

Data Structure

Classification Data Structure

↓ (Predefine)

Primitive Data type

→ Integer

→ Real

→ Character

→ Boolean

Non-Primitive Data type

(Required from higher level)

Linear DS

→ Array

→ Linked List

→ Stack (LIFO)

→ Queue (FIFO)

Non Linear DS

→ Tree

→ Graph

[Rear-Insert]

[Front-Delete]

→ Complexity of linked list is $(n)^{\text{Power}}$

Abstract Data type is a Mathematic model with the collection of operation define on that model.

Data structure deals with the implementation of various abstract data type for ex:

Stack, Queue, Linked list.



Abstract Data Type

Goals of Data Structure

- 1) Correctness
- 2) efficiency (space & Time)
- 3) robustness (correct output)
- 4) Adoptability (able to adjust new condⁿ)
- 5) Reusability

Performance Analysis

- 1) Time Complexity :- ex - os / networking /
- 2) Space Complexity

* To provide satisfactory real time response (Time complexity)

* Space for the Input also along with Algorithm / multiplier

Asymptotic Notations

To analyse the complexity of algorithms in terms of time and space we can never provide an exact no. to define the time & space required by an algorithm instead we express it using some standard notations also known as Asymptotic Notations.



at end / in different

1) O big ohh. ^ represent upper bound.

2) Ω omega lower bound

3) Θ Theta average bound.

* $1 < \log n < \sqrt{n} < n < n \log n < n^2 < n^3 <$
 $2^n < 3^n - \dots - n^n$

1) big Oh notation (big Oh O)

The fun. $F(n) = O(g(n))$ iff and only iff \exists (there exist) +ve Constant, C & n_0

such that $F(n) \leq C * g(n) \forall n \geq n_0$

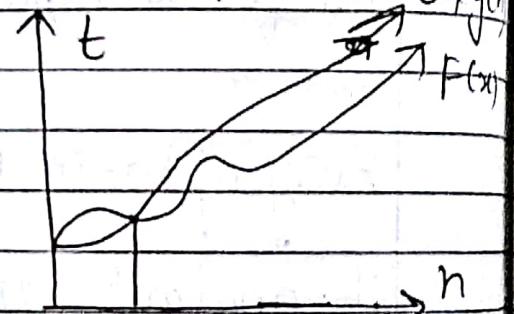
$$f(x) = 2n+3$$

$$2n+3 \leq ?$$

$$2n+3 \leq 10n$$

$$f(x) \leq g(n)$$

$$F(x) = O(n)$$



$$2n+3 \leq 10n$$

$$\frac{5n^2}{g(n)}$$



a) Omega notation Ω

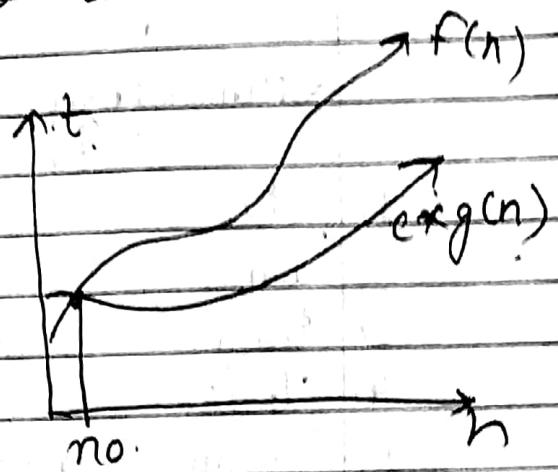
The $f(n) = \Omega(g(n))$ iff and only if there exist some +ve constant $c > 0$ such that $f(n) \geq c * g(n) \forall n \geq n_0$

$$f(x) = 2n+3$$

$$2n+3 \geq ?$$

$$2n+3 \geq cn / un / 2n / 2n / ln$$

$$f(n) = \Omega(n)$$



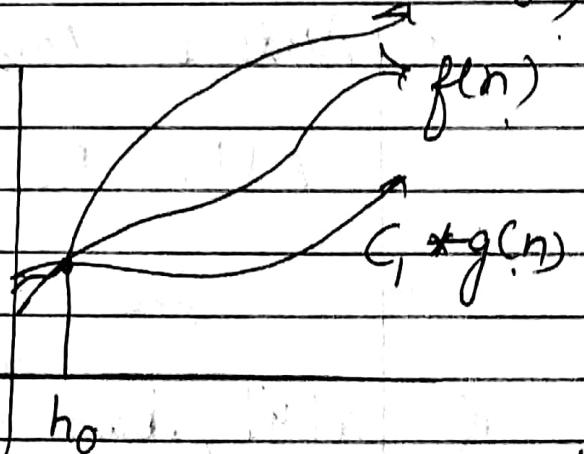
b) Theta notation Θ

The $f(n) = \Theta(g(n))$ iff & only iff there exist some +ve constants $c_1, c_2 \in \mathbb{R}$ & n_0 such that

$$c_1 * g(n) \leq f(n) \leq c_2 * g(n)$$

$$(c_2 g(n))$$

* If Omega & Big Oh is not equal then Theta is not calculated





Array

An array is a finite, ordered and collection of homogeneous data elements.

