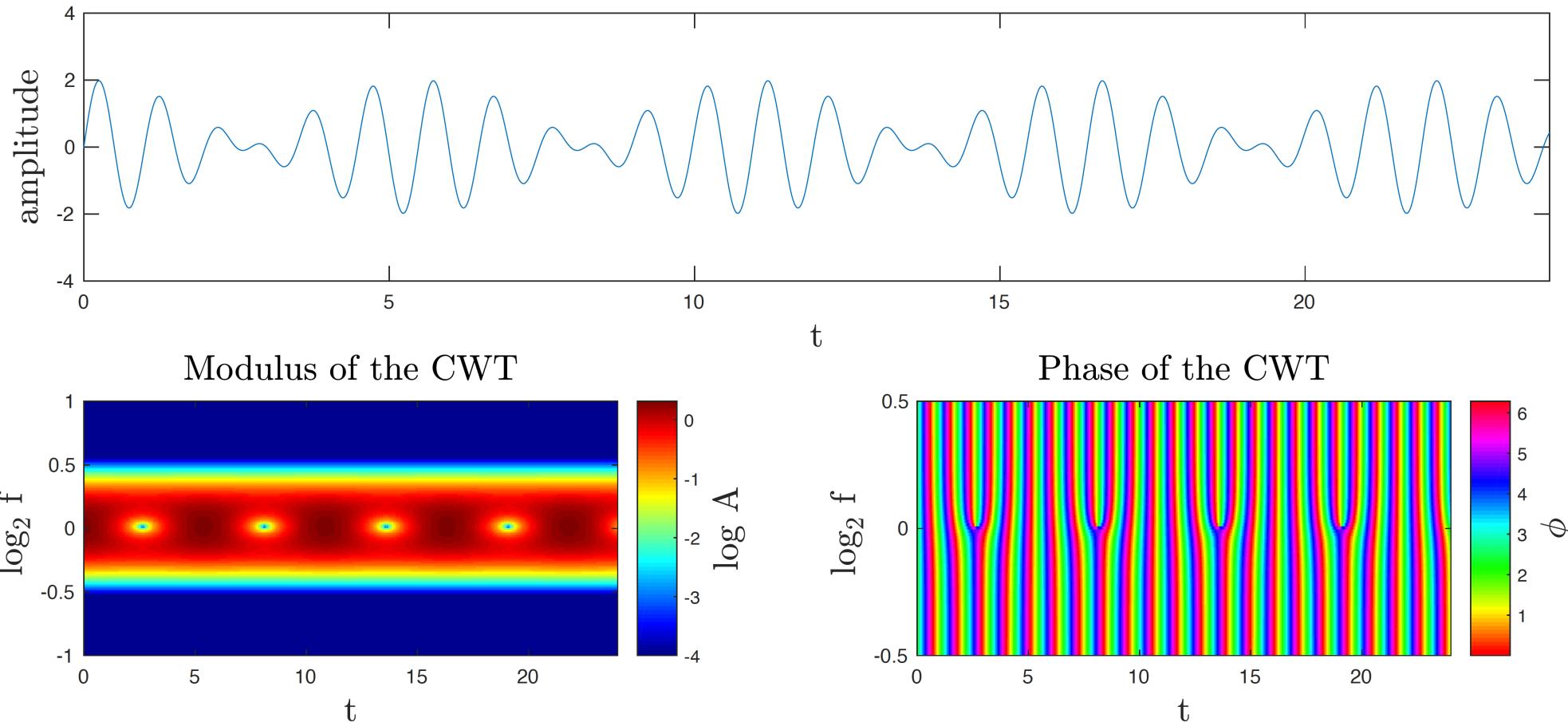
Frequency duet: ratio=1.2, Q=5



Wavelet transform analysis of model signals: frequency duets

$$S(t) = \sin(ft) + \sin((f+\delta f)t)$$

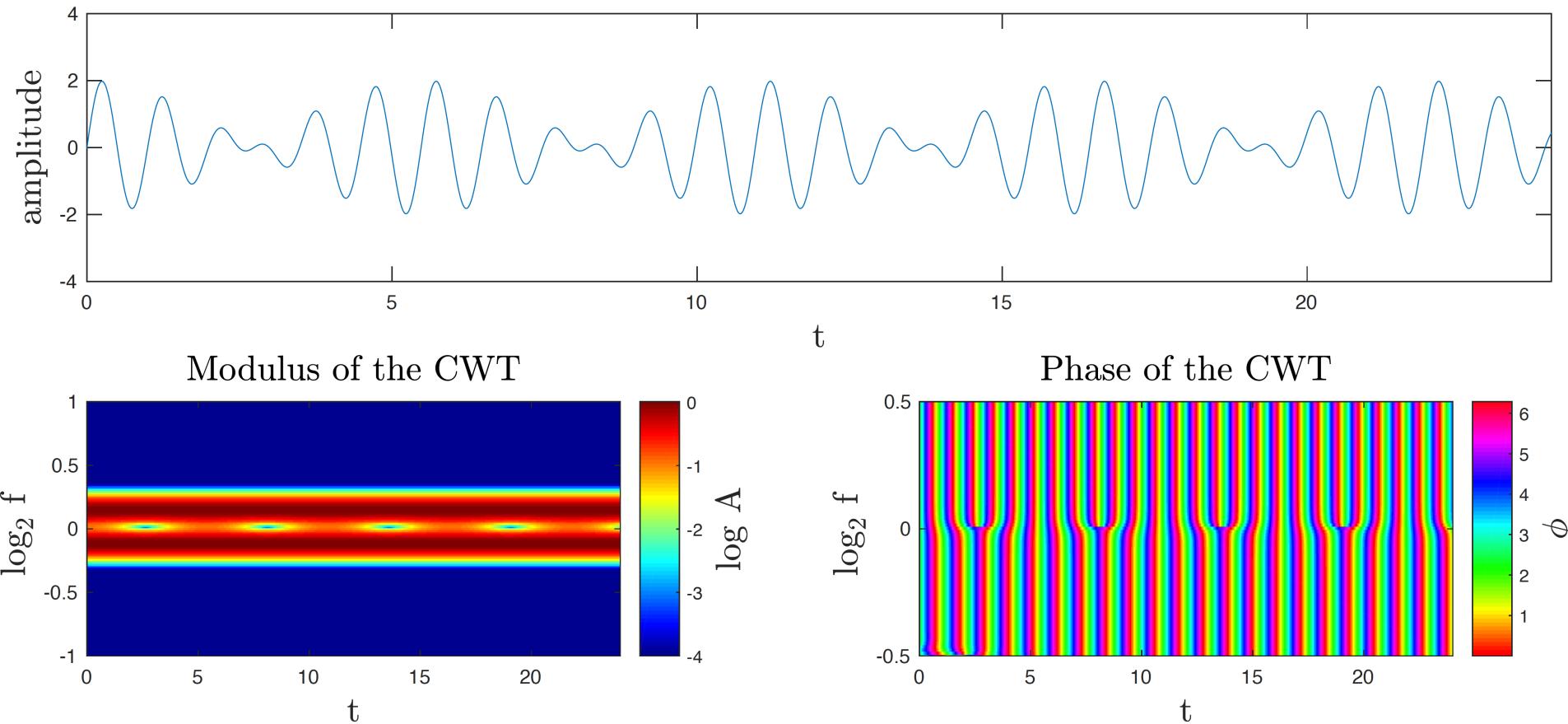
Frequency duet: ratio=1.2, Q=10



Wavelet transform analysis of model signals: frequency duets

$$S(t) = \sin(ft) + \sin((f+\delta f)t)$$

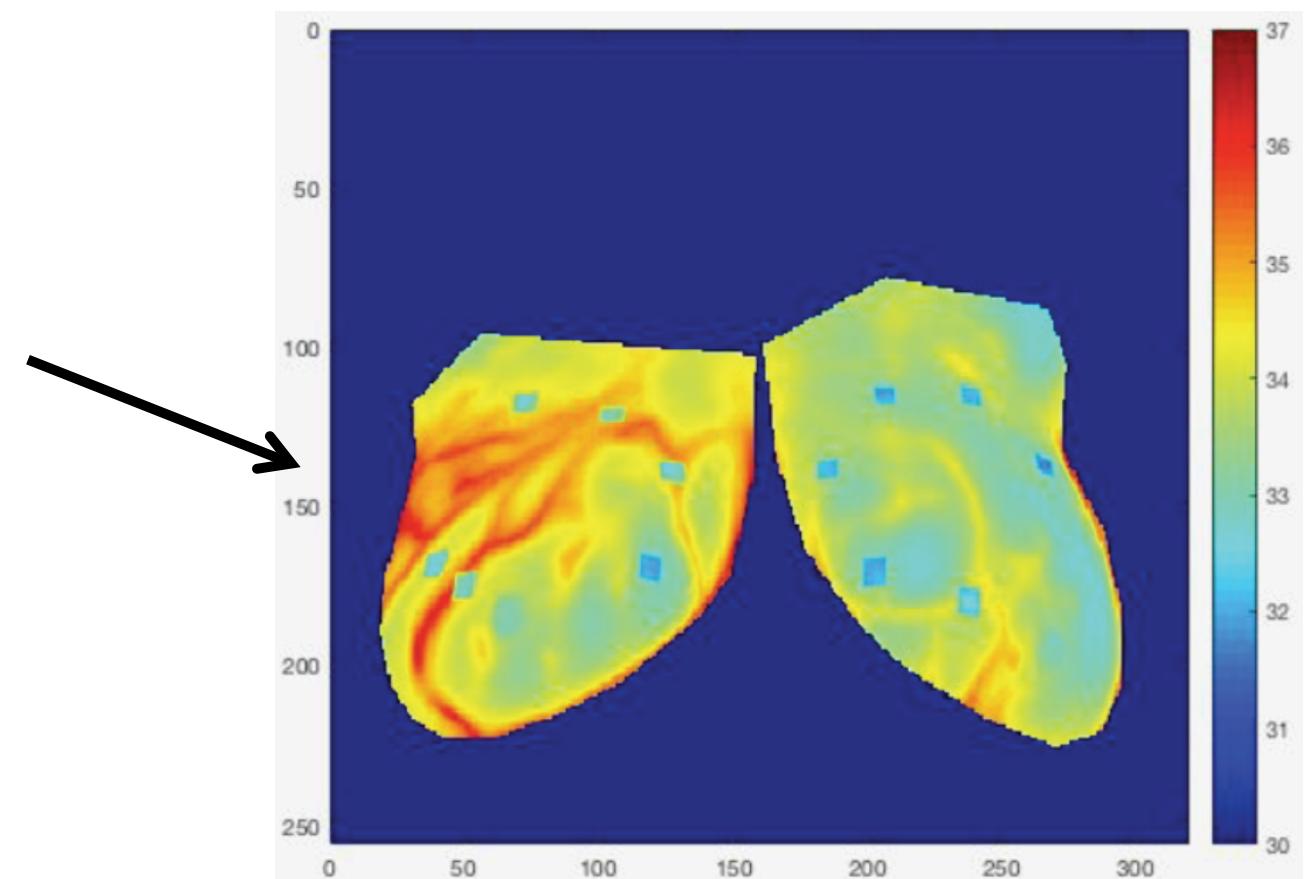
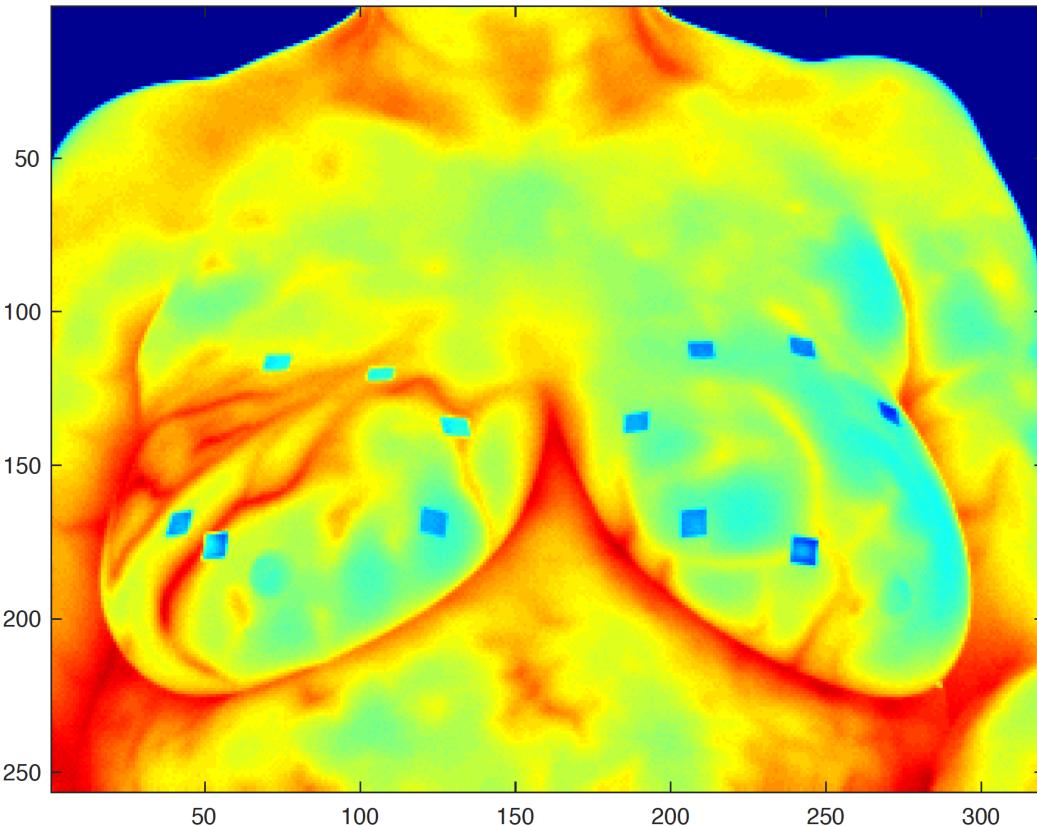
Frequency duet: ratio=1.2, Q=20



