

and

$$P_{k+1} = P_k + \Delta y$$

Otherwise The next point to plot is
 (x_{k+1}, y_{k+1}) . And

$$P_{k+1} = P_k + 2\Delta y - 2\Delta x$$

5) Repeat step 4 or $(\Delta x - 1)$ times.

The Bresenham Line Algorithm has the following advantages.

- An fast Incremental Algorithm
- use only Integer Calculation

Comparison:- DDA has following problem

- 1) Accumulation of round off error can make the pixel line drift away from what was intended.
- 2) The Rounding operation and floating point arithmetic are time consuming.


```

printf ("Enter the value of Y1 : ");
scanf ("%f", &Y1);
printf ("Enter the value of X2 : ");
scanf ("%f", &X2);
printf ("Enter the value of Y2 : ");
scanf ("%f", &Y2);

```

detectgraph (Eqd, Eqm);

initgraph (Eqd, Eqm, "");

$dx = abs(X2 - X1);$

$dy = abs(Y2 - Y1);$

if ($dx \geq dy$)

pixel = dx;

else

pixel = dy;

$dx = dx / pixel;$

$dy = dy / pixel;$

$x = X1;$

$y = Y1;$

$i = 1;$

while ($i \leq pixel$)

putpixel (x, y, 1);

$x = x + dx;$

$y = y + dy;$

$i = i + 1;$

delay (100);

} getch();

closegraph();

$f(n) = ?$ which give less error
 $f(s) = ?$ selected

Date: _____ Page no: _____
 $(x+1, y_k)$
 $(x+1, y_{k-1})$
 $x^2 + y^2 - r^2$
 $f(x, y) = x^2 + y^2 - r^2$

Bresenham's circle drawing algorithm

$$d = 3 - 2y$$

$(x+1, y_k)$

$$\boxed{d \leq 0}$$

$$d = d + 4x_{k+1} + 6$$

$$(x_{k+1}, y_{k+1}) \quad d > 0 \quad d = d + 4(x_{k+1} - y_{k+1}) + 10$$

If $R=3$

$$d = 3 - 2(3)$$

$$d = 3 - 6$$

$$= -3$$

R	D_P	x_{k+1}, y_{k+1}
0	-3	[1, 3]
1	7	(2, 1)

—x—

$$f(N) = (x_i + 1, y_i)$$

$$f(S) = (x_{i+1}, y_{i+1})$$

$$x^2 + y^2 - r^2$$

$$= (x_i + 1)^2 + y_i^2 - r^2$$

$$= (x_i + 1)^2 + (y_{i+1})^2 - r^2$$

decision parameter = $d_i = f(N) + f(S)$

(E) pos SE

1) Inside the circle (-ve) distance

2) outside the circle (+ve).

If $d \leq 0 \Rightarrow$ Point Selected

$$x_{i+1} = x_i + 1$$

$$y_{i+1} = y_i$$

$d > 0 \Rightarrow$ SE point Selected

$$x_{i+1} = x_{i+1}$$

$$y_{i+1} = y_i - 1$$

$$-3 + 4x_1 + 6$$

$$-3 + 10$$

7

$$-2 + 9 \cdot$$

$$= 2(y_{i+1})^2 + y_i^2 + (y_{i-1})^2 - 2R^2$$

$$\Rightarrow 2 + R^2 + (R-1)^2 - 2R^2$$

$$= 3 - 2R$$

CDD :-

automobile assembly
circuit design
simulation of

Presentation of graphics

- (i) 2 D
- (ii) 3 D

Applications :-

- (i) Computer art
- (ii) Entertainment
- (iii) Education and training
- (iv) Visualization
- (v) Image processing
- (vi) Internet
- (vii) Medical applications
- (viii) Simulation and virtual reality
- (ix) Computer aided learning (CAL)
- (x) Geographical information system (GIS)

1) Introduction slide with Book [9:2 pm]

(2)

2) 10/2/24 04:

"Computer graphics is a rapidly evolving field. Until the past two decades,

By graphics we will refer to any sketch, drawing special artwork or other material to pictorially depict an object or process or otherwise convey information as a supplement to or instead of written descriptions the sketch may be cartoon or landscape building electrical network or of the human anatomy.

"It may be just a few regular lines or 2D or 3D drawing.

The graphics may also include text in various sizes and shapes.

"Major use of CGMM is CAD".

Pixel :- in computer graphics, pictures or graphics objects are represented on a collection of discrete picture element called pixels (Picture element).

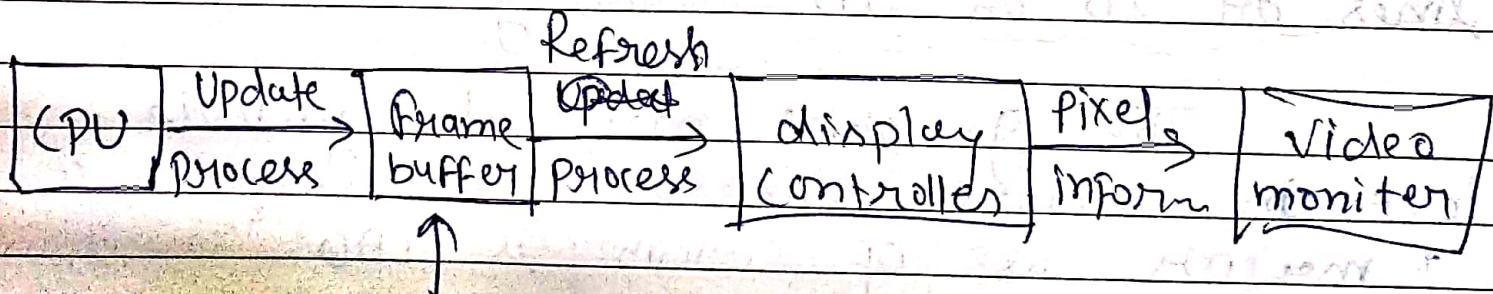
"the pixel is the smallest addressable screen element"

"it is a smallest piece of the display screen which we can control"

the control is achieved by setting the intensity and color of the pixel which compose the screen.

Components of Computer graphics

- (i) Digital memory buffer
- (ii) TV monitor
- (iii) Display controller



Picture definition is stored in a memory

(i) digital memory buffer :-

• picture stored in array
(matrix of 0 and 1)

frame buffer is the video RAM.

amount of memory Required

MB = X-resolution × Y-resolution × Bits
Per Pixel

$$8 \times 1024 \times 1024$$

(ii) TV monitor :- helps to view
the display and they make use
of CRT (cathode Ray tube)

(iii) Display Controller :-

interface betn digital memory
buffer and TV monitor.

The main function of this is to pass the content of frame buffer to the monitor. The display controller reads each successive byte of data from frame buffer memory and converts 0's and 1's into corresponding video signal. Produce black and white picture on the screen.

"Now display controller is recognized as display card 640×480

image resolution :-

Resolution of an image is the number of pixels per unit length in horizontal as well as vertical direction.

image aspect ratio :-

Can be defined as the ratio of its width to its height. unit length / number of pixels.

Persistence :- is defined as the time it takes the emitted light from the screen to decay to one-tenth of its original intensity.

Display Data Devices -

image resolution = ~~height × width~~ (pixel per inch)

image aspect ratio = ~~height~~ / width

image size = ~~height~~ / pixel per inch × width
 (resolution)

Numerical :-

Compute the following

(i) Size of "800 x 600 image" at 240 pixel per inch.

image size = ~~height~~ / resolution × ~~width~~ / resolution

$$800 \times 600 =$$

$$\text{Size} = \frac{800}{240} \times \frac{600}{240}$$

(ii) "Resolution" of 2x2 inch image size that has 512×512 pixels.

$$\text{image size} = \frac{\text{height}}{\text{resolution}} \times \frac{\text{width}}{\text{resolution}}$$

$$2 \times 2 = \frac{512}{\text{resolution}} \times \frac{512}{\text{resolution}}$$

$$\begin{aligned} \text{Resolution} &= \frac{512 \times 512}{2 \times 2} \\ &= \underline{\underline{512}} \end{aligned}$$

(iii) image aspect ratio = $\frac{\text{height}}{\text{width}}$

$$1.5 = \frac{5}{\text{width}}$$

$$\begin{aligned} \text{width} &= 5 \times 1.5 \\ &= 7.5 \end{aligned}$$

(iv)

Display devices :-

The display system where the graphics are rendered in console screen of the computer.

it is responsible for graphic display.

- ① Raster scan display
- ② Random scan display
- ③ Direct view storage tube
- ④ flat panel display

display systems are often referred to as Video monitor or Video display

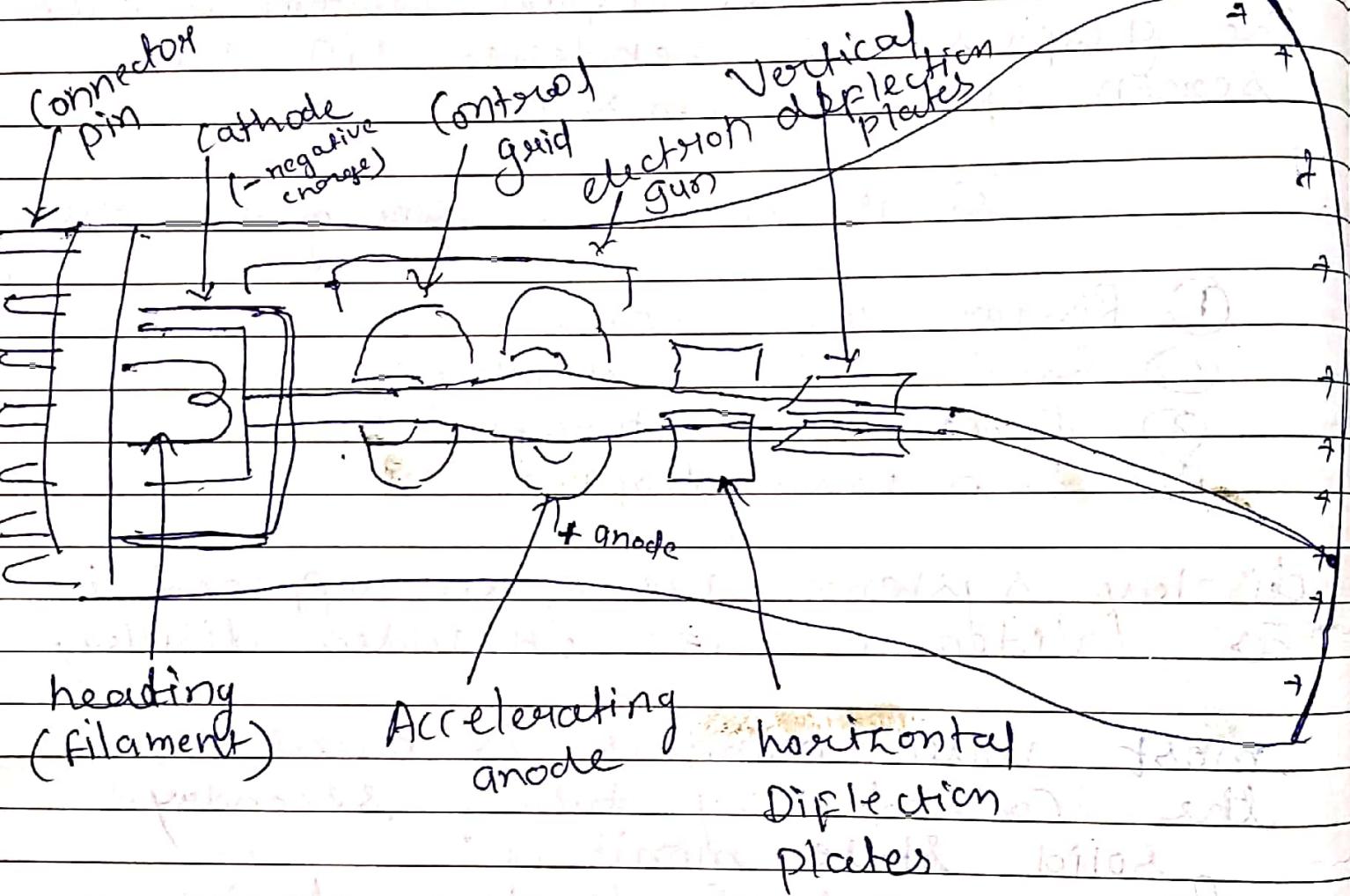
most video monitors is based on the Cathod ray tube. Secondary solid state monitors

Primary output display device video monitor secondary point.



