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1

```
map k gk
map j gj

map <C-h> <C-w>h
map <C-j> <C-w>j
map <C-k> <C-w>k
map <C-l> <C-w>k
map <C-l> <C-w>l

map <C-t> :vi <args>.cpp | vs <args>.in | sp <args>.out
```

2 Math

2.1 Basic Arithmetic

```
typedef long long 11;
typedef unsigned long long ull;
// calculate lg2(a)
inline int lg2(ll a) {
    return 63 - __builtin_clzll(a);
// calculate the number of 1-bits
inline int bitcount(ll a) {
    return __builtin_popcountl1(a);
// calculate ceil(a/b)
// |a|, |b| <= (2^63)-1 (does not dover -2^63)
11 ceildiv(ll a, ll b) {
    if (b < 0) return ceildiv(-a, -b);</pre>
    if (a < 0) return (-a) / b;
    return ((ull)a + (ull)b - 1ull) / b;
}
// calculate floor(a/b)
// |a|, |b| <= (2^63)-1 (does not cover -2^63)
11 floordiv(ll a, ll b) {
    if (b < 0) return floordiv(-a, -b);</pre>
    if (a >= 0) return a / b;
    return -(11)(((ull)(-a) + b - 1) / b);
}
// calculate a*b % m
// x86-64 only
11 large_mod_mul(ll a, ll b, ll m) {
    return 11((__int128)a*(__int128)b%m);
// calculate a*b % m
```

```
// |m| < 2^{62}, x86 available
// O(Logb)
11 large mod mul(ll a, ll b, ll m) {
    a \% = m; b \% = m; 11 r = 0, v = a;
    while (b) {
        if (b\&1) r = (r + v) \% m;
        b >>= 1;
        v = (v << 1) \% m;
    }
    return r;
}
// calculate n^k % m
11 modpow(ll n, ll k, ll m) {
    ll ret = 1;
    n \% = m;
    while (k) {
        if (k & 1) ret = large_mod_mul(ret, n, m);
        n = large_mod_mul(n, n, m);
        k /= 2:
    return ret;
// calculate qcd(a, b)
11 gcd(ll a, ll b) {
    return b == 0 ? a : gcd(b, a % b);
// find a pair (c, d) s.t. ac + bd = gcd(a, b)
pair<ll, ll> extended_gcd(ll a, ll b) {
    if (b == 0) return { 1, 0 };
    auto t = extended gcd(b, a % b);
    return { t.second, t.first - t.second * (a / b) };
}
// find x in [0,m) s.t. ax === gcd(a, m) \pmod{m}
11 modinverse(ll a, ll m) {
    return (extended_gcd(a, m).first % m + m) % m;
}
// calculate modular inverse for 1 ~ n
void calc_range_modinv(int n, int mod, int ret[]) {
    ret[1] = 1;
    for (int i = 2; i <= n; ++i)
        ret[i] = (ll)(mod - mod/i) * ret[mod%i] % mod;
}
```

2.2 Sieve Methods: Prime, Divisor, Euler phi

```
// find prime numbers in 1 ~ n
// ret[x] = false -> x is prime
// O(n*loglogn)
void sieve(int n, bool ret[]) {
```

```
for (int i = 2; i * i <= n; ++i)
        if (!ret[i])
            for (int j = i * i; j <= n; j += i)
                ret[i] = true;
}
// calculate number of divisors for 1 ~ n
// when you need to calculate sum, change += 1 to += i
// O(n*Logn)
void num_of_divisors(int n, int ret[]) {
   for (int i = 1; i <= n; ++i)
        for (int j = i; j <= n; j += i)
            ret[i] += 1;
}
// calculate euler totient function for 1 ~ n
// phi(n) = number of x s.t. 0 < x < n && qcd(n, x) = 1
// O(n*LogLogn)
void euler_phi(int n, int ret[]) {
    for (int i = 1; i <= n; ++i) ret[i] = i;
    for (int i = 2; i <= n; ++i)
        if (ret[i] == i)
            for (int j = i; j <= n; j += i)
                ret[j] -= ret[j] / i;
}
```

2.3 Primality Test

```
bool test_witness(ull a, ull n, ull s) {
    if (a >= n) a %= n;
   if (a <= 1) return true;</pre>
    ull d = n \gg s;
    ull x = modpow(a, d, n);
    if (x == 1 || x == n-1) return true;
    while (s-- > 1) {
        x = large mod mul(x, x, n);
        if (x == 1) return false;
        if (x == n-1) return true;
    return false:
// test whether n is prime
// based on miller-rabin test
// O(Logn*Logn)
bool is_prime(ull n) {
   if (n == 2) return true;
    if (n < 2 || n % 2 == 0) return false;</pre>
    ull d = n \gg 1, s = 1;
    for(; (d&1) == 0; s++) d >>= 1;
#define T(a) test_witness(a##ull, n, s)
    if (n < 4759123141ull) return T(2) && T(7) && T(61);
```

2.4 Integer Factorization (Pollard's rho)

```
11 pollard rho(ll n) {
    random_device rd;
    mt19937 gen(rd());
    uniform int distribution<ll> dis(1, n - 1);
    ll x = dis(gen);
    11 y = x;
    11 c = dis(gen);
    11 g = 1;
    while (g == 1) {
        x = (modmul(x, x, n) + c) \% n;
        y = (modmul(y, y, n) + c) % n;
        y = (modmul(y, y, n) + c) % n;
        g = gcd(abs(x - y), n);
    return g;
}
// integer factorization
// O(n^0.25 * logn)
void factorize(ll n, vector<ll>& fl) {
    if (n == 1) {
        return;
    if (n % 2 == 0) {
        fl.push back(2);
        factorize(n / 2, fl);
    else if (is prime(n)) {
        fl.push_back(n);
    }
    else {
        11 f = pollard_rho(n);
        factorize(f, fl);
        factorize(n / f, fl);
}
```

2.5 Chinese Remainder Theorem

```
ll tmp2 = (tmp * (a[1] - a[0]) % n[1] + n[1]) % n[1];
ll ora = a[1];
ll tgcd = gcd(n[0], n[1]);
a[1] = a[0] + n[0] / tgcd * tmp2;
n[1] *= n[0] / tgcd;
ll ret = chinese_remainder(a + 1, n + 1, size - 1);
n[1] /= n[0] / tgcd;
a[1] = ora;
return ret;
```

2.6 Modular Equation

}

 $x \equiv a \pmod{m}, x \equiv b \pmod{n}$ 을 만족시키는 x를 구하는 방법.

m과 n을 소인수분해한 후 소수의 제곱꼴의 합동식들로 각각 쪼갠다. 이 때 특정 소수에 대하여 모순이 생기면 불가능한 경우고, 모든 소수에 대해서 모순이 생기지 않으면 전체식을 CRT로 합치면 된다. 이제 $x\equiv x_1\pmod{p^{k_1}}$ 과 $x\equiv x_2\pmod{p^{k_2}}$ 가 모순이 생길조건은 $k_1\leq k_2$ 라고 했을 때, $x_1\not\equiv x_2\pmod{p^{k_1}}$ 인 경우이다. 모순이 생기지 않았을 때답을 구하려면 CRT로 합칠 때 $x\equiv x_2\pmod{p^{k_2}}$ 만을 남기고 합쳐주면 된다.

2.7 Rational Number Class

```
struct rational {
   long long p, q;
    void red() {
        if (q < 0) {
            p = -p;
            q = -q;
       11 t = gcd((p >= 0 ? p : -p), q);
        p /= t;
        q /= t;
   }
    rational(): p(0), q(1) {}
    rational(long long p_): p(p_), q(1) {}
    rational(long long p_, long long q_): p(p_), q(q_) { red(); }
    bool operator==(const rational& rhs) const {
        return p == rhs.p && q == rhs.q;
    bool operator!=(const rational& rhs) const {
        return p != rhs.p || q != rhs.q;
    bool operator<(const rational& rhs) const {</pre>
        return p * rhs.q < rhs.p * q;</pre>
    rational operator+(const rational& rhs) const {
        11 g = gcd(q, rhs.q);
```

```
return rational(p * (rhs.q / g) + rhs.p * (q / g), (q / g) * rhs.q);
}
rational operator-(const rational& rhs) const {
    l1 g = gcd(q, rhs.q);
    return rational(p * (rhs.q / g) - rhs.p * (q / g), (q / g) * rhs.q);
}
rational operator*(const rational& rhs) const {
    return rational(p * rhs.p, q * rhs.q);
}
rational operator/(const rational& rhs) const {
    return rational(p * rhs.q, q * rhs.p);
}
};
```

2.8 Catalan number

다양한 문제의 답이 되는 수열이다.

- 길이가 2n 인 올바른 괄호 수식의 수
- n+1개의 리프를 가진 풀 바이너리 트리의 수
- n+2각형을 n개의 삼각형으로 나누는 방법의 수

$$C_n = \frac{1}{n+1} \binom{2n}{n}$$

$$C_0 = 1$$
 and $C_{n+1} = \sum_{i=0}^{n} C_i C_{n-i}$

$$C_0 = 1$$
 and $C_{n+1} = \frac{2(2n+1)}{n+2}C_n$

2.9 Burnside's Lemma

경우의 수를 세는데, 특정 transform operation(회전, 반사, ..) 해서 같은 경우들은 하나로 친다. 전체 경우의 수는?

- 각 operation마다 이 operation을 했을 때 변하지 않는 경우의 수를 센다 (단, "아무것도 하지 않는다"라는 operation도 있어야 함!)
- 전체 경우의 수를 더한 후, operation의 수로 나눈다. (답이 맞다면 항상 나누어 떨어져야 한다)

2.10 Kirchoff's Theorem

그래프의 스패닝 트리의 개수를 구하는 정리.