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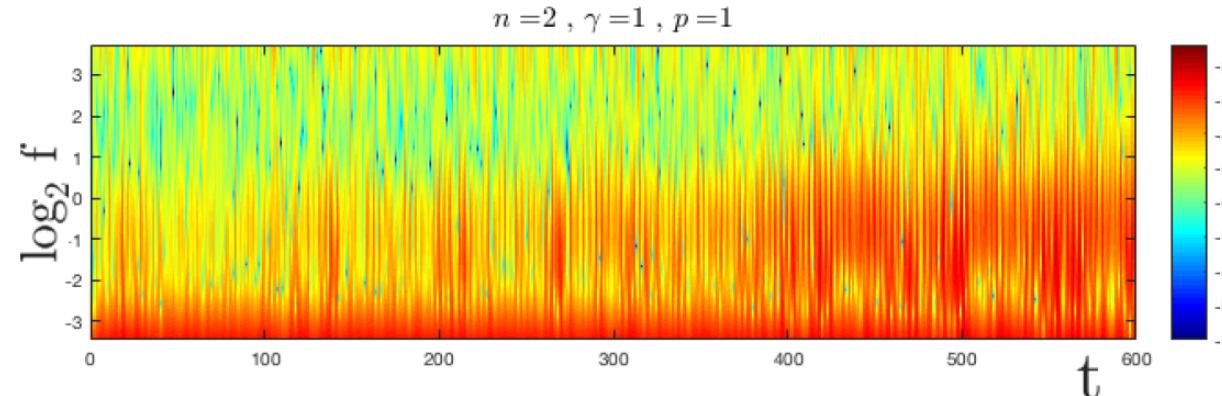
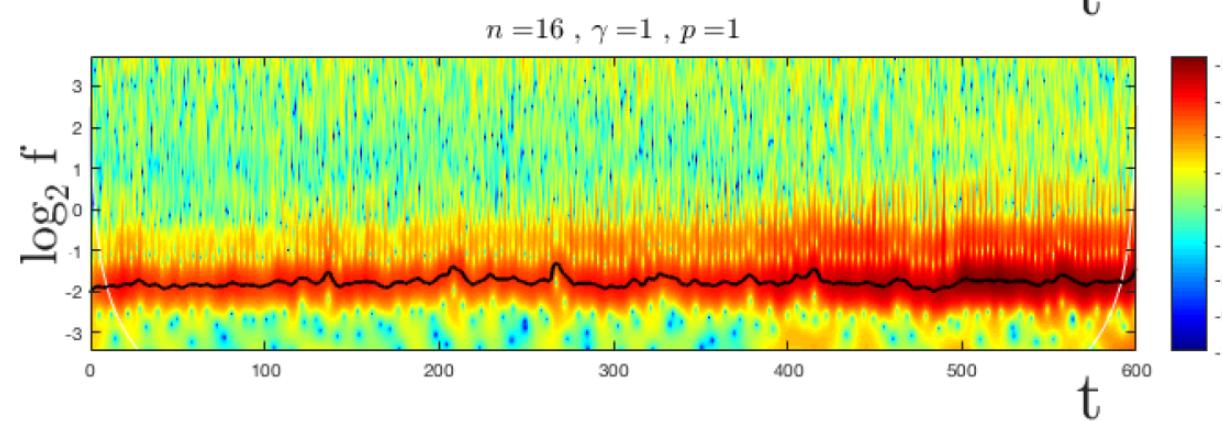
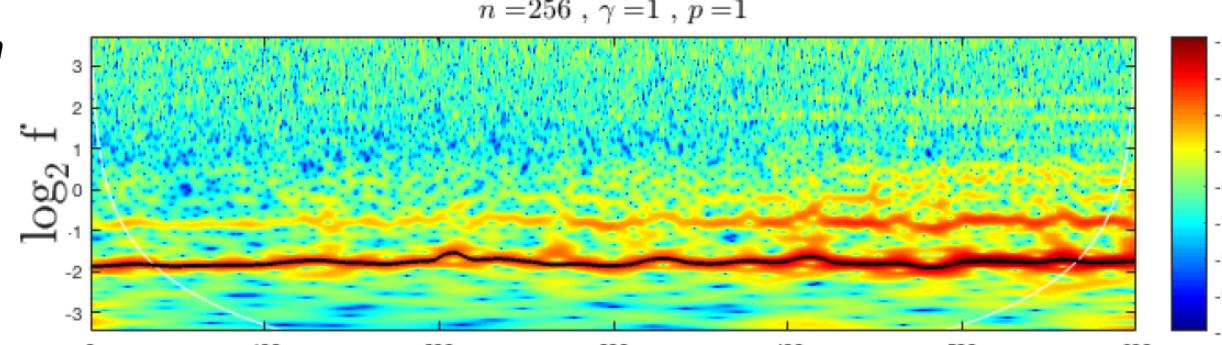
Global selection of the two breasts (R – L) with ellipse-like shapes



Influence of the quality factor Q on the detection of the rhythms

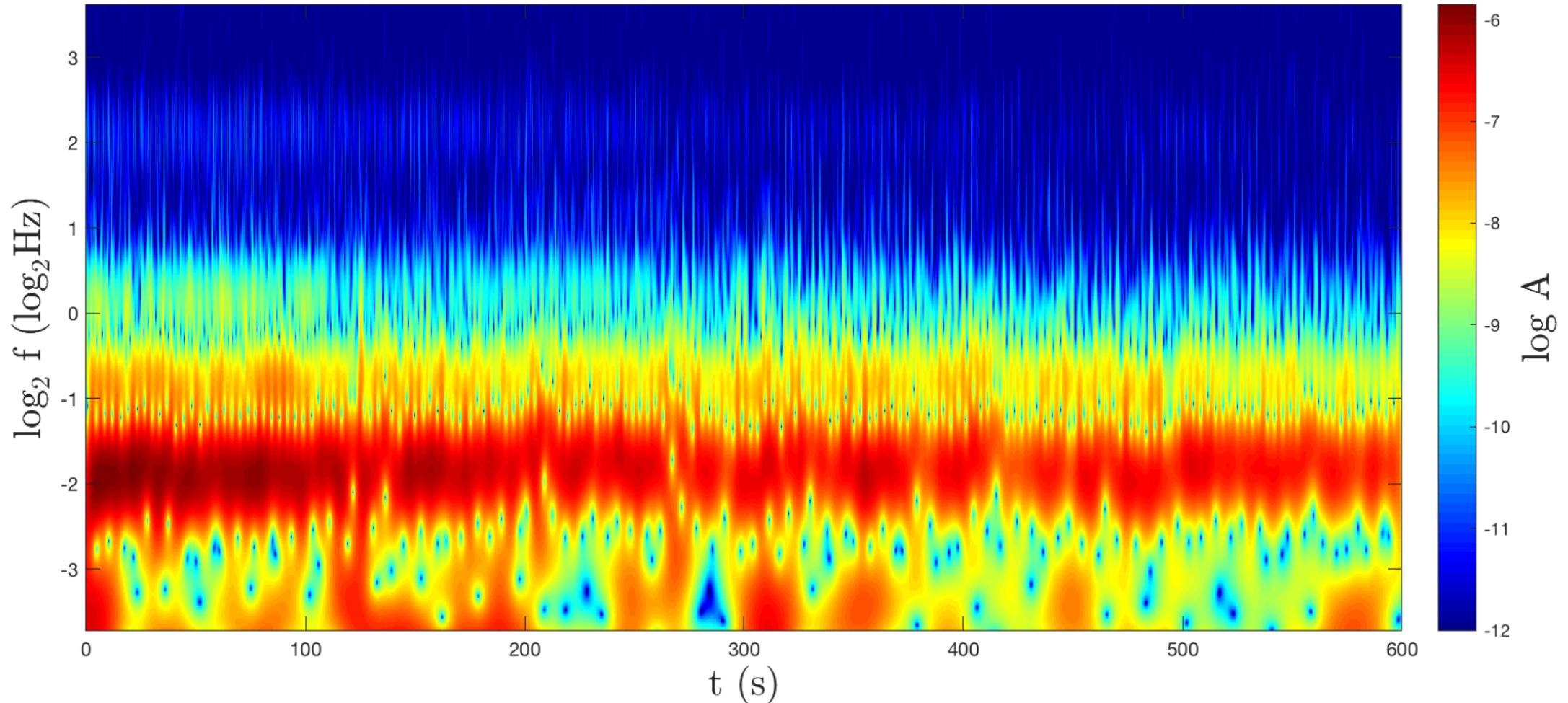
$Q = (n\gamma)^{1/2}$ quality factor

The larger Q , the sharpest the wavelet in frequency domain



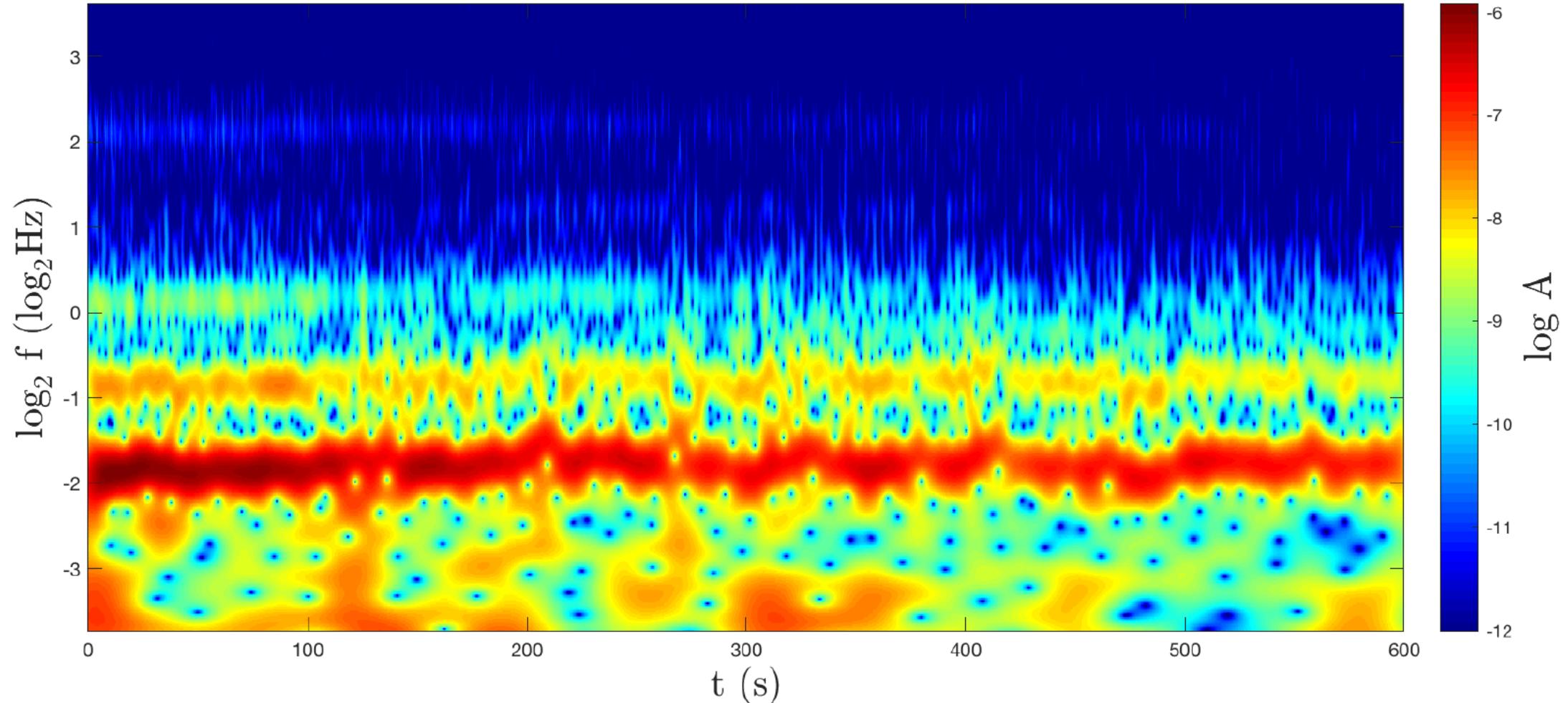
Playing on the wavelet function parameters to reveal both respiratory and cardiac rhythms

Mean of the temperature spatial distribution (p20 left): $Q = 4$, $p = 2$



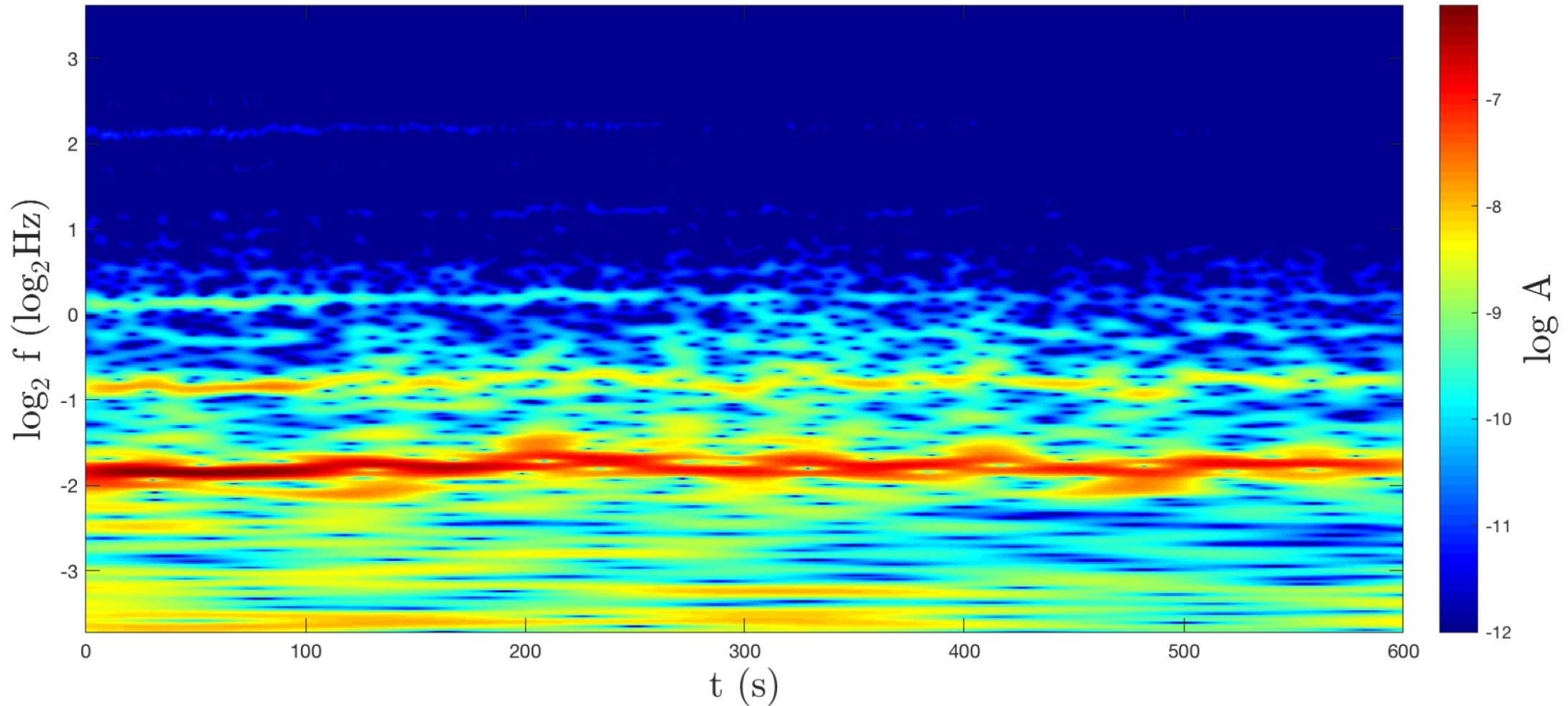
Playing on the wavelet function parameters to reveal both respiratory and cardiac rhythms