Vaccume inside

phosphor screen



heating (Filament) — heat is supplied to the cathod by directing a current through a coil of wire, called filament. magnetic field is generated.

This causes electrons to be "boiled off" — fully negative charged effect are then accelerate.

Control grid :- intensity of electron beam is controlled by setting voltage level. Control grid architecture.

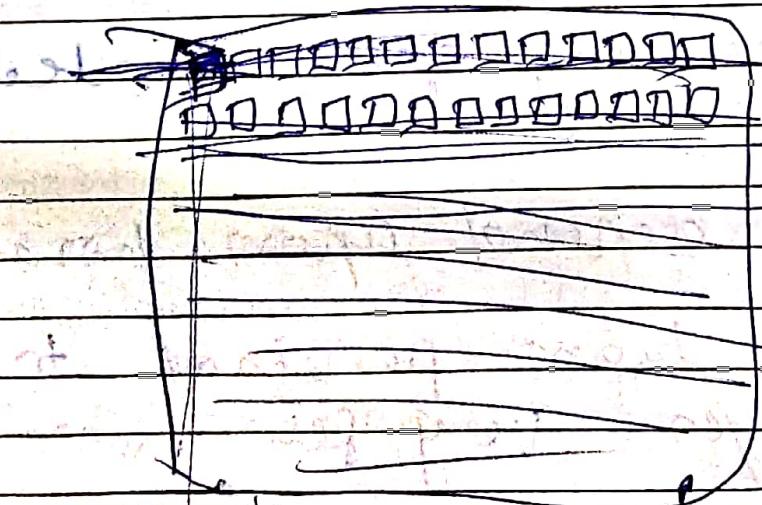
Accelerating anode :- +ve charge gives to focus and ~~retal~~ give a way to go on.

Horizontal deflection plate :-

to right to left

Vertical ~~in~~ up to down.

Refresh CRT :- one way to keep the phosphor glowing is to redraw the picture repeatedly by quickly directing the electron beam back over the same point. this type of display is called a Refresh CRT



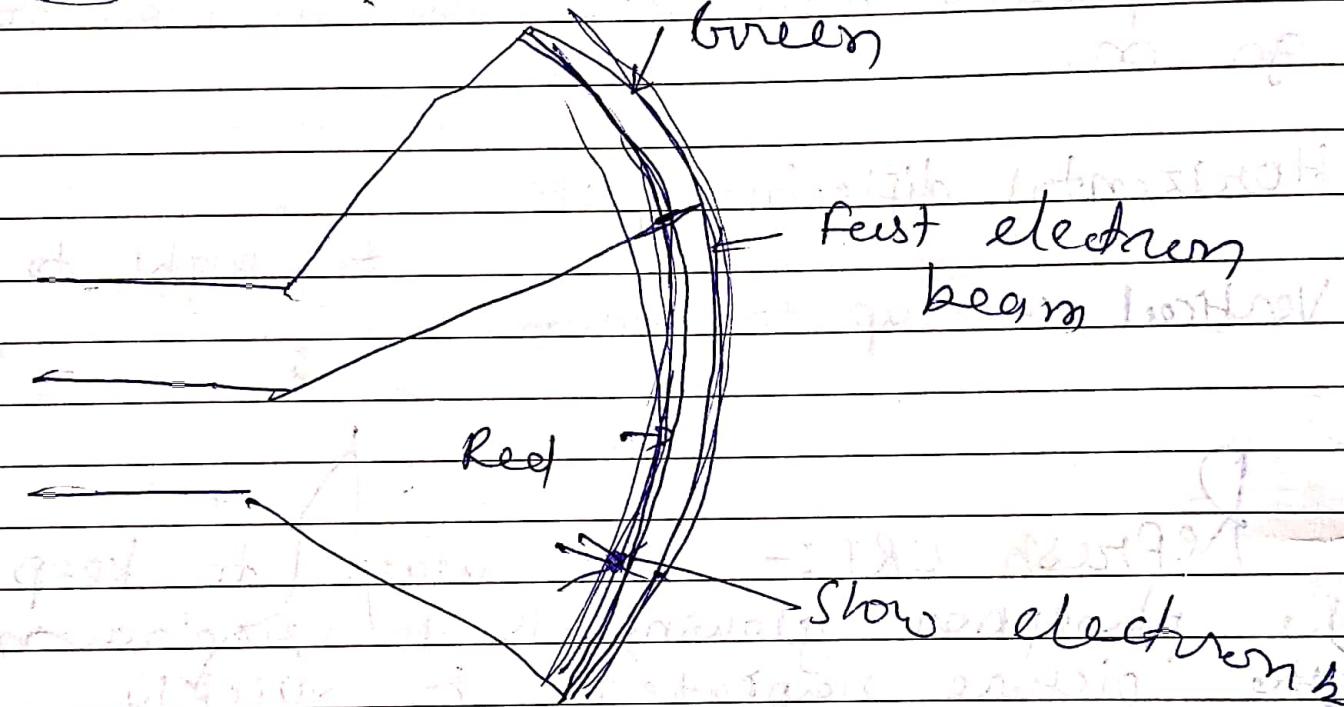
vertical

gates

Normal CRT is black n white

6 Two type of Color CRT

① Beam penetration



Used in Random Scan monitors

3 dots in a pixel.

Two colors Red and green coated to phosphor screen

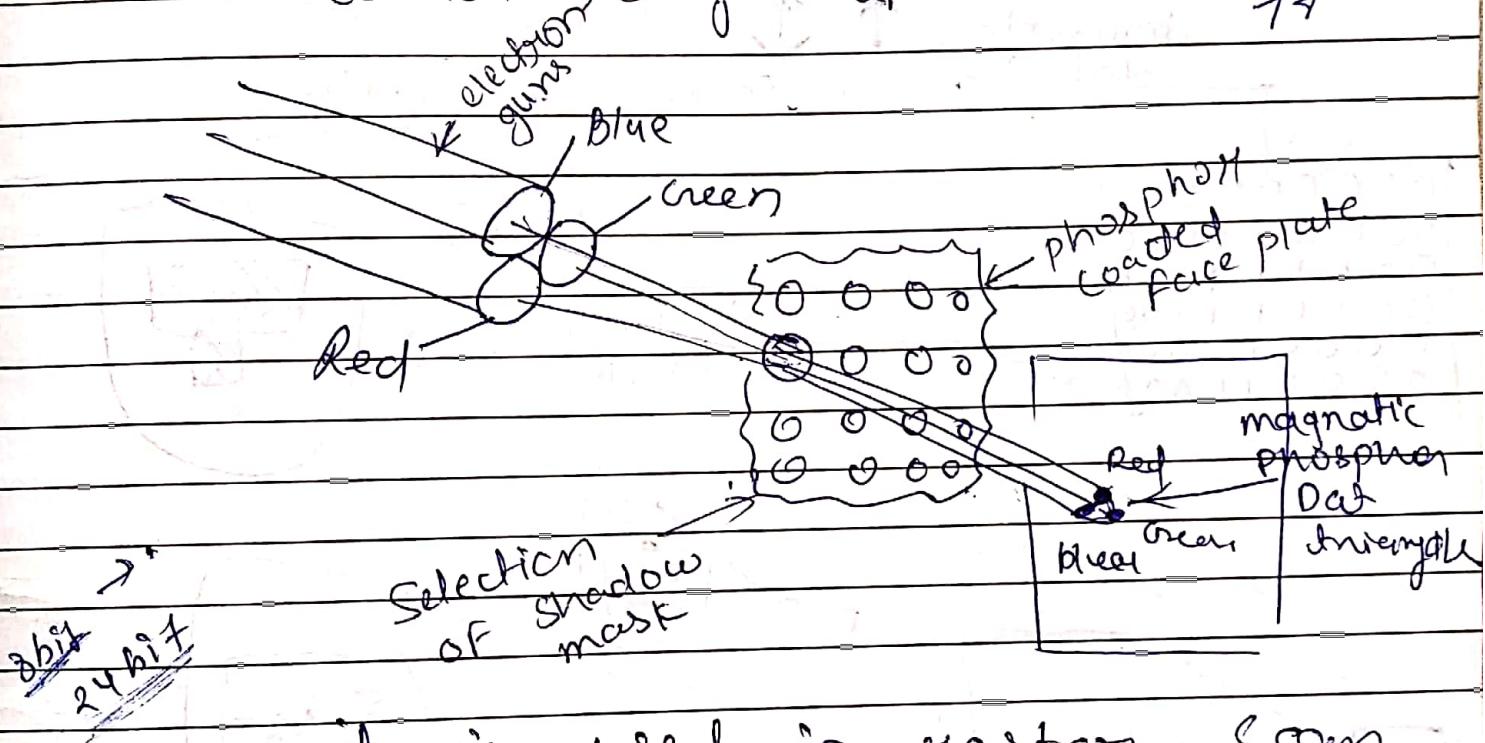
displaying color depend upon how deep electron beam penetrated to phosphor layer. very few colors

advantage: the biggest advantage is that it is at half cost of shadow mask and its resolution is better.

Date: _____ Page no: _____

② Shadow masking :- ~~A delta~~ shadow masking

used in Raster-scan model
wider range of colour.

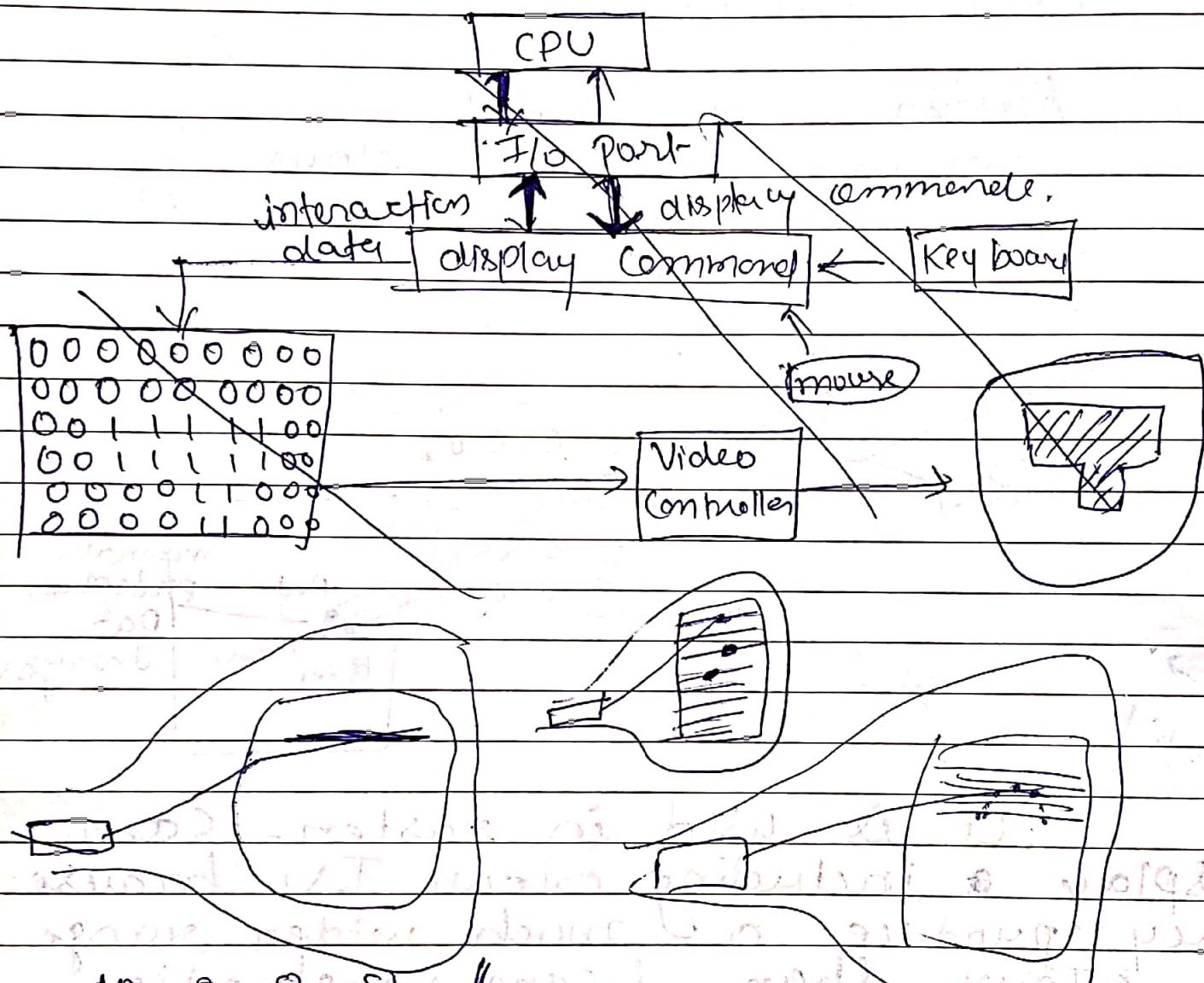


it is used in raster-scan display including colour T.V. because they produce a much wider range of colour than beam penetration method. A shadow mask CRT has three phosphor colour dots at each pixel position: one phosphor dot emits a red light, another emits a green light, and third emits blue light.