무향 그래프의 Laplacian matrix L를 만든다. 이것은 (정점의 차수 대각 행렬) - (인접행렬) 이다. L에서 행과 열을 하나씩 제거한 것을 L'라 하자. 어느 행/열이든 관계 없다. 그래프의 스패닝 트리의 개수는 det(L')이다.

2.11 Lucas Theorem

```
// calculate nCm % p when p is prime
int lucas theorem(const char *n, const char *m, int p) {
    vector<int> np, mp;
    int i;
    for (i = 0; n[i]; i++) {
        if (n[i] == '0' && np.empty()) continue;
        np.push_back(n[i] - '0');
    for (i = 0; m[i]; i++) {
        if (m[i] == '0' && mp.empty()) continue;
        mp.push back(m[i] - '0');
    }
    int ret = 1;
    int ni = 0, mi = 0;
    while (ni < np.size() || mi < mp.size()) {</pre>
        int nmod = 0, mmod = 0;
        for (i = ni; i < np.size(); i++) {</pre>
            if (i + 1 < np.size())</pre>
                 np[i + 1] += (np[i] \% p) * 10;
            else
                 nmod = np[i] % p;
            np[i] /= p;
        for (i = mi; i < mp.size(); i++) {</pre>
            if (i + 1 < mp.size())</pre>
                 mp[i + 1] += (mp[i] \% p) * 10;
            else
                 mmod = mp[i] \% p;
            mp[i] /= p;
        while (ni < np.size() && np[ni] == 0) ni++;</pre>
        while (mi < mp.size() \&\& mp[mi] == 0) mi++;
        // implement binomial. binomial(m,n) = 0 if m < n
        ret = (ret * binomial(nmod, mmod)) % p;
    return ret;
}
```

2.12 Fast Fourier Transform

```
void fft(int sign, int n, double *real, double *imag) {
    double theta = sign * 2 * pi / n;
    for (int m = n; m >= 2; m >>= 1, theta *= 2) {
        double wr = 1, wi = 0, c = cos(theta), s = sin(theta);
        for (int i = 0, mh = m >> 1; i < mh; ++i) {</pre>
            for (int j = i; j < n; j += m) {
                int k = j + mh;
                double xr = real[j] - real[k], xi = imag[j] - imag[k];
                real[j] += real[k], imag[j] += imag[k];
                real[k] = wr * xr - wi * xi, imag[k] = wr * xi + wi * xr;
            double wr = wr * c - wi * s, wi = wr * s + wi * c;
            wr = wr, wi = wi;
    for (int i = 1, j = 0; i < n; ++i) {
        for (int k = n >> 1; k > (j ^= k); k >>= 1);
        if (j < i) swap(real[i], real[j]), swap(imag[i], imag[j]);</pre>
}
// Compute Poly(a)*Poly(b), write to r; Indexed from 0
// O(n*logn)
int mult(int *a, int n, int *b, int m, int *r) {
    const int maxn = 100;
    static double ra[maxn], rb[maxn], ia[maxn], ib[maxn];
    int fn = 1;
    while (fn < n + m) fn <<= 1; // n + m: interested length
    for (int i = 0; i < n; ++i) ra[i] = a[i], ia[i] = 0;
    for (int i = n; i < fn; ++i) ra[i] = ia[i] = 0;</pre>
    for (int i = 0; i < m; ++i) rb[i] = b[i], ib[i] = 0;
    for (int i = m; i < fn; ++i) rb[i] = ib[i] = 0;
    fft(1, fn, ra, ia);
    fft(1, fn, rb, ib);
    for (int i = 0; i < fn; ++i) {
        double real = ra[i] * rb[i] - ia[i] * ib[i];
        double imag = ra[i] * ib[i] + rb[i] * ia[i];
        ra[i] = real, ia[i] = imag;
    fft(-1, fn, ra, ia);
    for (int i = 0; i < fn; ++i) r[i] = (int)floor(ra[i] / fn + 0.5);</pre>
    return fn:
}
2.13 Matrix Operations
const int MATSZ = 100;
inline bool is_zero(double a) { return fabs(a) < 1e-9; }</pre>
// out = A^{(-1)}, returns det(A)
// A becomes invalid after call this
double inverse_and_det(int n, double A[][MATSZ], double out[][MATSZ]) {
    double det = 1:
```

```
for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) out[i][j] = 0;
    out[i][i] = 1;
for (int i = 0; i < n; i++) {
    if (is zero(A[i][i])) {
        double maxv = 0;
        int maxid = -1;
        for (int j = i + 1; j < n; j++) {
            auto cur = fabs(A[j][i]);
            if (maxv < cur) {</pre>
                maxv = cur;
                maxid = j;
            }
        if (maxid == -1 || is_zero(A[maxid][i])) return 0;
        for (int k = 0; k < n; k++) {
            A[i][k] += A[maxid][k];
            out[i][k] += out[maxid][k];
        }
    det *= A[i][i];
    double coeff = 1.0 / A[i][i];
    for (int j = 0; j < n; j++) A[i][j] *= coeff;</pre>
    for (int j = 0; j < n; j++) out[i][j] *= coeff;</pre>
    for (int j = 0; j < n; j++) if (j != i) {
        double mp = A[j][i];
        for (int k = 0; k < n; k++) A[j][k] -= A[i][k] * mp;
        for (int k = 0; k < n; k++) out[j][k] -= out[i][k] * mp;
   }
return det;
```

Gaussian Elimination

}

```
const double EPS = 1e-10;
typedef vector<vector<double>> VVD;
// Gauss-Jordan elimination with full pivoting.
// solving systems of linear equations (AX=B)
            a[][] = an n*n matrix
// INPUT:
             b[][] = an n*m matrix
// OUTPUT: X
                   = an n*m matrix (stored in b[][])
             A^{-1} = an n*n matrix (stored in a[][])
//
// O(n^3)
bool gauss_jordan(VVD& a, VVD& b) {
    const int n = a.size();
    const int m = b[0].size();
    vector<int> irow(n), icol(n), ipiv(n);
   for (int i = 0; i < n; i++) {
        int pj = -1, pk = -1;
        for (int j = 0; j < n; j++) if (!ipiv[j])</pre>
```

```
for (int k = 0; k < n; k++) if (!ipiv[k])
                if (pj == -1 || fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk =
                  k; }
        if (fabs(a[pj][pk]) < EPS) return false; // matrix is singular</pre>
        ipiv[pk]++;
        swap(a[pj], a[pk]);
        swap(b[pj], b[pk]);
        irow[i] = pj;
        icol[i] = pk;
        double c = 1.0 / a[pk][pk];
        a[pk][pk] = 1.0;
        for (int p = 0; p < n; p++) a[pk][p] *= c;
        for (int p = 0; p < m; p++) b[pk][p] *= c;
        for (int p = 0; p < n; p++) if (p != pk) {
            c = a[p][pk];
            a[p][pk] = 0;
            for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
            for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;
    for (int p = n - 1; p >= 0; p --) if (irow[p] != icol[p]) {
        for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);
    }
    return true;
}
```

2.15 Simplex Algorithm

```
// Two-phase simplex algorithm for solving linear programs of the form
//
       maximize
                    c^T x
//
       subject to
                   Ax <= b
//
                     x >= 0
// INPUT: A -- an m x n matrix
         b -- an m-dimensional vector
         c -- an n-dimensional vector
         x -- a vector where the optimal solution will be stored
// OUTPUT: value of the optimal solution (infinity if unbounded
           above, nan if infeasible)
// To use this code, create an LPSolver object with A, b, and c as
// arguments. Then, call Solve(x).
typedef vector<double> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
const double EPS = 1e-9;
struct LPSolver {
    int m, n;
    VI B, N;
    VVD D;
    LPSolver(const VVD& A, const VD& b, const VD& c):
        m(b.size()), n(c.size()), N(n + 1), B(m), D(m + 2, VD(n + 2)) 
        for (int i = 0; i < m; i++) for (int j = 0; j < n; j++) D[i][j] = A[i][j]
```

```
];
    for (int i = 0; i < m; i++) { B[i] = n + i; D[i][n] = -1; D[i][n + 1] =
      b[i]; }
    for (int j = 0; j < n; j++) { N[j] = j; D[m][j] = -c[j]; }
    N[n] = -1; D[m + 1][n] = 1;
}
void pivot(int r, int s) {
    double inv = 1.0 / D[r][s];
    for (int i = 0; i < m + 2; i++) if (i != r)
        for (int j = 0; j < n + 2; j++) if (j != s)
            D[i][j] -= D[r][j] * D[i][s] * inv;
    for (int j = 0; j < n + 2; j++) if (j != s) D[r][j] *= inv;
    for (int i = 0; i < m + 2; i++) if (i != r) D[i][s] *= -inv;
    D[r][s] = inv;
    swap(B[r], N[s]);
}
bool simplex(int phase) {
    int x = phase == 1 ? m + 1 : m:
    while (true) {
        int s = -1;
        for (int j = 0; j <= n; j++) {
            if (phase == 2 && N[i] == -1) continue;
            if (s == -1 \mid | D[x][j] < D[x][s] \mid | D[x][j] == D[x][s] && N[j] <
               N[s]) s = j;
        if (D[x][s] > -EPS) return true;
        int r = -1;
        for (int i = 0; i < m; i++) {
            if (D[i][s] < EPS) continue;</pre>
            if (r == -1 || D[i][n + 1] / D[i][s] < D[r][n + 1] / D[r][s] ||</pre>
                (D[i][n + 1] / D[i][s]) == (D[r][n + 1] / D[r][s]) && B[i] <
                   B[r]) r = i;
        if (r == -1) return false;
        pivot(r, s);
double solve(VD& x) {
    int r = 0;
    for (int i = 1; i < m; i++) if (D[i][n + 1] < D[r][n + 1]) r = i;
    if (D[r][n + 1] < -EPS) {
        pivot(r, n);
        if (!simplex(1) || D[m + 1][n + 1] < -EPS)
            return -numeric_limits<double>::infinity();
        for (int i = 0; i < m; i++) if (B[i] == -1) {
            int s = -1:
            for (int j = 0; j <= n; j++)
                if (s == -1 || D[i][j] < D[i][s] || D[i][j] == D[i][s] && N[
                  j \mid \langle N[s] \rangle s = j;
            pivot(i, s);
    }
```

2.16 Nim Game

Nim Game의 해법: 각 더미의 돌의 개수를 모두 XOR했을 때 0이 아니면 첫번째, 0이면 두번째 플레이어가 승리

Grundy Number: 가능한 다음 state의 Grundy Number를 모두 모은 다음, 그 set에 포함 되지 않는 가장 작은 수가 현재 state의 Grundy Number가 된다. 만약 다음 state가 독립된 여러 개의 state들로 나뉠 경우, 각각의 state의 Grundy Number의 XOR 합을 생각한다.