Mean of the temperature spatial distribution (p20 left): $Q = 8$, $p = 2$



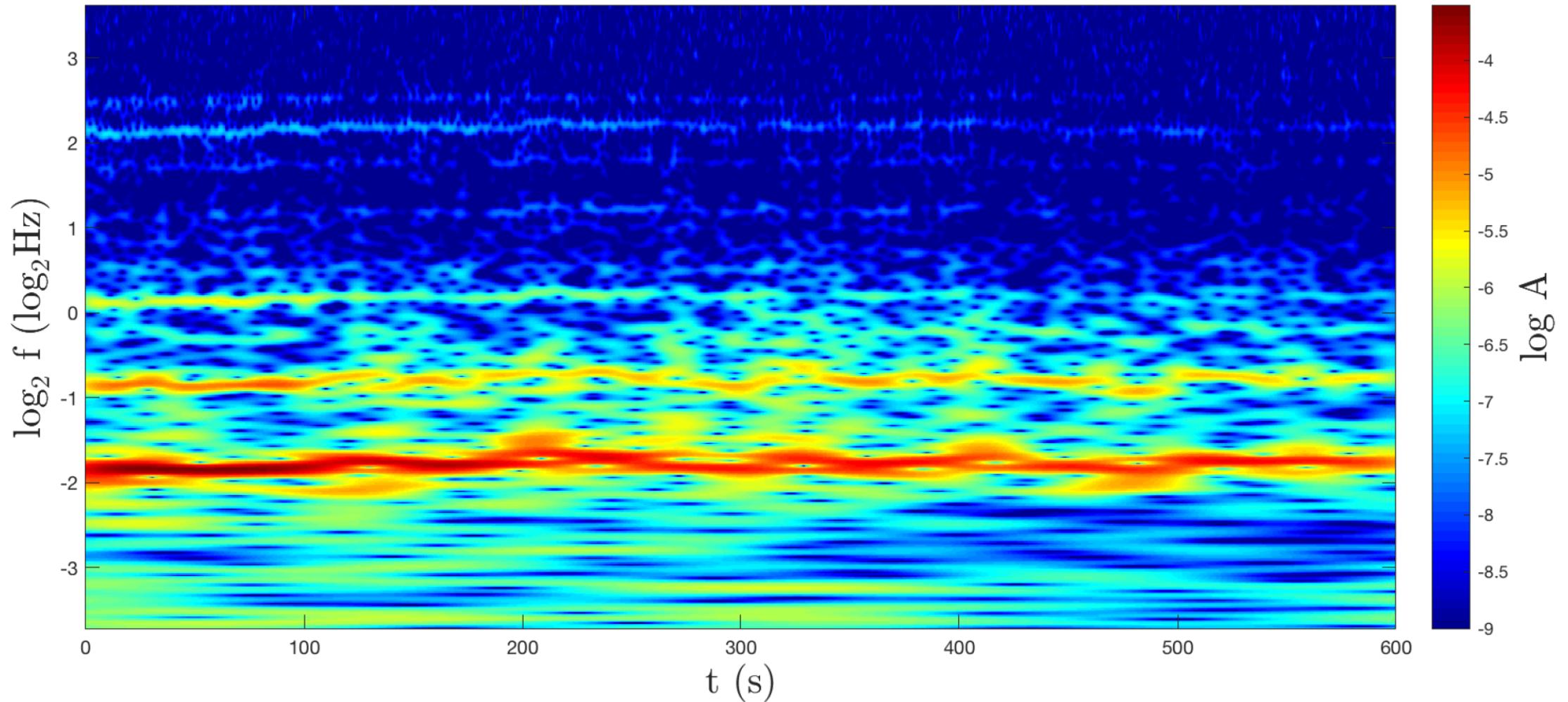
Playing on the wavelet function parameters to reveal both respiratory and cardiac rhythms

Mean of the temperature spatial distribution (p20 left): $Q = 32$, $p = 2$



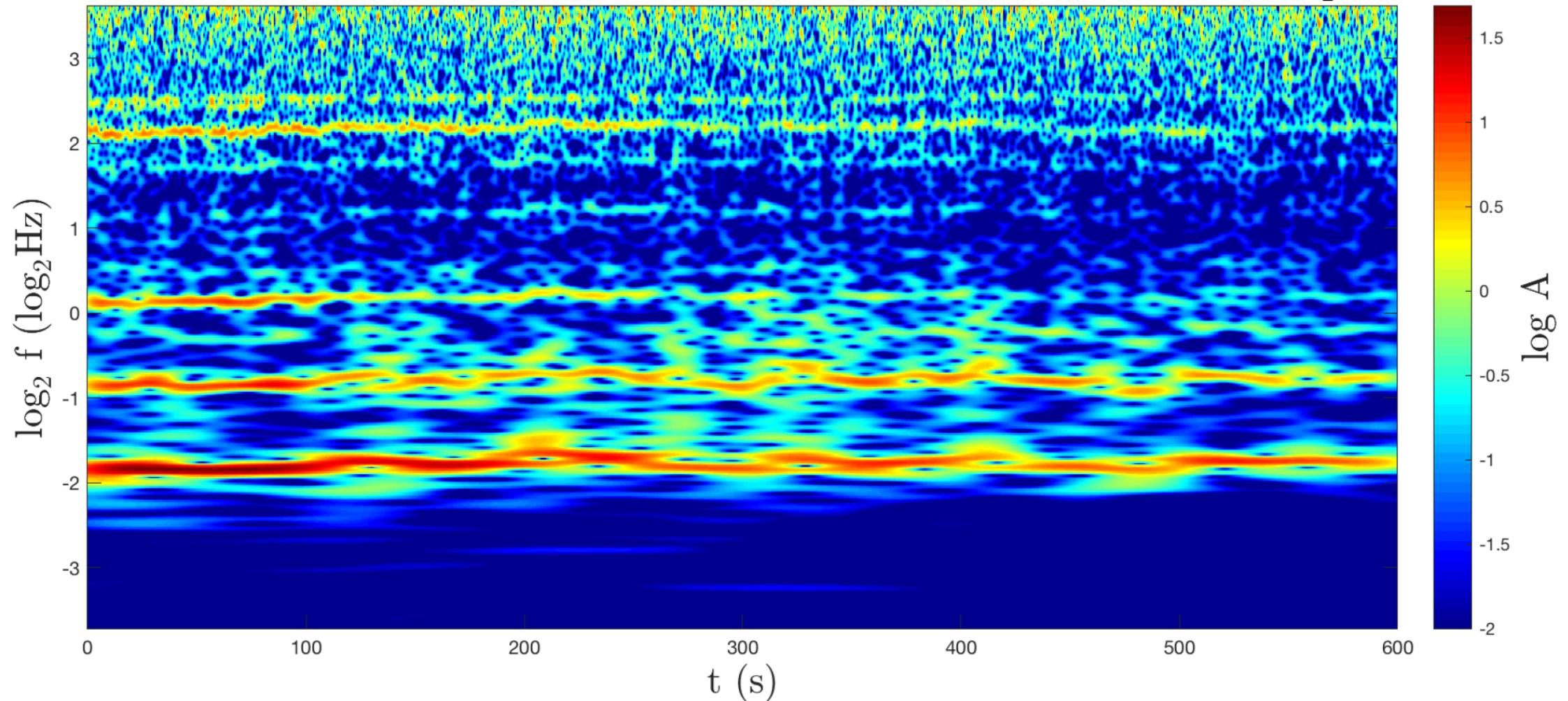
Playing on the wavelet function parameters to reveal both respiratory and cardiac rhythms

Mean of the temperature spatial distribution (p20 left): $Q = 32$, $p = 1$

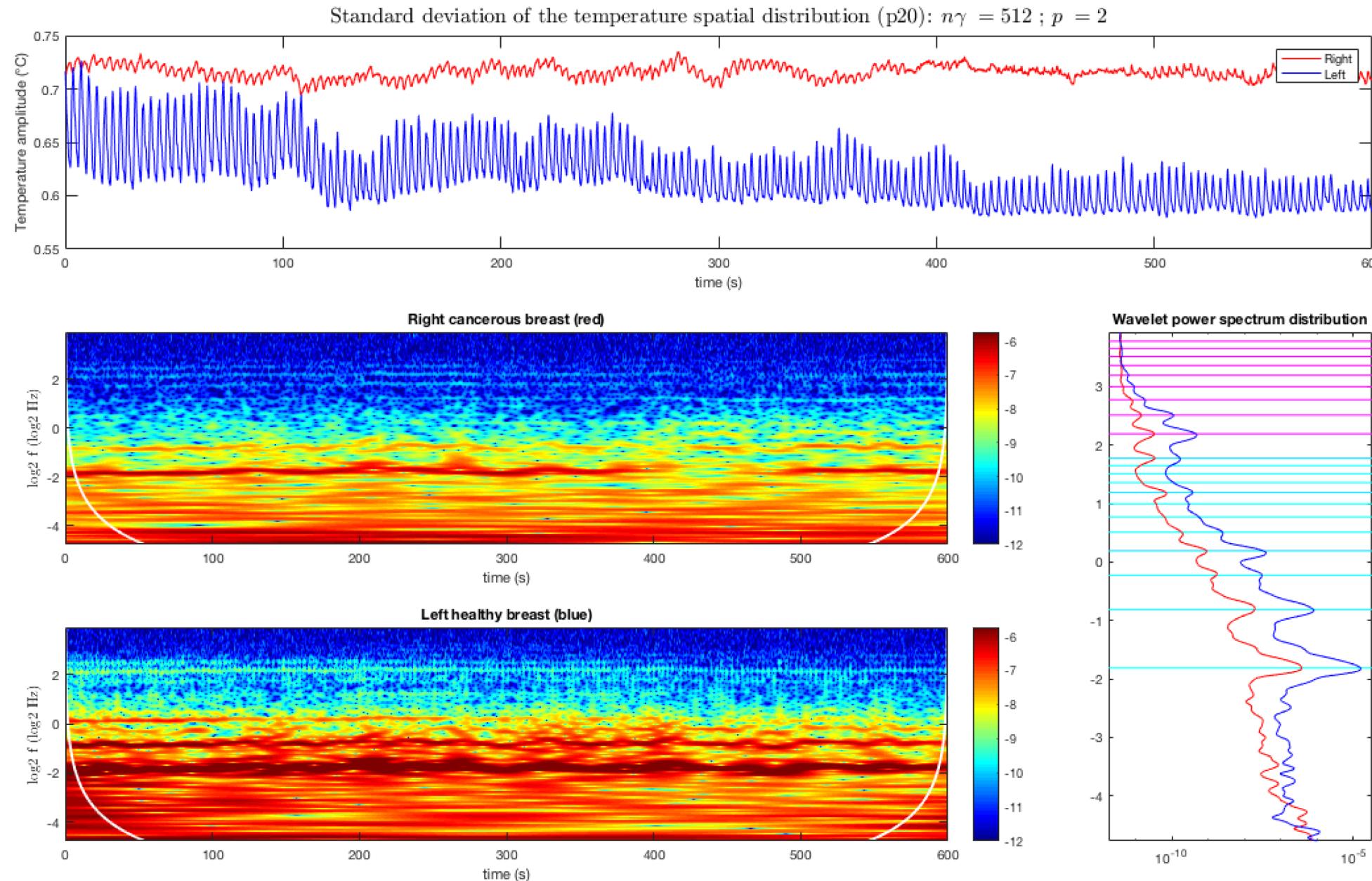


Playing on the wavelet function parameters to reveal both respiratory and cardiac rhythms

Mean of the temperature spatial distribution (p20 left): $Q = 32$, $p = \frac{1}{2}$



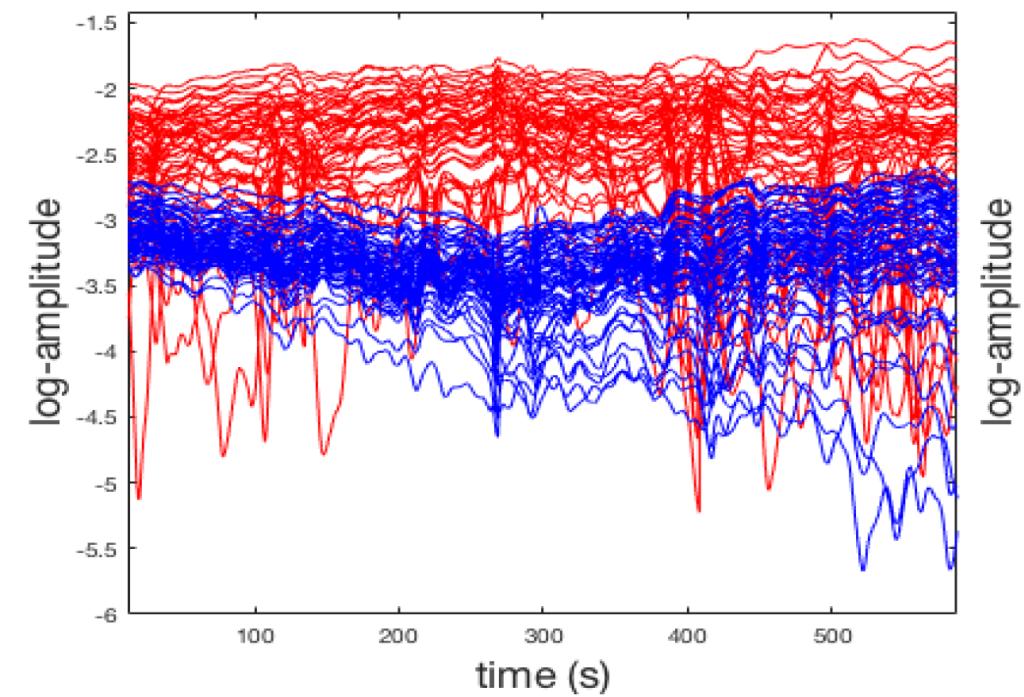
Comparison of right (cancerous) and left (healthy) breast global temperature signals