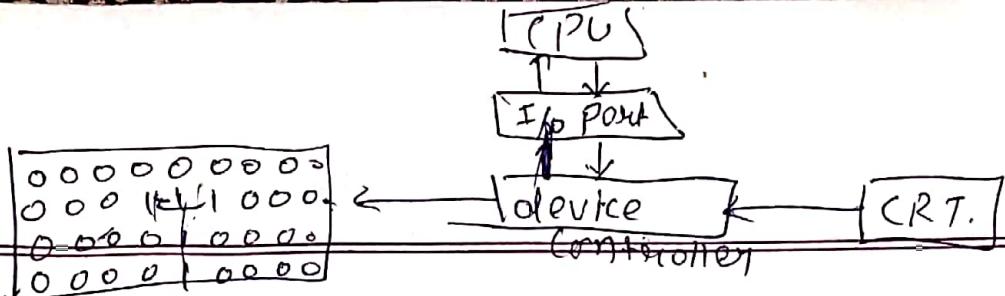
This type of CRT has three electron guns, one for each colour dots, and a shadow mask - a sheet of metal engraved with a

mask grid just behind the phosphor-coated screen, before the stream of electrons produced by the CRT's cathode reaches the phosphor.

Raster-Scan monitors :-



- ① The most common type on TV sets.
- ② electrons are moved in row left-to-right top-to-bottom.
- ③ Picture beam intensity turned on and off.



Date: _____ Page no: _____

- (4) Picture description stored in a memory area called frame buffer or refresh buffer.
- (5) Stored intensity value will retrieve from frame buffer to be painted.
- (6) For black and white only 1 bit is used 0 for white when the beam intensity is off vice versa.
- (7) Additional bits are needed when coloured up to 24 bits per pixel in high quality system depending upon resolution of system.

If 24 bits per pixel and resolution 1024 x 1024 will be have 3 megabyte of storage of frame buffer.

black and white 1 bit per pixel buffer \rightarrow bitmap.

Coloured multiple pixel

frame buffer - Pix map.

Each screen pixel on the screen can be specified by its row and column.

Shadow masking (Raster Scan display) used in

- :- ① In CRT colour monitors, we are using 3 e guns to produce the colour (single pixel is coated with Red, green, & blue dots of phosphorous)
- ② In Shadow masking technique we can generate wider range of colours.
- ③ Three dots are arranged in triangular shape, so it is also called Delta shadow mask method.

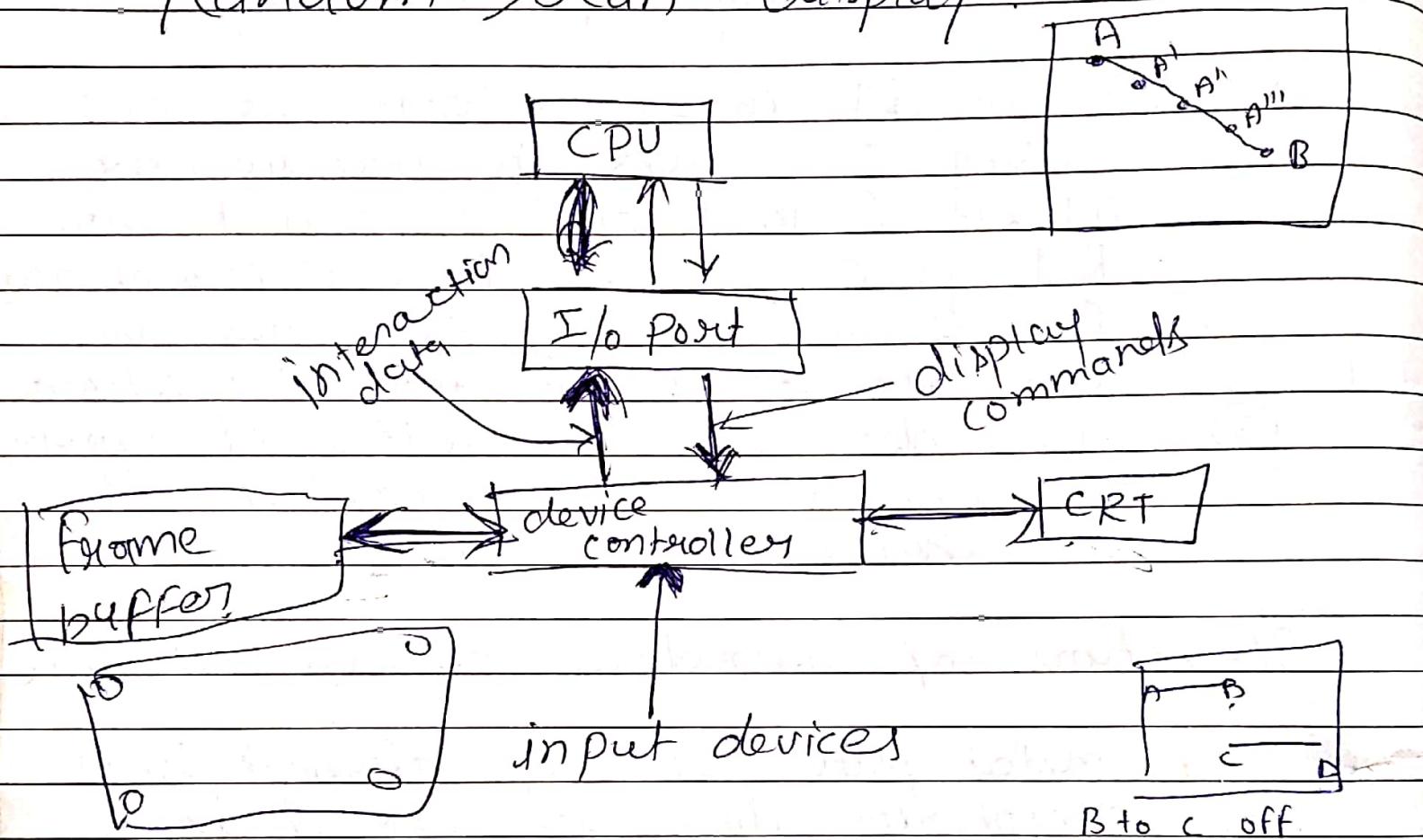
Structure of Shadow masking technique

A metal plate series of aligned holes with phosphores dots are placed in between electron guns and display screen

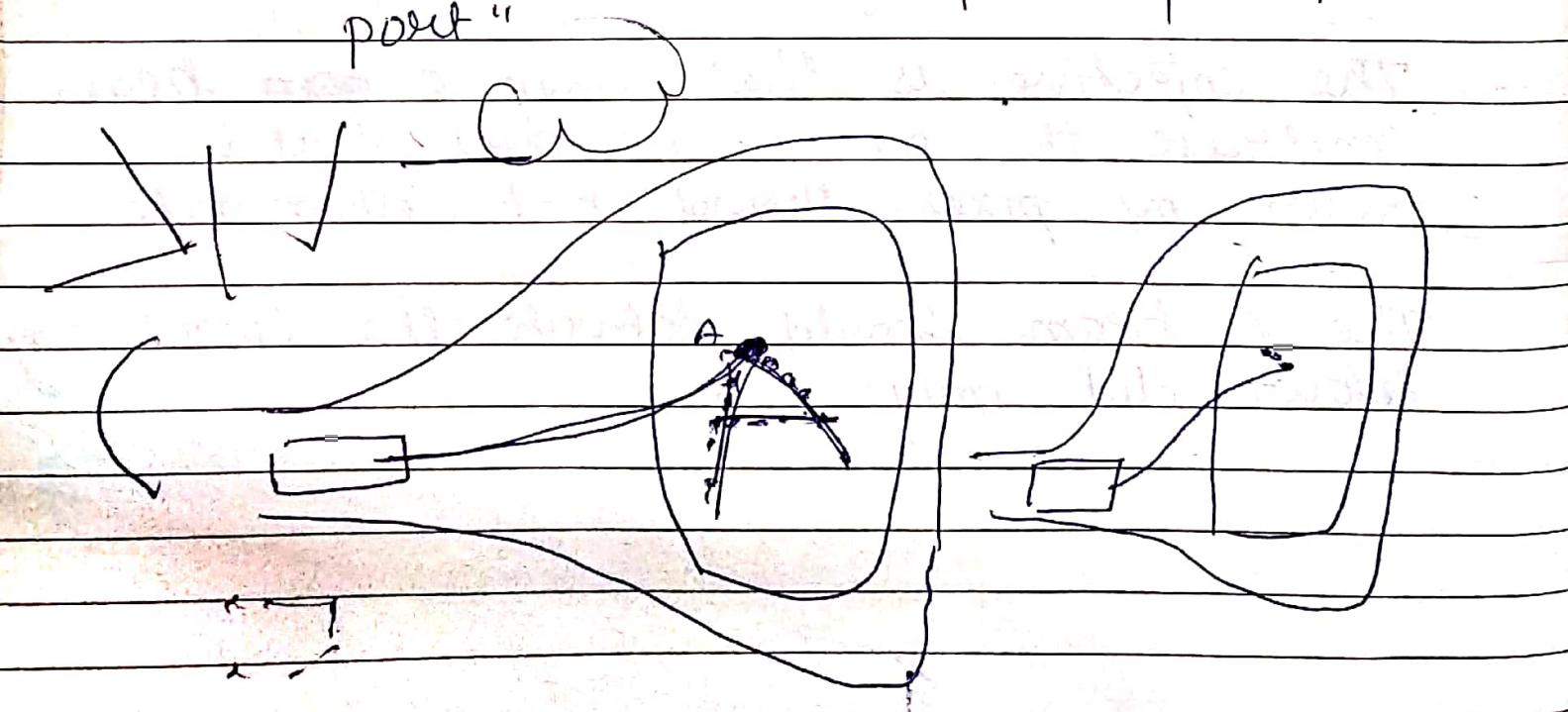
The objective is that when e gun beam penetrate the particular pixel, it's near by pixel should not illuminate.