Terminology

- 1) Size :
- 2) type
- 3) base → address of the first element
- 4) Index
- 5) Range → lower bound, upper bound are called the boundaries of array.

In case of C $A[100]$ LB=0 UB=99

In Case of Pascal - $A: \text{Array}[-5 \dots 19] \text{ of Integer}$

$$LB = -5 \text{ & } UB = 19$$

* Calculating the length of array :- $UB - LB + 1$.

* Address Calculation in 1D Array

$$A(K) = \text{Base}(A) + W(K-LB)$$

$$W = \text{Size}$$

Q $a[4]$, base=100, w=4, $A[3]=?$

$$A[3] = 100 + 4(3-0)$$

$$[a[n]] = a[n-1] \quad \text{Page No. } 10$$

$$[a[1]] = [a]$$

Q. Write a program to insert element at specific index of array.

10 20 30 40 50 25 70 80 90 10 11

9 - 9 7 = 100

n = 5

0	10
1	20
2	30 40
3	40 50
4	50 60
	50

2-D Array

A[3][4]

R M	Row Major			
C N	00	01	02	03
00	00	01	02	03
01	10	11	12	13
02	20	21	22	23

Column major

* Row Major order

$$A[k_1, k_2] = \text{Base}(A) + w(E_1 L_1 + E_2)$$

Column Major order

$$A[k_1, k_2] = \text{Base}(A) + w(E_2 L_1 + E_1)$$

[LB₁] & [UB₁] are lower bound & upper bound of A₁

simi LB₂ & UB₂ are lower & upper bound of A₂

L₁ & L₂ be length of first and 2nd subarray

$$L_1 = UB_1 - LB_1 + 1$$

$$L_2 = UB_2 - LB_2 + 1$$

E₁ for the subarr K₁ the effective index E₁ of L₁
is computed as. E₁ = K₁ - LB₁



Page No. _____

Date _____

Effective index of E_2 is calculated as $k_2 = L \delta_2 = E$

Q) $A_p = A [E_1 E_2]$
Ans



0 1 2 3 e

Enter the element of an array, pls enter an element.

else array element before inserting elem

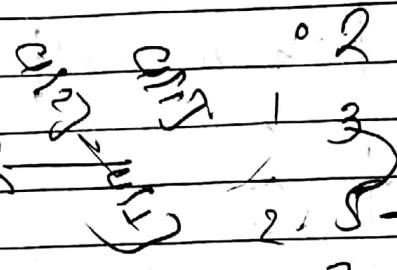
enter the position where u want to insert

enter the element to insert

array list after inserting an element

4,

P = 2



* Tutorial
Notation

$$F(n) = 2n^2 + 3n + 4 \quad \text{Calculation}$$

O, Ω, Θ

$$\textcircled{1} \quad F(x) = 2n^2 + 3n + 4$$

$$F(n) \leq c * g(n).$$

for

\sqrt{n}

$\sqrt{4}$

1

$2+3+4$

@

$$2n^2 + 3n + 4 \leq 2n^2 + 3n^2 + 4n^2$$

gn^2

$\uparrow \uparrow$

$c \cdot g(n)$

\uparrow

$O(n^2)$

(ii) Ohmega

$$F(n) \geq c * g(n)$$

$$2n^2 + 3n + 4 \geq 1 \cdot n^2$$

$\uparrow \uparrow$

$c + c(g)$

$\sqrt{n^2}$

(ii)



