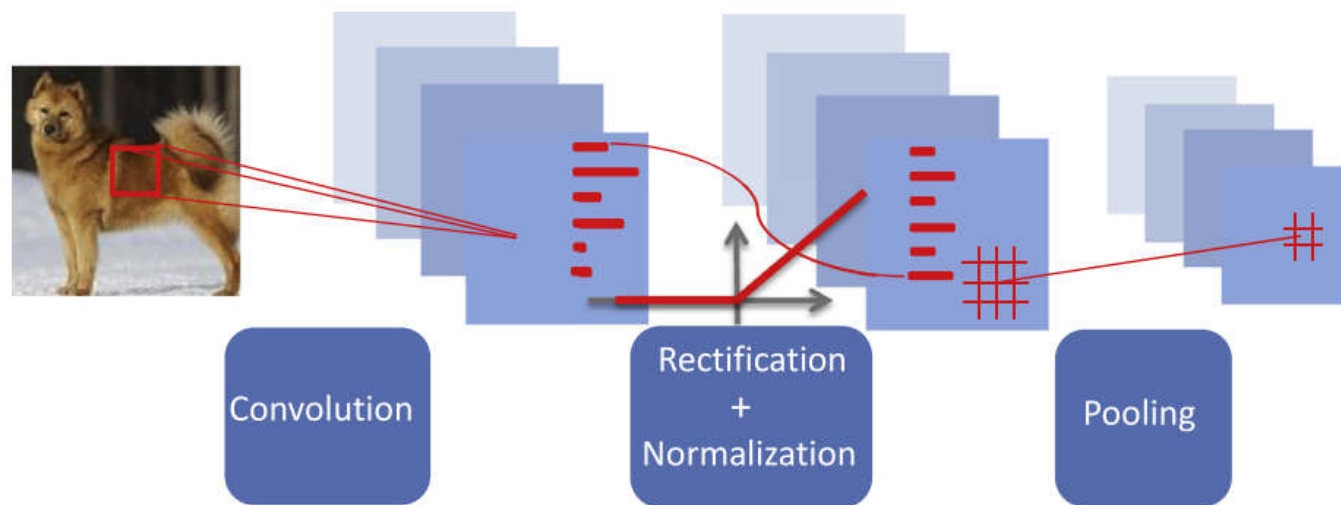


# Detail-Preserving Pooling in Deep Networks

Zenglin Shi

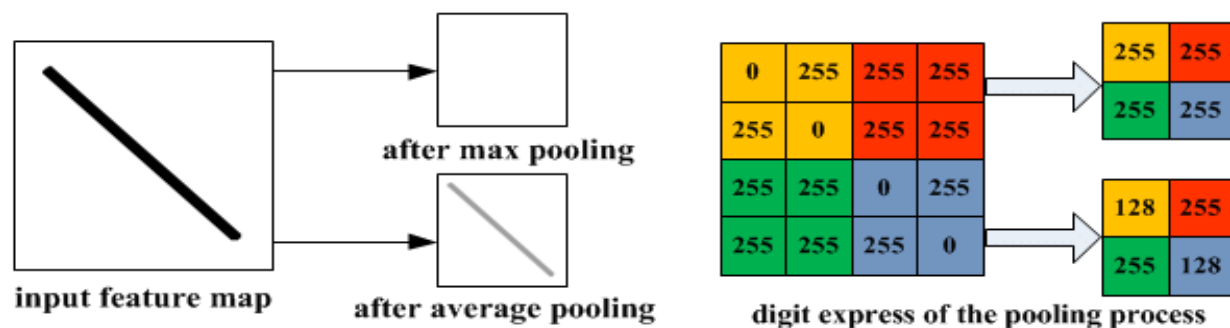
Dec. 10, 2018

# Pooling Mechanism

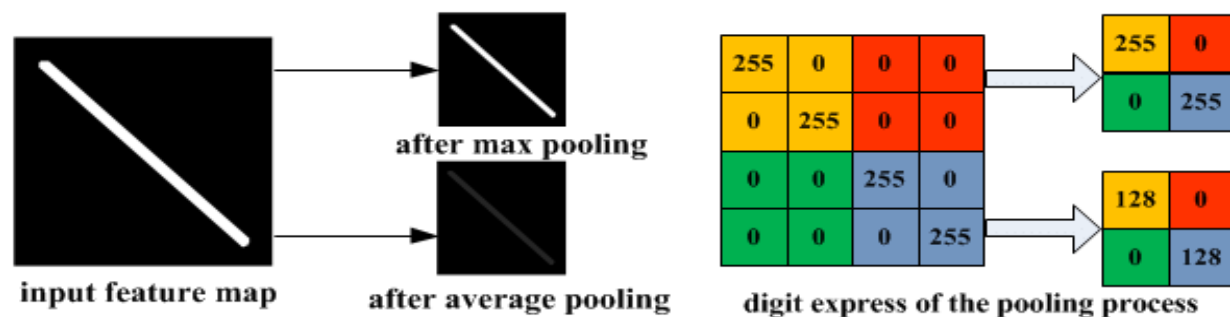


- Dimension Reduction
- Information Compression
- RF Enlarging
- Linear Transformation
- Translation Invariance