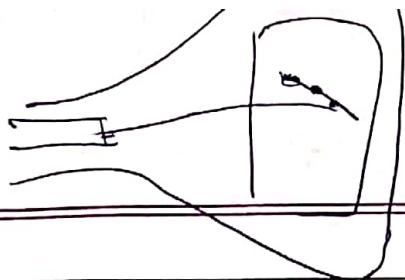
The e beam should activate the corresponding colour dot only

Random Scan display :-



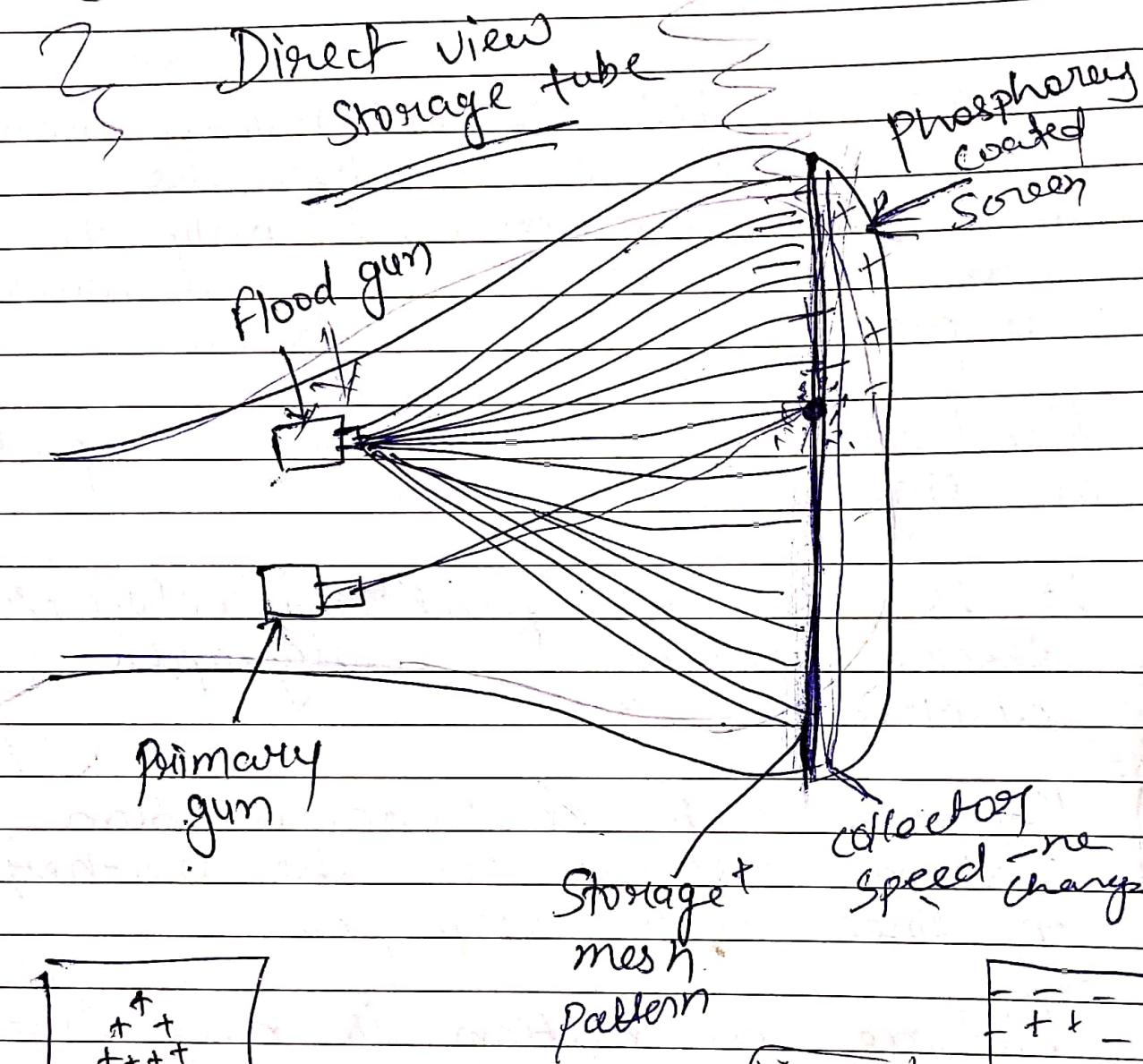
"Video monitors are primary output port"





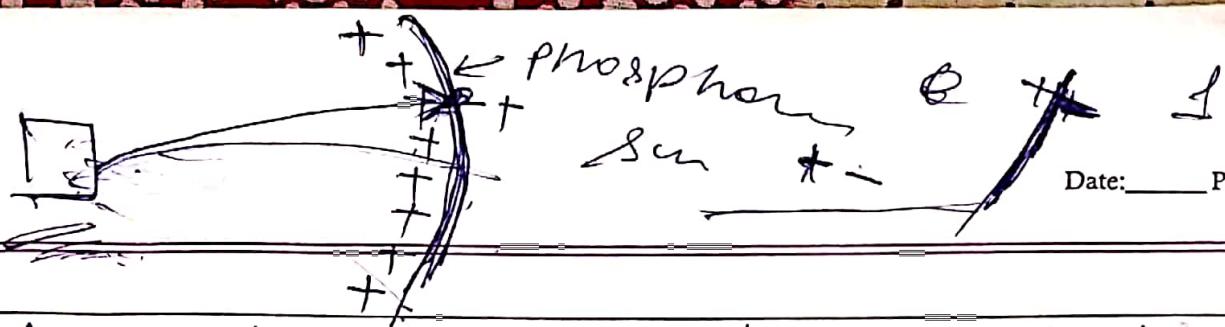
- (1) When operated as a random-scan display unit, a CRT has the electron beam directed only to the parts of the screen where a picture is to be drawn.
- (2) Random Scan monitors draw a picture on line at the time.
- (3) It is also referred as vector display, stroke writing or calligraphic display.
- (4) Refresh rate in random-scan system depends on the number of lines to be displayed.
- (5) Picture definition is now stored as a set of line-drawing commands in an area of memory referred to as the refresh display file.
it is also called display list or display program.
Refresh rate may be 60
- (6) Random-scan systems are designed for line drawing application and can not display realistic shades.

Why we use



+	+	+
++	+	+
+	+	+
+	+	+

++	-	-
-	-	-
-	-	-
-	-	-



Date: _____ Page no: _____

flat panel display :- used as both
Input devices & output
devices.

Devices :- smart phones
TV, computers

Plasma

LCD

e-reader (amazon)

advantages:

① more energy efficient than CRT

② Space saving

③ better picture

④ less eye strain (CRT slightly blurry)

two types categories :-

① Volatile ② Static

constantly refreshes even on stationary image

example

① TV - Plasma

LCD

② Computer

LCD

③ Smart

Phone

DVST :-

An alternative method for maintaining a screen image is to store the picture information inside the CRT instead of refreshing the screen. A direct-view storage tube (DVST) stores the picture information as a charge distribution just behind the phosphor-coated screen. Two electron guns are used in a DVST. One, the primary gun, is used to store the picture pattern, the second, the flood gun, maintains the picture display.

Advantages :- because no refreshing is needed very complex pictures can be displayed at very high resolution without flicker.

Disadvantages :- Disadvantages of DVST systems are that they ordinarily do not display color and that selected parts of a picture cannot be erased. To eliminate part of a picture section, the entire screen must be erased and the modified picture redrawn.

Flat-panel video displays

The term flat-panel display refers to a class of video devices that have reduced volume, weight, and power requirements compared to a CRT. A significant feature of flat-panel displays is that they are are thinner than CRTs, and we can hang them on walls or wear them on our wrists.

Types of flat panel displays.

① Emissive display :-

displays that convert electrical energy into light. plasma panel, thin film electroluminescent display, and light-emitting diodes are examples of emissive displays.

② Non-Emissive display :-

nonemissive displays (or no emitters) use optical effects to convert sunlight or light from some other source into graphics patterns. the most important example of a non-emissive flat-panel display is a liquid crystal device.

Scan Converting techniques

(line, circle, ellipses)

" Scan and convert the line from frame buffer into the screen.

line drawing :- given the specification for a straight line, find collection of addressable pixel which most closely approximates this line.

- (1) straight line should be straight
- (2) line should start and end accurately

DDA :- digital differential analyzer

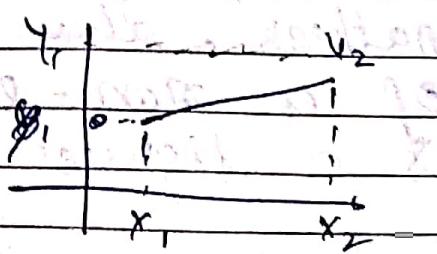
Pixel
Computer

Slope intercept line equation

$$\rightarrow Y = mx + b \quad \downarrow \quad y \text{ intercept}$$

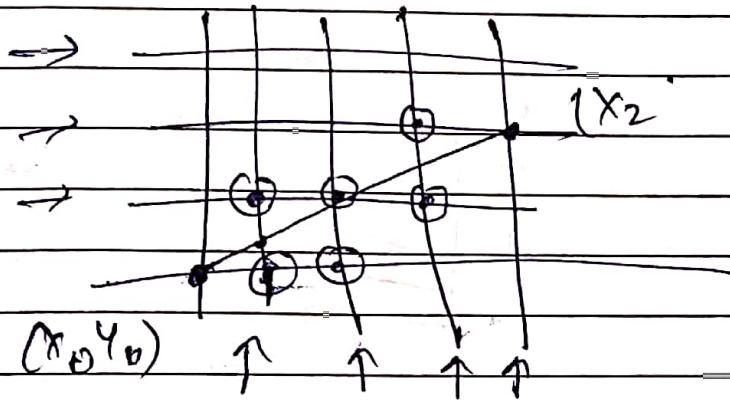
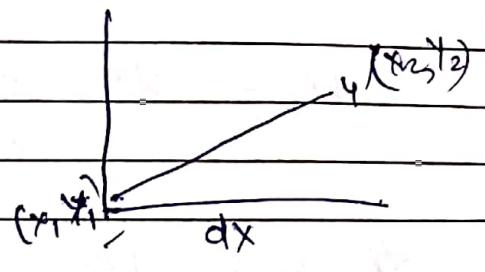
slope

$$m = \frac{dy}{dx}$$



$$m(\text{slop}) = \frac{y_2 - y_1}{x_2 - x_1}$$

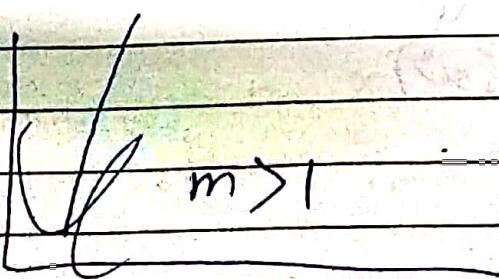
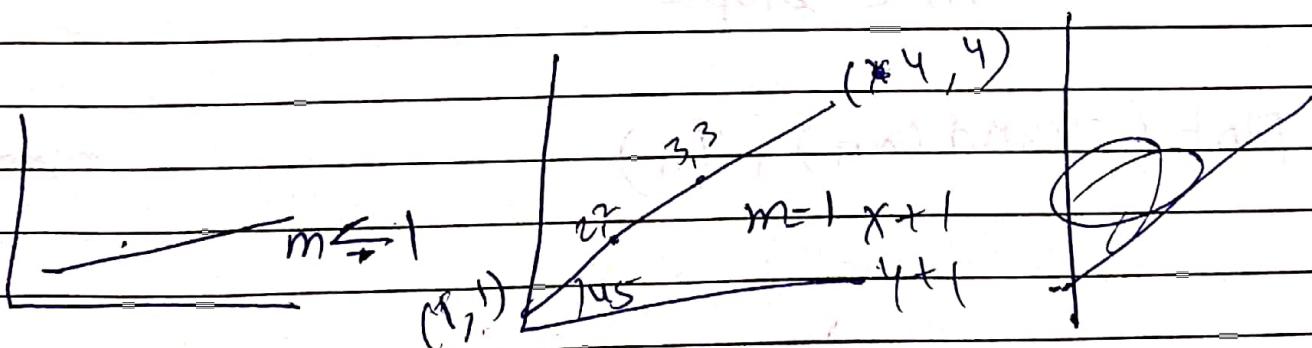
$$b = y_1 - mx_1$$