(11) Theta O

$$n(n^2) \leq 9n^2 + 3n + 4 \leq 100O(n^2)$$

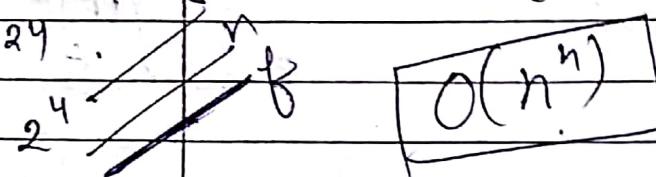
$$n(n^2) \leq O(n^2) \leq O(n^2)$$

~~O~~ $f(n) = n!$

(1) O big oh

$$f(n) \leq c * g(n)$$

$$n! \leq n^n$$

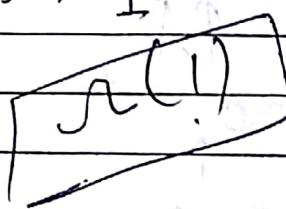


(ii) Omega. Ω

$$f(n) \geq c * g(n)$$

$$n! \geq 1$$

(13)



$$L^2 \sqrt{n}$$

$$f(n) = \lfloor \log n \rfloor \leq \log(1+1+1+\dots+1)$$

$$\leq \log(1 \times 2 \times 3 \times \dots \times n) \leq (\log n \times n \times n)$$

$$\log n^n$$

$$O(n \log n)$$



Ex:- 2D Array

$$A[4][3]$$

$$B = 52722$$

$$\text{Word} = 2 \times 16$$

$$\text{Cal. } A[2][1] = ?$$

Row major.

$$7 \times 2$$

$$14 + 52722$$

$$R[] = \text{Base} + w(E_1 L_2 + E_2) = 52736$$

$$52722 + 2(4 \times 1 + 2)$$

$$2 \times 3 + 91$$

$$52722 + 4(6)$$

$$7$$

$$24$$

$$\begin{array}{r} 52722 \\ - 24 \\ \hline 52746 \end{array}$$

By using formula

$$A[k_1][k_2] = \text{Base}(A) + w(E_1 L_2 + E_2)$$

$$A[2][1] = 52722 + 2(2 \times 3 + 1)$$

$$= 52722 + 14$$

$$L_1 = 3 - 0 + 1 = 4$$

$$\boxed{= 52736}$$

$$L_2 = 2 - 0 + 1 = 3$$

$$E_1 = 2 - 0 = 2$$

$$E_2 = 1 - 0 = 1$$

By using column major.

$$A[2][1] = 52722 + 2(1 \times 4 + 1)$$

$$= 52722 + 12$$

$$52734$$

00	10	20
01	11	21
02	12	22
03	13	23



Operations of Array

Insertion

Deletion

Sorting

Searching

Merging

Traversing



★ Insertion of an element in array

0	1	2	3	4	5	6
2	3	5	7	9	--	--

0	1	2	3	4	5	6
2	3	5	7	9	--	--

0	1	2	3	4	5	6
2	3	4	5	7	9	--

↑
newly inserted element

★ Deletion of an element from array

0	1	2	3	4	5	6
2	3	4	5	7	9	--

0	1	2	3	4	5	6
2	3	5	7	9	--	--

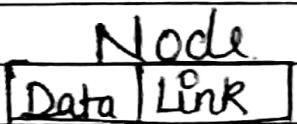
Traversing - Accessing elements of array
Atleast one operation of
traversing - transpose, add Ds



Linked list

Drawback of array

- 1) Extra size of array which is not come in use than it is wastage of memory.
- 2) Insertion and deletion is tedious task in array.
- 3) We define the size initially.



* We can eliminate the drawback of array.
Linked list support Dynamic memory allocation by creating Node at Runtime.

- Malloc
- Calloc
- Free
- Realloc

(i)

10	Null
----	------

 → single Node

(ii)

20	200
----	-----

 →

30	350
----	-----

 →

45	Null
----	------

- * Linked list Refers to a linear Collection of data items storing a linked list in memory is to have two parts
- 1) To store data call info field.
 - 2) To store the address of next node called as link (pointer field).



```
#include <stdio.h>
#include <conio.h>
#include <iostream.h>
#include <process.h>
```

Struct Node

```
struct Node
{
    int info;
    struct Node *link;
};
```

```
void main()
```

```
{
    struct node *node1, *node2;
    int data;
    node1 = (struct node *) malloc (sizeof(node));
    node2 = (struct node *) malloc (sizeof(node));
    printf ("Enter data for node1");
    scanf ("%d", &data);
    node1->info = data;
    printf ("Enter data for node2");
    scanf ("%d", &data);
    node2->info = data;
    node1->link = node2;
    node2->link = NULL;
    printf ("Address of Node1 is %u", node1);
    printf ("Info. of Node1 contains %d",
           node1->info);
    printf ("Address stored in link field of node1
is %u", node1->link);
    printf ("Repeat for node2")
```



Q Consider an array of size n. write a program to find max and min no. from list of element.