Subtraction Game : 한 번에 k개까지의 돌만 가져갈 수 있는 경우, 각 더미의 돌의 개수를 k+1로 나눈 나머지를 XOR 합하여 판단한다.

Index-k Nim : 한 번에 최대 k개의 더미를 골라 각각의 더미에서 아무렇게나 돌을 제거할 수 있을 때, 각 binary digit에 대하여 합을 k+1로 나눈 나머지를 계산한다. 만약 이 나머지가 모든 digit에 대하여 0이라면 두번째, 하나라도 0이 아니라면 첫번째 플레이어가 승리.

3 Data Structure

3.1 Order statistic tree

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb ds/detail/standard policies.hpp>
#include <functional>
#include <iostream>
using namespace __gnu_pbds;
using namespace std;
// tree<key_type, value_type(set if null), comparator, ...>
using ordered_set = tree<int, null_type, less<int>, rb_tree_tag,
    tree order statistics node update>;
int main()
    ordered set X;
    for (int i = 1; i < 10; i += 2) X.insert(i); // 1 3 5 7 9
    cout << boolalpha;</pre>
    cout << *X.find_by_order(2) << endl; // 5</pre>
    cout << *X.find by order(4) << endl; // 9</pre>
    cout << (X.end() == X.find_by_order(5)) << endl; // true</pre>
```

```
cout << X.order_of_key(-1) << endl; // 0
cout << X.order_of_key(1) << endl; // 0
cout << X.order_of_key(4) << endl; // 2
X.erase(3);
cout << X.order_of_key(4) << endl; // 1
for (int t : X) printf("%d_", t); // 1 5 7 9</pre>
```

3.2 Fenwick Tree

```
const int TSIZE = 100000;
int tree[TSIZE + 1];

// Returns the sum from index 1 to p, inclusive
int query(int p) {
   int ret = 0;
   for (; p > 0; p -= p & -p) ret += tree[p];
   return ret;
}

// Adds val to element with index pos
void add(int p, int val) {
   for (; p <= TSIZE; p += p & -p) tree[p] += val;
}</pre>
```

3.3 Segment Tree with Lazy Propagation

```
// example implementation of sum tree
const int TSIZE = 131072; // always 2^k form && n <= TSIZE</pre>
int segtree[TSIZE * 2], prop[TSIZE * 2];
void seg_init(int nod, int 1, int r) {
   if (1 == r) segtree[nod] = dat[1];
    else {
        int m = (1 + r) >> 1;
        seg init(nod << 1, 1, m);
        seg_init(nod << 1 | 1, m + 1, r);
        segtree[nod] = segtree[nod << 1] + segtree[nod << 1 | 1];</pre>
}
void seg relax(int nod, int 1, int r) {
   if (prop[nod] == 0) return;
   if (1 < r) {
        int m = (1 + r) >> 1;
        segtree[nod << 1] += (m - 1 + 1) * prop[nod];
        prop[nod << 1] += prop[nod];</pre>
        segtree[nod << 1 | 1] += (r - m) * prop[nod];
        prop[nod << 1 | 1] += prop[nod];</pre>
    prop[nod] = 0;
int seg query(int nod, int 1, int r, int s, int e) {
    if (r < s || e < 1) return 0;
    if (s <= 1 && r <= e) return segtree[nod];</pre>
```

```
seg relax(nod, 1, r);
    int m = (1 + r) >> 1;
    return seg_query(nod << 1, 1, m, s, e) + seg_query(nod << 1 | 1, m + 1, r, s
}
void seg update(int nod, int 1, int r, int s, int e, int val) {
    if (r < s || e < 1) return;
    if (s <= 1 && r <= e) {
        segtree[nod] += (r - l + 1) * val;
        prop[nod] += val;
        return;
    seg_relax(nod, 1, r);
    int m = (1 + r) >> 1;
    seg_update(nod << 1, 1, m, s, e, val);</pre>
    seg update(nod \langle\langle 1 \mid 1, m + 1, r, s, e, val);
    segtree[nod] = segtree[nod << 1] + segtree[nod << 1 | 1];</pre>
// usage:
// seg_update(1, 0, n - 1, qs, qe, val);
// seg_query(1, 0, n - 1, qs, qe);
3.4 Persistent Segment Tree
// persistent segment tree impl: sum tree
// initial tree index is 0
namespace pstree {
    typedef int val t;
    const int DEPTH = 18;
    const int TSIZE = 1 << 18;</pre>
    const int MAX_QUERY = 262144;
    struct node {
        val t v;
        node *1, *r;
    } npoll[TSIZE * 2 + MAX QUERY * (DEPTH + 1)], *head[MAX QUERY + 1];
    int pptr, last q;
    void init() {
        // zero-initialize, can be changed freely
        memset(&npoll[TSIZE - 1], 0, sizeof(node) * TSIZE);
        for (int i = TSIZE - 2; i >= 0; i--) {
            npoll[i].v = 0;
            npoll[i].l = &npoll[i*2+1];
            npoll[i].r = &npoll[i*2+2];
        head[0] = &npoll[0];
        last_q = 0;
        pptr = 2 * TSIZE - 1;
```

}

```
// update val to pos
    // 0 <= pos < TSIZE
                                                                                                 };
    // returns updated tree index
                                                                                                 node* root;
    int update(int pos, int val, int prev) {
         head[++last_q] = &npoll[pptr++];
                                                                                                 void update(node* x) {
         node *old = head[prev], *now = head[last q];
                                                                                                     x \rightarrow cnt = 1;
                                                                                                     x \rightarrow sum = x \rightarrow min = x \rightarrow max = x \rightarrow val;
         int flag = 1 << DEPTH;</pre>
                                                                                                     if (x\rightarrow 1) {
         for (;;) {
                                                                                                          x \rightarrow cnt += x \rightarrow 1 \rightarrow cnt;
             now->v = old->v + val;
                                                                                                          x \rightarrow sum += x \rightarrow 1 \rightarrow sum;
             flag >>= 1;
                                                                                                          x->min = min(x->min, x->l->min);
             if (flag==0) {
                                                                                                          x -> max = max(x -> max, x -> 1 -> max);
                  now->l = now->r = nullptr; break;
                                                                                                     if (x->r) {
             if (flag & pos) {
                                                                                                          x \rightarrow cnt += x \rightarrow r \rightarrow cnt;
                  now->1 = old->1;
                                                                                                          x \rightarrow sum += x \rightarrow r \rightarrow sum;
                  now->r = &npoll[pptr++];
                                                                                                          x - \min = \min(x - \min, x - r - \min);
                  now = now -> r, old = old->r;
                                                                                                          x->max = max(x->max, x->r->max);
             } else {
                                                                                                     }
                                                                                                 }
                  now->r = old->r;
                  now->1 = &npoll[pptr++];
                  now = now ->1, old = old->1;
                                                                                                 void rotate(node* x) {
                                                                                                     node* p = x->p;
         }
                                                                                                     node* b = nullptr;
                                                                                                     if (x == p->1) {
         return last q;
    }
                                                                                                          p->1 = b = x->r;
                                                                                                          x \rightarrow r = p;
    val t query(int s, int e, int l, int r, node *n) {
         if (s == 1 \&\& e == r) return n \rightarrow v;
                                                                                                     else {
         int m = (1 + r) / 2;
                                                                                                          p->r = b = x->1;
         if (m \ge e) return query(s, e, l, m, n \ge l);
                                                                                                          x \rightarrow 1 = p;
         else if (m < s) return query(s, e, m + 1, r, n->r);
                                                                                                     x - p = p - p;
         else return query(s, m, l, m, n->l) + query(m + 1, e, m + 1, r, n->r);
    }
                                                                                                     p \rightarrow p = x;
                                                                                                     if (b) b \rightarrow p = p;
    // query summation of [s, e] at time t
                                                                                                     x->p? (p == x->p->1? x->p->1: x->p->r) = x : (root = x);
    val_t query(int s, int e, int t) {
                                                                                                     update(p);
         s = max(0, s); e = min(TSIZE - 1, e);
                                                                                                     update(x);
                                                                                                 }
         if (s > e) return 0;
         return query(s, e, 0, TSIZE - 1, head[t]);
                                                                                                 // make x into root
                                                                                                 void splay(node* x) {
                                                                                                     while (x->p) {
                                                                                                          node* p = x->p;
      Splay Tree
                                                                                                          node* g = p - p;
                                                                                                          if (g) rotate((x == p->1) == (p == g->1) ? p : x);
                                                                                                          rotate(x);
// example : https://www.acmicpc.net/problem/13159
struct node {
                                                                                                 }
    node* 1, * r, * p;
    int cnt, min, max, val;
                                                                                                 void relax lazy(node* x) {
    long long sum;
                                                                                                     if (!x->inv) return;
    bool inv;
                                                                                                     swap(x->1, x->r);
    node(int val) :
                                                                                                     x->inv = false;
         cnt(1), sum(_val), min(_val), max(_val), val(_val), inv(false),
                                                                                                     if (x->1) x->1->inv = !x->1->inv;
         l(nullptr), r(nullptr), p(nullptr) {
```