~~join~~ initial points

analyse difference bet^m points

~~join~~ $x_m =$



$$m = \frac{dy}{dx} = \frac{y_2 - y_0}{x_2 - x_0}$$

• this differential equation can be used to obtain a rasterized straight line

Case 1

$$m < 1$$

$$Y_n = m x_n +$$

$$X_n = x_0 + 1$$

$$Y_n = Y_0 + m \leftarrow \text{slope}$$

Plot $\Rightarrow (x_n, Y_n)$ round Y_n

Case 2,

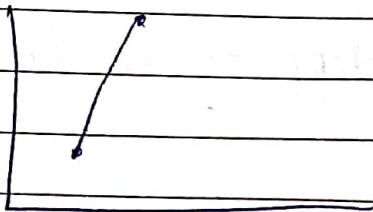
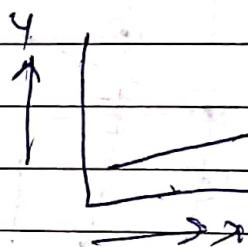
$$m > 1$$

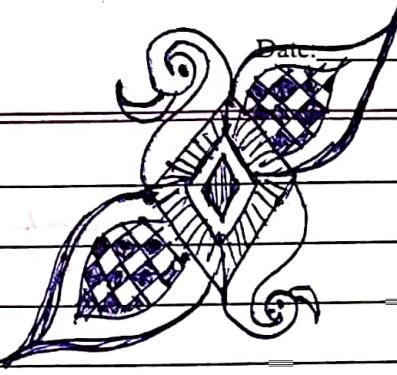
$$Y_n = Y_0 + 1$$

$$X_n = x_0 + \frac{1}{m} \leftarrow \text{slope}$$

Plot (round (x_n) , y_n)

$(\text{round } y_n)$
 $y_5 \approx 5$
 $y_3 \approx 3$





~~example :-~~

DDA algorithm

1. Read the line end points (x_1, y_1) and (x_2, y_2)

$$2. \Delta x = |x_2 - x_1|$$

$$\Delta y = |y_2 - y_1|$$

3. if $(\Delta x \geq \Delta y)$ then

$$\text{length} = \Delta x$$

else

$$\text{length} = \Delta y$$

4. Select the raster unit

$$\Delta x = \frac{(x_2 - x_1)}{\text{length}}$$

$$\Delta y = \frac{(y_2 - y_1)}{\text{length}}$$

5

$$x = x_1 + 0.5 * \text{sign}(\Delta x)$$

$$y = y_1 + 0.5 * \text{sign}(\Delta y)$$

Sign function

6. Now plot the point

$$i = 1$$

while ($i \leq \text{length}$)

{

 plot (integer(x), integer(y))

$$x = x + \Delta x$$

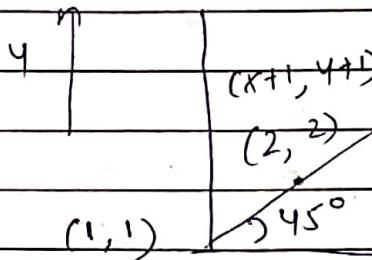
$$y = y + \Delta y$$

$$i = i + 1$$

}

DDA :-

$m = 1$
~~(Case 4)~~

Simple :- (y_{n+1}) $(\frac{y_{n+1}}{x_{n+1}})$ (x_{n+1}) (y, y) 

(Case 1 :-

 $m < 1$

$(y_0 + m)$ $(y_n + m)$ (y_{n+1}) $(x, \text{व्याप्ति लेखी से})$
 $(x_0 + 1)$ $(x_n + 1)$ (x_{n+1}) (x_1, y_1) $(y \text{ स्टॉप})$

 (x_0, y_0) Starting points $\rightarrow (x_0, y_0)$ (x_1, y_1) $m < 1$

↑ set pixel

Next point :-

$$x_n (\text{new}) = x_0 + 1$$

$$y_n (\text{new}) = y_0 + m \quad \text{plot } (x_0 + 1, y_0 + m)$$

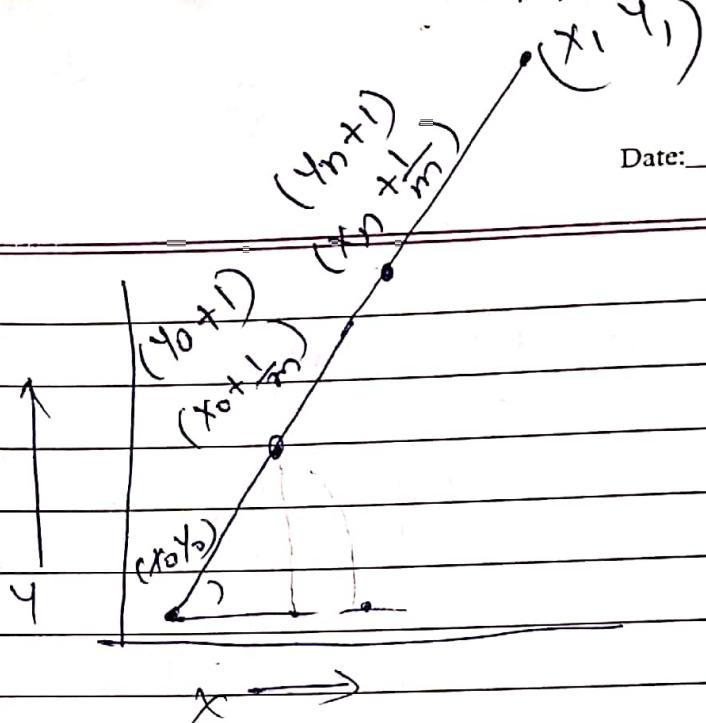
→ Plot $(x_n, \text{round off } y_n)$

1 (put pixel)

(condition through $x_{n+1} = x_1$)

$$y_n = y_1$$

$m > 1$



Starting points (x_0, y_0) (x_1, y_1)
 Set pixel

$m > 1$

Next points :-

$$x_n = x_0 + \frac{1}{m}$$

$$y_n = y + 1$$

$$\text{Plot} = (\text{round } x_0 + \frac{1}{m}, y + 1)$$

$$= (\text{round } x_n, y_n)$$

$$= (\text{round } x_n + \frac{1}{m}, y_n + 1)$$

$$= (\text{round } x_n, \text{round } y_n)$$

$$m = \frac{y_1 - y_0}{x_1 - x_0}$$

$$= \frac{3-1}{4-0} = \frac{2}{4} = 0.5$$

(4, 3)

Date: _____ Page no: _____

example :-

$$m = 0.5 \quad m < 1$$

		x_n	y_n
	Put Pixel	0	1
1	2	$0+1 = 1$	$1+0.5 = 1.5 = 2$
2	3	2	$2+0.5 = 2.5 = 3$
3		3	$2.5+0.5 = 3.05$

y_n	x_n	x_n	y_n
1	1	$0+1 = 1$	$1+0.5 = 1.5$
2	2	$1+1 = 2$	$1.5+0.5 = 2$
3	3	$2+1 = 3$	2.05
3	4	$3+1 = 4$	$2.5+0.5 = 3$

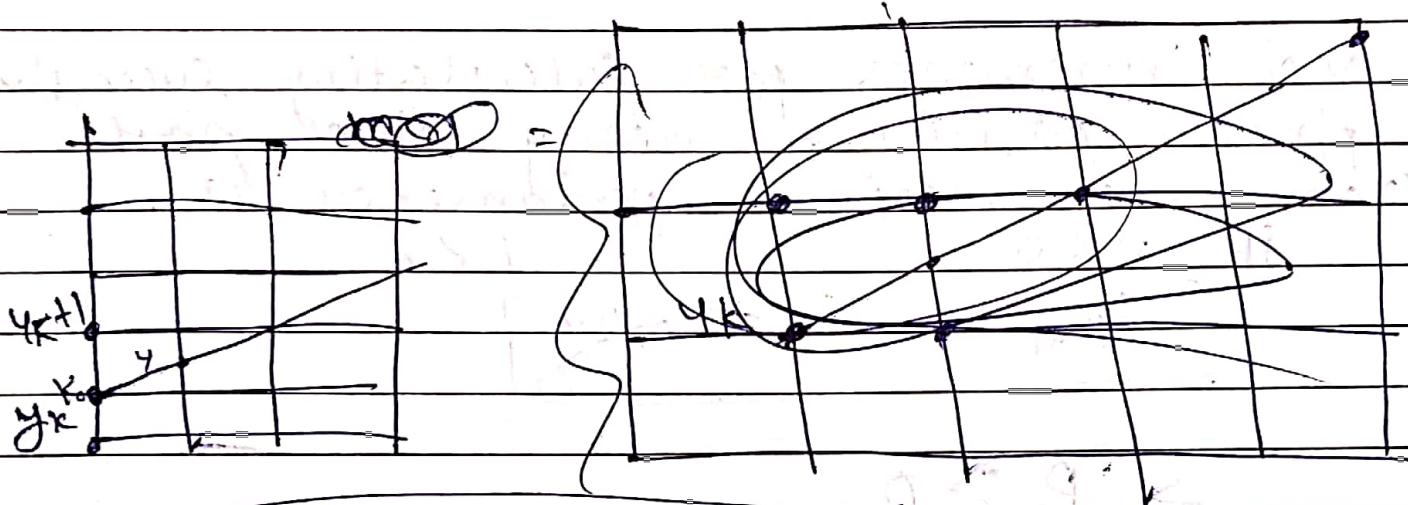
advantage of class and advantage book

Bresenham's Algorithm :-

- ① input the two endpoints and store the left end point in (x_0, y_0)
- ② load (x_0, y_0) into the frame buffer, that is, plot the first point.
- ③ calculate constants Δx , Δy , $2\Delta x$, $2\Delta y$ and $2\Delta y - \Delta x$, and obtain the starting value for the decision parameters as
- ④ At each x_k along the line starting at $k=0$ perform the following test
if $P_k < 0$, the next point to plot is $(x_k + 1, y_k)$ and
$$P_{k+1} = P_k + 2\Delta y$$
otherwise, the next point to plot is $(x_k + 1, y_k + 1)$ and
$$P_{k+1} = P_k + 2\Delta y - 2\Delta x$$
- ⑤ Repeat step 4 Δx times.

DFA - drawback (round function) to overcome

~~e = start point~~



decision parameter

$$m < 1$$

$$y = mx + c$$

$$m = \frac{\Delta y}{\Delta x}$$

calculate

Δx , Δy , $2\Delta y$, and $2\Delta y - \Delta y$ encase

$$m < 1$$

example $(20, 10)$ $(30, 18)$

$$\Delta x = 30 - 20 = 10$$

$$\Delta y = 18 - 10 = 8$$

initial decision parameter $= P_0 = 2\Delta y - \Delta x$

$$P_0 = 2\Delta Y - \Delta X$$

$$= 2 \times 8 - 10$$

$$= 16 - 10$$

$$= 6$$

and increments for calculating successive pixel position & along line path x from the decision parameter as.