# Max & AVG. Pooling

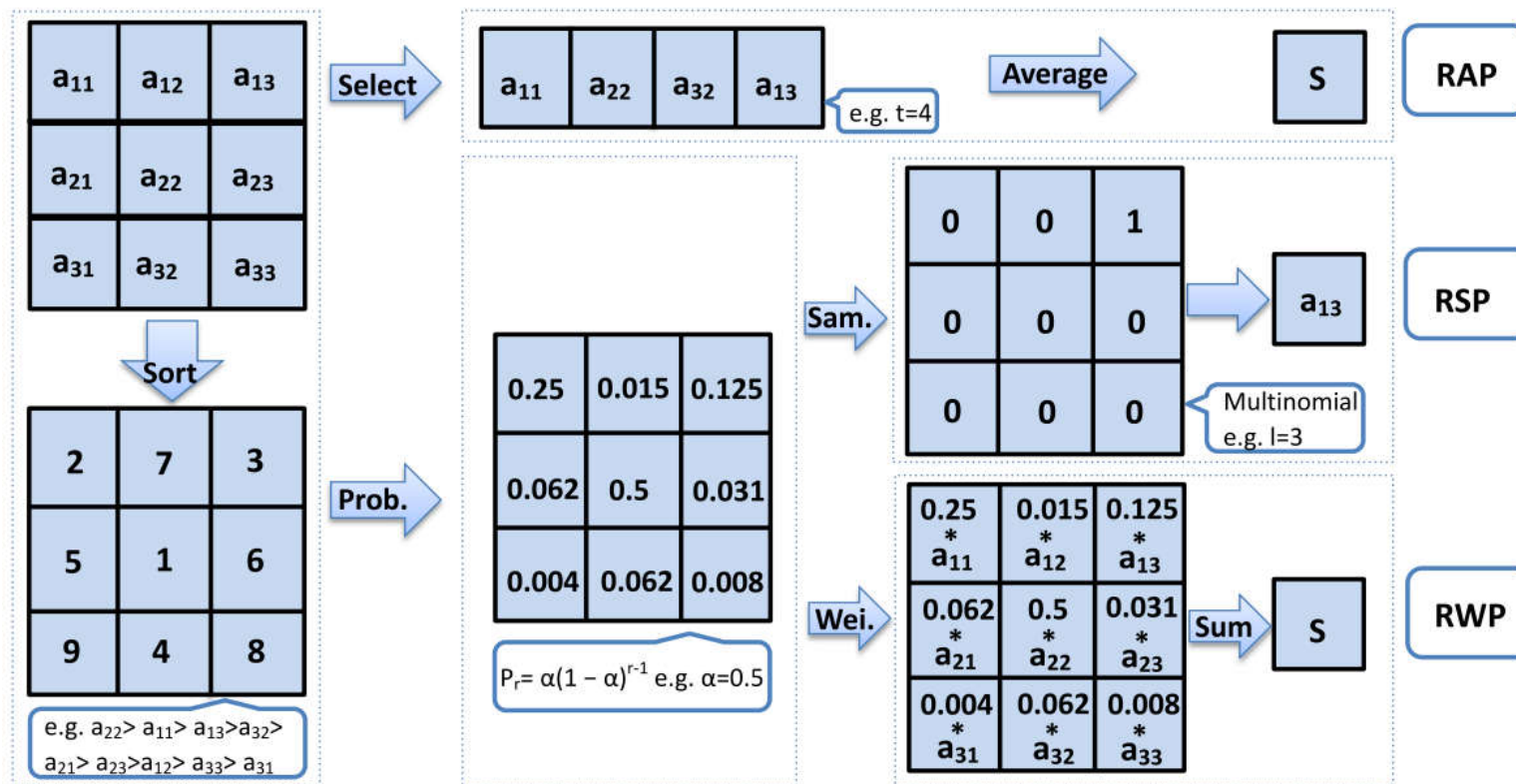


(a) Illustration of max pooling drawback

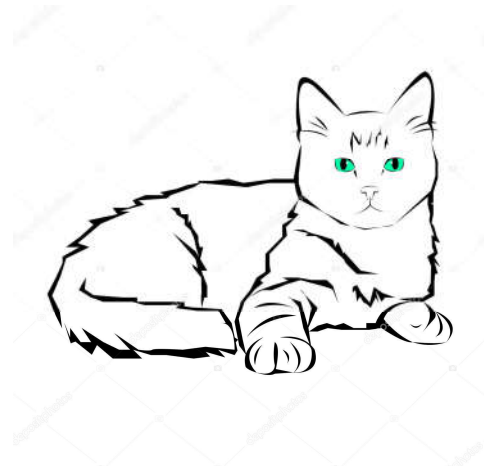


(b) Illustration of average pooling drawback

# Weighted AVG. Pooling



# Detail-Preserving Pooling-Motivation



## Detail-Preserving Pooling-DPID

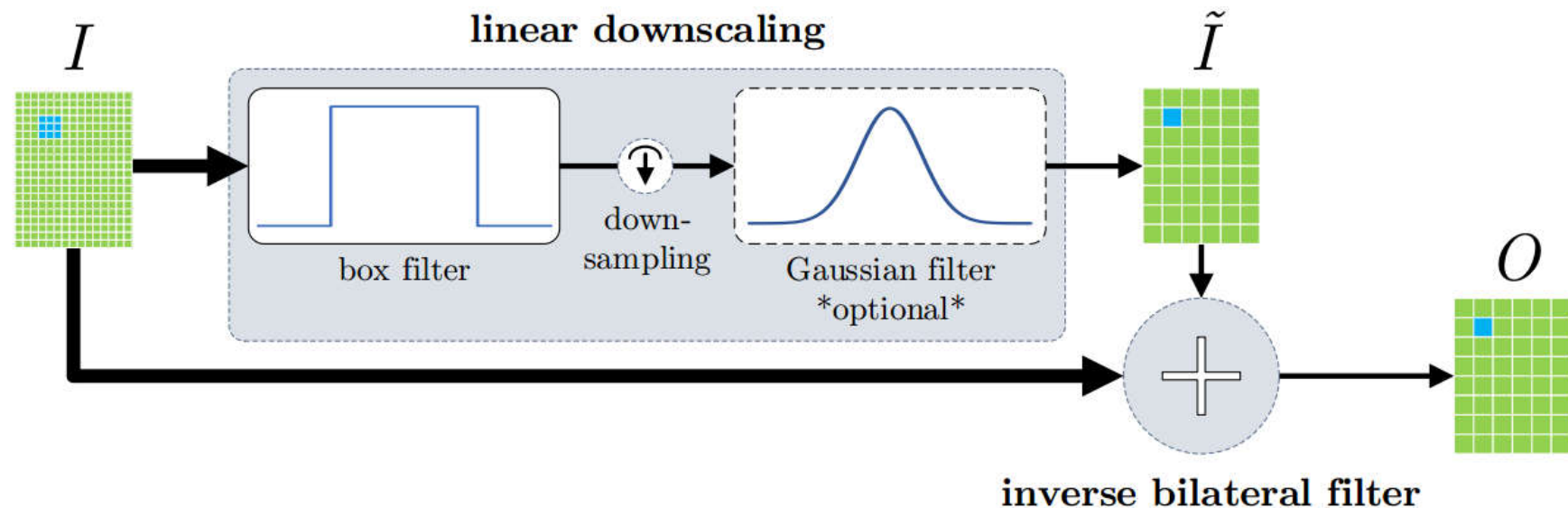


Figure 2. Diagram of detail-preserving downscaling (DPID) [31] and our detail-preserving pooling (DPP). DPP omits the Gaussian filter; Full-DPP replaces the box filter with a learned 2D filter.

## Detail-Preserving Pooling-DPID

- Given an input image  $I[\cdot]$ , detail-preserving image downscaling (DPID) calculates the downsampled output at pixel  $p$  as

$$O[p] = \frac{1}{k_p} \sum_{q \in \Omega_p} I[q] \cdot \|I[q] - \tilde{I}[p]\|^\lambda, \quad (1)$$

- in which the linearly downsampled image  $\tilde{I}$  is given by