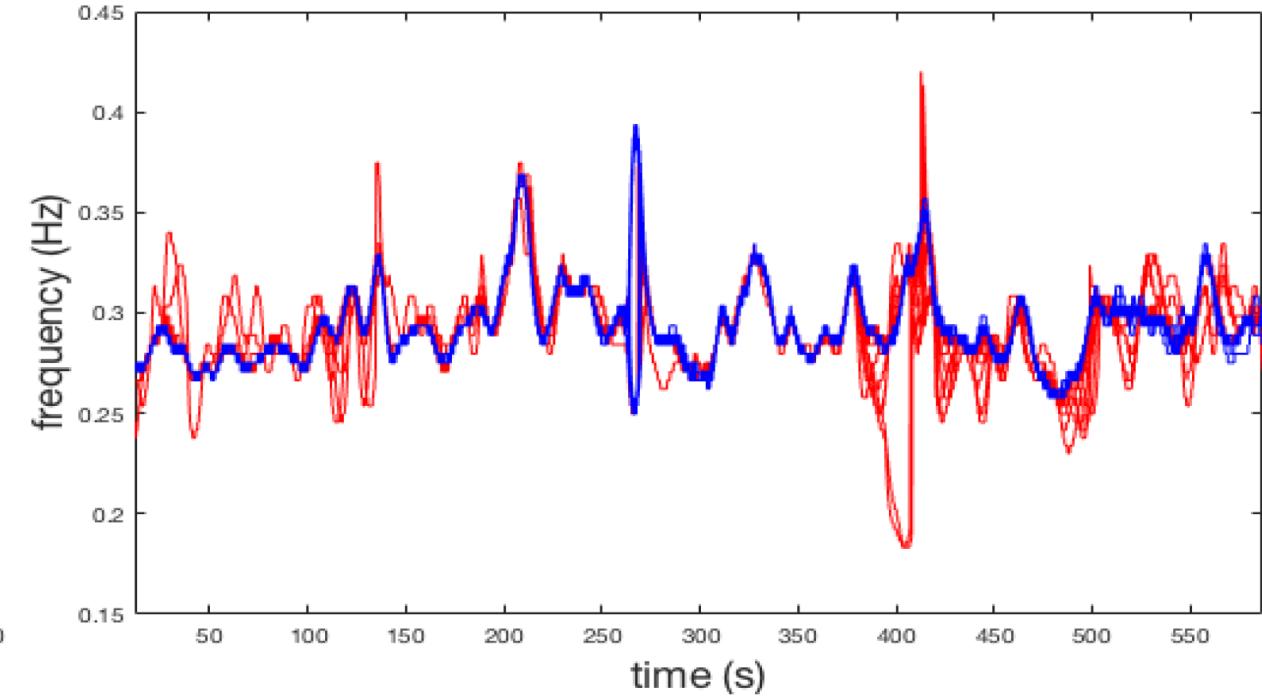
Comparison of right (cancerous) and left (healthy) breast global temperature signals

Focusing on the respiratory rhythm fundamental on the same patient (red: cancer breast, blue healthy)

Wavelet transform amplitude modulus



Temporal evolution of the instantaneous frequency

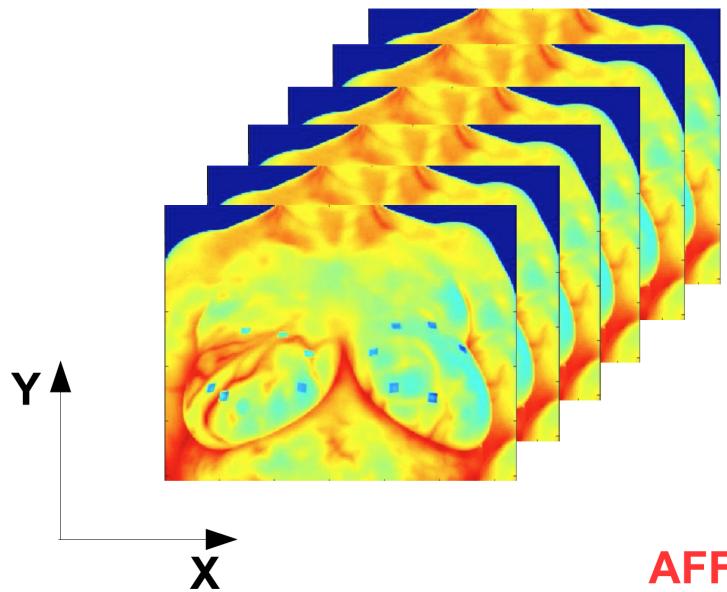


Skewed distributions
(long tails)

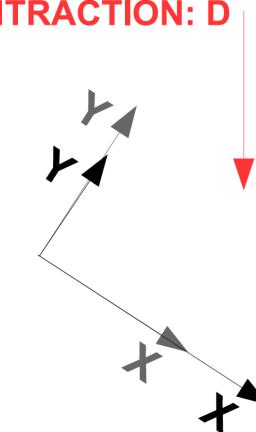
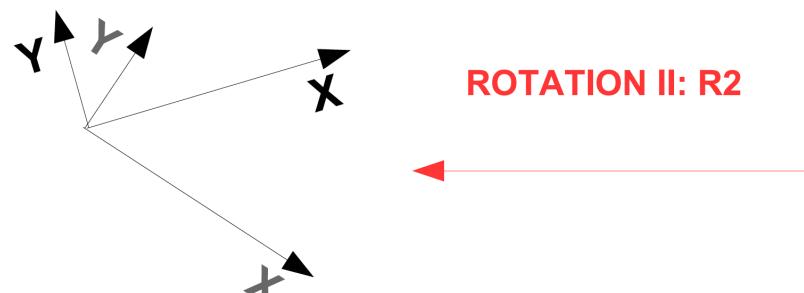
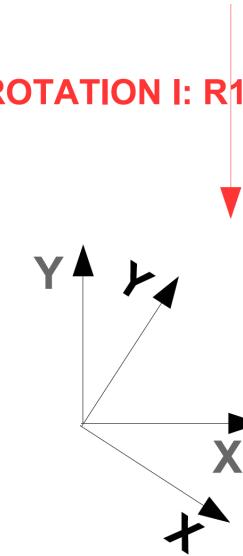
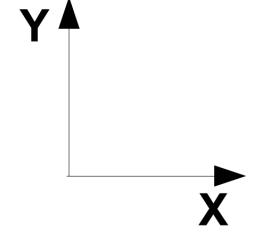
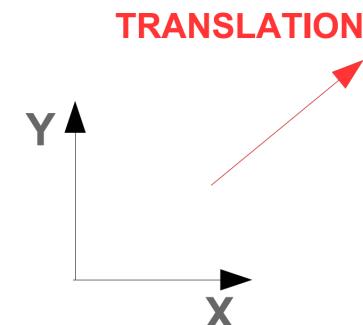
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Translation and Affine algorithm to extract these displacements



**AFFINE TRANSFORMATION
 $R_2 * D * R_1$**



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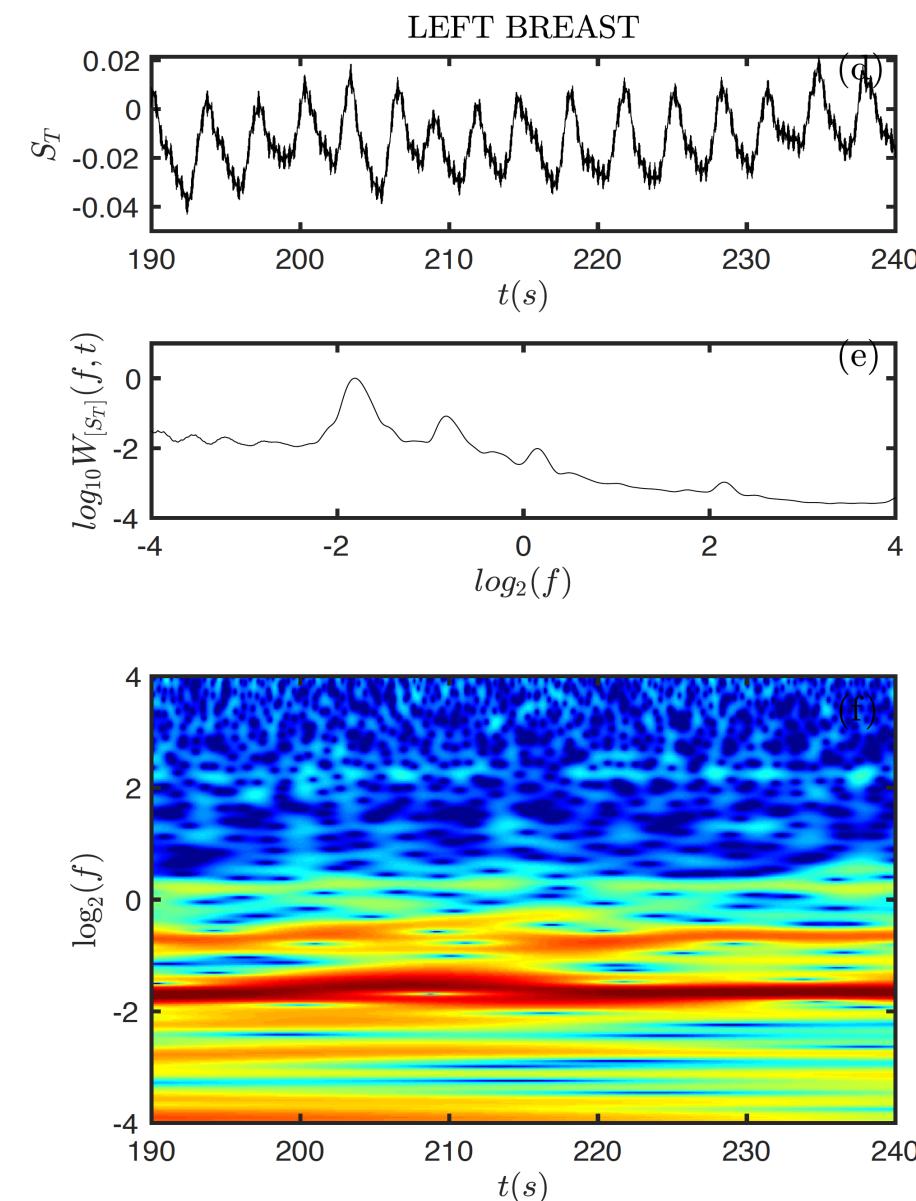
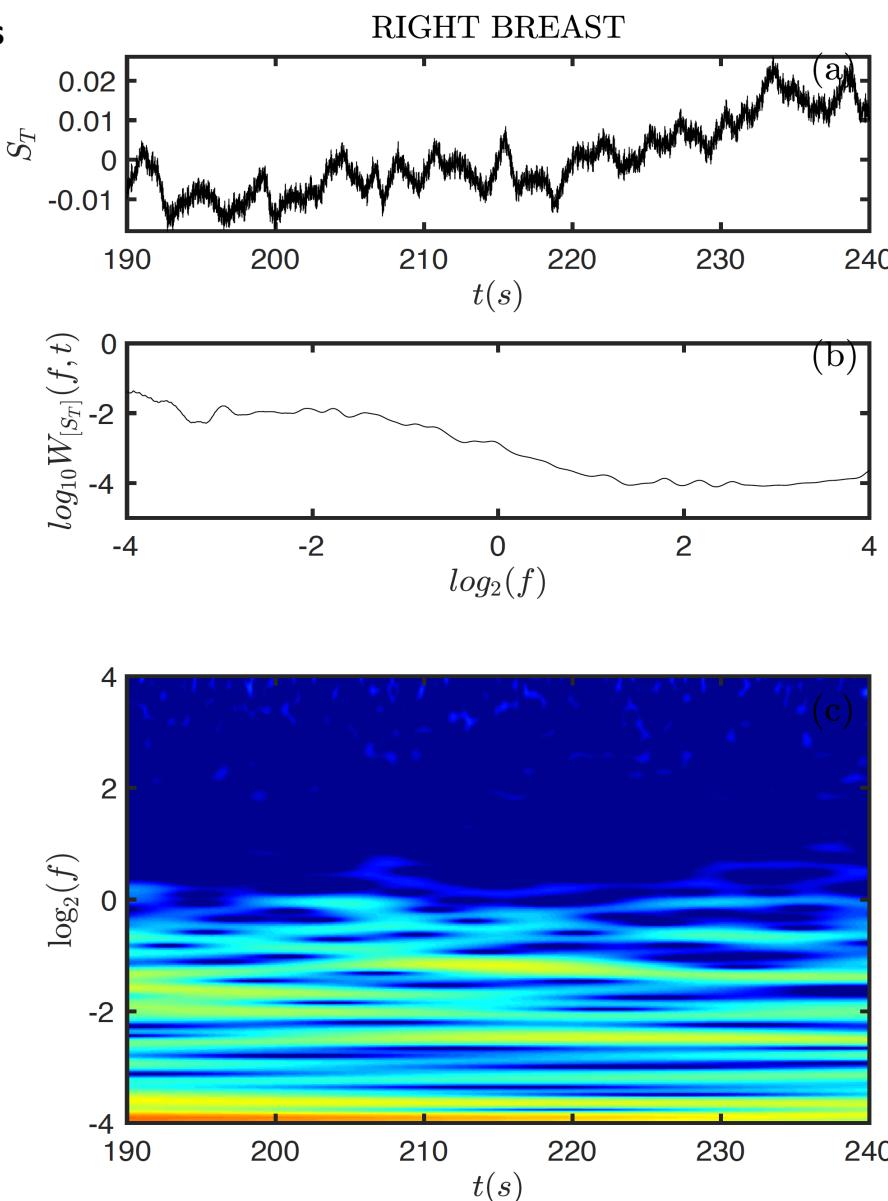
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Comparison of time-frequency decomposition of uncorrected and corrected signals