IF $P_0 < 0$

$P < 0$

$$P_{k+1} = P_k + 2\Delta Y$$

$$P_0 > 0$$

$$P_{k+1} = P_k + 2\Delta Y - 2\Delta X$$

$$\begin{aligned} P_0 &= 6 & P > 0 & \text{initial param.} \\ P_k &= 6 + 16 - 16 & = 2\Delta Y - 2\Delta X \\ &= 16 - 20 \\ &= -4 \end{aligned}$$

$$P_{k+1} = P_k + 2\Delta Y - 2\Delta X$$

$$\begin{aligned} (R) \Rightarrow 6 - 4 &= 2 \\ &= 2 \end{aligned}$$

$$\begin{aligned} P_{k+1} &= 2 - 4 & P_{k+1} &= P_k + 2\Delta Y \\ &= -2 & & = -2 + 16 \end{aligned}$$

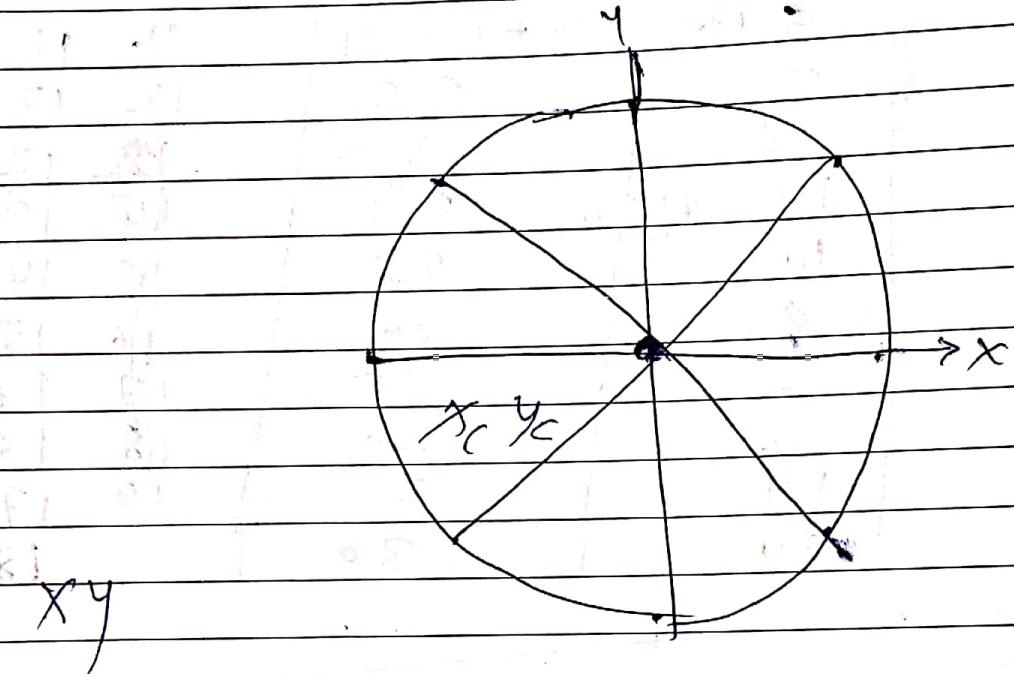
$\checkmark u_{k+1}$ $P_k > 0$

iteration no.	R_k	$X_{k+1} = 20$	$Y_{k+1} = 10$
0	6 (P_0)	$20 + 1 = 21$	11
1	2	22	12
2	-2	23	12 (4b)
3	14	$P_k < 0$	13
4	10	25	14
5	6	26	15
6	+2	27	16
7	-2	28	16
8	14	29	17
9	10	30	18

if $P_k < 0$ $\Rightarrow Y_k \rightarrow Y_{k+1}$

$P_k > 0$ $\Rightarrow Y_k$

Mid point circle :-



$$r^2 = x^2 + y^2$$

$$y = \pm \sqrt{r^2 - x^2}$$

8 fold symmetry.

Algo :-

- ① Input radius r and circle centre (x_c, y_c) and obtain the first point on the circumference of a circle centered on the origin as -

$$(x_0, y_0) = (0, r)$$

- ② Calculate the initial value of the decision parameters as.

$$P_0 = \frac{5}{4} - 4 \approx 1 - 2$$

- ③ at each x_k position, starting at $k=0$, perform the following test if $P_k < 0$, the next point along the circle centered on $(0, 0)$ is (x_{k+1}, y) and

$$P_{k+1} = P_k + 2x_{k+1} + 1$$

otherwise, the next point along the circle is (x_{k+1}, y_{k+1}) and

$$P_{k+1} = P_k + 2x_{k+1} + 1 - 2y_{k+1}$$

where $2x_{k+1} = 2x_k + 2$ and $2y_{k+1} = 2y_k - 2$

$$2y_{k+1} = 2y_k - 2$$

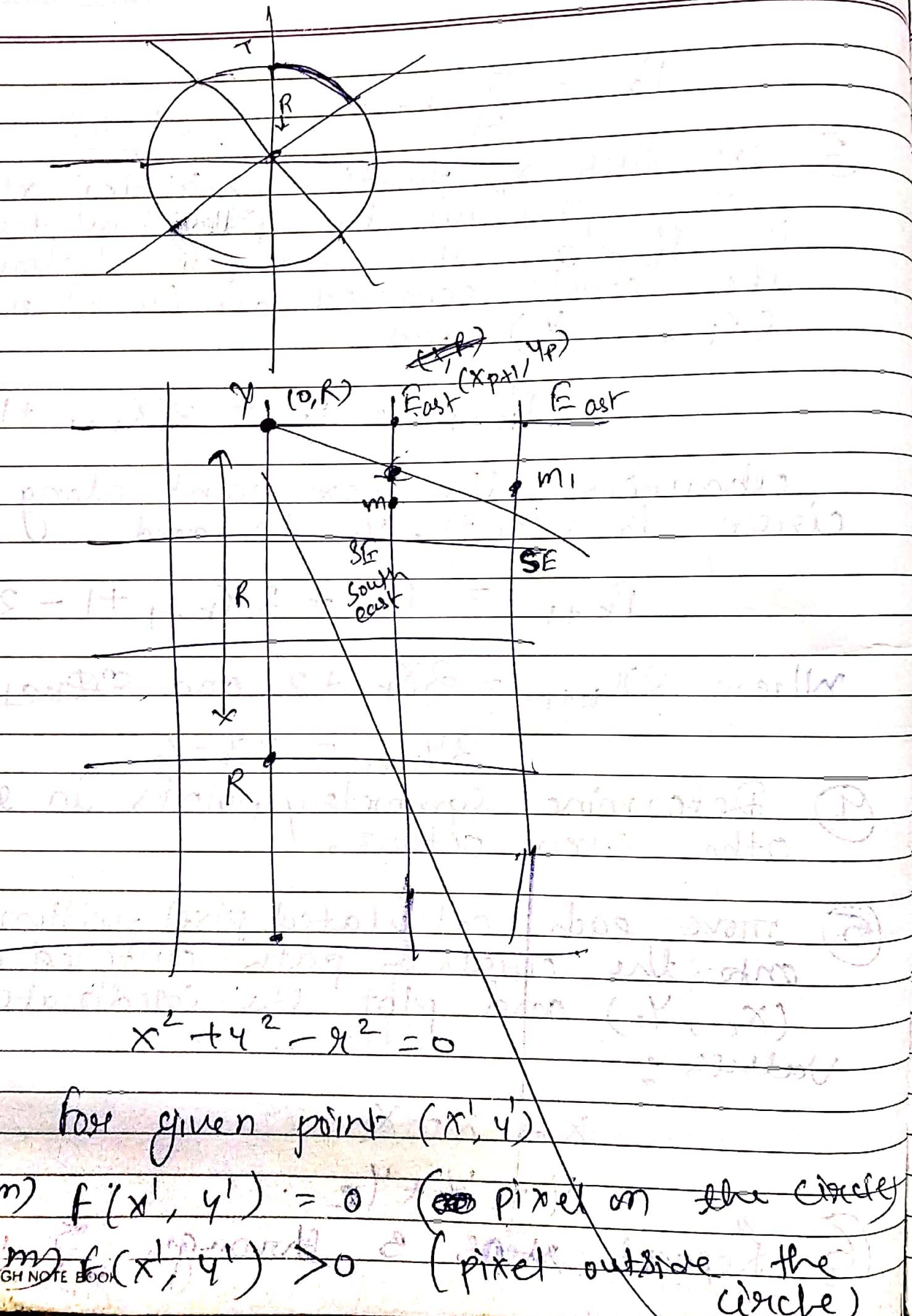
- ④ Determine symmetry points in the other seven octants.

- ⑤ move each calculated pixel position (x, y) onto the circular path centered on (x_c, y_c) and plot the coordinate values?

$$x = x + x_c$$

$$y = y + y_c$$

- ⑥ Repeat steps 3 through 5 until $x \geq y$.



$f(x, y) < 0$ (pixel inside the circle)

$m > 0$ (circle line near to east)

$$f(x, y) = x^2 + y^2 - R^2 = 0$$

evaluate $f(m)$
if $f(m) < 0$ (inside circle)

Choose ΔE
if $f(m) > 0$ (outside circle)

Choose ΔE

decision point (x_p, y_p)

$$d = f(m) = f(x_{p+1}, y_p - \frac{1}{2})$$

$$d = (x_{p+1})^2 + (y_p - \frac{1}{2})^2 - R^2$$

when $d < 0$ (when A selected)
 x at value $\alpha \leq 0$

$$d_{new} = (f(m)) = f(x_{p+2}, y - \frac{1}{2})$$

$$d_{new} = (x_{p+2})^2 + (y_p - \frac{1}{2})^2 - R^2$$

$$\Delta E = d_{new} = 2x_p + 3$$

when SF selected (x diff 0.5, y diff 1 pixel decrease)

$$d_{\text{new}} = f(m) = r \left(x+2, y_p - \frac{3}{2} \right)$$

$$\Delta SE = d_{\text{new}} - d$$

$$= 2x_p - 2y_p + 5$$

~~if $x > 0$ $y = R$~~

$$\begin{aligned} d &= (0+1)^2 + (R - \frac{1}{2})^2 - r^2 \\ &= \frac{5}{4} - R \end{aligned}$$