```
if (x\rightarrow r) x\rightarrow r\rightarrow inv = !x\rightarrow r\rightarrow inv;
}
// find kth node in splay tree
void find_kth(int k) {
    node* x = root;
    relax lazy(x);
    while (true) {
         while (x->1 && x->1->cnt > k) {
             x = x \rightarrow 1;
             relax lazy(x);
         if (x->1) k -= x->1->cnt;
        if (!k--) break;
         x = x - r;
         relax_lazy(x);
    splay(x);
}
// collect [l, r] nodes into one subtree and return its root
node* interval(int 1, int r) {
    find_kth(1 - 1);
    node* x = root;
    root = x->r;
    root->p = nullptr;
    find kth(r - l + 1);
    x->r = root;
    root -> p = x;
    root = x;
    return root->r->l;
}
void traverse(node* x) {
    relax lazy(x);
    if (x\rightarrow 1) {
         traverse(x->1);
    // do something
    if (x->r) {
         traverse(x->r);
}
void uptree(node* x) {
    if (x->p) {
         uptree(x->p);
    relax_lazy(x);
}
```

3.6 Link/Cut Tree

4 DP

4.1 Convex Hull Optimization

```
O(n^2) \to O(n \log n)
DP 점화식 꼴
D[i] = \max_{j < i} (D[j] + b[j] * a[i]) \ (b[k] \le b[k+1])
D[i] = \min_{i < i} (D[j] + b[j] * a[i]) \ (b[k] \ge b[k+1])
특수조건) a[i] \le a[i+1] 도 만족하는 경우, 마지막 쿼리의 위치를 저장해두면 이분검색이
필요없어지기 때문에 amortized O(n) 에 해결할 수 있음
struct CHTLinear {
    struct Line {
        long long a, b;
        long long y(long long x) const { return a * x + b; }
    };
    vector<Line> stk;
    int qpt;
    CHTLinear() : qpt(0) { }
    // when you need maximum : (previous l).a < (now l).a
    // when you need minimum : (previous L).a > (now L).a
    void pushLine(const Line& 1) {
        while (stk.size() > 1) {
            Line& 10 = stk[stk.size() - 1];
            Line& l1 = stk[stk.size() - 2];
            if ((10.b - 1.b) * (10.a - 11.a) > (11.b - 10.b) * (1.a - 10.a))
              break;
            stk.pop_back();
        stk.push_back(1);
    // (previous x) <= (current x)</pre>
    // it calculates max/min at x
    long long query(long long x) {
        while (qpt + 1 < stk.size()) {</pre>
            Line& 10 = stk[qpt];
            Line& 11 = stk[qpt + 1];
            if (l1.a - l0.a > 0 && (l0.b - l1.b) > x * (l1.a - l0.a)) break;
            if (l1.a - l0.a < 0 && (l0.b - l1.b) < x * (l1.a - l0.a)) break;
            ++qpt;
        return stk[qpt].y(x);
};
```

4.2 Divide & Conquer Optimization

```
O(kn^2) 	o O(kn\log n) 조건 1) DP 점화식 꼴 D[t][i] = \min_{j < i} (D[t-1][j] + C[j][i]) 조건 2) A[t][i] \vdash D[t][i]의 답이 되는 최소의 j 라 할 때, 아래의 부등식을 만족해야 함 A[t][i] \le A[t][i+1] 조건 2-1) 비용C가 다음의 사각부등식을 만족하는 경우도 조건 2)를 만족하게 됨 C[a][c] + C[b][d] \le C[a][d] + C[b][c] \;\; (a \le b \le c \le d)
```

4.3 Knuth Optimization

```
O(n^3) \to O(n^2)
조건 1) DP 점화식 꼴 D[i][j] = \min_{i < k < j} (D[i][k] + D[k][j]) + C[i][j] 조건 2) 사각 부등식 C[a][c] + C[b][d] \le C[a][d] + C[b][c] \ \ (a \le b \le c \le d) 조건 3) 단조성 C[b][c] \le C[a][d] \ \ (a \le b \le c \le d)
```

결론) 조건 2, 3을 만족한다면 A[i][j]를 D[i][j]의 답이 되는 최소의 k라 할 때, 아래의 부등 식을 만족하게 됨

 $A[i][j-1] \le A[i][j] \le A[i+1][j]$

3중 루프를 돌릴 때 위 조건을 이용하면 최종적으로 시간복잡도가 $O(n^2)$ 이 됨

5 Graph

5.1 SCC

```
const int MAXN = 100;
vector<int> graph[MAXN];
int up[MAXN], visit[MAXN], vtime;
vector<int> stk;
int scc_idx[MAXN], scc_cnt;
```

```
void dfs(int nod) {
    up[nod] = visit[nod] = ++vtime;
    stk.push back(nod);
    for (int next : graph[nod]) {
        if (visit[next] == 0) {
            dfs(next);
            up[nod] = min(up[nod], up[next]);
        else if (scc_idx[next] == 0)
            up[nod] = min(up[nod], visit[next]);
    if (up[nod] == visit[nod]) {
        ++scc_cnt;
        int t;
        do {
            t = stk.back();
            stk.pop back();
            scc_idx[t] = scc_cnt;
        } while (!stk.empty() && t != nod);
}
// find SCCs in given directed graph
// the order of scc idx constitutes a reverse topological sort
void get_scc() {
    vtime = 0:
    memset(visit, 0, sizeof(visit));
    scc cnt = 0;
    memset(scc_idx, 0, sizeof(scc_idx));
    for (int i = 0; i < n; ++i)
        if (visit[i] == 0) dfs(i);
}
```

5.2 2-SAT

 $(b_x \lor b_y) \land (\neg b_x \lor b_z) \land (b_z \lor \neg b_x) \land \cdots$ 같은 form을 2-CNF라고 함. 주어진 2-CNF 식을 참으로 하는 $\{b_1, b_2, \dots\}$ 가 존재하는지, 존재한다면 그 값은 무엇인지 구하는 문제를 2-SAT 이라 함.

boolean variable b_i 마다 b_i 를 나타내는 정점, $\neg b_i$ 를 나타내는 정점 2개를 만듦. 각 clause $b_i \lor b_j$ 마다 $\neg b_i \to b_j$, $\neg b_j \to b_i$ 이렇게 edge를 이어줌. 그렇게 만든 그래프에서 SCC를 다구함. 어떤 SCC 안에 b_i 와 $\neg b_i$ 가 같이 포함되어있다면 해가 존재하지 않음. 아니라면 해가 존재함.

해가 존재할 때 구체적인 해를 구하는 방법. 위에서 SCC를 구하면서 SCC DAG를 만들어 준다. 거기서 위상정렬을 한 후, 앞에서부터 SCC를 하나씩 봐준다. 현재 보고있는 SCC에 b_i 가 속해있는데 얘가 $\neg b_i$ 보다 먼저 등장했다면 b_i = false, 반대의 경우라면 b_i = true, 이미 값이 assign되었다면 pass.

5.3 BCC, Cut vertex, Bridge

```
const int MAXN = 100;
vector<pair<int, int>> graph[MAXN]; // { next vertex id, edge id }
int up[MAXN], visit[MAXN], vtime;
vector<pair<int, int>> stk;
int is cut[MAXN];
                            // v is cut vertex if is cut[v] > 0
vector<int> bridge;
                           // list of edge ids
vector<int> bcc idx[MAXN]; // list of bccids for vertex i
int bcc_cnt;
void dfs(int nod, int par_edge) {
   up[nod] = visit[nod] = ++vtime;
   int child = 0;
   for (const auto& e : graph[nod]) {
        int next = e.first, edge_id = e.second;
        if (edge_id == par_edge) continue;
        if (visit[next] == 0) {
            stk.push_back({ nod, next });
            ++child;
            dfs(next, edge_id);
            if (up[next] == visit[next]) bridge.push back(edge id);
            if (up[next] >= visit[nod]) {
                ++bcc_cnt;
                do {
                    auto last = stk.back();
                    stk.pop back();
                    bcc_idx[last.second].push_back(bcc_cnt);
                    if (last == pair<int, int>{ nod, next }) break;
                } while (!stk.empty());
                bcc idx[nod].push back(bcc cnt);
                is_cut[nod]++;
            up[nod] = min(up[nod], up[next]);
        }
        else
            up[nod] = min(up[nod], visit[next]);
    if (par_edge == -1 && is_cut[nod] == 1)
        is cut[nod] = 0;
}
// find BCCs & cut vertexs & bridges in undirected graph
// O(V+E)
void get_bcc() {
   vtime = 0:
    memset(visit, 0, sizeof(visit));
    memset(is_cut, 0, sizeof(is_cut));
   bridge.clear();
    for (int i = 0; i < n; ++i) bcc_idx[i].clear();</pre>
    bcc cnt = 0;
    for (int i = 0; i < n; ++i) {
        if (visit[i] == 0)
            dfs(i, -1);
```

}

5.4 Block-cut Tree

각 BCC 및 cut vertex가 block-cut tree의 vertex가 되며, BCC와 그 BCC에 속한 cut vertex 사이에 edge를 이어주면 된다.

5.5 Shortest Path Faster Algorithm