Uncorrected signals

N=256

p=1

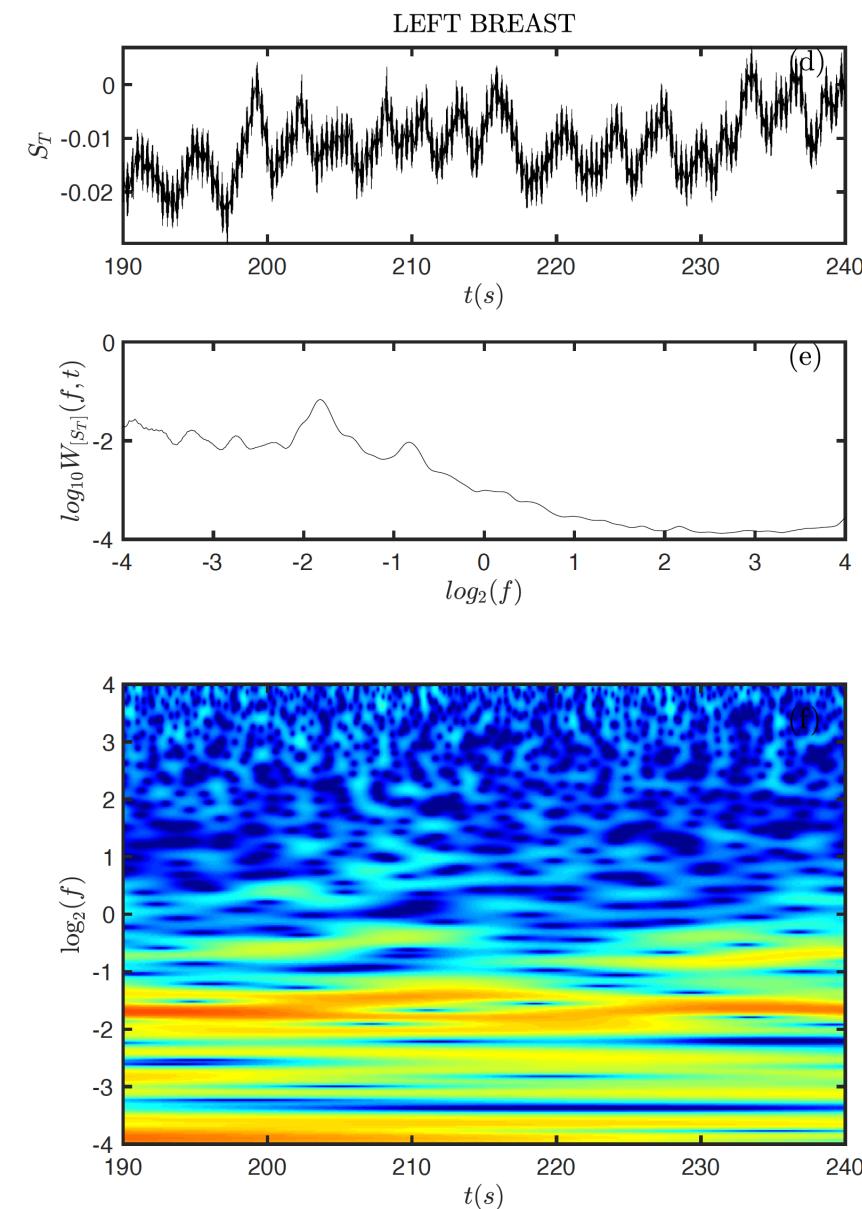
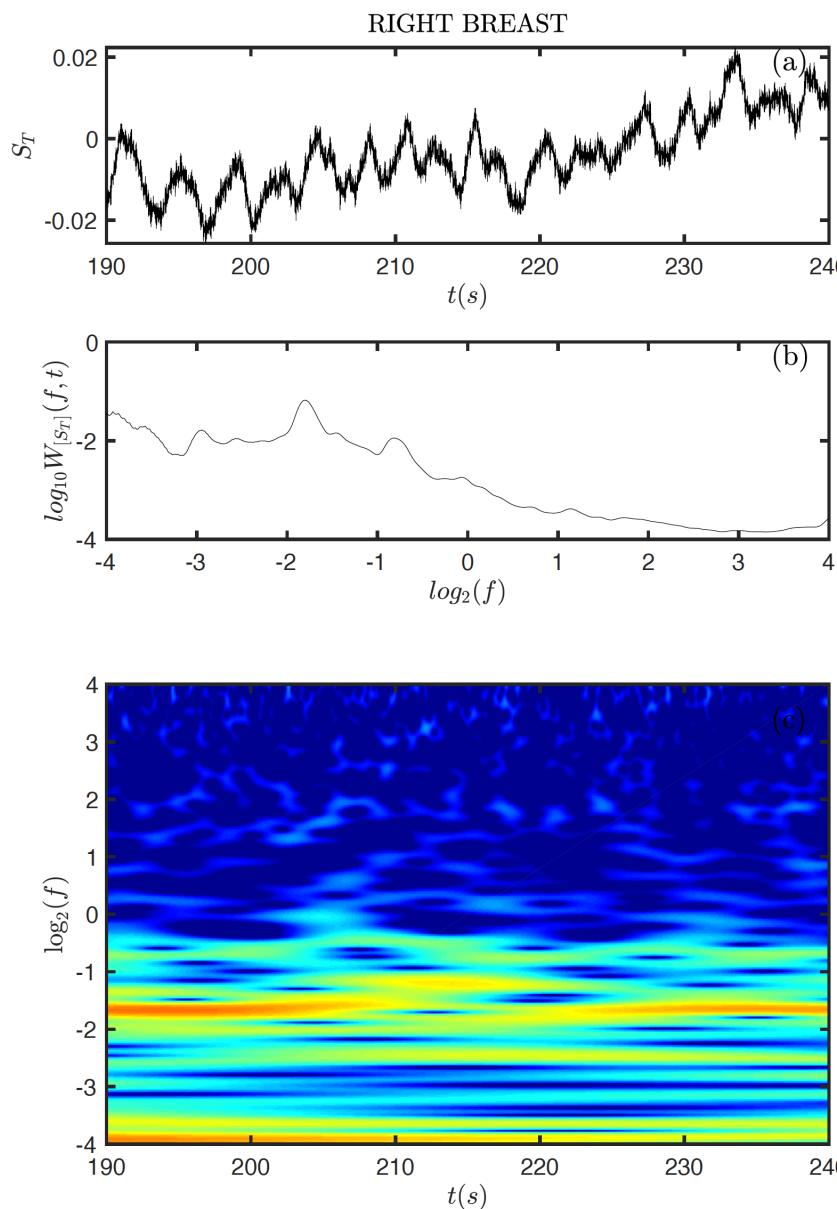


Comparison of time-frequency decomposition of uncorrected and corrected signals

Corrected signals

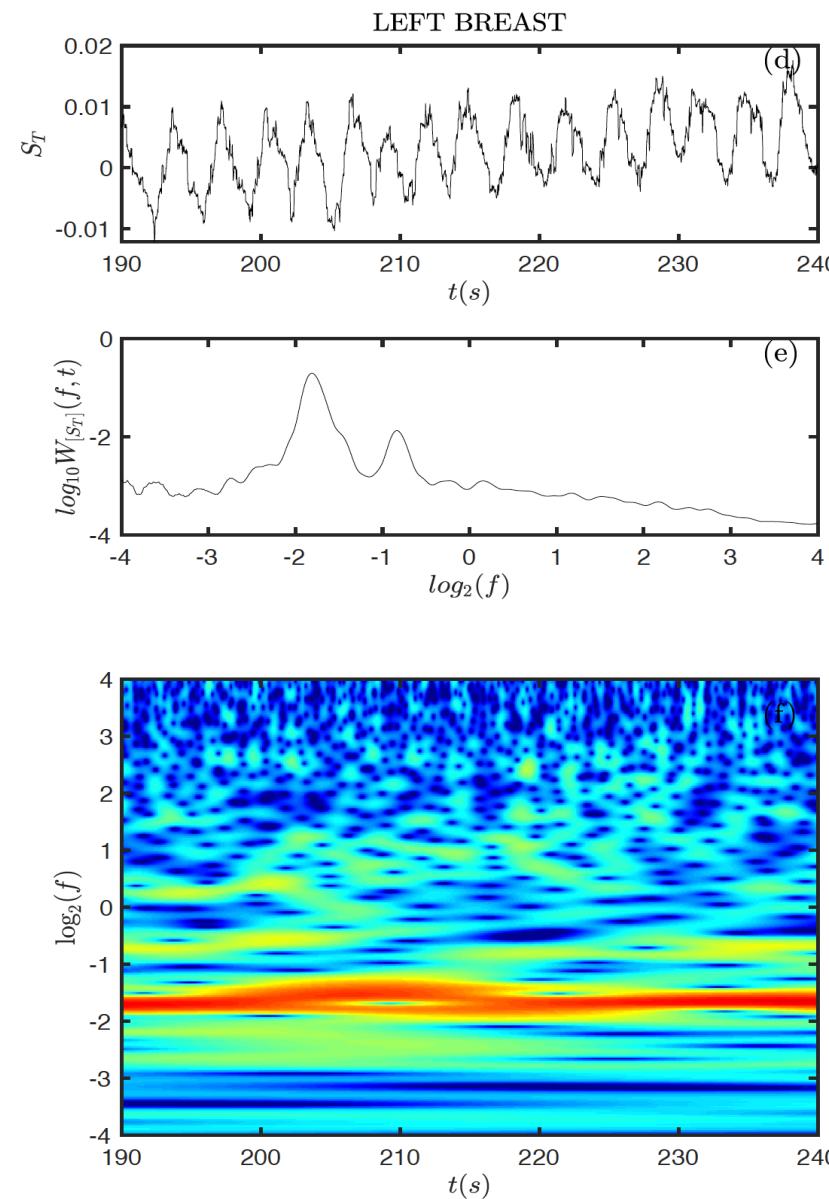
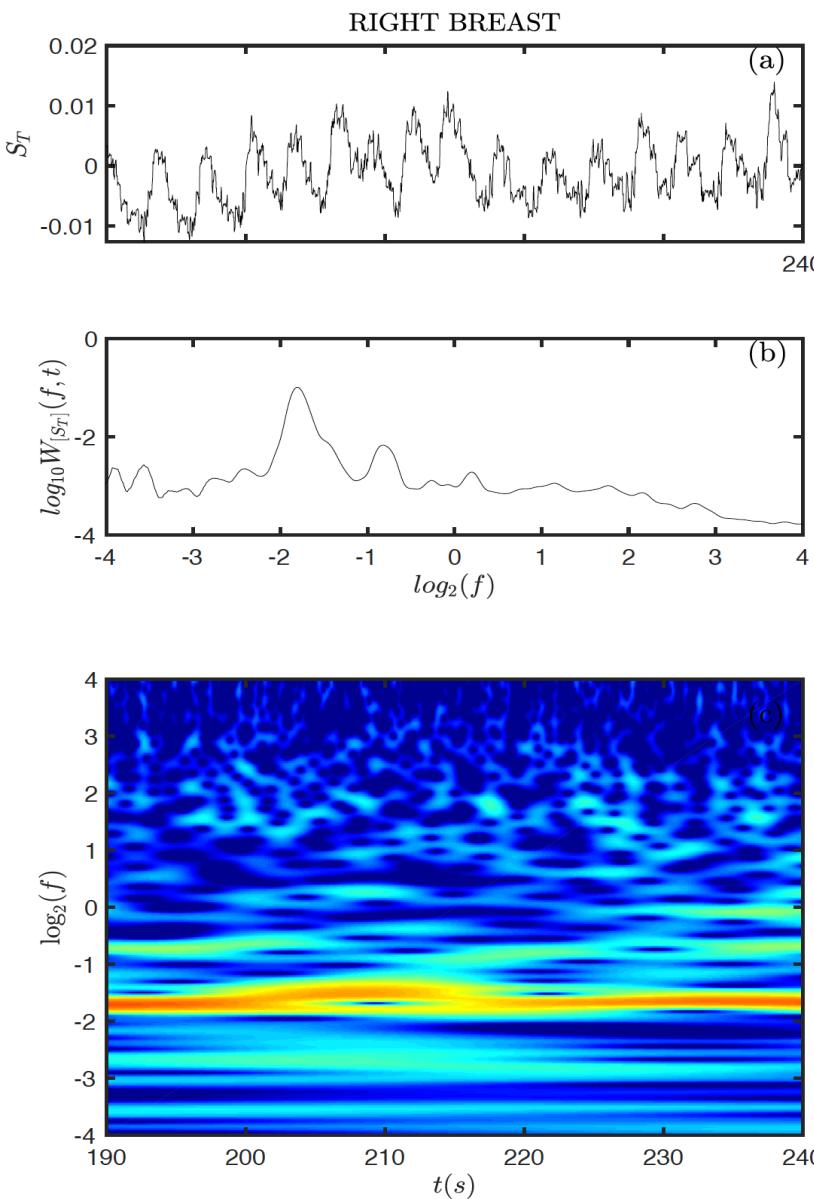
N=256