~~put pixel ($x_{\text{center}} + x$,
 $y_{\text{center}} + y$);~~

~~PP_r ($x_{\text{center}} - x$, $y_{\text{center}} + y$);~~

~~PP_r (" + x, " - y);~~

~~PP_r (" - x, " - y);~~

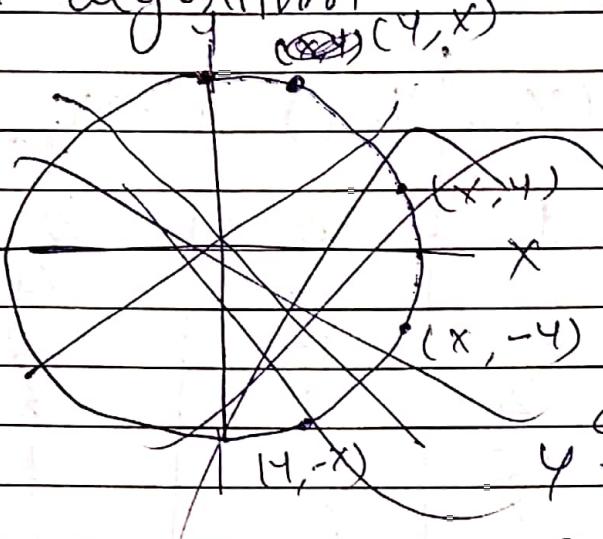
~~PP_r (" + y, " + x);~~

~~PP_r (" - y, " + x);~~

~~PP_r (" + y, " - x);~~

~~PP_r (" - y, " - x);~~

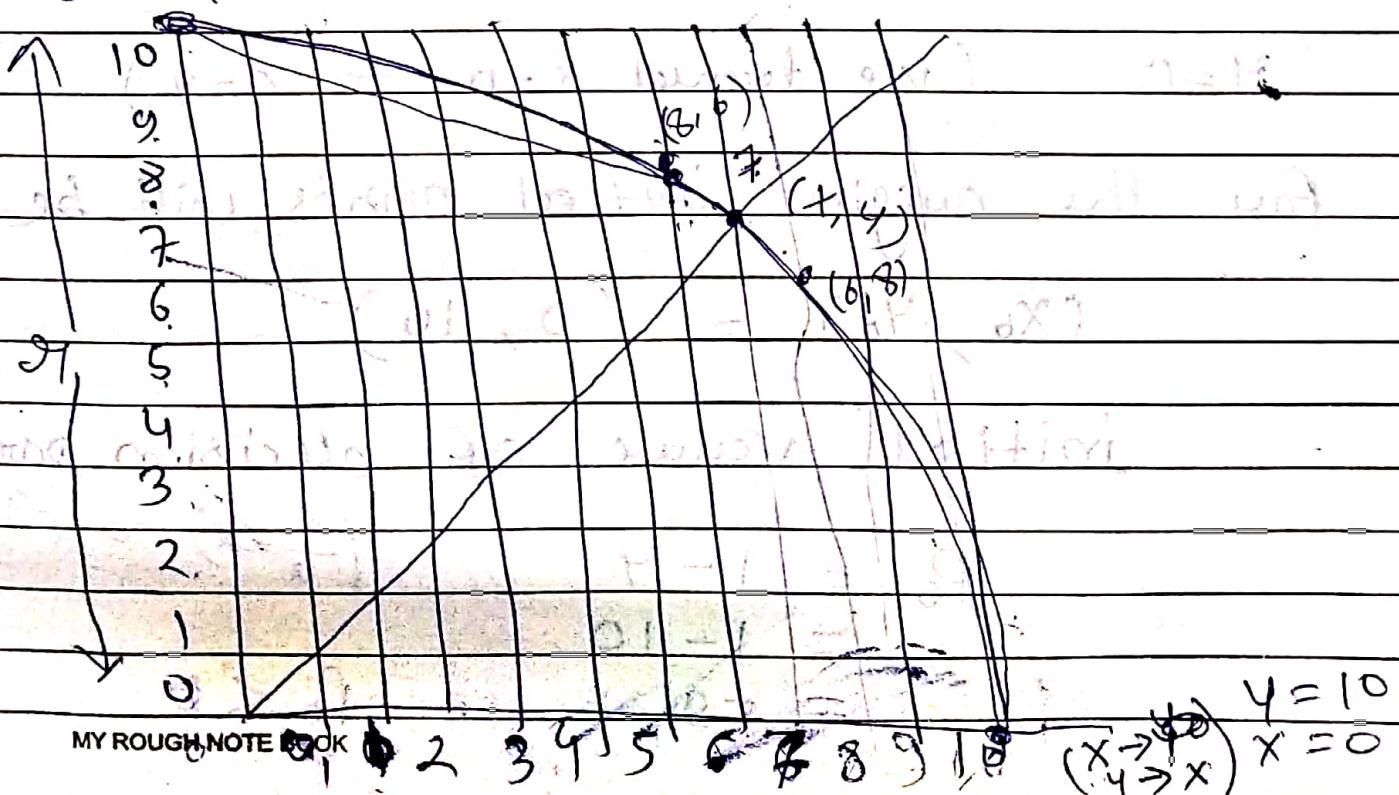
mid point algorithm



and x moves
to positive
direction and
 y moves in -ve

$$f_{\text{circle}}(x, y) = x^2 + y^2 - 912$$

$$f_{\text{circle}} \left\{ \begin{array}{l} < 0 \text{ if } (x, y) \text{ is inside circle boundary} \\ = 0 \text{ if } (x, y) \text{ is on circle} \\ > 0 \text{ if } (x, y) \text{ is outside circle} \end{array} \right.$$



numerical :-

k	P_k	(x_{k+1}, y_{k+1})	$2x_{k+1}$	$2y_{k+1}$
0	-9	1 10	2	20
1	-6	2 10	4	20
2	-1	3 10	6	20
3	6	4 9	8	18
	-3	5 9	10	18
	6	6 8	12	16
	3	7 7	14	14

Iteration performed

$H=0$ (We decided x_0 to $x=y$)

For the origin initial points will be

$$(x_0, y_0) = (0, 10)$$

initial value of decision parameter

$$P_0 = 1 - 4 \quad (\frac{5-4}{6} \approx -9)$$

$$= 1 - 10$$

$$= -9$$

$$P_0 < 0$$

and $2x_0 = 0$ $2y_0 = 20$

$$\textcircled{1} \quad P_k (P_0) < 0 \quad (-9) \quad \text{So}$$

$$x_{k+1} = 0 + 1 = 1$$

$$y_{k+1} = y_k = 10$$

$$[2x_{k+1} = 1 \times 1 = 2]$$

$$[2y_{k+1} = 2 \times 10 = 20]$$

$$\textcircled{2} \quad \text{because } P_k < 0$$

So

$$P_{k+1} = P_k + 2x_{k+1} + 1$$

$$P_{k+1} = -9 + 2 + 1$$

$$P_{k+1} = -6$$

$$P_{k+1} < 0 \quad (-6) \quad \text{So}$$

$$\text{So } x_{k+1} = 1 + 1 \\ = 2$$

$$y_{k+1} = y_k = 10$$

$$2x_{k+1} = 2 \times 2 = 4$$

$$2y_{k+1} = 10 \times 2 = 20$$

(3)

$$P_k < 0$$

$$P_{k+1} = P_k + 2x_{k+1} + 1$$

$$= -6 + 4 + 1$$

$$\boxed{P_{k+1} = -1}$$

$$x_{k+1} = 2 + 1 = 3$$

$$y_{k+1} = y_k = 10$$

$$2x_{k+1} = 2 \times 3 = 6$$

$$2y_{k+1} = 2 \times 10 = 20$$

(4)

$$P_k > 0$$

$$P_{k+1} = P_k + 2x_{k+1} + 1$$

$$= -1 + 2 \times 3 + 1$$

$$= -1 + 7 = 6$$

$$\boxed{P_{k+1} = 6}$$

$$x_{k+1} = 3 + 1 = 4$$

$$y_{k+1} = 10 + 1 = 11$$

$$2y_{k+1} = 18$$

$$= 9$$

(5)

$$P_k > 0$$

$$P_{k+1} = P_k + 2x_{k+1} + 1 - 2y_{k+1}$$

$$= 6 + 8 + 1 - 18$$

$$= 15 - 18 = -3$$

$$P = -3 + 10 + 1 \\ = 6 + 12 + 1 - 16 \\ = 6 + 12 - 16 \\ = 2$$

10:30

Date: _____ Page no: _____

$$x_{k+1} = 4 + 1 = 5$$

$$y_{k+1} = y_k = 9 \quad (\because P_k < 0)$$

$$2x_{k+1} = 10 \quad 2y_{k+1} = 18$$



till (7, 7)

Bresenham's algorithm for circle drawing :-

- ① Read the radius r_1 of the circle.
- ② Initialize the decision variable $d = 3 - 2r_1$
- ③ $x = 0$
 $y = r_1$
- ④ If we are using octants symmetry to plot the pixels then until ($x < y$) we have to perform following steps,

if ($d < 0$) then

$$d = d + 4x + 6$$

$$x = x + 1$$

$$y = y$$

$$d = d + 4x + 10$$

else

$$d = d + 4x + 8$$

$$x = x + 1$$

$$d = d + 4(x-y) + 10$$

$$y = y - 1$$

$$x = x + 1$$

$$x = x + 1$$

$$y = y$$

(5) Plot (x, y)

(6) Determine the symmetry points in other octants also

(7) Stop.

B. Algo

① Bresenham algo uses fixed points, integer arithmetic

② B. uses only subtraction and addition in its operators

③ Bresenham is faster than DDA

④ B. algo. is more efficient and much accurate than DDA Algo

⑤ B. algo. is less expensive than DDA algo

DDA Algo

① DDA uses floating points that is real arithmetic

② DDA uses multiplication and division in its

③ DDA is rather slower than B. Algo.

④ DDA algo is not as accurate and efficient as B. A

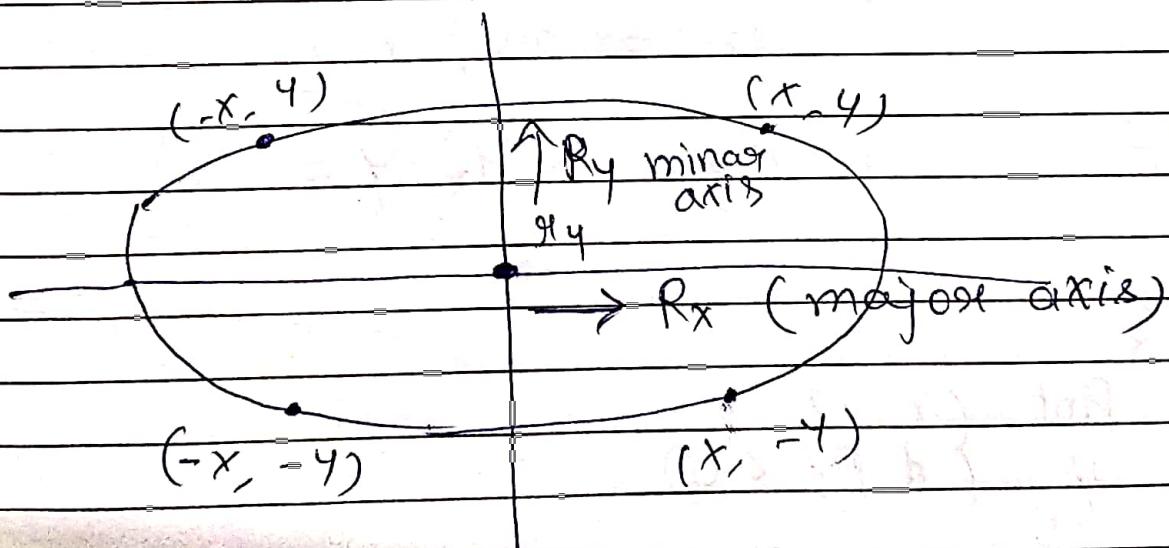
⑤ DDA algorithm uses an enormous number of floating point multiplication so it is expensive

(C) B. algo does not round off but takes the incremental value in it's operation

(D) DDA algo. round off the coordinates to integer that is nearest to the line. Round off of the pixel position obtained by multiplication or division causes an accumulation of error in the proceeding pixels

Ellipse generation :-

$$\text{Basic equation} \Rightarrow \left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2 = 1$$



\mathbb{Z}_p symmetry

$$2a = \text{major axis}$$

$$2b = \text{minor axis}$$

Mid point ellipse algorithm

- ① Read radii: r_x and r_y
- ② initialise starting point as

$$x = 0$$

$$y = r_y$$

Plot (x, y)

- ③ Calculate the initial value of a decision parameter in region 1 as,

$$P_1 = r_y^2 - r_x^2 r_y + \frac{1}{4} r_x^2$$

- ④ Initialize dx and dy as,

$$dx = 2r_x^2 x$$

$$dy = 2r_x r_y y$$

- ⑤ do

Plot (x, y)

if $(P_1 < 0)$

$$x = x + 1$$

$$y = y$$

$$dx = dx + 2r_y^2$$

$$P_1 = P_1 + dx + r_y^2$$

$(P_1 > 0)$

else

$$x = x + 1$$

$$y = y - 1$$

$$\Delta x = \Delta x + 2H_y^2$$

$$\Delta y = \Delta y - 2H_x^2$$

$$P_f = P_f + \Delta x - \Delta y + 9H^3$$

}
}

while

$$(\Delta x \leq \Delta y)$$

- ⑥ Calculate the initial value of decision parameter in region 2 as

$$P_2 = H_y^2 (x + \frac{1}{2})^2 + H_x^2 (y - 1)^2 - H_x^2 H_y^2$$

F.

do

{

Plot. (x, y)

if $(P_2 \geq 0)$

{

$$x = x$$

$$y = y - 1$$

$$\Delta y = \Delta y - 2H_x^2$$

$$P_2 = P_2 - \Delta y + 9H_x^2$$

else

2

$$x = x + 1$$

$$y = y - 1$$

$$\Delta y = \Delta y - 2Hx_2^2$$

$$\Delta x = \Delta x + 2Hy^2$$

$$P_2 = P_2 + \Delta x - \Delta y + Hx^2$$

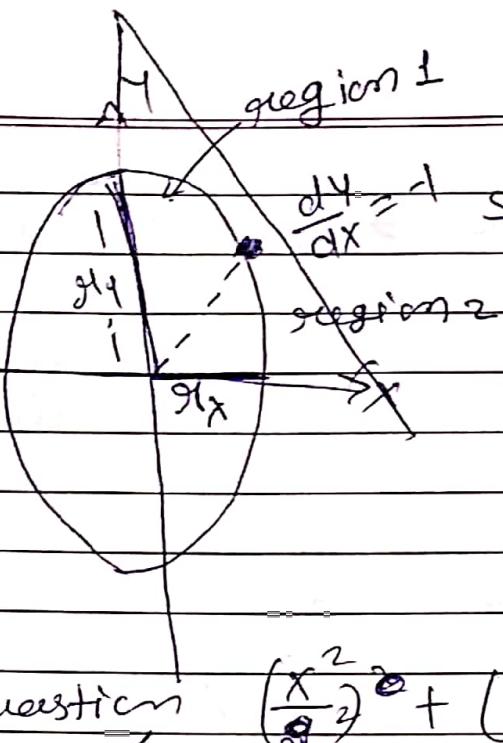
3

}

while ($y > 0$)