$$\tilde{I} = I_D * \frac{1}{16} \begin{bmatrix} 1 & 2 & 1 \end{bmatrix}^T \begin{bmatrix} 1 & 2 & 1 \end{bmatrix}. \quad (2)$$

- The weights are normalized with  $k_p$

$$k_p = \sum_{q \in \Omega_p} \|I[q] - \tilde{I}[p]\|^\lambda \quad (3)$$



# Detail-Preserving Pooling-DPID



(a) Original Image



(b) DPID ( $\lambda = 1$ )



(c) Box filter (average pooling)



(d) Spatial maximum \ extremum



# Detail-Preserving Pooling-DPP

- Detail-preserving pooling of an input activation map  $I$  at spatial output position  $p$  as

$$\mathcal{D}_{\alpha,\lambda}(I)[p] = \frac{1}{\sum_{q' \in \Omega_p} w_{\alpha,\lambda}[p, q']} \sum_{q \in \Omega_p} w_{\alpha,\lambda}[p, q] I[q]. \quad (4)$$

- Equation (4) computes a spatially weighted average of the input nodes in a neighborhood  $I[q]_{q \in \Omega_p}$  for which we define weights  $w_{\alpha,\lambda}[p, q]$  as

$$w_{\alpha,\lambda}[p, q] = \alpha + \rho_\lambda \left( I[q] - \tilde{I}[p] \right). \quad (5)$$

# Detail-Preserving Pooling-DPP

- For the symmetric variant of the reward function  $\rho_\lambda(\cdot)$ , employ the differentiable (generalized) Charbonnier penalty,

$$\rho_{\text{Sym}}(x) = \left( \sqrt{x^2 + \epsilon^2} \right)^\lambda \quad (6)$$

- The asymmetric variant of  $\rho_\lambda(\cdot)$  only rewards positive arguments and is formulated as,

$$\rho_{\text{Asym}}(x) = \left( \sqrt{\max(0, x)^2 + \epsilon^2} \right)^\lambda, \quad (7)$$

# Detail-Preserving Pooling-DPP

- For the sake of simplicity in notation, we reformulate this such that the weights are normalized as

$$\tilde{w}_{\alpha,\lambda}[p, q] = \frac{w_{\alpha,\lambda}[p, q]}{\sum_{q' \in \Omega_p} w_{\alpha,\lambda}[p, q']} \quad (8)$$

- which allows us to write DPP as

$$\mathcal{D}_{\alpha,\lambda}(I)[p] = \sum_{q \in \Omega_p} \tilde{w}_{\alpha,\lambda}[p, q] I[q] \quad (9)$$