p=1



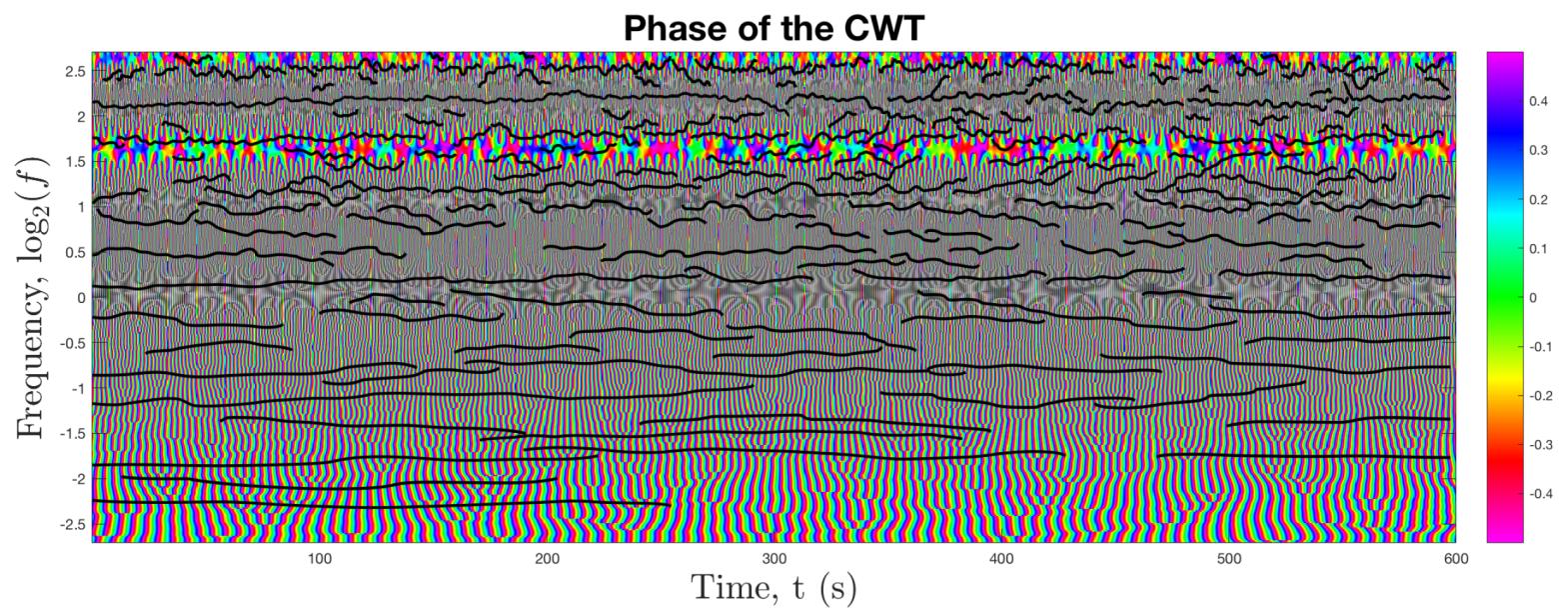
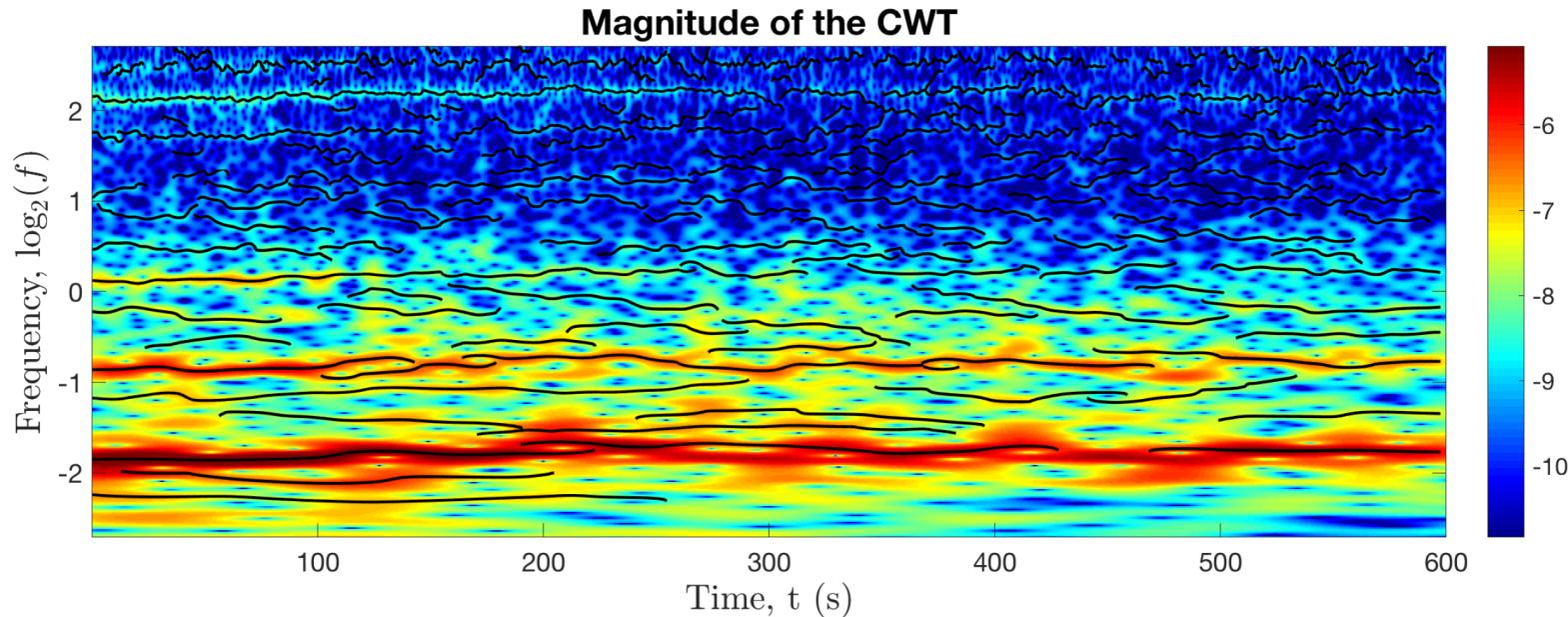
Comparison of time-frequency decomposition of uncorrected and corrected signals

Transformation
Affine matrix
determinant
N=256
p=1

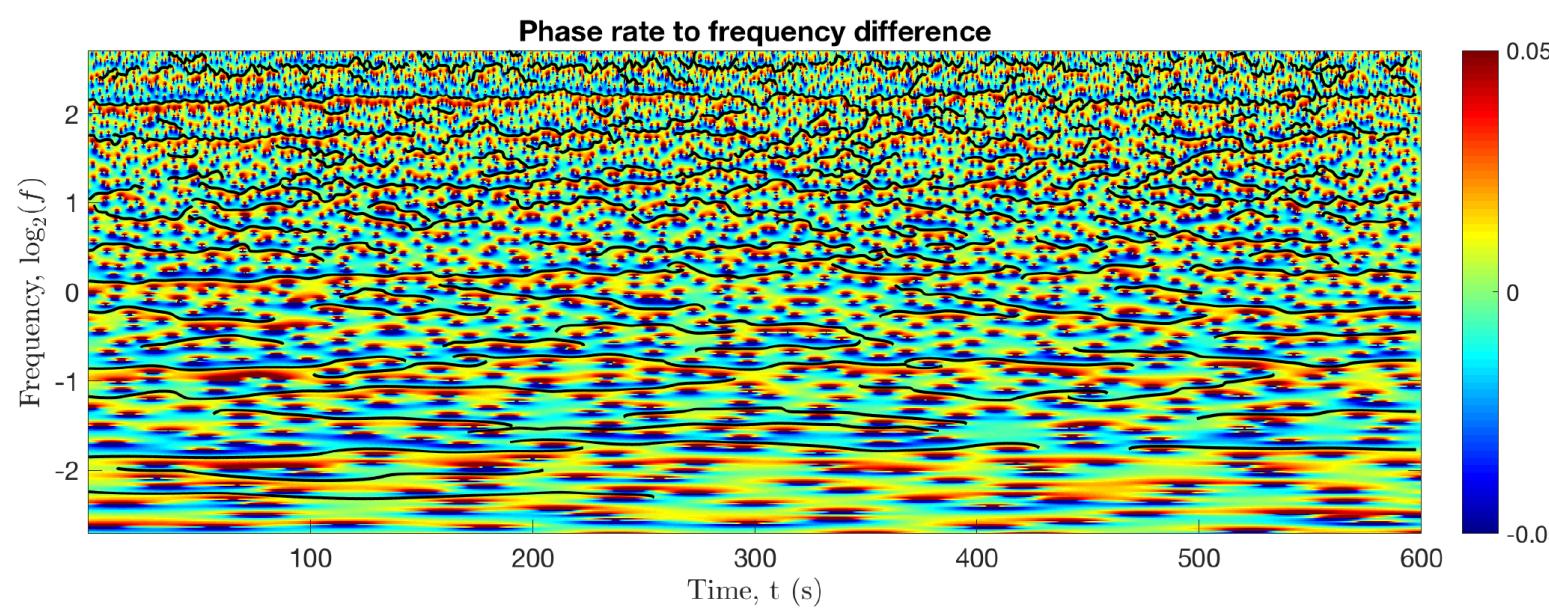
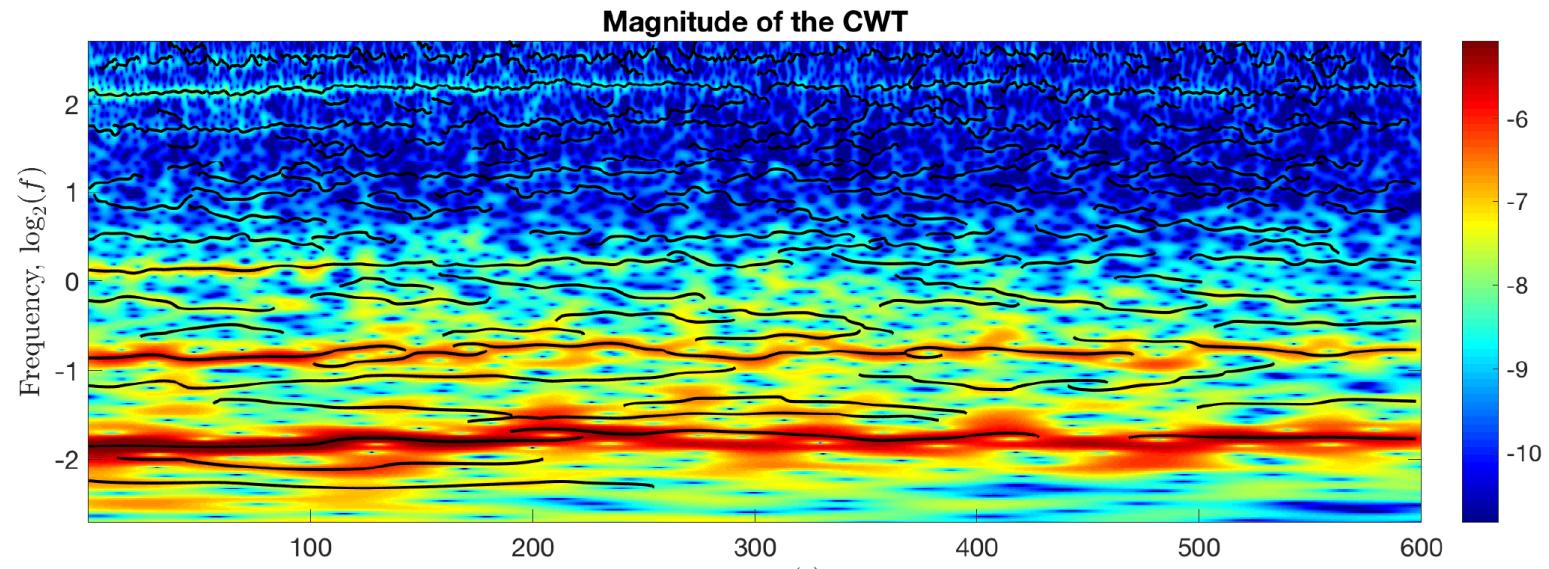


Detection of the ridges of the CWT (from the magnitude or modulus of the CWT)

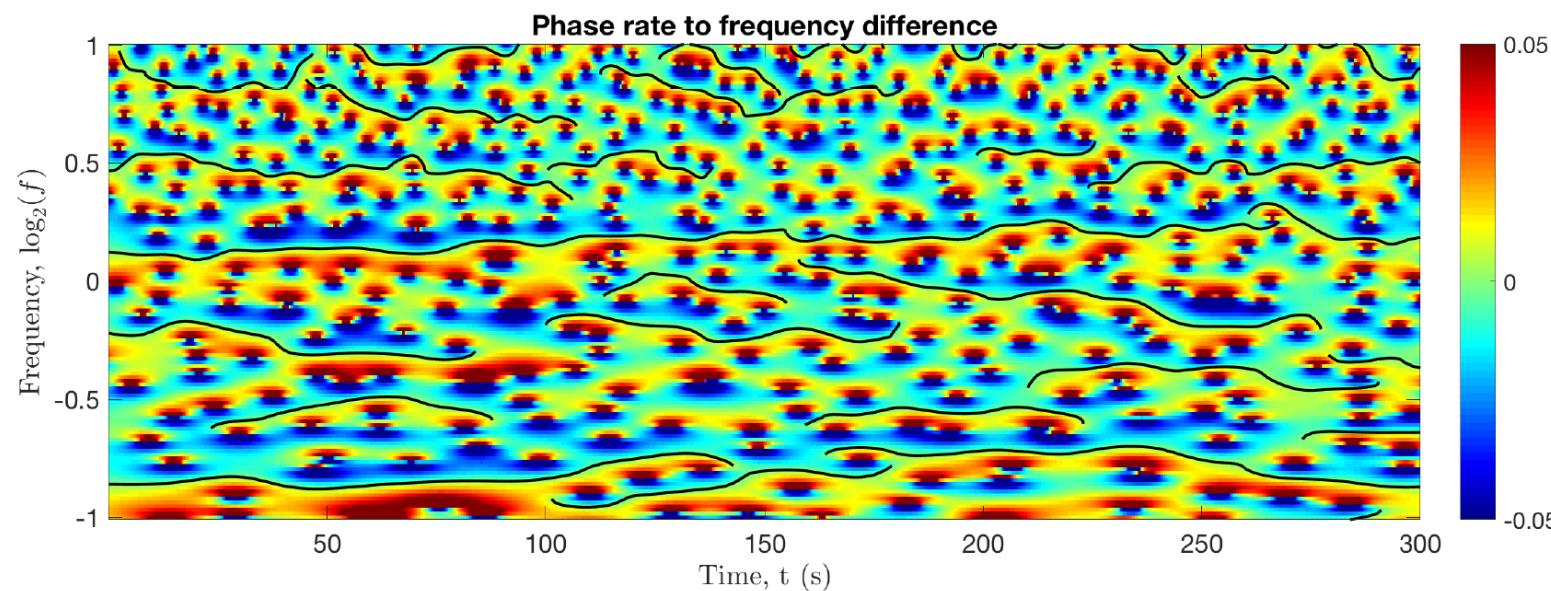
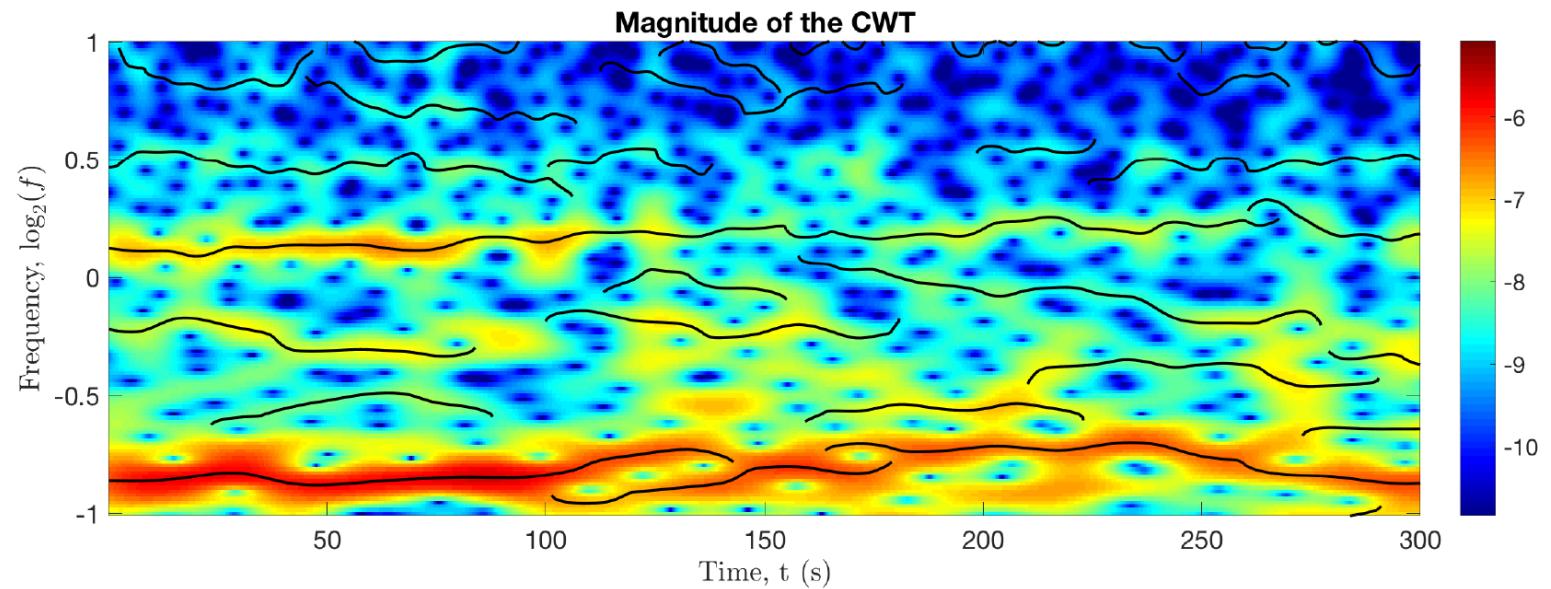
Q=32



Detection of the ridges of the CWT (comparing modulus and phase difference methods)



Detection of the ridges of the CWT (comparing modulus and phase difference methods)



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Disentangling respiratory from cardiogenic rhythms

Recognition of the presence of two (or more rhythms) inside the signal: multiplicative cross-correlation of the modulus of the CWT in the frequency variable f (the integral is performed in $\log(f)$ scales)

Here we take $s_1 = s_2$, the log-frequency variable for s_2 is shifted by $\log(q)$

$$R_\psi[s_1, s_2](q, t) = C_{\psi, \psi}^{-1} \int_0^\infty |W_\psi[s_1](f, t) W_\psi[s_2](qf, t)| df/f ,$$

where $C_{\psi, \psi} = \int_0^\infty |\tilde{\psi}(f)|^2 df/f$.