Q Consider an array of size n:-

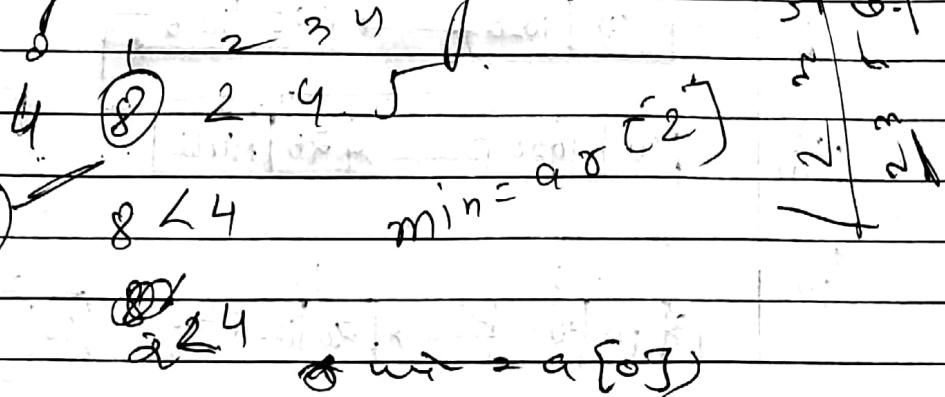
1) Insert element into array

2) Display

3) Search

4) Sort array element ascending/descending

Q Consider two arrays of size n, m respectively. write a program to merge these arrays.



Q. $\text{for } (j=0; j < n; j++)$

$\text{if } (a[i] > a[j], \text{ then } a[i] = a[j])$

~~8 4 6 1 4 2 10~~

~~a[0]~~

~~x~~

~~6 < 3~~

~~x~~

~~1 < 3~~

~~x~~

$\min = 1$

~~2 3 4 5~~

~~1 2 3 4~~

~~x~~

~~C~~

~~D~~

~~E~~

~~F~~

~~G~~

~~H~~

~~I~~

~~J~~

~~K~~

~~L~~

~~M~~

~~N~~

~~O~~

~~P~~

~~Q~~

~~R~~

~~S~~

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~~E~~

Type of Linked List

(Linear)

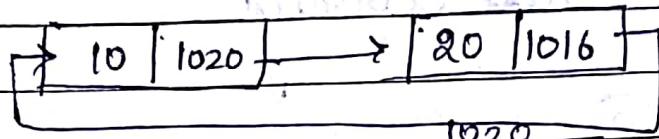
- 1) Single linked List
- 2) Circular linked List
- 3) Linear
- 4) Doubly linear linked list
- 5) Circular doubly linear linked list

1020

(i)



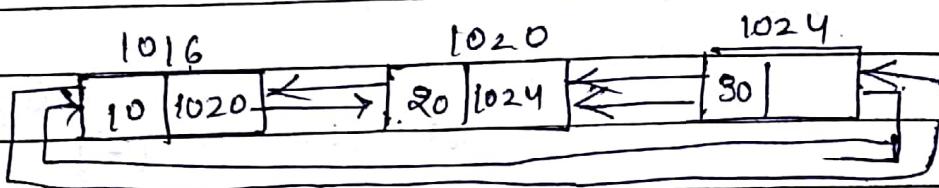
(ii)



(iii)



(iv)



Operations on Linked List

- (1) Creation
- (2) Traversing
- (3) Searching
- (4) Inserting
- (5) Deleting
- (6) Merging
- (7) Sorting



```
#include <stdio.h>
#include <conio.h>
#include <malloc.h>
```

Struct node

{

```
int info;
```

```
Struct node*link;
```

{

```
Struct node *first = NULL,
```

```
*last = NULL;
```

```
Void create();
```

```
Void display();
```

Void main()

```
{ int choice;
```

```
clrscr();
```

```
printf ("Enter choice");
```

```
scanf ("%d", &choice);
```

```
while (printf ("Press 1. Create,
```

```
2. display,
```

```
3. Quit"));
```

While (choice)

```
{ choice.
```

```
Switch (case)
```

```
{ Case 1 : Create; break;
```

```
Case 2 : Display; break;
```

```
: Case 3 : exit();
```

```
}.
```



```
printf ("Enter the choice");
printf (" 1-Create .
& display
3-Quit");
scanf ("%d", &choice);
{
```

```
Void create ()
```

```
{ struct node *new = malloc sizeof (struct
    printf ("Enter item to be inserted");
    scanf ("%d", &new->info);
    new->link = null;
```

```
if (first == null)
    first = new;
```

```
else
    last->link = new;
    last = new;
```

```
}
```

```
Void display ()
```

```
{ if (first == null)
    printf ("no element");
```

```
else
```

```
{ struct node *temp = first;
```

```
printf ("Element are ");
    while (temp != null)
```

```
{ printf ("%d", temp->info);
    temp = temp->link;
```

```
}
```

```
printf ("Null")
```