② determine symmetrical points in other three quadrants

③ Stop.



ellipse equation $\left(\frac{x^2}{a^2}\right) + \left(\frac{y^2}{b^2}\right) = 1$

~~$F(x, y) = a^2x^2 + b^2y^2 - a^2b^2$~~

$x^2/a_y^2 +$ { < 0 implies (x, y) inside the ellipse
 $y^2/a_x^2 = y^2/a_y^2$ } $= 0$ implies (x, y) on the ellipse
 > 0 implies (x, y) outside the ellipse

origin's 1's ending point will become
 origin's starting 0 point.

$$F(x, y) = a^2x^2/a_y^2 + b^2y^2/a_x^2 - a_x^2/a_y^2$$

$$\frac{dy}{dx} = -1 \quad (\text{region 1 to 2})$$

shifting)

$$\frac{-2a_x^2y^2}{2a_y^2x^2} = -1$$

$$2\pi y^2 x \geq 2\pi x^2 y$$

[before this we enclose
x then y increase]

Numerical :-

$$\pi x = 8 \quad \pi y = 6$$

$$\begin{aligned}
 P_L &= \pi y^2 - \pi x^2 \cdot \pi y + \frac{1}{4} \pi x^2 \\
 &= 6^2 - 8^2 \times 6 + \frac{1}{4} 8^2 \\
 &= 36 - 64 \times 6 + \frac{1}{4} 64 \\
 &= 36
 \end{aligned}$$

Polygon filling :-

Introduction :-

A polygon may be represented as a number of line segments connected, end to end to form a closed figure. Alternatively, it may be represented as the points where the sides of the polygon connected. The line segments which make up the polygon boundary are called "Sides" or edges. The end points of the sides are called the polygon "Vertices". The simplest polygon is the triangle, having three sides and three vertex points.

Polygon can be divided into two classes : (1) convex (2) concave.

"A convex polygon is a polygon such that for any two points inside the polygon all points on the line segment connecting them are also inside the polygon."

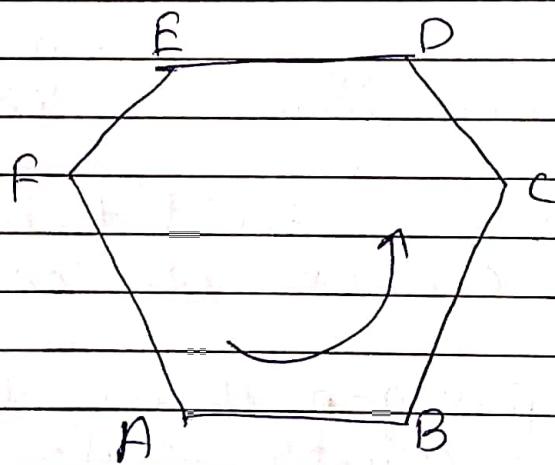
A concave polygon is one which is not convex.

Thus to determine whether or not a polygon is convex ask the following question

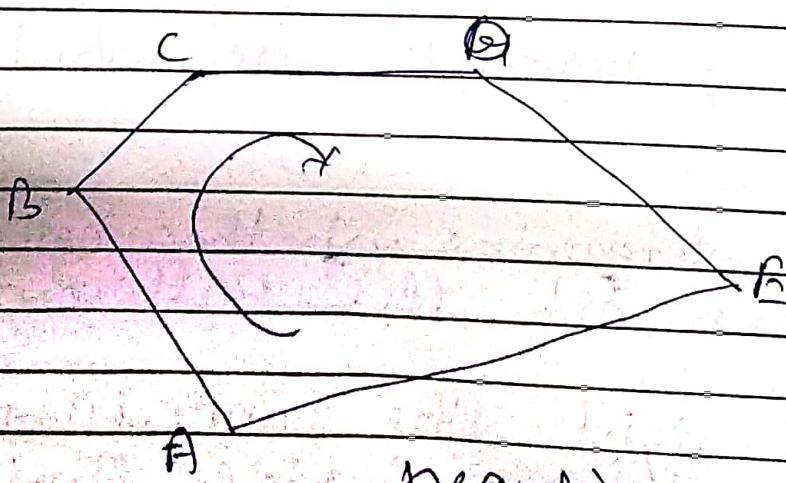
Does a straight line connecting any two points that are inside the polygon?

If the answer is no, the polygon is convex, otherwise it is concave.

We have a normal convention of writing the polygon as P_1, P_2, \dots, P_n . A polygon is said to be "positively oriented" if visiting of all the vertices in the given order produces a counter-clockwise circuit, otherwise it is said to be negative-oriented polygon.



Positive orientation



negative orientation

~~Polygon Representation~~

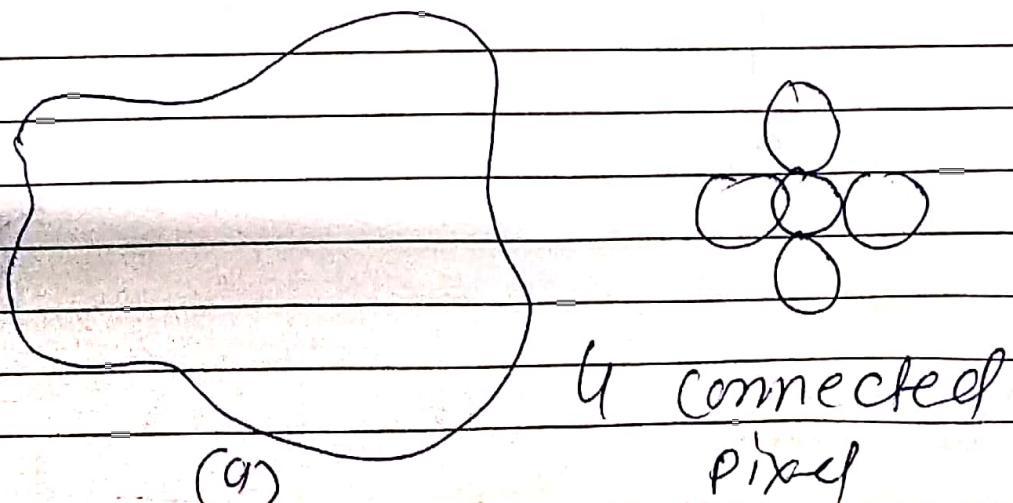
Polygon filling :-

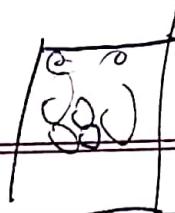
Filling is the process of "colouring in" a fixed area or of a region. There are two basic approaches to area filling in raster system. One way to fill an area is scan line fill algorithm another method for area filling is to start from a given interior position and point outward from this point, until we encounter the specified boundary condition.

- ① Boundary fill } seed fill
- ② Flood fill
- ③ Edge fill
- ④ Fence fill

Boundary fill algorithm

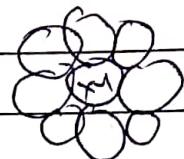
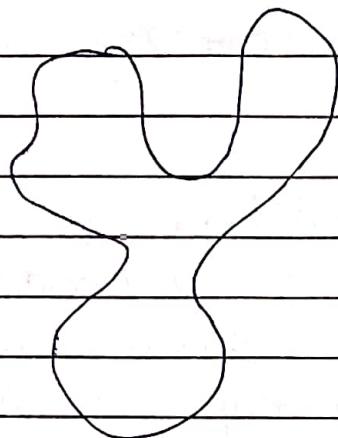
①





(2)

(200)



8- Connected pixel

↓
color inside
↓
boundary

void fill (int x, int y, int fill, int boundary)

{

int current = getPixel(x, y);

if (current != boundary) & current != fill)

{

setColor(fill);

setPixel(x, y);

boundaryFill (x+1, y, fill, boundary);

boundaryFill (x-1, y, fill, boundary);

boundaryFill (x, y+1, fill, boundary);

boundaryFill (x, y-1, fill, boundary);

}

{



Flood fill algorithm :-

this algorithm also begins with a seed (starting pixel) inside the region, it checks to see if the pixel has the region original colour. if the answer is yes, it returns to the caller.

This method shares great similarities in its operating principle with the boundary fill also.

Void floodfill (int x, int y, int fill, int color);

§

IF (getPixel (x, y) ≠ oldcolor)

§

SetColor (fill);

SetPixel (x, y);

Floodfill (x+1, y, fill, oldcolor);

Floodfill (x-1, y, fill, oldcolor);

Floodfill (x, y-1, fill, oldcolor);

§

3



2nd Unit

2-D transformation :- (translation,

Rotation

Flood fill

boundary fill

① Area filling is started from a point

Byte code

Secure
Pointer of zone

K

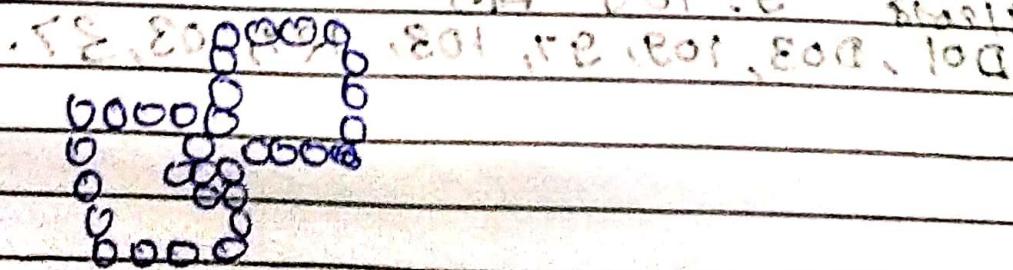
and 8-connected

4-connected :- these are techniques in which pixels are considered as connected to each other. In 4-connected method the pixels may have upto 4 neighbouring pixels, as right, above, left and below of the current pixel.

Similarly, in 8-connected method the pixels may have upto 8 neighbouring pixels.

Boundary fill algorithm:-

This is recursive algorithm that begins with a starting pixel called a seed, inside a region and continues painting toward the boundary. The algorithm checks to see if this pixel is a boundary pixel or has already filled. If "answering is NO" it implies the pixel is not a boundary pixel and makes a recursive call to the function.



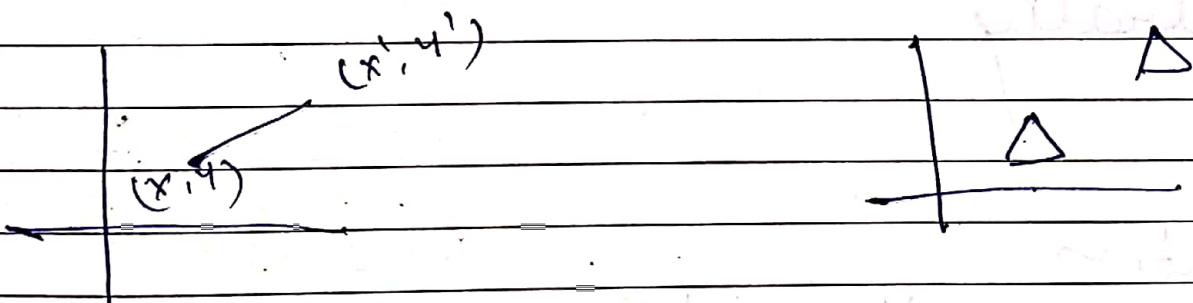
2-D transformation, translation, rotation.

Geometric Transformation :-

Change in orientation, size and shape are accomplished with geometric transformation that alter the co-ordinates description of objects.

The basic geometric transformations are translation, rotation and scaling.

Translation :-



Translation consists of a shift of the object parallel to itself in any direction in the (x, y) plane, any such shift can be accomplished by a shift in x -direction plus a shift in y direction.

If the amount of x -shift