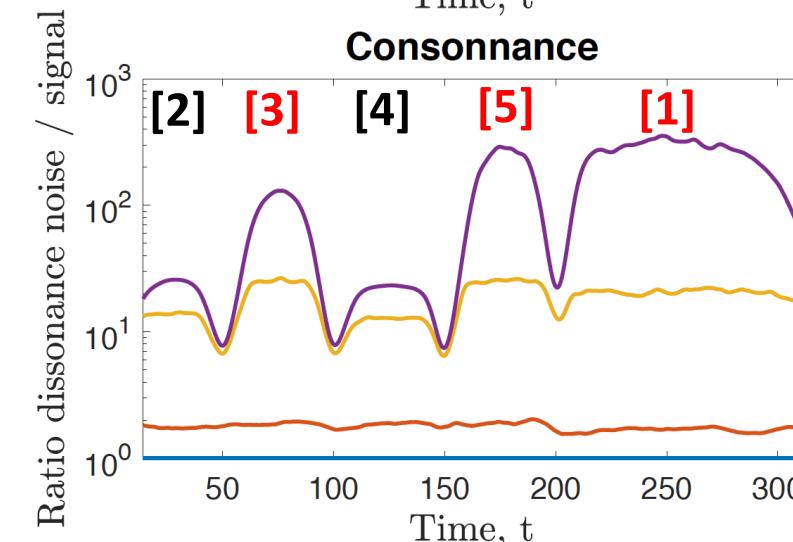
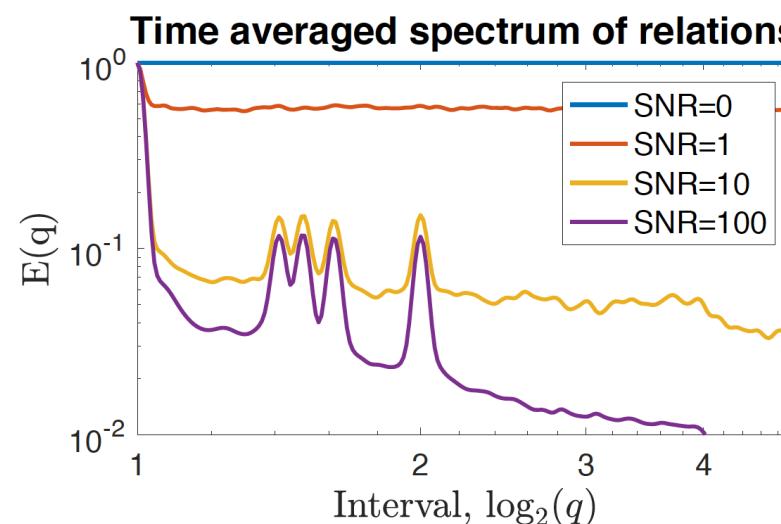
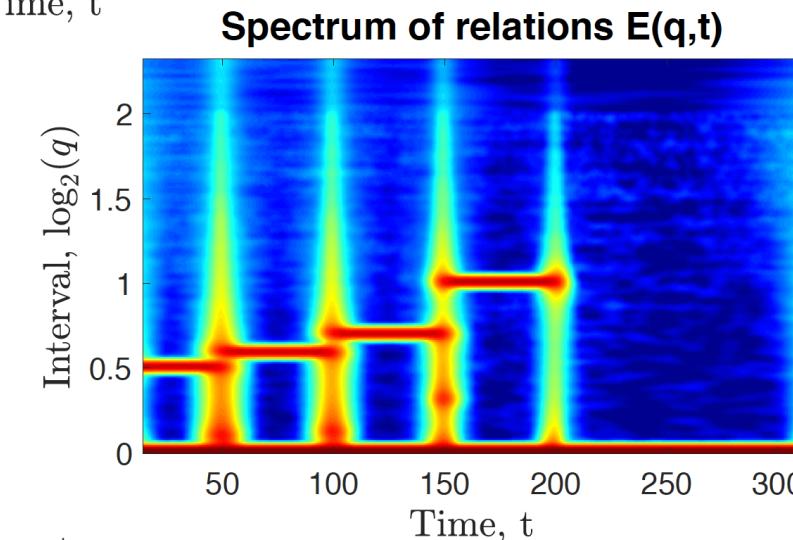
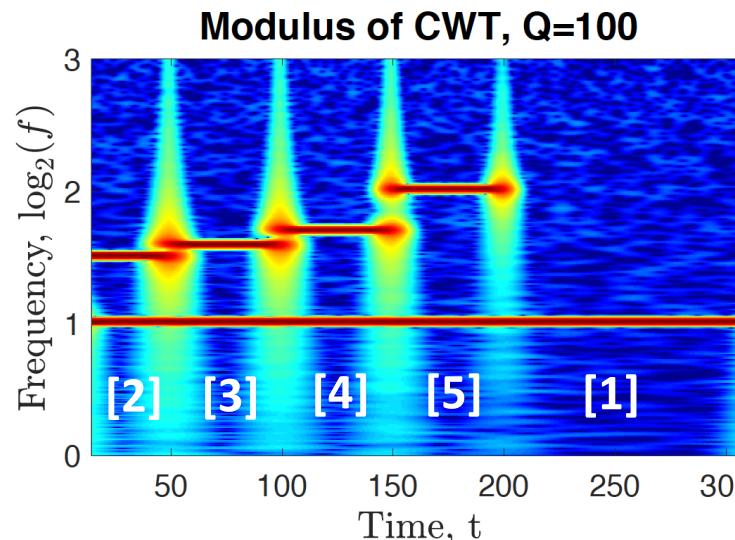
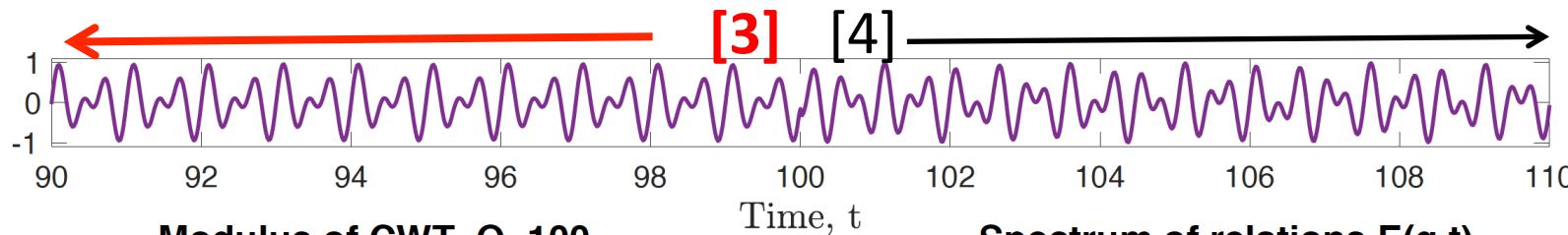
$E(q, t) = R_\psi[s_1, s_2](q, t)$: is the spectrum of relations of the two signals s_1 and s_2

Identification of irreducible fractions of the frequency ratios occurring in the spectrum of relations of the signal with itself -> « **consonance of the rhythms** »

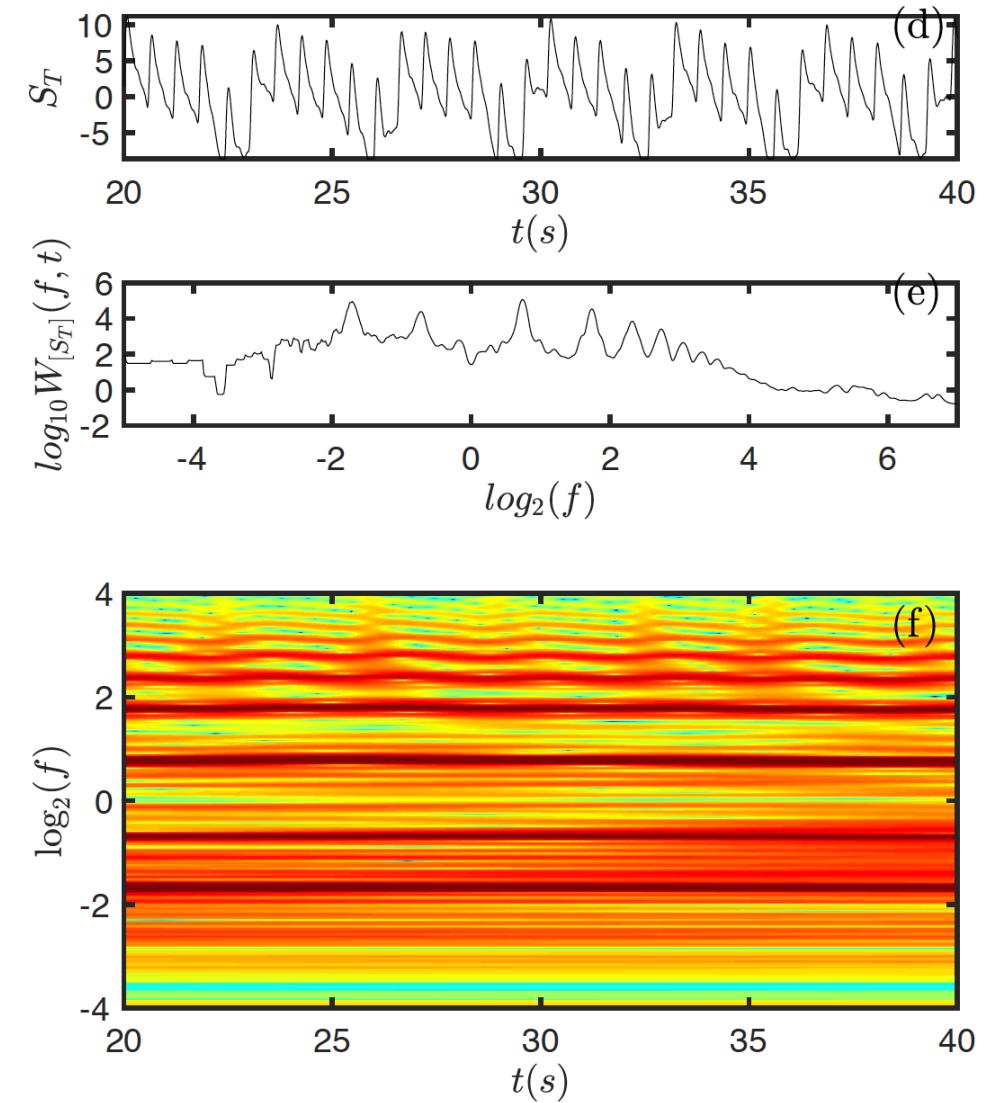
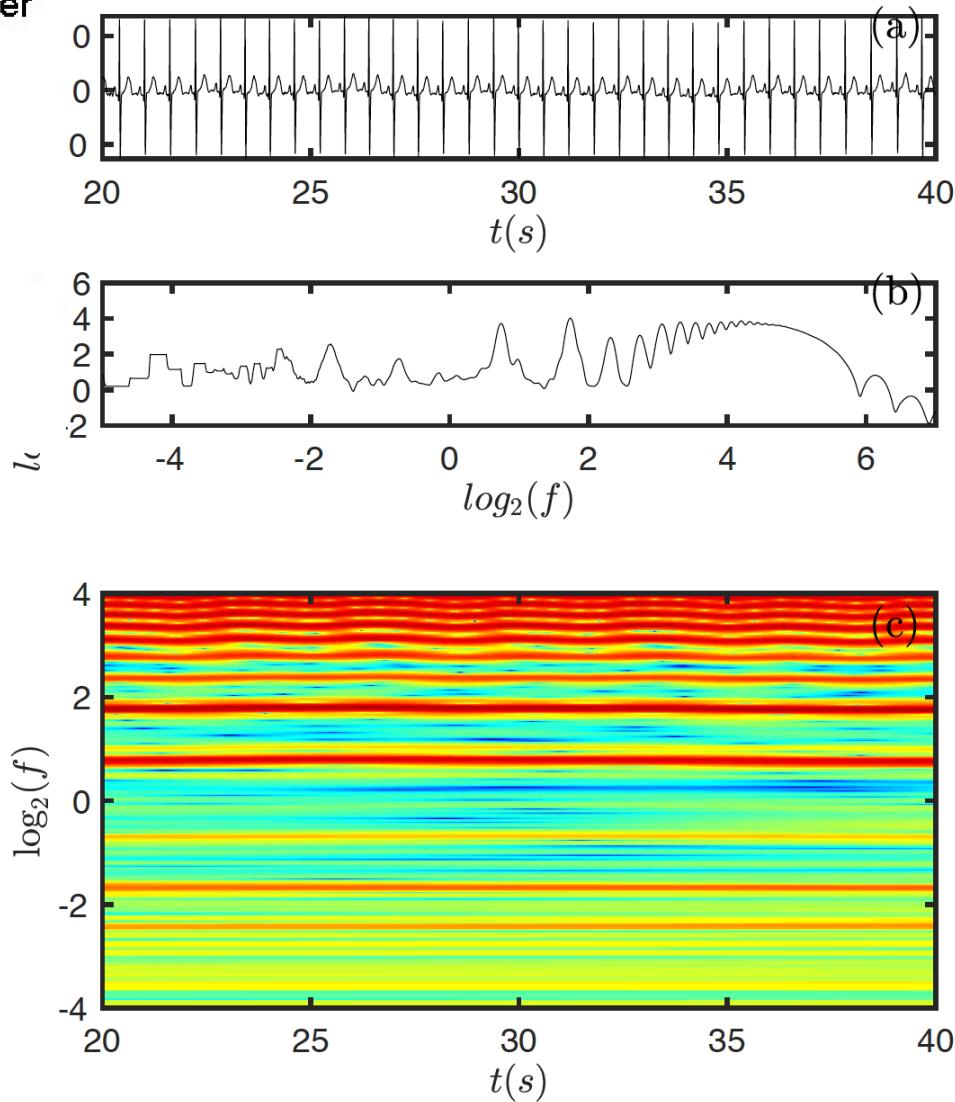
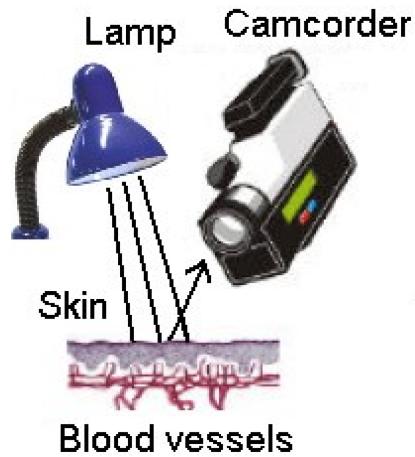
Searching for the “consonance” of a synthetic signal