```
// shortest path faster algorithm
// average for random graph : O(E) , worst : O(VE)
const int MAXN = 20001;
const int INF = 100000000;
int n, m;
vector<pair<int, int>> graph[MAXN];
bool inqueue[MAXN];
int dist[MAXN];
void spfa(int st) {
    for (int i = 0; i < n; ++i) {
        dist[i] = INF;
    dist[st] = 0;
    queue<int> q;
    q.push(st);
    inqueue[st] = true;
    while (!q.empty()) {
        int u = q.front();
        q.pop();
        inqueue[u] = false;
        for (auto& e : graph[u]) {
            if (dist[u] + e.second < dist[e.first]) {</pre>
                dist[e.first] = dist[u] + e.second;
                if (!inqueue[e.first]) {
                    q.push(e.first);
                    inqueue[e.first] = true;
            }
}
```

5.6 Lowest Common Ancestor

```
const int MAXN = 100;
const int MAXLN = 9;
vector<int> tree[MAXN];
```

```
int depth[MAXN];
int par[MAXLN][MAXN];
void dfs(int nod, int parent) {
    for (int next : tree[nod]) {
        if (next == parent) continue;
        depth[next] = depth[nod] + 1;
        par[0][next] = nod;
        dfs(next, nod);
}
void prepare_lca() {
    const int root = 0;
    dfs(root, -1);
    par[0][root] = root;
    for (int i = 1; i < MAXLN; ++i)</pre>
        for (int j = 0; j < n; ++j)
            par[i][j] = par[i - 1][par[i - 1][j]];
}
// find lowest common ancestor in tree between u & v
// assumption : must call 'prepare_lca' once before call this
// O(LogV)
int lca(int u, int v) {
    if (depth[u] < depth[v]) swap(u, v);</pre>
    if (depth[u] > depth[v]) {
        for (int i = MAXLN - 1; i >= 0; --i)
            if (depth[u] - (1 << i) >= depth[v])
                u = par[i][u];
    if (u == v) return u;
    for (int i = MAXLN - 1; i >= 0; --i) {
        if (par[i][u] != par[i][v]) {
            u = par[i][u];
            v = par[i][v];
        }
    }
    return par[0][u];
}
     Heavy-Light Decomposition
// heavy-light decomposition
//
// hld h;
// insert edges to tree[0~n-1];
// h.init(n, root);
// h.decompose(root);
// h.hldquery(u, v); // edges from u to v
struct hld {
    static const int MAXLN = 18;
    static const int MAXN = 1 << (MAXLN - 1);</pre>
```

vector<int> tree[MAXN];

```
int subsize[MAXN], depth[MAXN], pa[MAXLN][MAXN];
int chead[MAXN], cidx[MAXN];
int lchain;
int flatpos[MAXN + 1], fptr;
void dfs(int u, int par) {
    pa[0][u] = par;
    subsize[u] = 1;
    for (int v : tree[u]) {
        if (v == pa[0][u]) continue;
        depth[v] = depth[u] + 1;
        dfs(v, u);
        subsize[u] += subsize[v];
}
void init(int size, int root)
    lchain = fptr = 0:
    dfs(root, -1);
    memset(chead, -1, sizeof(chead));
    for (int i = 1; i < MAXLN; i++) {
        for (int j = 0; j < size; j++) {</pre>
            if (pa[i - 1][j] != -1) {
                pa[i][j] = pa[i - 1][pa[i - 1][j]];
        }
    }
}
void decompose(int u) {
    if (chead[lchain] == -1) chead[lchain] = u;
    cidx[u] = lchain;
    flatpos[u] = ++fptr;
    int maxchd = -1;
    for (int v : tree[u]) {
        if (v == pa[0][u]) continue;
        if (maxchd == -1 || subsize[maxchd] < subsize[v]) maxchd = v;</pre>
    if (maxchd != -1) decompose(maxchd);
    for (int v : tree[u]) {
        if (v == pa[0][u] || v == maxchd) continue;
        ++lchain; decompose(v);
}
int lca(int u, int v) {
    if (depth[u] < depth[v]) swap(u, v);</pre>
    for (logu = 1; 1 << logu <= depth[u]; logu++);</pre>
```

```
logu--;
                                                                                         vector<int> reached[2];
                                                                                         BipartiteMatching(int n, int m): n(n), m(m), graph(n), matched(m, -1),
        int diff = depth[u] - depth[v];
                                                                                           match(n, -1) {}
        for (int i = logu; i >= 0; --i) {
            if ((diff >> i) & 1) u = pa[i][u];
                                                                                         bool assignLevel() {
                                                                                              bool reachable = false;
        if (u == v) return u;
                                                                                              level.assign(n, -1);
                                                                                              reached[0].assign(n, 0);
                                                                                              reached[1].assign(m, 0);
        for (int i = logu; i >= 0; --i) {
            if (pa[i][u] != pa[i][v]) {
                                                                                              queue<int> q;
                u = pa[i][u];
                                                                                              for (int i = 0; i < n; i++) {
                v = pa[i][v];
                                                                                                  if (match[i] == -1) {
                                                                                                     level[i] = 0;
        }
                                                                                                     reached[0][i] = 1;
        return pa[0][u];
                                                                                                     q.push(i);
                                                                                                 }
    }
    // TODO: implement query functions
                                                                                              while (!q.empty()) {
    inline int query(int s, int e) {
                                                                                                  auto cur = q.front(); q.pop();
        return 0:
                                                                                                  for (auto adj : graph[cur]) {
   }
                                                                                                      reached[1][adj] = 1;
                                                                                                      auto next = matched[adj];
    int subquery(int u, int v) {
                                                                                                     if (next == -1) {
        int uchain, vchain = cidx[v];
                                                                                                          reachable = true;
        int ret = 0;
        for (;;) {
                                                                                                      else if (level[next] == -1) {
            uchain = cidx[u];
                                                                                                          level[next] = level[cur] + 1;
            if (uchain == vchain) {
                                                                                                          reached[0][next] = 1;
                ret += query(flatpos[v], flatpos[u]);
                                                                                                          q.push(next);
                break;
            }
                                                                                                 }
            ret += query(flatpos[chead[uchain]], flatpos[u]);
                                                                                              return reachable;
            u = pa[0][chead[uchain]];
        }
        return ret;
                                                                                         int findpath(int nod) {
   }
                                                                                              for (int &i = edgeview[nod]; i < graph[nod].size(); i++) {</pre>
                                                                                                  int adj = graph[nod][i];
   inline int hldquery(int u, int v) {
                                                                                                  int next = matched[adj];
        int p = lca(u, v);
                                                                                                  if (next >= 0 && level[next] != level[nod] + 1) continue;
                                                                                                  if (next == -1 || findpath(next)) {
        return subquery(u, p) + subquery(v, p) - query(flatpos[p], flatpos[p]);
                                                                                                      match[nod] = adj;
};
                                                                                                     matched[adj] = nod;
                                                                                                     return 1;
                                                                                                 }
      Bipartite Matching (Hopcroft-Karp)
                                                                                              return 0;
                                                                                         }
// in: n, m, graph
// out: match, matched
                                                                                         int solve() {
// vertex cover: (reached[0][left node] == 0) || (reached[1][right node] == 1)
                                                                                              int ans = 0;
// 0(E*sqrt(V))
                                                                                              while (assignLevel()) {
struct BipartiteMatching {
                                                                                                  edgeview.assign(n, 0);
    int n, m;
                                                                                                  for (int i = 0; i < n; i++)
    vector<vector<int>> graph;
                                                                                                      if (match[i] == -1)
    vector<int> matched, match, edgeview, level;
```

ans += findpath(i);

```
}
        return ans;
};
     Maximum Flow (Dinic)
// usage:
// MaxFlowDinic::init(n);
// MaxFlowDinic::add_edge(0, 1, 100, 100); // for bidirectional edge
// MaxFlowDinic::add edge(1, 2, 100); // directional edge
// result = MaxFlowDinic::solve(0, 2); // source -> sink
// graph[i][edgeIndex].res -> residual
//
// in order to find out the minimum cut, use `l'.
// if l[i] == 0, i is unrechable.
//
// O(V*V*E)
// with unit capacities, O(min(V^{(2/3)}, E^{(1/2)}) * E)
struct MaxFlowDinic {
    typedef int flow t;
    struct Edge {
        int next;
        size t inv; /* inverse edge index */
        flow t res; /* residual */
    };
    int n;
    vector<vector<Edge>> graph;
    vector<int> q, l, start;
    void init(int _n) {
        n = n;
        graph.resize(n);
        for (int i = 0; i < n; i++) graph[i].clear();</pre>
    void add_edge(int s, int e, flow_t cap, flow_t caprev = 0) {
        Edge forward{ e, graph[e].size(), cap };
        Edge reverse{ s, graph[s].size(), caprev };
        graph[s].push back(forward);
        graph[e].push back(reverse);
    bool assign_level(int source, int sink) {
        int t = 0;
        memset(&l[0], 0, sizeof(l[0]) * l.size());
        1[source] = 1;
        q[t++] = source;
        for (int h = 0; h < t && !1[sink]; h++) {</pre>
            int cur = q[h];
            for (const auto& e : graph[cur]) {
                if (l[e.next] || e.res == 0) continue;
                l[e.next] = l[cur] + 1;
                q[t++] = e.next;
            }
```