- In Eq. (4),  $\tilde{I}$  is the result of a linear downscaling, achieving full flexibility with

$$\tilde{I}_F[p] = \sum_{q \in \tilde{\Omega}_p} F[q] I[q] \quad (10)$$

# Detail-Preserving Pooling-DPP

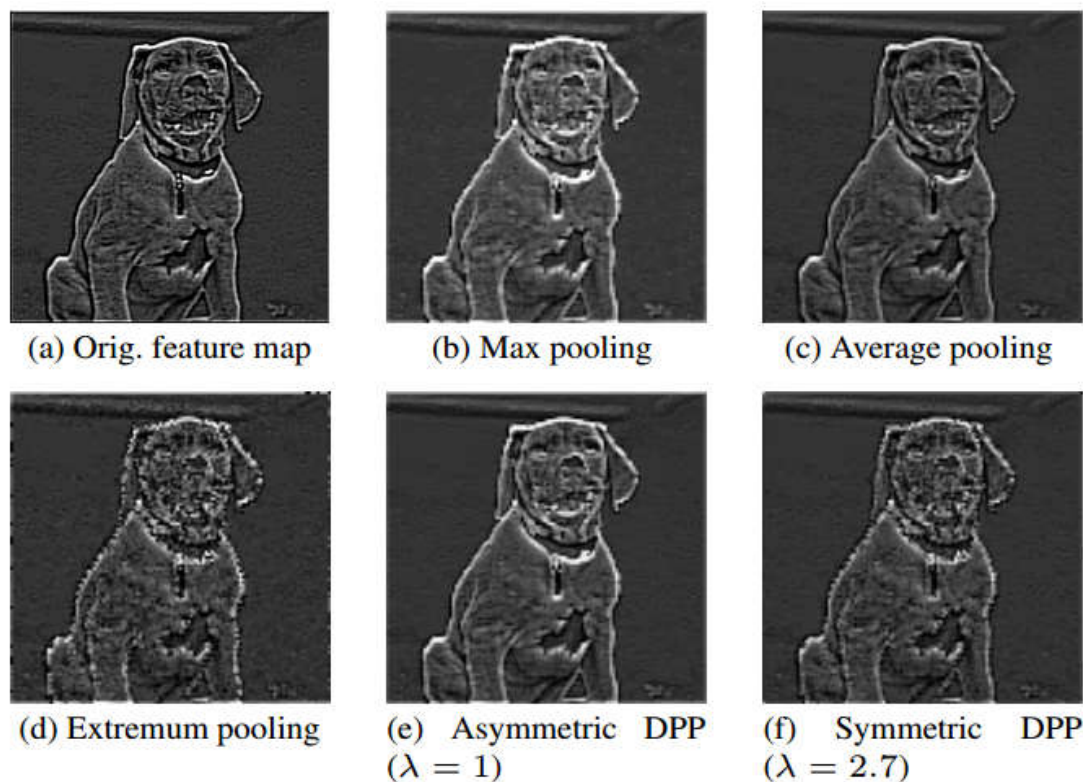


Figure 4. Visualization of different pooling methods on an example feature map taken from the second layer of VGG-16. For both reward variants, the bias  $\alpha$  is set to 0 to visually magnify the effect of the inverse bilateral weights. *Best viewed on screen.*

# Detail-Preserving Pooling-DPP


	Method	VGG	NIN	ResNet
Deterministic methods	Strided conv.	$8.43 \pm 0.20$	$10.97 \pm 0.10$	$6.23^{(*)}$
	Max	$7.43 \pm 0.20^{(*)}$	$9.42 \pm 0.07$	6.52
	Average	$7.12 \pm 0.18$	$8.75 \pm 0.15$	6.33
	NIN	–	$9.01 \pm 0.11^{(*)}$	–
	Mixed (50/50)	$7.27 \pm 0.20$	$8.68 \pm 0.23$	6.05
	Gated	$7.25 \pm 0.14$	$8.67 \pm 0.22$	7.12
	$L_2$	$7.15 \pm 0.18$	$8.65 \pm 0.12$	7.29
	Lite-DPP <sub>Asym</sub>	$7.10 \pm 0.15$	$8.62 \pm 0.10$	6.17
	Full-DPP <sub>Asym</sub>	$7.17 \pm 0.18$	$8.73 \pm 0.05$	6.23
	Lite-DPP <sub>Sym</sub>	$7.19 \pm 0.10$	$8.58 \pm 0.11$	6.05
	Full-DPP <sub>Sym</sub>	<b><math>7.02 \pm 0.18</math></b>	$8.70 \pm 0.14$	5.97
Stoch.	Stochastic	$7.67 \pm 0.10$	$8.92 \pm 0.09$	5.83
	S3pool	$7.21 \pm 0.14$	<u><math>7.23 \pm 0.08</math></u>	<u>5.55</u>
	Lite-S3DPP <sub>Sym</sub>	–	<b><math>7.13 \pm 0.09</math></b>	<b>5.42</b>