Searching in Single linked list

Void Search()

```
if (First == Null)
    printf ("There are no elements in the list");
else
    Struct node *temp = First;
    int element, position = 1;
    printf ("Enter the element");
    scanf ("%d", &element);
```

```
while ((temp != last) && (temp->info != element))
```

```
    temp = temp->link;
    position++;
```

```
if (temp->info == element)
```

```
    printf ("The element is present in the position %d",  
           position);
```

```
else
```

```
    printf ("Element not found");
```

Traversing of Single Linear Linklist

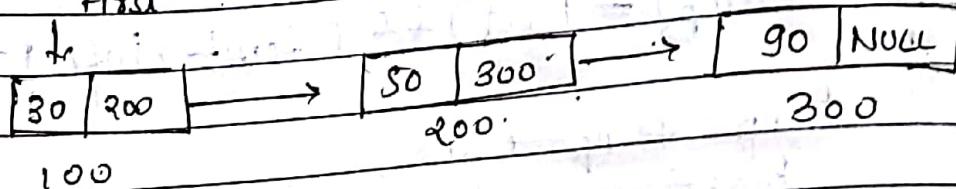
while ($(\text{temp}) = (\text{last}) \& \& (\text{temp} \rightarrow \text{info}) = \text{current}$)

temp = temp \rightarrow link;
position ++;

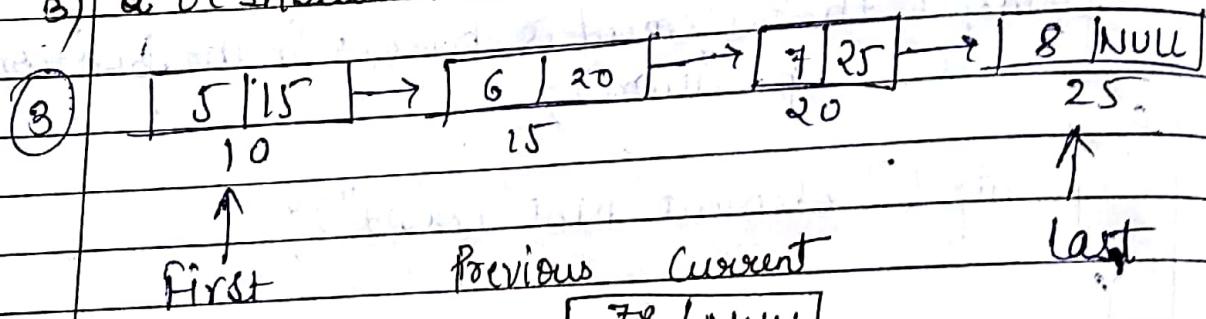
Insertion into Single linear linklist

first

↓
last



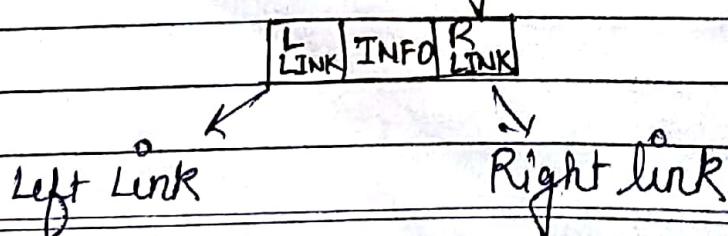
- at beginning
- at end.
- a or Inbetween (location)



Previous \rightarrow link = NEW

New \rightarrow link = Current

Insertion Doubly linklist





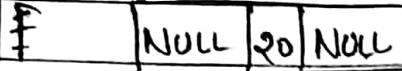
struct dnode

{ int info;

struct dnode * llink;

struct dnode * rlink;

} Insertion in first-



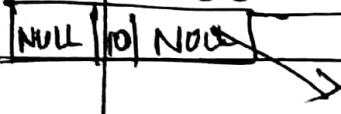
New 25

New \rightarrow rlink = FIRST.

FIRST \rightarrow llink = New.

FIRST = New.

Insertion at the End



15 | 78 | NULL.

30

New \rightarrow llink = FIRST.

FIRST \rightarrow Rlink = new

Last = New.

FIRST Node - Llink = NULL

Last Node - Rlink = NULL