```
return 1[sink] != 0;
    flow t block flow(int cur, int sink, flow t current) {
        if (cur == sink) return current;
        for (int& i = start[cur]; i < graph[cur].size(); i++) {</pre>
            auto& e = graph[cur][i];
            if (e.res == 0 || l[e.next] != l[cur] + 1) continue;
            if (flow t res = block flow(e.next, sink, min(e.res, current))) {
                e.res -= res;
                graph[e.next][e.inv].res += res;
                return res;
            }
        return 0;
    flow t solve(int source, int sink) {
        a.resize(n);
        1.resize(n);
        start.resize(n);
        flow_t ans = 0;
        while (assign level(source, sink)) {
            memset(&start[0], 0, sizeof(start[0]) * n);
            while (flow t flow = block flow(source, sink, numeric limits<flow t
              >::max()))
                ans += flow;
        }
        return ans;
};
```

5.10 Maximum Flow with Edge Demands

그래프 G=(V,E) 가 있고 source s와 sink t가 있다. 각 간선마다 $d(e) \leq f(e) \leq c(e)$ 를 만족하도록 flow f(e)를 흘려야 한다. 이 때의 maximum flow를 구하는 문제다.

먼저 모든 demand를 합한 값 D를 아래와 같이 정의한다.

$$D = \sum_{(u \to v) \in E} d(u \to v)$$

이제 G 에 몇개의 정점과 간선을 추가하여 새로운 그래프 G'=(V',E') 을 만들 것이다. 먼저 새로운 source s' 과 새로운 sink t' 을 추가한다. 그리고 s' 에서 V의 모든 점마다 간선을 이어주고, V의 모든 점에서 t'로 간선을 이어준다.

새로운 capacity function c'을 아래와 같이 정의한다.

- 1. V의 점 v에 대해 $c'(s' \to v) = \sum_{u \in V} d(u \to v)$, $c'(v \to t') = \sum_{w \in V} d(v \to w)$
- 2. E의 간선 $u \to v$ 에 대해 $c'(u \to v) = c(u \to v) d(u \to v)$
- 3. $c'(t \to s) = \infty$

이렇게 만든 새로운 그래프 G'에서 $\max flow$ 를 구했을 때 그 값이 D라면 원래 문제의 해가 존재하고, 그 값이 D가 아니라면 원래 문제의 해는 존재하지 않는다.

위에서 maximum flow를 구하고 난 상태의 residual graph 에서 s'과 t'을 떼버리고 s에서 t사이의 augument path 를 계속 찾으면 원래 문제의 해를 구할 수 있다.

5.10.1 Source Code

```
struct MaxFlowEdgeDemands
    MaxFlowDinic mf;
   using flow_t = MaxFlowDinic::flow_t;
    vector<flow t> ind, outd;
    flow_t D; int n;
    void init(int _n) {
        n = _n; D = 0; mf.init(n + 2);
        ind.clear(); outd.clear();
        ind.resize(n, 0); outd.resize(n, 0);
   }
    void add_edge(int s, int e, flow_t cap, flow_t demands = 0) {
        mf.add edge(s, e, cap - demands);
        D += demands; ind[e] += demands; outd[s] += demands;
   }
   // returns { false, 0 } if infeasible
   // { true, maxflow } if feasible
    pair<bool, flow t> solve(int source, int sink) {
        mf.add_edge(sink, source, numeric_limits<flow_t>::max());
        for (int i = 0; i < n; i++) {
            if (ind[i]) mf.add_edge(n, i, ind[i]);
            if (outd[i]) mf.add edge(i, n + 1, outd[i]);
        }
       if (mf.solve(n, n + 1) != D) return{ false, 0 };
        for (int i = 0; i < n; i++) {
            if (ind[i]) mf.graph[i].pop_back();
            if (outd[i]) mf.graph[i].pop back();
        return{ true, mf.solve(source, sink) };
};
```

5.11 Min-cost Maximum Flow

```
// precondition: there is no negative cycle.
// usage:
```

```
// MinCostFlow mcf(n);
// for(each edges) mcf.addEdge(from, to, cost, capacity);
// mcf.solve(source, sink); // min cost max flow
// mcf.solve(source, sink, 0); // min cost flow
// mcf.solve(source, sink, goal_flow); // min cost flow with total_flow >=
 goal flow if possible
struct MinCostFlow {
    typedef int cap_t;
    typedef int cost t;
    bool iszerocap(cap t cap) { return cap == 0; }
    struct edge {
        int target;
        cost_t cost;
        cap_t residual_capacity;
        cap t orig capacity;
        size_t revid;
    };
    int n;
    vector<vector<edge>> graph;
    MinCostFlow(int n) : graph(n), n(n) {}
    void addEdge(int s, int e, cost_t cost, cap_t cap) {
        if (s == e) return;
        edge forward{ e, cost, cap, cap, graph[e].size() };
        edge backward{ s, -cost, 0, 0, graph[s].size() };
        graph[s].emplace back(forward);
        graph[e].emplace back(backward);
    pair<cost_t, cap_t> augmentShortest(int s, int e, cap_t flow_limit) {
        auto infinite cost = numeric limits<cost t>::max();
        auto infinite flow = numeric limits<cap t>::max();
        vector<pair<cost_t, cap_t>> dist(n, make_pair(infinite_cost, 0));
        vector<int> from(n, -1), v(n);
        dist[s] = pair<cost_t, cap_t>(0, infinite_flow);
        queue<int> q;
        v[s] = 1; q.push(s);
        while(!q.empty()) {
            int cur = q.front();
            v[cur] = 0; q.pop();
            for (const auto& e : graph[cur]) {
                if (iszerocap(e.residual_capacity)) continue;
                auto next = e.target;
                auto ncost = dist[cur].first + e.cost;
                auto nflow = min(dist[cur].second, e.residual_capacity);
                if (dist[next].first > ncost) {
                    dist[next] = make pair(ncost, nflow);
                    from[next] = e.revid;
                    if (v[next]) continue;
                    v[next] = 1; q.push(next);
```

```
}
        auto p = e;
        auto pathcost = dist[p].first;
        auto flow = dist[p].second;
        if (iszerocap(flow)|| (flow_limit <= 0 && pathcost >= 0)) return pair
         cost t, cap t>(0, 0);
        if (flow_limit > 0) flow = min(flow, flow_limit);
        while (from[p] != -1) {
            auto nedge = from[p];
            auto np = graph[p][nedge].target;
            auto fedge = graph[p][nedge].revid;
            graph[p][nedge].residual_capacity += flow;
            graph[np][fedge].residual capacity -= flow;
            p = np;
        return make pair(pathcost * flow, flow);
    }
    pair<cost_t,cap_t> solve(int s, int e, cap_t flow_minimum = numeric_limits
      cap t>::max()) {
        cost t total cost = 0;
        cap_t total_flow = 0;
        for(;;) {
            auto res = augmentShortest(s, e, flow minimum - total flow);
            if (res.second <= 0) break;</pre>
            total cost += res.first;
            total flow += res.second;
        return make pair(total cost, total flow);
};
5.12 General Min-cut (Stoer-Wagner)
// implementation of Stoer-Wagner algorithm
// O(V^3)
//usage
// MinCut mc;
// mc.init(n);
// for (each edge) mc.addEdge(a,b,weight);
// mincut = mc.solve();
// mc.cut = \{0,1\}^n describing which side the vertex belongs to.
struct MinCutMatrix
    typedef int cap t;
    int n;
    vector<vector<cap_t>> graph;
    void init(int _n) {
        n = _n;
```

```
graph = vector<vector<cap_t>>(n, vector<cap_t>(n, 0));
void addEdge(int a, int b, cap t w) {
    if (a == b) return;
    graph[a][b] += w;
    graph[b][a] += w;
pair<cap t, pair<int, int>> stMinCut(vector<int> &active) {
    vector<cap_t> key(n);
    vector<int> v(n);
    int s = -1, t = -1;
    for (int i = 0; i < active.size(); i++) {</pre>
        cap_t maxv = -1;
        int cur = -1;
        for (auto j : active) {
            if (v[j] == 0 \&\& maxv < key[j]) {
                maxv = key[j];
                cur = j;
        t = s; s = cur;
        v[cur] = 1;
        for (auto j : active) key[j] += graph[cur][j];
    return make_pair(key[s], make_pair(s, t));
}
vector<int> cut;
cap_t solve() {
    cap_t res = numeric_limits<cap_t>::max();
    vector<vector<int>> grps;
    vector<int> active;
    cut.resize(n);
    for (int i = 0; i < n; i++) grps.emplace_back(1, i);</pre>
    for (int i = 0; i < n; i++) active.push_back(i);</pre>
    while (active.size() >= 2) {
        auto stcut = stMinCut(active);
        if (stcut.first < res) {</pre>
            res = stcut.first;
            fill(cut.begin(), cut.end(), 0);
            for (auto v : grps[stcut.second.first]) cut[v] = 1;
        }
        int s = stcut.second.first, t = stcut.second.second;
        if (grps[s].size() < grps[t].size()) swap(s, t);</pre>
        active.erase(find(active.begin(), active.end(), t));
        grps[s].insert(grps[s].end(), grps[t].begin(), grps[t].end());
        for (int i = 0; i < n; i++) { graph[i][s] += graph[i][t]; graph[i][t</pre>
        for (int i = 0; i < n; i++) { graph[s][i] += graph[t][i]; graph[t][i</pre>
          1 = 0;
        graph[s][s] = 0;
```