### Learnability and behavior adjustment

- Owing to differentiability:

spatial average —  
detail smoothed away



DPID [1] — detail plausibly preserved

- **DPID [1]:** downscale such that pixels that deviate more from a guidance  $I$  have larger contribution

is the role of  $\lambda$ ?

Level of detail-preservation is adjusted by  $\lambda$

## Properties

- DPP is **differentiable** w.r.t input and parameters
- For  $\lambda = 0$ , Lite-DPP equals *average pooling*
- For large values of  $\lambda$ , Lite-DPP<sub>Sym (Asym)</sub> equals *extremum pooling (max pooling)*

- Lite-DPP has 2 parameters per feature map ( $\lambda, \alpha$ )
- Full-DPP has extra 10 parameters (3x3 filter) per feature map
  - Example: Full-DPP adds 0.172% and 0.098% parameters to ResNet-50 and 101
- Time for pooling is **independent of network depth**; quite minor for deeper networks
  - Worst case scenario in our experiments: 20% overhead for VGG-16

- Owing to differentiability:  
→ Pooling behavior is adjusted through learning the parameters
- $\lambda$  and  $\alpha$  are constrained to remain positive

DPP adjusts its behavior for every feature channel by learning all parameters

Three different networks: basic pooling methods and recent compound pooling layers compared

Model	VOC	SIS	Real
Simulated case	8.61	10.97	8.20
Max	5.45 <sup>(*)</sup>	9.40	8.05
Average case	7.12	8.79	8.30
	- 0.002 <sup>(*)</sup>		
Mixed (50/50)			
class	7.27	8.68	8.05
class	7.28	8.67	7.93
all	7.15	8.65	7.98
Low-DIFF <sub>max</sub>	7.28	8.62	8.17
High-DIFF <sub>max</sub>	7.17	8.70	8.25
Low-DIFF <sub>avg</sub>	7.18	<b>8.88</b>	8.19
High-DIFF <sub>avg</sub>	<b>5.82</b>	8.70	<b>8.38</b>

(\*) indicates the original choice of pooling for the network

Data augmentation and preparation according to [2]

DPP increases accuracy for networks

- DPP is a learnable pooling layer that can perform similar to max / extremum or average pooling, or on a **nonlinear continuum** of intermediate functions

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- Constant and **affordable computational cost** and low parameter count
- **Consistently improves the performance** of networks on a wide range of architectures and datasets
- Can be paired with regularization to achieve **impressive performance**

- Similar to [3], S3DPP consists of DPP with a of 1, followed by a stochastic pixel selection
  - Performs importance sampling
- S3DPP helps with both downscaling and regularization

Method	VGG	SIN	ResNet
Included area	6.40	10.97	6.25 <sup>(*)</sup>
Max	7.43 <sup>(**)</sup>	9.42	6.52
Average	7.12	8.35	6.33
SIN	-	9.88 <sup>(*)</sup>	-
Stochastic	7.67	8.91	5.83
Staged	7.23	7.23	5.51
Low VGG <sub>max</sub>	-	<b>7.13</b>	<b>5.42</b>

S3DPP combines stochastic regularization and pooling

- VGG-16 with 5 pooling layers tr

- VGG-16 with 5 pooling layers trained on CIFAR-10
- Lite-DPP<sub>sym</sub> used for pooling
- Similar results for DPP<sub>Asym</sub>

First layers act similar to max, later layers similar to average pooling

Similar to m  
pooli

Code available



### Plug & play cooling layer