

Project report

Algorithm 1

Group 1

1. Name

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2. Pseudocode

Problem : To find the minimum swaps needed to seat n couples together in a row of $2n$ seats, where couples are defined by consecutive IDs like $(0, 1)$, $(2, 3)$, etc.

Inputs:

- An array row with a length of $2n$, where n is the number of couples.
- $row[i]$ represents the ID of the person sitting in the i th seat.
- Couples are represented as $(2k, 2k+1)$, where k is the index of each couple.

Outputs:

- The minimum number of swaps required to make every couple sit next to each other (integer value).

Constraints and Assumptions:

- The array row has a length of $2n$ (even number), where n is the number of couples.
- IDs range from 0 to $2n-1$ and each ID appears exactly once in the array.
- Couples are defined as consecutive pairs: $(0, 1)$, $(2, 3)$, and so on.
- A swap involves exchanging two people in the array.

Pseudocode :

```
function minSwapsCouples(row):
```

```
n = length of row / 2
couple_map = {}
swaps = 0
```

```
couple_map[row[i]] = i
```

```
for i from 0 to length of row step 2:
```

```
    first_person = row[i]
```

```
    second_person = row[i + 1]
```

```
    couple_id = first_person ^ 1
```

```
    if second_person != couple_id:
```

```
        swaps += 1
```

```
        swap_pos = couple_map[couple_id]
```

```
        row[i + 1], row[swap_pos] = row[swap_pos], row[i + 1]
```

```
    couple_map[second_person] = swap_pos
```

```
    couple_map[couple_id] = i + 1
```

```
return swaps
```

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        if second_person != couple_id:
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            swaps += 1
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```
            swap_pos = couple_map[couple_id]
```

```
            row[i + 1], row[swap_pos] = row[swap_pos], row[i + 1]
```

```
couple_map[second_person] = swap_pos  
couple_map[couple_id] = i + 1
```

```
return swaps
```

3. Proving efficiency of the pseudocode

Time complexity

1. $O(n)$ - this loop goes through the row of length n where n is the number of people.
2. $O(n)$ - this loop goes through row in 2 steps, meaning $n/2$, but since the operation loop is the constant time, it becomes $O(n/2)$ simplifies to $O(n)$
3. $O(n) + O(n) = O(n)$ - combining both steps

Space Complexity

1. $O(2n) = O(n)$ - couple_map stores each person and their index, using space proportional to the number of people in the row
2. $O(n)$

Time complexity: $O(n)$

Space Complexity: $O(n)$