```
}
return res;
}
```

5.13 Hungarian Algorithm

```
int n, m;
int mat[MAX_N + 1][MAX_M + 1];
// hungarian method : bipartite min-weighted matching
// O(n^3) or O(m*n^2)
// http://e-maxx.ru/algo/assignment hungary
// mat[1][1] ~ mat[n][m]
// matched[i] : matched column of row i
int hungarian(vector<int>& matched) {
    vector<int> u(n + 1), v(m + 1), p(m + 1), way(m + 1), minv(m + 1);
    vector<char> used(m + 1);
    for (int i = 1; i <= n; ++i) {
        p[0] = i;
        int j0 = 0;
        fill(minv.begin(), minv.end(), INF);
        fill(used.begin(), used.end(), false);
        do {
            used[j0] = true;
            int i0 = p[j0], delta = INF, j1;
            for (int j = 1; j <= m; ++j) {
                if (!used[j]) {
                    int cur = mat[i0][j] - u[i0] - v[j];
                    if (cur < minv[j]) minv[j] = cur, way[j] = j0;</pre>
                    if (minv[j] < delta) delta = minv[j], j1 = j;</pre>
                }
            for (int j = 0; j <= m; ++j) {
                if (used[i])
                    u[p[j]] += delta, v[j] -= delta;
                    minv[j] -= delta;
            j0 = j1;
        } while (p[j0] != 0);
        do {
            int j1 = way[j0];
            p[j0] = p[j1];
            j0 = j1;
        } while (j0);
    for (int j = 1; j <= m; ++j) matched[p[j]] = j;</pre>
    return -v[0];
}
```

6 Geometry

6.1 Basic Operations

```
const double eps = 1e-9;
inline int diff(double lhs, double rhs) {
    if (lhs - eps < rhs && rhs < lhs + eps) return 0;</pre>
    return (lhs < rhs) ? -1 : 1;</pre>
}
inline bool is_between(double check, double a, double b) {
    if (a < b)
        return (a - eps < check && check < b + eps);</pre>
    else
        return (b - eps < check && check < a + eps);</pre>
}
struct Point {
    double x, v;
    bool operator==(const Point& rhs) const {
        return diff(x, rhs.x) == 0 && diff(y, rhs.y) == 0;
    Point operator+(const Point& rhs) const {
        return Point{ x + rhs.x, y + rhs.y };
    Point operator-(const Point& rhs) const {
        return Point{ x - rhs.x, y - rhs.y };
    Point operator*(double t) const {
        return Point{ x * t, y * t };
};
struct Circle {
    Point center;
    double r;
};
struct Line {
    Point pos, dir;
};
inline double inner(const Point& a, const Point& b) {
    return a.x * b.x + a.y * b.y;
inline double outer(const Point& a, const Point& b) {
    return a.x * b.y - a.y * b.x;
inline int ccw_line(const Line& line, const Point& point) {
    return diff(outer(line.dir, point - line.pos), 0);
```

```
}
                                                                                    }
inline int ccw(const Point& a, const Point& b, const Point& c) {
                                                                                    vector<Point> circle line(const Circle& circle, const Line& line) {
   return diff(outer(b - a, c - a), 0);
                                                                                         vector<Point> result:
                                                                                         double a = 2 * inner(line.dir, line.dir);
                                                                                         double b = 2 * (line.dir.x * (line.pos.x - circle.center.x)
                                                                                             + line.dir.y * (line.pos.y - circle.center.y));
inline double dist(const Point& a, const Point& b) {
    return sqrt(inner(a - b, a - b));
                                                                                         double c = inner(line.pos - circle.center, line.pos - circle.center)
                                                                                             - circle.r * circle.r;
                                                                                         double det = b * b - 2 * a * c;
inline double dist2(const Point &a, const Point &b) {
                                                                                         int pred = diff(det, 0);
    return inner(a - b, a - b);
                                                                                         if (pred == 0)
}
                                                                                             result.push back(line.pos + line.dir * (-b / a));
                                                                                         else if (pred > 0) {
inline double dist(const Line& line, const Point& point, bool segment = false) {
                                                                                             det = sqrt(det);
    double c1 = inner(point - line.pos, line.dir);
                                                                                             result.push back(line.pos + line.dir * ((-b + det) / a));
    if (segment && diff(c1, 0) <= 0) return dist(line.pos, point);</pre>
                                                                                             result.push back(line.pos + line.dir * ((-b - det) / a));
    double c2 = inner(line.dir, line.dir);
   if (segment && diff(c2, c1) <= 0) return dist(line.pos + line.dir, point);</pre>
                                                                                         return result:
   return dist(line.pos + line.dir * (c1 / c2), point);
}
                                                                                     vector<Point> circle circle(const Circle& a, const Circle& b) {
bool get_cross(const Line& a, const Line& b, Point& ret) {
                                                                                         vector<Point> result;
                                                                                         int pred = diff(dist(a.center, b.center), a.r + b.r);
    double mdet = outer(b.dir, a.dir);
   if (diff(mdet, 0) == 0) return false;
                                                                                         if (pred > 0) return result;
    double t2 = outer(a.dir, b.pos - a.pos) / mdet;
                                                                                         if (pred == 0) {
                                                                                             result.push back((a.center * b.r + b.center * a.r) * (1 / (a.r + b.r)));
    ret = b.pos + b.dir * t2;
    return true;
                                                                                             return result:
}
                                                                                         double aa = a.center.x * a.center.x + a.center.y * a.center.y - a.r * a.r;
bool get_segment_cross(const Line& a, const Line& b, Point& ret) {
                                                                                         double bb = b.center.x * b.center.x + b.center.y * b.center.y - b.r * b.r;
    double mdet = outer(b.dir, a.dir);
                                                                                         double tmp = (bb - aa) / 2.0;
    if (diff(mdet, 0) == 0) return false;
                                                                                         Point cdiff = b.center - a.center;
    double t1 = -outer(b.pos - a.pos, b.dir) / mdet;
                                                                                         if (diff(cdiff.x, 0) == 0) {
    double t2 = outer(a.dir, b.pos - a.pos) / mdet;
                                                                                             if (diff(cdiff.y, 0) == 0)
    if (!is_between(t1, 0, 1) || !is_between(t2, 0, 1)) return false;
                                                                                                 return result; // if (diff(a.r, b.r) == 0): same circle
    ret = b.pos + b.dir * t2;
                                                                                             return circle_line(a, Line{ Point{ 0, tmp / cdiff.y }, Point{ 1, 0 } });
   return true;
                                                                                         return circle_line(a,
                                                                                             Line{ Point{ tmp / cdiff.x, 0 }, Point{ -cdiff.y, cdiff.x } });
Point inner center(const Point &a, const Point &b, const Point &c) {
                                                                                    }
    double wa = dist(b, c), wb = dist(c, a), wc = dist(a, b);
                                                                                     Circle circle_from_3pts(const Point& a, const Point& b, const Point& c) {
   double w = wa + wb + wc;
   return Point{ (wa * a.x + wb * b.x + wc * c.x) / w, (wa * a.y + wb * b.y +
                                                                                         Point ba = b - a, cb = c - b;
                                                                                         Line p{ (a + b) * 0.5, Point{ ba.y, -ba.x } };
     wc * c.y) / w };
}
                                                                                         Line q\{(b + c) * 0.5, Point\{cb.y, -cb.x\}\};
                                                                                         Circle circle;
Point outer center(const Point &a, const Point &b, const Point &c) {
                                                                                         if (!get_cross(p, q, circle.center))
   Point d1 = b - a, d2 = c - a;
                                                                                             circle.r = -1:
    double area = outer(d1, d2);
                                                                                         else
    double dx = d1.x * d1.x * d2.y - d2.x * d2.x * d1.y
                                                                                             circle.r = dist(circle.center, a);
        + d1.y * d2.y * (d1.y - d2.y);
                                                                                         return circle;
    double dy = d1.y * d1.y * d2.x - d2.y * d2.y * d1.x
                                                                                    }
        + d1.x * d2.x * (d1.x - d2.y);
    return Point{ a.x + dx / area / 2.0, a.y - dy / area / 2.0 };
                                                                                    Circle circle_from_2pts_rad(const Point& a, const Point& b, double r) {
```

```
double det = r * r / dist2(a, b) - 0.25;
Circle circle;
if (det < 0)
    circle.r = -1;
else {
    double h = sqrt(det);
    // center is to the left of a->b
    circle.center = (a + b) * 0.5 + Point{ a.y - b.y, b.x - a.x } * h;
    circle.r = r;
}
return circle;
```

6.2 Compare angles

6.3 Convex Hull

}

```
// find convex hull
// O(n*Logn)
vector<Point> convex_hull(vector<Point>& dat) {
    if (dat.size() <= 3) return dat;</pre>
    vector<Point> upper, lower;
    sort(dat.begin(), dat.end(), [](const Point& a, const Point& b) {
        return (a.x == b.x)? a.y < b.y: a.x < b.x;
   });
    for (const auto& p : dat) {
        while (upper.size() >= 2 && ccw(*++upper.rbegin(), *upper.rbegin(), p)
         >= 0) upper.pop_back();
        while (lower.size() >= 2 && ccw(*++lower.rbegin(), *lower.rbegin(), p)
          <= 0) lower.pop back();
        upper.emplace_back(p);
        lower.emplace back(p);
    upper.insert(upper.end(), ++lower.rbegin(), --lower.rend());
    return upper;
}
```

6.4 Rotating Calipers

6.5 Point in Polygon Test

```
typedef double coord_t;
inline coord_t is_left(Point p0, Point p1, Point p2) {
    return (p1.x - p0.x) * (p2.y - p0.y) - (p2.x - p0.x) * (p1.y - p0.y);
// point in polygon test
// http://geomalgorithms.com/a03- inclusion.html
bool is_in_polygon(Point p, vector<Point>& poly) {
    int wn = 0;
    for (int i = 0; i < poly.size(); ++i) {</pre>
        int ni = (i + 1 == poly.size()) ? 0 : i + 1;
        if (poly[i].y <= p.y) {</pre>
            if (poly[ni].y > p.y) {
                 if (is_left(poly[i], poly[ni], p) > 0) {
                     ++wn;
            }
        else {
            if (poly[ni].y <= p.y) {</pre>
                 if (is_left(poly[i], poly[ni], p) < 0) {</pre>
                     --wn;
            }
    return wn != 0;
```

6.6 Polygon Cut