Rhythm ratios

- [1] 1
- [2] $\sqrt{2}$
- [3] $3/2$
- [4] $(\sqrt{5} + 1)/2$ (golden)
- [5] 2



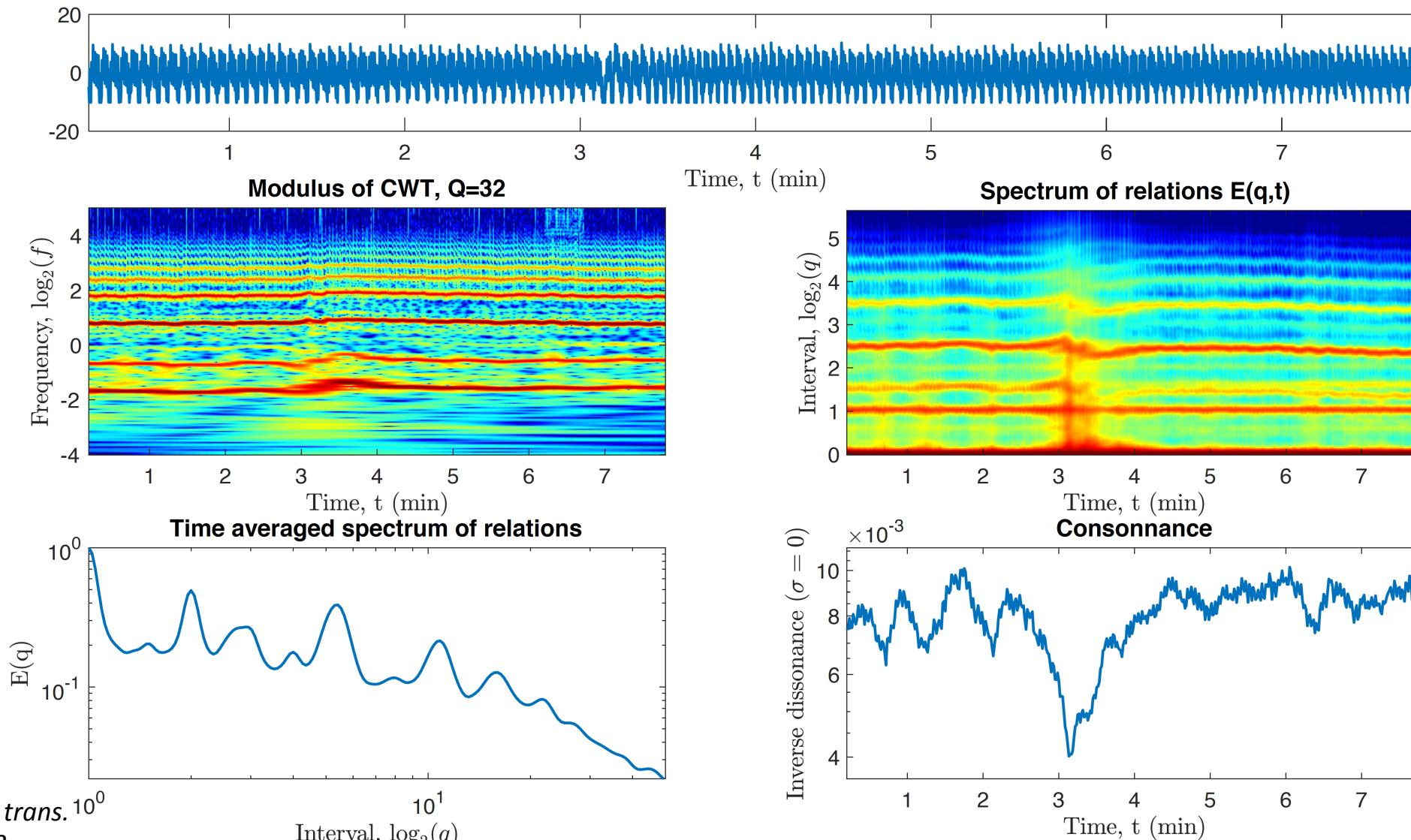
CWT analysis of photoplethysmogram signals



W. Karlen et al., IEEE trans.
on biomed Eng. 2013,

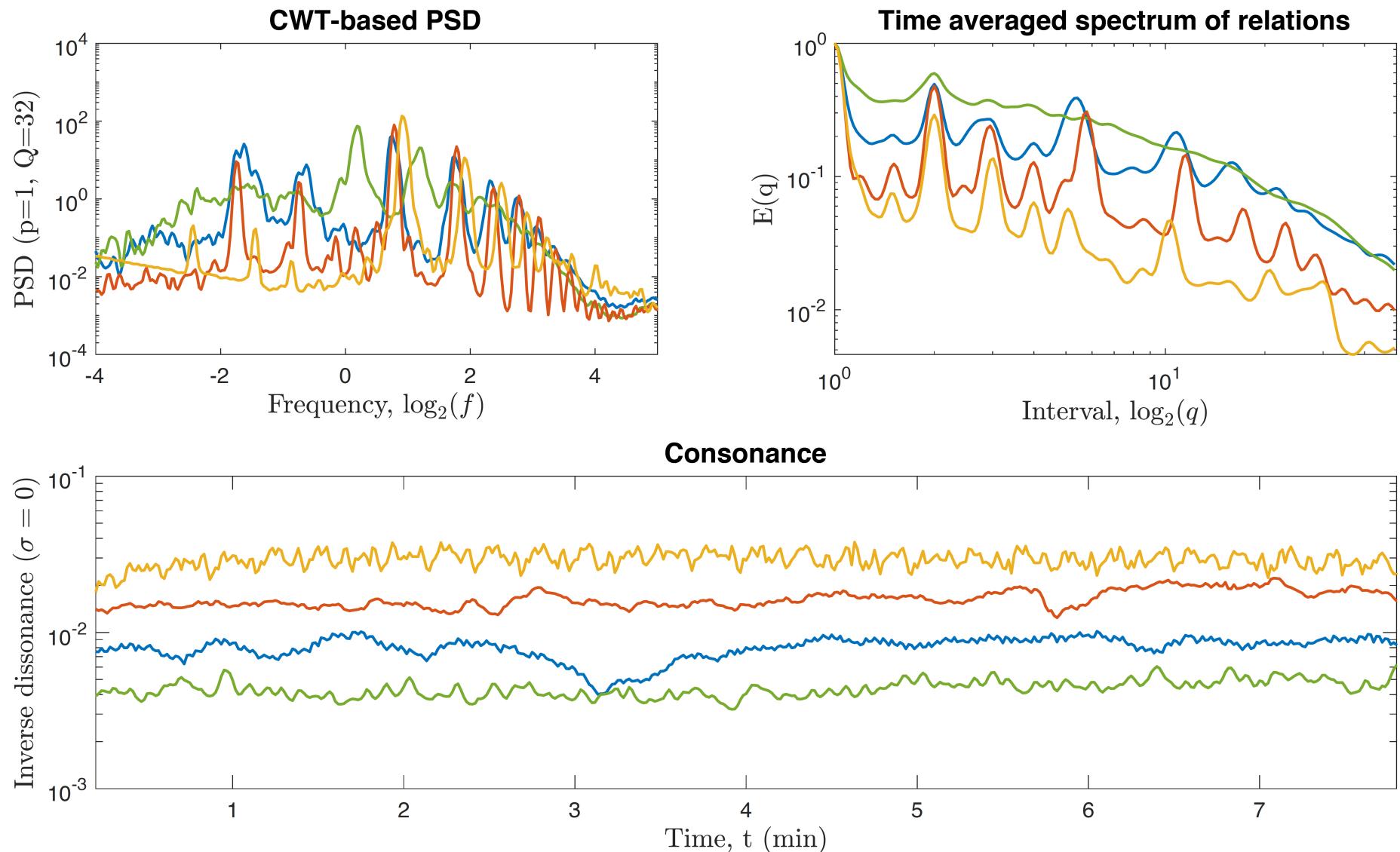
Signals downloaded from
<http://www.capnibase.org/index.php?id=857>

Wavelet based computation of consonance of photoplethysmogram signals



W. Karlen et al., IEEE trans. on biomed Eng. 2013,

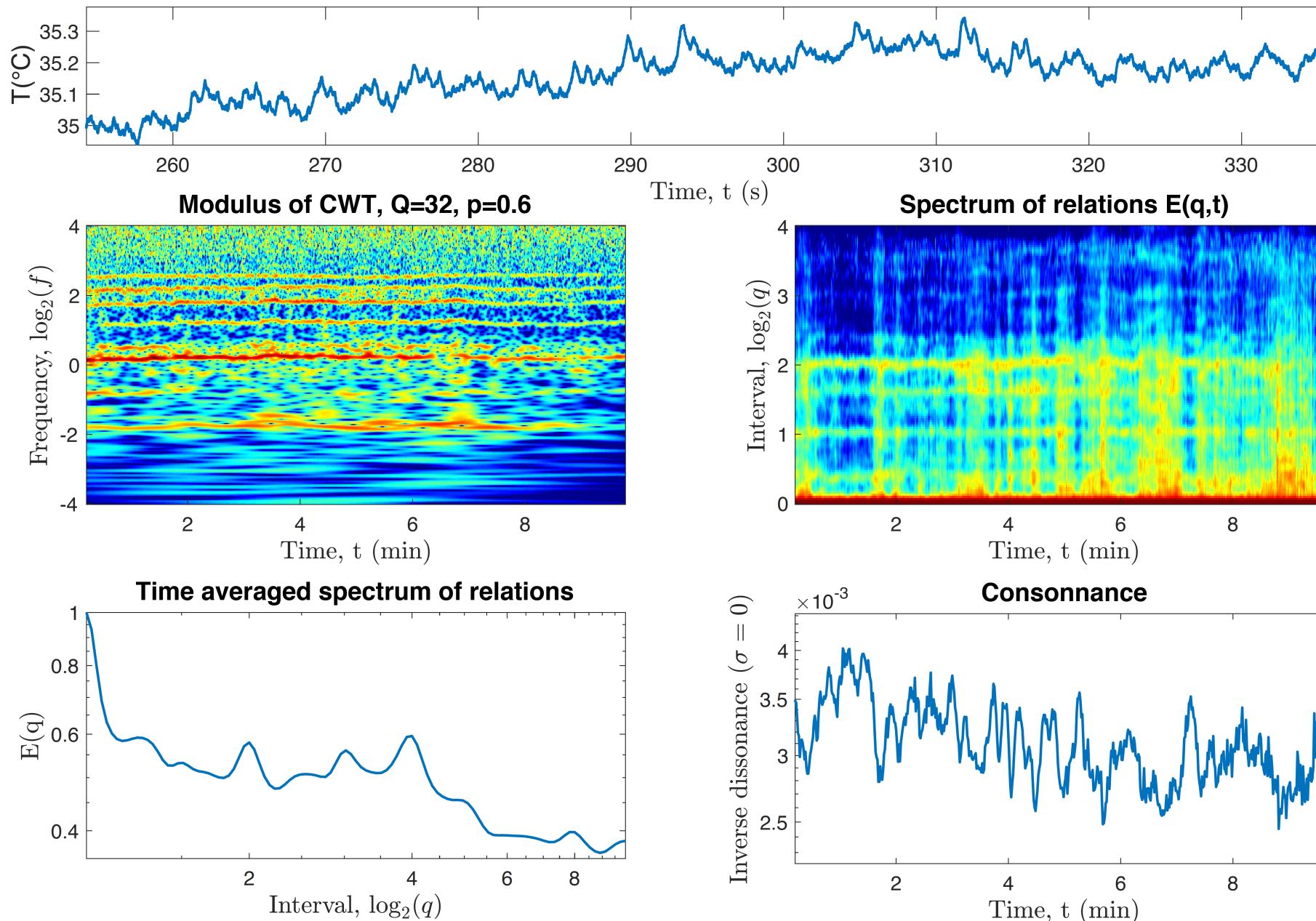
CWT analysis of photoplethysmogram signals



W. Karlen et al., IEEE trans.
on biomed Eng. 2013,

Signals downloaded from
<http://www.capnibase.org/index.php?id=857>

Wavelet based computation of the consonance of a thermogram signal



CONCLUSIONS

Time-frequency decomposition allows a complete characterization of the intertwining of rhythms in physiology

**The introduction of consonance (or disonance) of rhythm ratios and its temporal change (or variability)
as a marker of the dynamical adjustement of the body**

Can this quantity be used as a ‘dynamical’ hint for assisting clinician diagnosis?

Statistical tests on large data sets need to be performed

**A statistical physics formalism accounting for the spectrum of rhythm ratios is currently under progress
(in the same line as the singularity spectrum has been elaborated for fractal signals)**