```
// left side of a->b
vector<Point> cut_polygon(const vector<Point>& polygon, Line line) {
    if (!polygon.size()) return polygon;
    typedef vector<Point>::const_iterator piter;
    piter la, lan, fi, fip, i, j;
    la = lan = fi = fip = polygon.end();
   i = polygon.end() - 1;
   bool lastin = diff(ccw_line(line, polygon[polygon.size() - 1]), 0) > 0;
    for (j = polygon.begin(); j != polygon.end(); j++) {
        bool thisin = diff(ccw_line(line, *j), 0) > 0;
        if (lastin && !thisin) {
            la = i;
            lan = j;
       if (!lastin && thisin) {
           fi = j;
            fip = i;
       i = j;
       lastin = thisin;
    if (fi == polygon.end()) {
        if (!lastin) return vector<Point>();
        return polygon;
   }
    vector<Point> result;
    for (i = fi ; i != lan ; i++) {
       if (i == polygon.end()) {
           i = polygon.begin();
            if (i == lan) break;
        result.push back(*i);
    Point lc, fc;
    get_cross(Line{ *la, *lan - *la }, line, lc);
    get_cross(Line{ *fip, *fi - *fip }, line, fc);
    result.push_back(lc);
    if (diff(dist2(lc, fc), 0) != 0) result.push back(fc);
    return result;
}
```

6.7 Pick's theorem

격자점으로 구성된 simple polygon이 주어짐. i는 polygon 내부의 격자점 수, b는 polygon 선분 위 격자점 수, A는 polygon의 넓이라고 할 때, 다음과 같은 식이 성립한다.

$$A = i + \frac{b}{2} - 1$$

7 String

7.1 KMP

```
typedef vector<int> seq_t;
void calculate pi(vector<int>& pi, const seq t& str) {
    pi[0] = -1;
    for (int i = 1, j = -1; i < str.size(); i++) {
        while (j >= 0 && str[i] != str[j + 1]) j = pi[j];
        if (str[i] == str[j + 1])
            pi[i] = ++j;
        else
            pi[i] = -1;
    }
}
// returns all positions matched
// 0(|text|+|pattern|)
vector<int> kmp(const seq_t& text, const seq_t& pattern) {
    vector<int> pi(pattern.size()), ans;
    if (pattern.size() == 0) return ans;
    calculate pi(pi, pattern);
    for (int i = 0, j = -1; i < text.size(); i++) {</pre>
        while (j >= 0 && text[i] != pattern[j + 1]) j = pi[j];
        if (text[i] == pattern[j + 1]) {
            j++;
            if (j + 1 == pattern.size()) {
                ans.push_back(i - j);
                j = pi[j];
            }
    }
    return ans;
}
```

7.2 Z Algorithm

```
// Z[i] : maximum common prefix length of &s[0] and &s[i]
// O(|s|)
using seq_t = string;
vector<int> z_func(const seq_t &s) {
    vector<int> z(s.size());
    z[0] = s.size();
    int l = 0, r = 0;

for (int i = 1; i < s.size(); i++) {
        if (i > r) {
            int j;
            for (j = 0; i + j < s.size() && s[i + j] == s[j]; j++) ;
            z[i] = j; l = i; r = i + j - 1;
        } else if (z[i - l] < r - i + 1) {</pre>
```

maxid = max(maxid, id);

vector<char> visit(dfa.size());

auto cur = q.front(); q.pop();

dfa[cur].output_link = dfa[cur].back; if (dfa[dfa[cur].back].report.empty())

void build() {

queue<int> q;

visit[0] = 1;q.push(0);

while(!q.empty()) {

```
z[i] = z[i - 1];
       } else {
           int j;
           for (j = 1; r + j < s.size() && s[r + j] == s[r - i + j]; j++);
           z[i] = r - i + j; l = i; r += j - 1;
   }
   return z;
     Aho-Corasick
#include <algorithm>
#include <vector>
#include <queue>
using namespace std;
struct AhoCorasick
   const int alphabet;
   struct node {
        node() {}
        explicit node(int alphabet) : next(alphabet) {}
       vector<int> next, report;
        int back = 0, output_link = 0;
   };
   int maxid = 0;
   vector<node> dfa;
   explicit AhoCorasick(int alphabet) : alphabet(alphabet), dfa(1, node(
   template<typename InIt, typename Fn> void add(int id, InIt first, InIt last,
      Fn func) {
       int cur = 0;
        for ( ; first != last; ++first) {
            auto s = func(*first);
           if (auto next = dfa[cur].next[s]) cur = next;
            else {
                cur = dfa[cur].next[s] = (int)dfa.size();
                dfa.emplace_back(alphabet);
           }
       }
        dfa[cur].report.push_back(id);
```

```
dfa[cur].output_link = dfa[dfa[cur].back].output_link;
            for (int s = 0; s < alphabet; s++) {</pre>
                auto &next = dfa[cur].next[s];
                if (next == 0) next = dfa[dfa[cur].back].next[s];
                if (visit[next]) continue;
                if (cur) dfa[next].back = dfa[dfa[cur].back].next[s];
                visit[next] = 1;
                q.push(next);
            }
    template<typename InIt, typename Fn> vector<int> countMatch(InIt first, InIt
      last, Fn func) {
        int cur = 0;
        vector<int> ret(maxid+1);
        for (; first != last; ++first) {
            cur = dfa[cur].next[func(*first)];
            for (int p = cur; p; p = dfa[p].output_link)
                for (auto id : dfa[p].report) ret[id]++;
        return ret;
};
7.4 Suffix Array with LCP
typedef char T;
```

```
// calculates suffix array.
// O(n*logn)
vector<int> suffix array(const vector<T>& in) {
   int n = (int)in.size(), c = 0;
   vector<int> temp(n), pos2bckt(n), bckt(n), bpos(n), out(n);
   for (int i = 0; i < n; i++) out[i] = i;
    sort(out.begin(), out.end(), [&](int a, int b) { return in[a] < in[b]; });</pre>
   for (int i = 0; i < n; i++) {
       bckt[i] = c;
       if (i + 1 == n || in[out[i]] != in[out[i + 1]]) c++;
   for (int h = 1; h < n && c < n; h <<= 1) {
       for (int i = 0; i < n; i++) pos2bckt[out[i]] = bckt[i];</pre>
       for (int i = n - 1; i >= 0; i--) bpos[bckt[i]] = i;
       for (int i = 0; i < n; i++)
           if (out[i] >= n - h) temp[bpos[bckt[i]]++] = out[i];
       for (int i = 0; i < n; i++)
           if (out[i] >= h) temp[bpos[pos2bckt[out[i] - h]]++] = out[i] - h;
       for (int i = 0; i + 1 < n; i++) {
           int a = (bckt[i] != bckt[i + 1]) || (temp[i] >= n - h)
                   bckt[i] = c;
           c += a:
       bckt[n - 1] = c++;
```

```
temp.swap(out);
    return out;
}
// calculates lcp array. it needs suffix array & original sequence.
vector<int> lcp(const vector<T>& in, const vector<int>& sa) {
    int n = (int)in.size();
    if (n == 0) return vector<int>();
    vector<int> rank(n), height(n - 1);
    for (int i = 0; i < n; i++) rank[sa[i]] = i;</pre>
    for (int i = 0, h = 0; i < n; i++) {
        if (rank[i] == 0) continue;
        int j = sa[rank[i] - 1];
        while (i + h < n \& j + h < n \& in[i + h] == in[j + h]) h++;
        height[rank[i] - 1] = h;
        if (h > 0) h--;
   }
    return height;
}
```

7.5 Suffix Tree

7.6 Manacher's Algorithm

8 Miscellaneous

8.1 Fast I/O

```
namespace fio {
    const int BSIZE = 524288;
    char buffer[BSIZE];
    int p = BSIZE;
    inline char readChar() {
        if(p == BSIZE) {
            fread(buffer, 1, BSIZE, stdin);
            p = 0;
        return buffer[p++];
    }
    int readInt() {
        char c = readChar();
        while ((c < '0' | c > '9') \& c != '-') {
            c = readChar();
        int ret = 0; bool neg = c == '-';
        if (neg) c = readChar();
        while (c >= '0' && c <= '9') {
            ret = ret * 10 + c - '0';
            c = readChar();
        return neg ? -ret : ret;
}
```

8.2 Magic Numbers

소수: 10007, 10009, 10111, 31567, 70001, 1000003, 1000033, 4000037, 99999989, 9999997, 1000000007, 1000000009, 999999967, 999999977

8.3 Java Examples

8.4 체계적인 접근을 위한 질문들

"알고리즘 문제 해결 전략" 에서 발췌함

- 비슷한 문제를 풀어본 적이 있던가?
- 단순한 방법에서 시작할 수 있을까? (brute force)
- 내가 문제를 푸는 과정을 수식화할 수 있을까? (예제를 직접 해결해보면서)
- 문제를 단순화할 수 없을까?
- 그림으로 그려볼 수 있을까?
- 수식으로 표현할 수 있을까?
- 문제를 분해할 수 있을까?
- 뒤에서부터 생각해서 문제를 풀 수 있을까?
- 순서를 강제할 수 있을까?
- 특정 형태의 답만을 고려할 수 있을까? (정규화)